

## Assignment of master's thesis

Title: Math expression evaluator for literal types in TypeScript

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Study program: Informatics

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**Department:** Department of Software Engineering

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#### Instructions

Template literal types [1], introduced in TypeScript 4.1, expand on string literal types for narrowing down a type to a particular string constant, with the ability to expand into many string literal types.

- 1. Analyze and describe relevant constructs of the TypeScript type system (concatenation, recursive types, conditional types etc.)
- 2. Implement a typesafe math expression evaluator with a set of basic operations, using a string literal type both as the input and output of the evaluator.
- 3. Pick appropriate tools for testing type annotations and ensure the validity of the evaluator with functional tests.
- 4. Discuss the practical uses of implemented meta types and theoretical and practical shortcomings of the TypeScript type system.
- 5. Publish the implementation as an open-source TypeScript library, which can be used for meta-programming, including source code and corresponding documentation.
- [1] https://www.typescriptlang.org/docs/handbook/2/template-literal-types.html

#### Master's thesis

# MATH EXPRESSION EVALUATOR FOR LITERAL TYPES IN TYPESCRIPT

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Faculty of Information Technology Department of Software Engineering Supervisor: Ing. Jaroslav Šmolík April 16, 2023

Czech Technical University in Prague Faculty of Information Technology

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## Seznam zkratek

TC39 ECMA International, Technical Committee 39

W3C World Wide Web Consortium

xii Seznam zkratek

## Chapter 1

# Introduction

## 1.1 Motivation

TypeScript, a typed superset of JavaScript, is quickly gaining popularity in the JavaScript development ecosystem, and type-safety, the concept of validating data types, is "eating the world" [1]. As of 2023, over 66% of developers are using TypeScript most of the time, either avoiding JavaScript entirely or spending the majority of time working with TypeScript codebases [2]. Over the years, TypeScript has transformed from a simple type annotation tool to a full-fledged programming language within the type system itself. Multiple libraries with advanced Type-Script types have emerged to improve the developer experience. Libraries such as Prisma for database type-safety [3], Zod for combining schema validation and static type inference [4], or tRPC for API end-to-end type-safety across boundaries [5]. With intelligent suggestions in the editor of choice, TypeScript ensures high code quality while avoiding any runtime costs due to the type system being evaluated during compilation. With editors and IDEs using a language server powered by Language Server Protocol (LSP) to provide the developer with valuable suggestions, there is an incentive to utilise the type system instead of running a daemon alongside or adding a build step.

However, TypeScript is only as powerful as the types declared and received. A significant burden is laid on the maintainers of libraries to provide descriptive and valuable types. This thesis aims to lay out and highlight the capabilities and techniques of the TypeScript type system when applied to a non-trivial problem domain. The type-only implementation of the math expression evaluator serves as a practical case study, demonstrating the power of the TypeScript type system and the benefits of type safety.

## 1.2 What is a static type system

For years, type systems in programming languages have been a well-known and heavily discussed topic. The main goal of a type system is to provide a formal specification of the types of data that a program can manipulate.

2 Introduction

In statically typed languages, the type of a variable is known at compile time. The compiler uses the additional information about data types to verify the source code during compilation. The data type itself can be deduced from the usage in the code (type inference), or a programmer explicitly specifies the data type of a variable before usage. Examples of such languages using static typing are, for instance, Java, C# or C++.

Whereas in dynamically typed languages, the type of a variable is determined at runtime based on the value being assigned, it does not need to be explicitly declared by the developer or known at compile time via type inference. Some of the popular dynamically typed languages include Python, Ruby, PHP, and, most notably, JavaScript, which is widely used to create interactive and dynamic user interfaces on the web platform. Dynamically typed languages tend to be more flexible and allow developers, notably beginner developers, to write code faster and iterate quicker.

Static typing offers numerous compelling benefits that can enhance the development process. First, a large class of errors is caught earlier in the development process. This reduces the likelihood of bugs and runtime issues that can be difficult to diagnose and debug. With static typing, developers can rely on a compiler system to ensure the code conforms to the expected data types. Developers can also refactor existing typed code more confidently, as the system gives developers direct feedback when refactoring.

Furthermore, by writing type annotations, developers are actively self-documenting the code, making the code more readable and easier to understand, especially when dealing with unfamiliar code. Finally, even though an initial commitment is necessary by writing type annotations at first, a more powerful type system can determine the developer's intent without writing additional code as the development progresses.

#### 1.3 Structure of the work

This thesis will provide a comprehensive analysis of relevant advanced constructs found in the TypeScript type system and how they can be used to allow robust meta-programming within the types themselves. An implementation of a generic math expression evaluator library that operates strictly on the type level is provided to demonstrate the capabilities of the type system, followed by a discussion on testing and performance of the library and the impact on type checking and development experience in the editor.

## 2.1 Static Typing in JavaScript

JavaScript is a dynamically typed programming language where users do not need to assign types to a variable or a function, and the type is inferred automatically by the JavaScript engine at runtime. This feature lowers the barrier of entry to writing JavaScript code allowing developers to prototype and write code quickly. It can plausibly be one of the possible growth drivers of JavaScript in the last decade, making it the most commonly used programming language according to the 2022 Stack Overflow Developer Survey [6].

However, dynamic typing has its drawbacks. It is harder to detect trivial errors in the code without running it beforehand, and it is more difficult to refactor the code without breaking it, which often leads to poor software quality [7]. Proponents of static typing insist that static types allow developers to spot potential bugs and mistakes earlier during development and that it allows for better tooling, such as more rich code completion and refactoring tools.

