

- In the last lecture we:
 - Constructed an iterative implementation of the function *Sum* to sum the numbers in a list.
 - Drew a flowchart for this iterative implementation.
 - Annotated the flowchart with assertions.
 - Proved by induction that the iterative implementation of the recursive definition was correct.

- In this lecture we look at a final example of:
 - Constructing a recursive definition of a function;
 - Implementing the recursive definition recursively;
 - Implementing the recursive definition iteratively;
 - Constructing a flowchart for the iterative implementation, annotating the flowchart with assertions and proving by induction that the iterative implementation is correct.

- The Fibonacci Numbers
- 0,1,1,2,3,5,8,13,21,34,55,89,144,...
- What is the pattern here?

- Recursive definition of function to return a specific number in the sequence:
 - Base Case: $Fib(0) = 0, Fib(1) = 1$
 - Recurrence Relation:
$$Fib(n) = Fib(n - 1) + Fib(n - 2)$$
- Recursive Implementation:

```
int Fibonacci(int n)
{
    if (n==0)
        return 0;
    else if (n==1)
        return 1;
    else
        return (Fibonacci(n-1) +
                Fibonacci(n-2));
}
```

- An iterative implementation of *Fib*.

```
int Fibonacci(int n)
{
    int i=1;
    int fib1=0;
    int fib2=1;

    /* initialisation corresponding
       to the base case */

    int fib3;
    if (n==0)
        fib2=fib1;
    else {
        while(i<n)
        {
            fib3=fib1+fib2;
            fib1=fib2;
            fib2=fib3;
            // implementation of
            // recurrence relation
            i=i+1;
        }
        return fib2;
    }
}
```

- The following will be provided in the lectures:
 1. A flowchart for this iterative implementation.
 2. Annotate the flowchart with assertions.
 3. Prove the correctness of the iterative implementation using the assertions.