## Unit 4 Group Work 2 PCHA 2021-22 / Dr. Kessner

## No calculator! Have fun!

**1.** Let

$$f(x) = \begin{cases} x+1 & \text{if } x < 0\\ 0 & \text{if } x - 0\\ \cos x & \text{if } x > 0 \end{cases}$$

a) Sketch the graph of f(x).

- b) On what intervals is f increasing and/or decreasing? Is f bounded? Does it have any local or global maxima or minima?
- c) Does f have any discontinuities? Where, and what type?
- d) Describe the end behavior of f using limits.

2. Consider the same function from the previous problem.

$$f(x) = \begin{cases} x+1 & \text{if } x < 0\\ 0 & \text{if } x - 0\\ \cos x & \text{if } x > 0 \end{cases}$$

Sketch the graphs of the following transformed functions:

- p(x) = -f(x)

- q(x) = f(|x|)• q(x) = f(|x|)• r(x) = -f(|x|)• s(x) = f(-|x|)• t(x) = |f(-|x|)|

**3.** Factor the following polynomial completely, both over  $\mathbb{R}$  (as a product of real linear and irreducible quadratic factors) and over  $\mathbb{C}$  (as a product of complex linear factors). Sketch the graph of the function.

$$p(x) = x^4 + 6x^3 + 13x^2 + 12x + 4$$

**4.** Factor the following polynomial completely, both over  $\mathbb{R}$  (as a product of real linear and irreducible quadratic factors) and over  $\mathbb{C}$  (as a product of complex linear factors). Sketch the graph of the function.

$$q(x) = x^5 + 2x^4 - 16x - 32$$

5. Sketch the graph of the following rational function.

$$r(x) = \frac{x^3 + x^2 - x - 1}{x}$$

Write limits to describe its end behavior, and its behavior near asymptotes. Challenge: Describe its asymptotic end behavior.