There is an upcoming TC39 proposal for adding type annotations, broadly inspired by Type-Script syntax [8]. These annotations are only useful for build-time tooling as they are ignored in runtime. The proposal suggests that these annotations should be erased by an additional compilation step. Even though users can already provide static types using JSDoc right now, the syntax is not as clean as the proposed TypeScript-like syntax.

Regardless, many projects aim to introduce static typing to JavaScript, such as Flow or TypeScript, or alternative languages which compile back to JavaScript, such as Elm or ReScript.

#### 2.1.1 Elm

Elm is a functional programming language designed specifically for building web applications [9]. The language compiles to JavaScript and has a strong static Hindley-Milner-based type system, which allows inferring types more often and reliably. Elm does not provide any escape hatches such as any in TypeScript. Thus it is harder to write unsafe code, as the types must be valid for the code to be compiled.

Elm also includes a lot of quality-of-life improvements and benefits, for instance: enforced purity of functions, out-of-the-box immutability, case pattern matching, JSON decoders and encoders for strict parsing, Maybe and Result monads for avoiding null and undefined references or its own virtual DOM implementation for efficient rendering of interactive user interfaces. Notably, the Elm Architecture, where the application code is organised into three parts: model, update and view [10], has greatly inspired other libraries and frameworks like Redux [11].

## 2.1.2 ReScript

ReScript is a programming language built on top of the OCaml toolchain. Unlike Flow or Type-Script, ReScript is not a superset of JavaScript. Instead, the language compiles to JavaScript. ReScript was created as a spin-off from the Reason programming language and accompanying BuckleScript compiler, aiming to vertically integrate and streamline the adoption barrier caused by the need to be familiar with multiple unrelated tools and toolchains [12].

The language aims to be more sound with more powerful type inference than TypeScript, borrowing the Hindler-Milner type system from OCaml implementation [13, 14]. Thus, most of the time, the types can be inferred automatically without the need to annotate them explicitly, whereas TypeScript utilises bidirectional type checking [15].

#### 2.1.3 Flow

Flow is a static type checker for JavaScript [16, 17], which allows developers to annotate their code with static types. Flow is developed by Meta and is internally used in production by Facebook, Instagram and React Native. Type annotations in Flow are fully erasable, which means that the type annotations can be fully removed from the Flow code to emit valid JavaScript code. The checking of these types occurs at compile-time before removal in build-time. Flow is also a superset of JavaScript, which means any JavaScript code is a valid Flow code.

One of the primary goals of Flow is to provide type soundness, the ability to catch every error that might happen in runtime at compile-time, no matter how likely it is to happen. A valid Flow code can provide developers with some guarantees about the type a value has in runtime, at the expense of catching errors, which are unlikely to happen in runtime.

Both Flow and TypeScript are similar regarding features at the time of writing. Most of the soundness differences between Flow and TypeScript have been addressed with the newer versions of TypeScript, even though soundness is a specific non-goal by the TypeScript team [18]. However, developers must opt-in to these features by setting "strict" to "true" in tsconfig.json, whereas these features are enabled by default in Flow.

## 2.1.4 TypeScript

TypeScript is a statically typed programming language developed and maintained by Microsoft [19]. It is a language that transpiles to JavaScript and adds static type checking to JavaScript [20]. Unlike Elm or ReScript, TypeScript is a syntactical superset of JavaScript, which means

that any valid JavaScript code can be a valid TypeScript code.<sup>1</sup> Similar to Flow, type annotations provided by the developer are fully erasable either by the TypeScript tsc type checker or by other community build tools, such as babel[21], esbuild[22] or swc[23].

Type system in TypeScript is considered to be less sound and more forgiving, as soundness is stated as an explicit non-goal for the design team of TypeScript [18], with emphasis on striking a balance between productivity and correctness. By default, the TypeScript type checker is not strict, and the language itself includes an escape hatch for developers to opt out of type checking by using the any type or using <code>@ts-ignore</code> comment annotations. Nevertheless, with proper type checker configuration, the type system of TypeScript can be as sound as in Flow.

Both Flow and TypeScript support advanced features such as generics and utility types, with the latter supporting template string literal types and better support for conditional types, unlocking the potential of writing more expressive types, which this master thesis will further explore in more detail.

TypeScript has become the de-facto standard for writing JavaScript code with static types. With deep integration with Visual Studio Code [24], the rich build ecosystem and high compatibility with existing JavaScript libraries and tools, TypeScript has become one of the fastest growing languages in terms of usage according to the 2022 Octoverse report by Github [25].

## 2.2 Usage of TypeScript

The TypeScript project is made of two major parts available to developers:

- tsc: the TypeScript Compiler, which is responsible for both type checking and outputting valid JavaScript files,
- tsserver: the TypeScript Standalone Server, which encapsulates the TypeScript Compiler and language services for use in editors and IDEs [26].

While a type-checker is most likely executed manually more often and is the entry point for developers when using TypeScript, the language server is equally as useful, as it communicates with the editor via Language Server Protocol (LSP) to provide important language services. These include code completion, auto-importing, symbol renaming etc.

Unlike in the other languages, the compilation step itself is understood to only mean the type erasure itself. Even though the source code itself can have various type errors, tsc will still, by default, emit JavaScript files as long as the input source file can be parsed by both the scanner and the parser. This allows developers to progressively update their code and iterate quickly on the functionality without immediately dealing with the type errors, acting more as a linter than a compiler. Regardless, in this thesis, "compiling" and "type-checking" will be used interchangeably.

