

IP#1 - Graph Non-Isomorphism & PSPACE Upper Bound

Instructor: Alessandro Chiesa

Scribe: Shuangjun Zhang

1 The class \mathcal{NP}

The class \mathcal{NP} can be regarded as traditional mathematical proof systems. Let's recall the definition of \mathcal{NP} :

Definition 1 A language $L \in \mathcal{NP}$ if and only if there exists a polynomial time decider \mathcal{D} such that

- (1) $\forall x \in \mathcal{L}, \exists \text{ witness } w, \text{ such that } \mathcal{D}(x, w) = 1.$
- (2) $\forall x \notin \mathcal{L}, \forall \text{ witness } w, \mathcal{D}(x, w) = 0.$

For example, consider the boolean satisfiable problem \mathcal{SAT} , x is a boolean formula $\phi(x_1, x_2, \dots, x_n)$, w is an assignment $(a_1, a_2, \dots, a_n) \in \{0, 1\}^n$ and \mathcal{D} checks that $\phi(a_1, a_2, \dots, a_n)$ is true.

\mathcal{NP} captures classical mathematical proofs.

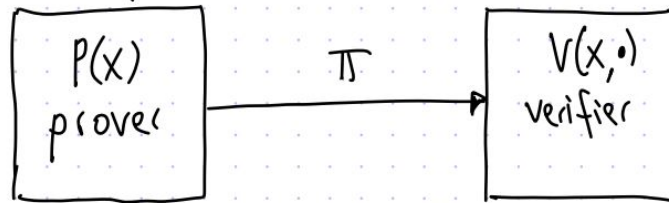


Figure 1: \mathcal{NP} Proof Systems

2 Interactive Proofs

Here is a demonstration of the theorem environments.

Theorem 2 *This is a theorem.*

Definition 3 *This is a definition.*

Remark 4 *This is a remark.*

Lemma 5 *This is a lemma.*

Corollary 6 *This is a corollary.*

Proposition 7 *This is a proposition.*

Claim 8 *This is a claim.*

Observation 9 *This is an observation.*

Fact 10 *This is a fact.*

Assumption 11 *This is an assumption.*

2.1 Proof Environments

Here is a demonstration of the proof environments.

Theorem 12 *This is a theorem with a proof.*

Proof: This is the theorem's proof.

□

Theorem 13 *This is a theorem with a proof claim.*

This is the theorem's proof claim.

◇

Proof of Theorem 12: This is another proof of Theorem 12.

□