## Test Unit 2 PCHA 2020-21 / Dr. Kessner

Name:

No calculator, no notes - just your brain! Have fun!

1. Evaluate the following:

a) 
$$\sec \frac{5\pi}{3} = (12) = 2$$

b) 
$$\sin(-\frac{2\pi}{3}) = -\frac{\pi}{2}$$

c) 
$$\cos^{-1}\left(\cot(-\frac{5\pi}{4})\right)$$
 = 7

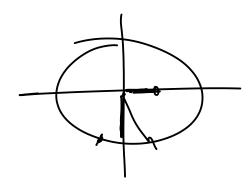
d) 
$$\sin^{-1}\left(\cos\left(-\frac{\pi}{2}\right)\right)$$
 —  $\bigcirc$ 

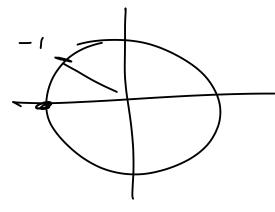
e) 
$$\tan^{-1}\left(\cot\left(\frac{\pi}{6}\right)\right) = \frac{\pi}{3}$$

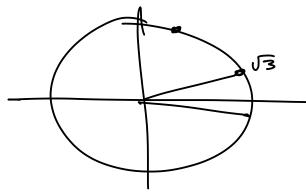
f) 
$$\sin(-\frac{\pi}{12}) = \sin(\frac{T}{4} - \frac{\pi}{3})$$

$$= \cos(\frac{T}{4} - \frac{\pi}{3})$$

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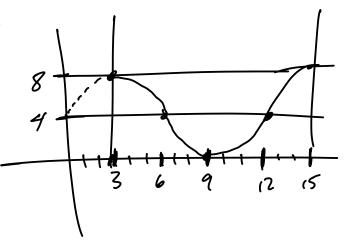


2. Write down all the relevant properties (period, amplitude, shifts/scales, asymptotes) of the following trig functions, and then graph by hand.

$$f(x) = 4 + 4\cos\left(\frac{\pi}{6}x - \frac{\pi}{2}\right)$$
$$= 4 + 4\cos\left(\frac{\pi}{6}(\chi - 3)\right)$$

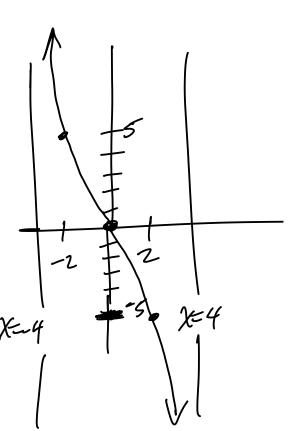
period 2# = 12

Sheft right 3, up4 amplitude 4



$$g(x) = 5\cot\left(\frac{\pi}{8}(x-4)\right)$$

shift left 4 vartical scale 5



**Bonus** Write f as a transformed sin and g as a transformed tan.

4+4511(Tx) -5tan(Tx)

## **3.** Prove the identities:

$$\frac{\cos x + \sin x}{\cos x - \sin x} = \sec 2x + \tan 2x$$

$$\frac{(\delta 3 \times + \sin x)}{(\delta 5 \times - \sin x)} = \frac{(\delta 3 \times + \sin x)}{(\delta 5 \times + \sin x)^2}$$

$$= \frac{(\delta 5 \times + \sin x)^2}{(\delta 5 \times + \sin^2 x)}$$

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$$Sin(\pi - x) = \sin x$$

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$$= \sin x - \cos x - \cos x$$

$$= \sin x$$

$$= \sin x$$

$$= \sin x$$

Bonus Prove this using cofactor identities.

**4.** Find all solutions of  $\sin 2\theta + \cos \theta = 0$ .

$$2 \operatorname{SNO}(x) O + (x) O = 0$$

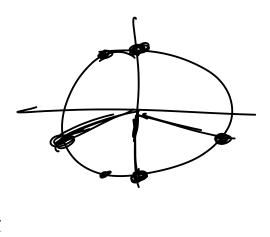
$$\operatorname{COSO}(2 \operatorname{SNO} + 1) = 0$$

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Derive the following half angle formula from the relevant double angle formula:

$$\cos u = \pm \sqrt{\frac{1 + \cos 2u}{2}}$$

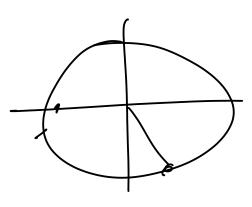
Use the half angle formula above to find  $\cos(-\frac{5\pi}{12})$ .

$$CO(\frac{-5}{1}) = + \underbrace{1 + ca(-57)}_{2}$$

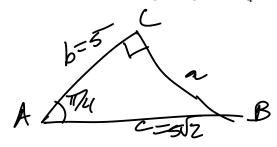
$$= \underbrace{1 + (-5\frac{1}{2})}_{2}$$

$$= \underbrace{1 + (-5\frac{1}{2})}_{2}$$

$$= \underbrace{1 - 2}_{2} \underbrace{1 - 2}_{3}$$



**5.** Solve the following triangle:  $A = \frac{\pi}{4}$ , b = 5,  $c = 5\sqrt{2}$ .



$$a^{2} = b^{2} + c^{2} - 2abcasA$$

$$= 25 + 50 - 2.5 \cdot 5\sqrt{2} \text{ row } = 25 + 50 - 50$$

$$= 25 + 50 - 50$$

$$= 25$$

$$a=5$$

$$SinC = C SinA = \frac{5\sqrt{2} \sin^{7}4}{5} = 1$$

$$= C = \frac{1}{2}$$

$$B = \frac{1}{4}$$