<sup>&</sup>lt;sup>1</sup>With a lax type checker configuration

## 2.3 Typescript syntax

In TypeScript, types are typically annotated using :[type annotation] syntax, adding annotations to any of the symbols found in JavaScript, such as variables, function parameters and function return values, to add constraints to values. Type annotations in TypeScript can be categorised into primitive types, literal types, data structure types, union types, intersection types and type parameters. In the following sections, we will explore each of these types in more detail. The following listing 2.1 shows a basic example of TypeScript annotations:

#### ■ Listing 2.1 Basic TypeScript annotation example

```
const prefix: string = "Hello world"
const user: {
  name: string;
  age: number
}

function formatUserGreeting(
  user: {
    name: string;
    age: number;
  },
  message: string
): string {
  return [message, user.name].join(" ");
}

const greeting: string = formatUserGreeting(user, prefix);
```

At runtime, every variable has a single concrete value, but in TypeScript, the variable has only a type. A useful mental model for understanding types is to think of the type as a set of permitted values [27], effectively describing the domain of the type.

Developers can declare types directly in type annotations, but sometimes developers need to reuse the same type in multiple annotations. To avoid repeating the same declaration, we can use type aliases to refer to a type by a name. These type variables act as an alias, which can be used in place of the type itself. The listing 2.2 shows a refactored formatUserGreeting function of the previous listing 2.1 using type aliases.

## 2.3.1 Primitive Types

A primitive value is data that is not an object and has no methods or properties. These primitives are immutable. Thus, they cannot be altered. The TypeScript type system provides a comprehensive representation of these primitives, as seen in listing 2.3:

Some primitive values represent a singular data value, such as null or undefined, but many of these primitives can represent multiple values (boolean can represent either true or false), or even an infinite amount of values, like number, bignumber or string.

Typescript syntax 7

## Listing 2.2 Type aliases

```
type User = {
  name: string;
  age: number
}

const prefix: string = "Hello world"
const user: User

function formatUserGreeting(
  user: User,
  message: string
): string {
  return [message, user.name].join(" ");
}
```

#### Listing 2.3 Primitive Types

```
type StringPrimitive = string
type NumberPrimitive = number
type BigintPrimitive = bigint
type BooleanPrimitive = boolean
type UndefinedPrimitive = undefined
type NullPrimitive = null
type SymbolPrimitive = symbol
```

## 2.3.2 Literal Types

Literal types are used to describe an exact value as a type. From the point of view of the type system, a literal type is a subset of one of the following primitive types: string, number, bignumber or boolean,<sup>2</sup> as seen in Listing 2.4.

#### **Listing 2.4** Literal Types

```
type Literal = "foo" | 42 | true | 100n;

// Valid code
const Valid: Literal = "foo"

// @ts-expect-error Type '"bar"' is not assignable to type 'Literal'
const Invalid: Literal = "bar"
```

## 2.3.3 Types for data structures

TypeScript also allows annotating data structures such as objects and arrays with four possible types, depending on the enumerability of items and their types. The syntax overview can be

<sup>&</sup>lt;sup>2</sup>Both null and undefined are literal types as well

seen here in Listing 2.5.

■ tuple type for describing an array with a fixed number of elements, possibly with a different type for each element,

- array type for describing an array with an unknown length, and the values are of the same type,
- record type for describing an object with an unknown number of keys, and the values are of the same type,
- object type or an interface for describing an object with a finite set of keys with values of different types per key.

#### Listing 2.5 Data structures

```
interface ObjectStructure {
  foo: string;
  bar: number;
}

type ObjectStructure =
  | { foo: string, bar: number }

type RecordStructure
  | { [key: string]: number }
  | Record<string, number>

type TupleStructure = [number, string]

type ArrayStructure = number[]
```

TypeScript syntax offers two notations which can be used for describing objects with a finite set of key-value pairs in TypeScript: object and interface. There are some key differences between these two notations:

- 1. The object type uses the type alias syntax, whereas an interface is defined using a special interface keyword.
- 2. TypeScript allows multiple declarations of interface later merged during interpretation. This can be especially useful when augmenting non-TypeScript modules [28].
- 3. Even though both support object merging, interface can be implemented by classes, ensuring that the class adheres to the structure defined by the interface. object types cannot be directly implemented by a class.
- 4. Merging interface declarations is more performant when merging multiple declarations than an intersection of object types [29].

Typescript syntax 9

TypeScript uses structured typing, which means that TypeScript only validates the shape of the data. Essentially, if the data has the same shape as the type, it is considered to be of that type, as seen in Listing 2.6. This is also known as duck typing, essentially: "If it walks like a duck and quacks like a duck, it is a duck."

#### Listing 2.6 Structured typing

```
type DuckLike = { quack: () => void; type: string };

const Duck: DuckLike = {
  quack: () => console.log("duck!"),
  type: "duck",
};

// This will be still valid
const Goose: DuckLike = {
  quack: () => console.log("goose!"),
  type: "goose",
};
```

Structured typing does have some drawbacks, unlike in nominal type systems, where each type is unique, and the same data cannot be assigned across types, but these can be easily mitigated using literal types to act as brands, as seen in Listing 2.7.

#### Listing 2.7 Nominal typing in TypeScript

```
type DuckLike = { quack: () => void; type: "duck" };

const Duck: DuckLike = {
   quack: () => console.log("duck!"),
   type: "duck",
};

// This will not be valid
const Goose: DuckLike = {
   quack: () => console.log("goose!"),
   type: "goose",
};
```

## 2.3.4 Union and intersection types

Revisiting the notion of types as sets of values, as seen in Listing 2.4, when attempting to assign a value not permitted by the literal type, a type error occurs. In TypeScript, a type is "assignable", if it is either a "member of" the set of permitted values defined by the type (when describing relationships between a value and a type, or it is a "subset of" the sets (when describing relationships between two types).

