PHD Proposal

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1 Introduction

The problem of *pattern matching* is one of the most studied topics in the field of algorithmics and bioinformatics. For example the interest in such problems is due to the need to align sequences or search for specific patterns within the *DNA*.

In this context, a large number of data structure algorithms have been modeled. Among these, one of the most used is the **Burrows-Wheeler transform** (BWT) thanks to the studies of Ferragina and Manzini who proposed its use together with the so-called FM-index [1].

In recent years, in the field of bioinformatics, there is a change of interest. While until a few years ago the research was focused on the study of the *genome*, we are now starting to deepen the topic of *pangenome*. Currently, the need to take into account the high variability in population genomes as well as the specificity of an individual genome in a personalized approach to medicine is rapidly pushing the abandonment of the traditional paradigm of using a single reference genome [2].

In this context, various algorithms and various data structures have been implemented in order to study the so called *haplotypes* and *genotypes*. Briefly we could define *haplotypes* as a combination of allelic variants, inherited from a parent. Instead we can define the *genotype* as the complete set of genes contained in the DNA. From a biological point of view it is indeed interesting to note that each individual shares about 99% of the genetic code, while the remaining 1% differs mostly with **Single Nucleotide Polymorphisms** (*SNPs*), i.e. variations of a single nucleotide in a precise *locus* of the DNA Thanks to the last developments in sequencing technologies, which have led both to reduce the costs of single sequencing and to produce sequences of ever higher quality in less and less time, the researchers were able to theorize the *pangenome graph*, replacing the old representation of the single genome by a single sequence.

One of the most important data structure developed in order to handle the

study of haplotypes sequences is the **positional Burrows-Wheeler transform** (*PBWT*), proposed by Durbin in 2014 [3]. With this particular data structure it was possible both to study possible matches inside a haplotype panel and to search for set maximal matches between an external haplotype and a panel, as well as the set maximal matches inside the panel itself. Furthermore, for example, variants have also been studied for the management of the multiallelic case [4].

In 2021 Rossi et al. proposed MONI as a data structure to handle a **runlength version of BWT** (RLPBWT) with the ultimate intention of indexing and using multiple genomes as a reference [5]. Together with this data structure the authors proposed the concept of $matching\ statistics$ in order to efficiently compute the matches between a pattern and a text. A recent improvement, regarding the RLPBWT, has been made through the implementation of PHONI [6], where where the so-called $longest-common-extension\ (LCE)\ queries$ are used.

During the development of my master's thesis I worked in collaboration with the authors of MONI in order to create a run length encoded variant of the PBWT. In this work I used practically all concepts applied to the "classic" *BWT* in *MONI* and *PHONI*.

During my PhD I will focus my studies on the development of new algorithms in various topics such as variants of the *PBWT* (and any related uses), *hap-lotyping/genotyping* or solutions concerning the study of *SNPs*.It is also my intention to deepen the more experimental themes relating to pattern matching, in detail the new developments on BWT and new indexing structures, as well as the theme of *succinct data structures*, with particular attention to the use of *bitvectors*.

2 State of the art

I will now present a brief overview of the main algorithms, data structures, methods etc that will be the core of my studies during my PhD.

BWT

The Burrows-Wheeler Transform (BWT) [7] was introduced in 1994 in order to compress texts but it has had then wide use in bioinformatics, above all thanks to the already cited FM-index. Given a text T, \$-terminated, such that |T| = n, we can define the BWT_T , denoting with SA_T the suffix array of T, as: $BWT_T[i] = T[SA_T[i] - 1]$, if $SA_T[i] > 0$, and $BWT_T[i] = \$$ otherwise. Less formally we can say that $BWT_T[i]$ is the character that

precedes the i-th suffix in the lexicographically order. It is important to note that this transform is reversible so we can reconstruct the text T from its transform BWT_T using the so-called **LF-mapping**. Given BWT_T and an array, called F_T , with all the characters of T in the lexicographically order, we can say that, thanks to the LF-mapping, the j-th occurrence of a certain character in BWT_T corresponds to the j-th occurrence of the same character in F_T , so we can reconstruct T starting from its last character \$. With the use of the LF-mapping we can perform the backward-search in order to use the BWT_T to look for a pattern P within T. This can be done efficiently thank to the FM-index which consists of two functions. The first one is C function, such that, given an alphabet Σ (that includes the ending character $(S), C: \Sigma \to [1, n]$. This function, given a character $\sigma \in \Sigma$ returns the number of occurrences of characters lexicographically than the one given as argument in T. The second one is the Occ function, $Occ: \Sigma \times [1,n] \to [1,n]$, has as arguments a character $\sigma \in \Sigma$ and an index i of BWT_T and returns the count of occurrences of σ in $BWT_T[1,i]$ (CONTROLLARE E RISCRIVERE MEGLIO).

The use of BWT has allowed the construction of efficient algorithms both in the field of pattern matching and in that of sequence alignment.

Bitvectors

Bitvectors are ones of the most important data structure when mentioning succinct data structures.

A bitvector is an array on n bits which allows two particular operations, called **rank** and **select**, in addition to the classic operations possible on Boolean arrays, such as random access in constant time (**DA VERIFICARE**). More in detail the rank function allows you to calculate how many values of 1 are up to a certain index. Instead the select function allows to obtain the index of any one present in the bitvector. Formally, given a bitvector B, such that |B| = n, and given an index i, such that $0 \le i < n$, we can define $rank_B(i) = \sum_{k=0}^{k < i} B[k]$. Instead, about the select function, given an integer i, such that $0 < i \le rank_B(n)$, where n = |B|, we can define $select(i) = \min\{j \mid rank_B(j+1) = i\}$.

From a purely theoretical point of view, with the additional cost of $\mathcal{O}(n)$ bits in memory, these two operations can be supported with constant time. In more practical terms there are several implementations of the same within **SDSL** (Succint Data Structures Library) [8], one of the most important C++ library used in bioinformatics. As the implementation changes (for example plain bitvector, interleaved bitvector, sparse bivector etc...) the computational time of the two operations varies (usually only one of the two

is in constant time) and the amount of additional bits needed. An example of the use of bitvectors is to track the runs in the run-length encoded implementations of BWT and PBWT, where we put one at each head of run.

RLBWT, Matching Statistics, MONI and PHONI PBWT

RLPBWT

3 Research goals

References

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