Sometimes, we need to describe a type, which is a combination of multiple types, combining two sets of values into a single set. This is achievable by using the union operator represented by

the | symbol to describe a type that represents a value, which may be any of one of the combined types referred to as "union members" [30]. Essentially,  $X \mid Y$  can be read as a type for a value that can either be of type X or Y.

Because behind a union type may be a value of any of the union member types, TypeScript will allow only operations which are valid for every union member. If we want to perform an operation which valid for some of the union members, we must perform type narrowing, which refines a broader type to a more specific narrow one, capturing a subset of values of the original broader type.

An example can be seen in Listing 2.8, where the function printUserId can accept both a string or a number as an argument. To invoke toUpperCase(), a method valid only for values of string type, we must perform a check if the parameter is a string. Afterwards, TypeScript has the necessary information to infer that the type of the checked value must be necessary a string and permits the invocation of toUpperCase().

#### Listing 2.8 Union types with simple narrowing

```
function printUserId(id: string | number) {
  if (typeof id === "string") {
    return id.toUpperCase()
  } else {
    return id
  }
}
```

An intersection of types can be represented by the & operator. Similarly to the union type, X & Y can be read as a type for a value that can simultaneously belong to type X and Y. These intersection types are of particular interest when working with object types, as an intersection of two object types has all properties of both object types, as an object with both of the properties can be assigned to both of the intersection member types. For this particular reason, intersection types are commonly used to merge two object types, as seen in 2.9.<sup>3</sup>

#### **Listing 2.9** Intersection types

```
type Intersection = { a: string } & { b: number }
const item: Intersection = { a: "a", b: 1 }
```

## 2.3.5 keyof type and indexed access types

The indexed access type is used to access a specific property type of a record or a tuple type. The syntax of indexed access types mirrors the syntax for accessing an object in JavaScript, as seen in Listing 2.10. We can also use unions as keys to get types of multiple properties of an object type.

The keyof keyword operator can be used to get all possible keys of an object type. This will

 $<sup>^3 \</sup>mathrm{We}$  can also use extends keyword to merge two interfaces

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#### **Listing 2.10** Indexed access types

```
type User = { firstName: string; lastName: string; age: number }

type Age = User["age"]
type Names = User["firstName" | "lastName"]
```

return an union of all keys of the provided data structure type. These are especially useful when working with mapped types later on. An example can be seen in Listing 2.11.

#### **Listing 2.11** Usage of keyof

```
type User = { firstName: string; lastName: string; age: number }
type Keys = keyof User
// ^? "firstName" | "lastName" | "age"
```

TODO: indexed access type

## 2.3.6 Special data types

When working with unions and intersections, we need to be able to describe a type, which can describe a union of all possible types or a type, which is created by intersecting two types with no related properties. We refer to these types as universal supertypes and universal subtypes, respectively. Universal supertypes, also known as top types, are types that are a superset of all other types and are used to represent any possible value. Whereas universal subtypes, also known as bottom types, are types that are a subset of all other types and are often used to describe a type that has no permitted values.

TypeScript includes two top universal supertypes: any and unknown. In the case of any, every type is assignable to type any and type any is assignable to every type [31]. any is acting as an escape hatch to opt out of type checking. This does have unintended consequences, as any is assignable to every type; it can be assigned to a different type without any warnings. This is especially problematic when dealing with external data as the return type of JSON.parse() is any. An example of assignability can be seen at Listing 2.12.

#### Listing 2.12 Assignability of any

```
let data: any = JSON.parse("...")

// All of these are valid TypeScript code
data = null
data = true
data = {}

// Still valid code, opting out of type checking
const a: null = data
const b: boolean = data
const c: object = data
```

unknown acts as a more restrictive version of any. Every type is assignable to type unknown, but unknown is not assignable to any other type, which can be seen at Listing 2.13. To assign unknown to a different type, we must narrow the types using either type guards, type assertions, equality checks or other assertion functions.

#### Listing 2.13 Assignability of unknown

```
let data: unknown = JSON.parse("...")

// All of these are valid TypeScript code
data = null
data = true
data = {}

// Not valid, as unknown is not assignable to any other type
const a: null = data
const b: boolean = data
const c: object = data
```

Finally, never is a bottom type, acting as a subtype of all other types, representing a value that should never occur. In the context of the theory of mathematical logic, never acts as a logical contradiction, describing a value that may never exist. No other type can be assigned to never nor never cannot be assigned to any other type. never can be found when attempting to intersect two types that have no properties in common, such as string & number.

void is a specific type used to signify a function which does not return a value. There is a notable difference between the usage of void when used in context, describing a type for a function with void return type, and when used in the function declaration, as seen in Listing 2.14. The former is used to describe a situation when an implementation of a "void function" does return a value but should be ignored. The latter does enforce that a function should not return a value at all.

#### **Listing 2.14** Return type void

```
type voidFn = () => void

// Valid code
const fn1: voidFn = () => true

function fn2(): void {
    // @ts-expect-error Not valid, as void functions cannot return a value return true
}
```

#### 2.3.7 Enumerations

enum type is a distinct subtype used to describe a set of named constants. Instead of using individual variables for each constant, an enum provides an organised way to express a collection

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of related values. enum is one of the few TypeScript features which introduce an additional code added to the compiler output, and enums refer to real objects at runtime.

An enum type consists of members and their corresponding initialisers for the runtime value of the member. There are two types of enums in TypeScript: numeric enums and string-based enums. In numeric enums, each member is assigned a numeric value, as seen in Listing 2.15. Each member can have an optional initialiser to specify an exact number corresponding to a member. If omitted, the value of the member will be generated by auto-incrementing from previous members.

#### Listing 2.15 Numeric enums

```
enum Direction {
   Up = 1,
   Down,
   Left,
   Right,
}
```

String-based enums are similar in nature, where each member is assigned a string value instead. Each member thus must have an initialiser with a string literal, as seen in Listing 2.16. The key benefit of string-based enums is that they tend to keep their semantic value well when serialising, which is especially helpful when debugging, as the values of numeric enums tend to be opaque.

#### Listing 2.16 String-based enums

```
enum Direction {
   Up = "UP",
   Down = "DOWN",
   Left = "LEFT",
   Right = "RIGHT",
}
```

## 2.3.8 Generic Types

Sometimes we need to write code which needs to work and accept types we don't know in advance. Generic types allow the development of such reusable components that can work over a variety of types rather than a single one. Generic types are created by defining a type parameter that can be used as a placeholder for a specific type. The consumers can then replace the placeholder with their desired types when using the component. In TypeScript, generic types can be defined on interfaces, functions and classes.

To illustrate the point, consider the implementation of the built-in Array type found in the lib.\*.d.ts files (a subset can be seen at Listing 2.17). The Array<T> is a generic type, which accepts a single type argument T and is used to describe the type of the elements in the array. The type argument T is later used both in arguments and return types of the methods of the

Array<T> type: push() accepts only elements of the same type as the array while pop() will return an element of the same type.

#### Listing 2.17 Array type

```
interface Array<T> {
    push(...items: T[]): number;

    pop(): T | undedfined;
}

const strArr: Array<string> = []
const numArr: Array<number> = []

strArr.push("one", "two")
numArr.push(1, 2)

const a = strArr.pop()
// ^? string

const b = numArr.pop()
// ^? number
```

Generic types can be interpreted as functions in a meta-programming language found inside the TypeScript type system itself. The meta-programming language implements some of the key concepts found in the functional programming paradigm.

Generic types are considered first-class citizens in the language, being able to be passed as arguments into other generic types, similar to functions in a functional programming language. Generic types are also pure and cannot have any side effects during type checking. We also use recursion in the meta-programming language to break down complex problems into smaller ones and solve them independently.

There is a notable omission, however: generic types cannot receive other generic types as type arguments [32]. Thus, higher-order functions are not permitted.<sup>4</sup>

## 2.3.9 Type constraints with extends

When writing generic types, sometimes we need to be able to describe some expectations that a type argument must satisfy. For example, we might want to accept types which do have a certain property, such as length as seen in Listing 2.18. To achieve this, we use the extends keyword to describe our constraints to the type.

The generic function will not be able to accept any types anymore, as desired and we must only pass types, which satisfy the constraints instead.

 $<sup>^4</sup>$ There is a way to create such type using HOTS cript, more on that later

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#### **Listing 2.18** Type constraints with extends

```
function getLength<T extends HasLength>(obj: T): number {
   return obj.length
}

const a = getLength("hello")
   const b = getLength([1, 2, 3])
   const c = getLength({ length: 10 })

// @ts-expect-error
// Argument of type '{ foo: string; }' is not
// assignable to parameter of type 'HasLength'.
   const d = getLength({ foo: "bar" })
```

#### 2.3.10 Conditional types

Within the TypeScript meta-language, developers can write conditions and branching logic using conditional types. Conditional types follow a syntax similar to the conditional ternary operators with another case of overloading the extends keyword: Input extends Expect? A: B. This can be read as "If type Input is assignable to type Exepct, then the type resolves to type A, otherwise to type B." An example can be seen in Listing 2.19, where the IsString<T> type will resolve to true if the type argument T is assignable to string and to false otherwise.

#### Listing 2.19 Conditional types

```
type IsString<T> = T extends string ? true : false
```

We can use the infer keyword to deduce or extract a specific type within the scope of conditional types, essentially acting as a way to perform pattern matching. With infer, we introduce a new generic type variable, which can be later used within the true branch of the conditional type, as seen in the implementation of the ReturnType<T> utility type in Listing 2.20. The ReturnType<T> type will resolve to the return type of the type argument T.

#### Listing 2.20 Infer in conditional types

```
type ReturnType<T> = T extends (...args: any) => infer R ? R : never;
```

Since TypeScript version 4.7 [33], we can also add an additional type constraint for the inferred type, which will be checked before the conditional type is resolved. This is useful when we want to avoid an additional nested conditional type, as seen in Listing 2.21, where we want to return the first element of the tuple type only if it is a string.

When given a union type within the conditional type, the conditional type will be resolved for each member type in the union separately, essentially distributing the union type. To prevent such behaviour, we can wrap the type argument in a tuple or any other structure type.

#### Listing 2.21 Type constraints within infer

```
type FirstIfString<T> =
   T extends [infer S extends string, ...unknown[]]
   ? S
   : never;

// is equivalent to
type FirstIfString<T> =
   T extends [infer S, ...unknown[]]
   ? S extends string ? S : never
   : never;
```

#### **Listing 2.22** Distributing union types

```
type ToArray<Type> = Type extends any ? Type[] : never;

// $ExpectType string[] | number[]
type A = ToArray<string | number>

type ToArrayNonDist<Type> = [Type] extends [any] ? Type[] : never;

// $ExpectType (string | number)[]
type B = ToArrayNonDist<string | number>
```

## 2.3.11 Mapped types

Sometimes we need to transform a type into another type. For example, we might want to create a new type, which is a copy of the original type, but with all properties being optional. This can be achieved using mapped types. Mapped types are types which are created using the syntax for index signatures, commonly used in JavaScript for properties not declared ahead of time. An example is shown in Listing 2.23, where the generic type ToBoolean<T> will create a new type which will take all properties from T and change their values to boolean.

We can also specify mapping modifiers to affect the mutability or optionality of a property: readonly and? respectively. Prefixing the modifier with either + or - will either add or remove the modifier to the property.<sup>5</sup> This can be seen in the Optional<T> type in Listing 2.23, which will create a new type, which is a copy of the original type, but with all properties being optional.

#### **Listing 2.23** Mapped types

```
type ToBoolean<T> = {
   [K in keyof T]: boolean
}

type Optional<T> = {
   [K in keyof T]+?: T[K]
}
```

 $<sup>^5+</sup>$  is assumed by default if omitted

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Introduced in TypeScript 4.1 [34], we can also use the as keyword to re-map keys in mapped types. This can allow us to create, transform or filter out keys when creating a new type. An example is shown in Listing 2.24, where the Omit<T, Key> creates a new object type based on type T with omitted properties which are assignable to Key.

#### **Listing 2.24** Using as in mapped types

```
type Omit<T, Key> = {
   [K in keyof T as Exclude<K, Key>]: T[K]
}
```

## 2.3.12 Recursive Types

A recursive data type is a data type that includes a reference to itself within the type definition. Recursive types are useful for modelling complex or hierarchical data structures, such as linked lists or trees.

An example can be seen in Listing 2.25, where the Tree<Value> generic type represents an object with a value of type Value and optional left and right subtrees of the same type.

#### **Listing 2.25** Modeling a binary tree with recursive types

```
type Tree<Value> = {
  value: Value,
  left?: Tree<Value>,
  right?: Tree<Value>
}
```

Using recursive types combined with generic types, we can implement typical recursive algorithms useful for this thesis. One such example can be seen at Listing 2.26, where we implement a FromEntries<Entries> generic type, converting a list of [Key, Value] tuples into a single object type.

First, we define an additional optional generic type parameter <code>Accumulator</code> with an initial type value of . For every tuple in a list, we create an object type containing the current key-value pair with { <code>[K in Key]: Value }</code> and merge it with the accumulator using the <code>&</code> operator. The merged object type is then passed as the accumulator to the next iteration. Finally, when the list is empty, we return the accumulator, which will be the final object type.

There are some limitations regarding recursive types. To prevent infinite recursion, Type-Script limits the instantiation depth to ensure a consistent and performant developer experience. As of writing, the limit is set to 100 levels for type aliases and 5 million type instantiations [35]. Thanks to the tail-recursion elimination optimisation, the limit is set to 1000 levels for tail-optimized recursion types. Thus, it is desired to use tail recursion whenever possible.

Another limitation related to recursive generic types is that the variables declared with infer do not inherit the constraints of the parent type, as seen in Listing 2.27. As the Tail type lost the type constraint of Haystack, we cannot pass the tail as the new haystack of the FilterWrong type. To remedy this issue, we need to add an additional type constraint to the inferred type.

#### **Listing 2.26** Reduce example

```
type FromEntries<Entries, Accumulator = {}> =
   Entries extends [infer Entry, ...infer Rest]
   ? FromEntries<
        Rest,
        Entry extends [infer Key, infer Value]
        ? { [K in Key]: Value } & Accumulator
        : Accumulator
        >
        : Accumulator;
```

#### **Listing 2.27** Recursive types and type constraints

## 2.3.13 Template Literal Types

Finally, template literal types are based on the string literal types, allowing string interpolation and manipulation within the TypeScript type system. For this thesis, we use template literal types to create a parser of mathematical expressions. However, template literal types can be used to create fully typed string-based Domain Specific Languages (DSLs).

Similar to the syntax of JavaScript template literal strings, we use backticks to create a new template literal type. When used with a string literal type, a template literal will create a new string literal type by concatenation [36]. For example, the type 'Hello \${"World"}' will create a new string literal type "Hello World".

Template literal types can be used with primitive types as well, the only limitation being that the primitive type must be stringifiable. That includes all of the primitive types except the symbol type. When created, these types are as a subset of their primitive type and can be used to work as a validation mechanism matching a string of an expected format. For instance, the type 'localhost:\${number}` will create a new string literal type that will match a string of the format localhost:PORT, where PORT is a number.

The distributive nature of union types applies to template literal strings as well: the type will be applied for every member type of the union to the template literal, as seen in the Listing

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2.28, where we create a new Style type with all of the possible combinations of the Variants and Weights types. Generally, it is preferable to avoid combinations of big union types, as it can lead to worse type-checking performance or an error if a union type reaches 1 000 000 member types.

**Listing 2.28** Distributive nature of unions in template literal types

Finally, we can use inference in template literal types to perform pattern matching within string literals with the combination of conditional types and the infer keyword. In Listing 2.29, we create a generic type SplitString, which splits a string literal type into a tuple of substrings with a space as the delimiter. We attempt to perform pattern matching a string with Head, containing the first character, and Rest, including the rest of the split string, as the two inferred types as a result. We also apply type constraints for the inferred types to ensure the types are assignable to string.<sup>6</sup> Both of the inferred types are used to create a new tuple type, with Head being the first element of the tuple and Rest used in a recursive call to split the rest of the string.

**Listing 2.29** Pattern matching with template literal types

```
type SplitString<Input extends string> =
   Input extends `${infer Head extends string} ${infer Rest extends string}`
    ? [Head, ...SplitString<Rest>]
    : [Input];
```

#### 2.4 Prior Art

There are multiple basic implementations of math operations in TypeScript. Tasks regarding basic math operations are even part of the TypeChallenges collection[37]. However, most of them only work on integers, as they work on tuple expansion, which will be further discussed in the implementation part of this thesis.

Nevertheless, multiple libraries in the NPM registry provide basic math calculations within the TypeScript type system, but none provide a fully typed parser of mathematical expressions. Some of the libraries found do provide type utilities that operate on floating-point numbers instead of integers, such as type-fest [38] or typescript-lodash[39]. The most comprehensive implementation of math operations can be found in the ts-arithmetic library [40], which provides a fully typed implementation of division.

<sup>&</sup>lt;sup>6</sup>Albeit unnecessarily, as TypeScript automatically applies the string type constraint in this instance

# **Implementation**

This chapter delves into the implementation of the math expression evaluator using the Type-Script type system. The work being done in this thesis is realised into two major parts: the realisation of mathematical operations and parsing and evaluating string literals with a mathematical expression. The limitations and workarounds for TypeScript literal types are discussed, and by the end of this chapter, readers should gain a deeper understanding of the TypeScript type system when applied to non-trivial problem domains.

## 3.1 Type representation of numbers

As powerful as the type system in TypeScripts, there are certain limitations that need to be addressed when working with literal numerical types. Namely, although TypeScript type syntax includes literal number types, useful for representing specific numeric values, these types do not directly support mathematical operations, such as addition or subtraction. Due to these limitations, other methods of representing numbers are explored in this thesis.

One approach to representing numbers in TypeScript is to use tuples types. As described in 2.3.3, tuple types allow developers to describe a fixed-length JavaScript array where each element can have a specific type. As it represents a JavaScript array, the type includes all of the properties and methods found in an array, including length property, which contains the actual number of elements in the tuple. This feature can be used to represent a number, as the length of the tuple can represent the number itself, as seen in Listing 3.1. The actual type of a member item in a tuple is irrelevant, as the type system only cares about the length of the tuple, but for clarity purposes, the literal type 0 can be used as the element type of a tuple.

However, manually describing a tuple is tedious. Recursion can be employed to parse a literal number type to a tuple type, as seen in 3.2. The ParseNumber<Value> generic type accepts a mandatory type argument Value that should be the length of the final tuple and an optional type argument Acc used to preserve the state of the recursion.

First, a check is performed to see if the length of Acc is equal to the Value by checking the assignability of types. If that is the case, the tuple type found in Acc is returned. Otherwise,

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#### Listing 3.1 Tuple representation of a number

```
type Zero = []
type Four = [0, 0, 0, 0]

// $ExpectType 0
type ZeroValue = Zero['length']

// $ExpectType 4
type ZeroValue = Four['length']
```

the list is extended with a new 0 element being prepended, and the function is called recursively. The function is called recursively until the length of Acc is assignable to Value.

#### Listing 3.2 Parse a literal number type to a tuple type

```
type ParseNumber<
  Value extends number,
  Acc extends Array<0> = []
> = Acc["length"] extends Value ? Acc : ParseNumber<Value, [0, ...Acc]>
```

It is possible to improve the number of recursions to create a tuple by expanding by a whole digit instead of by single increments. As seen in Listing 3.3, where ParsedNumber2 will first perform stringification of the literal number type T and infer the first digit recursively. The accumulator type parameter Rest is first expanded ten times by the ExpandArrayTenTimes generic type, and then the parsed digit is spread into Rest as well. The recursion is performed until the stringified number is empty and the final Rest type is returned.

#### **Listing 3.3** Parse by digit expansion

Even though this method of representing numbers is reasonably simple, it does come at a performance cost, as the tuple must contain the number of elements equal to the number itself. As such, the checking time of the addition and subtraction operations grows as the number grows. This issue alone poses a significant problem, primarily when representing large numbers, as TypeScript has an upper limit on the number of elements in a tuple to avoid performance degradation. As of writing, the limit is set to 10 000 elements[35], which is only enough for

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representing integer numbers no greater than 10000.

Another approach is to represent each digit of a number type into a tuple. This approach does avoid the limitation of the tuple size imposed by TypeScript, as it is now possible to represent much larger numbers whilst reducing the performance overhead as the checking time can be reduced for some operations, which work on individual digits. The number type is parsed into object types beforehand to improve the developer experience when implementing arithmetic operations, keeping the sign, the integer and the fractional parts of a decimal representation number separate. An example can be seen in Listing 3.4, where two object types are created: FloatNumber, representing a number with both integer and fractional digits, and SignFloatNumber, which is used to provide number sign of an existing parsed number.

#### Listing 3.4 Interface representation of numbers

```
type Sign = "+" | "-"
type Digit = 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

type FloatNumber<
    IntDigits extends Digit[] = Digit[],
    FracDigits extends Digit[] = Digit[]
> = {
    int: IntDigits
    frac: FracDigits
}

type SignFloatNumber<
    Sign extends "+" | "-" = "+" | "-",
    Float extends FloatNumber<Digit[], Digit[]> = FloatNumber
> = {
    sign: Sign
    float: Float
}
```

Parsing a number type into digits can be done by recursive types, as seen in Listing 3.5. First, ParseSignFloatNumber attempts to infer the sign of the stringified number literal type into a new TSign type. Afterwards, ParseFloatNumber generic type attempts to split the stringified literal into an integer and a fractional part. Both parts are later parsed separately in ParseNumber, matching if each string contains only digits.

The formatting of the object representation of a number is implemented in a similar fashion, where a digit is concatenated with a string-type accumulator, as seen in a short code snippet in Listing 3.6.

#### 3.2 Addition and Subtraction

When representing the numbers as tuple lengths, some operations, such as addition and subtraction, can be easily implemented by spreading or inference, as seen in Listing 3.7. In the case of the addition operation, a new tuple type is created by spreading the elements of both tuples into

#### **Listing 3.5** Number parsing into objects

```
type ParseNumber<S extends string> =
   S extends `${infer TInt extends Digit}${infer Rest}`
    ? [TInt, ...ParseNumber<Rest>]
    : []

type ParseFloatNumber<S extends NumberLike> =
    `${S}` extends `${infer Int}.${infer Frac}`
    ? FloatNumber<ParseNumber<Int>, ParseNumber<Frac>>
    : FloatNumber<ParseNumber<`${S}`>, []>

type ParseSignFloatNumber<T extends NumberLike> =
    `${T}` extends `${infer TSign extends Sign}${infer Rest}`
    ? SignFloatNumber<TSign, ParseFloatNumber<Rest>>
    : SignFloatNumber<"+", ParseFloatNumber<T>>
```

#### **Listing 3.6** Formatting of object types

```
type JoinDigit<T extends number[]> = T extends [
  infer A extends number,
  ...infer R extends number[]
]
  ? `${A}${JoinDigit<R>}`
  : ""
```

a new tuple, which is then used to obtain the length representing the result.

#### **Listing 3.7** Addition with tuple types

```
type Add<A extends number, B extends number> = [
    ...ParseNumber<A>,
    ...ParseNumber<B>
]['length']
```

The subtraction operation, assuming the first number is larger than the second one, is implemented with the idea that the tuple type of a first number contains all of the elements of the second number with a remainder. As seen in Listing 3.8, the Subtract generic type accepts two type arguments, A and B, which represent the numbers to subtract. A conditional type is used to check if ParseNumber<A> is assignable to a tuple that contains the elements of ParseNumber<B> followed by a remainder of the number[] type, inferred in a new type named Remainder. If true, the length of the Remainder is returned as the result of the subtraction operation. Otherwise, the never type is returned instead.

As described in the previous section, the final implementation of the addition operation based on object representation of numbers is the traditional schoolbook addition with carry. The algorithm adds the numbers digit by digit and keeps track of the carry as it moves from one digit to the next. This technique has a time complexity of  $\Theta(n)$ , where n is the number of digits in the number being added.

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**Listing 3.8** Subtraction with tuple types

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```
type Subtract<
  A extends string | number,
  B extends string | number
> = ParseNumber<A> extends [
    ...infer Remainder extends number[],
    ...ParseNumber<B>
]
  ? Remainder["length"]
  : never
```

The core building block of the schoolbook addition and subtraction algorithm is the ability to obtain the next digit alongside the carry or borrow flag when performing the operation on single decimal digits. This can be purely done in the type system alone using tuple expansion and checking for the stringified length of the tuple, as seen in 3.9, but to improve the performance and avoid unnecessary type instantiations, a lookup table is used to obtain the next digit and the carry flag instead. The subtraction operation is implemented similarly, where a two-dimensional lookup table of tuples is used to obtain the next digit and the borrow flag.

The lookup table is created by iterating over all possible combinations of two digits and storing the result of the addition and the carry flag in a two-dimensional map. To improve the performance even further, the lookup tables of both the addition and subtraction operations are generated as a built step in JavaScript and stored in a separate file, which is later imported into the type system.

#### Listing 3.9 Lookup table for addition operation

```
type AddDigitsResult<A extends Digit, B extends Digit> =
    [...ParseNumber<A>, ...ParseNumber<B>]["length"] extends
    infer Length extends number
    ? `${Length}` extends `${Digit}${infer Value extends Digit}`
        ? [Value, true]
        : `${Length}` extends `${infer Value extends Digit}`
            ? [Value, false]
            : never
            : never

// This is generated by a build step
type AddMapCarry = {
    [A in Digit]: {
        [B in Digit]: AddDigitsResult<A, B>
        }
    }
}
```

The schoolbook addition algorithm, seen in Listing 3.13, is implemented as three generic types. AddWithCarry accepts two digits named Left and Right and a carry flag as type arguments and is responsible for adding the two digits and propagating the carry flag to the next digit. It will first check if the Carry type is assignable to true, and if it is assignable, it will increment the

Left digit. The AddMapCarry is used to obtain the result, and the Or generic type implements the binary disjunction operation to determine the carry flag in case of multiple additions due to Carry being true.

AddArr is responsible for adding two tuples of digits. AddArr will attempt to extract the rightmost digit from both tuples and add them using AddWithCarry. The AddArr will be called recursively with the remaining digits and the carry flag from the previous addition until both of the tuples are empty. Note that both of the digit tuples must have the same length to prevent premature bailouts.

Finally, AddInt will add two digit tuples by first padding them into tuples of the same length by prefixing them with zeroes and then calling AddArr to perform addition itself. If Carry is assignable to true, an extra 1 digit is prepended to the result.

These foundational blocks can be further chained to add support for fractional numbers and signed numbers. As seen in Listing 3.13, AddFloatNumber will first extract the integer and fractional parts of a number, performing integer addition on both parts separately. The carry flag is propagated appropriately from the fractional part to the integer part by recursively calling AddFloatNumber to increment the result.

When working with subtraction, underflows are resolved by implementing digit comparison. Similarly to addition and subtraction, the comparison operation is performed per digit, utilising an additional two-dimensional lookup table with all possible digit comparison results represented as a number from the following set:  $\{-1,0,1\}$ . Based on the comparison result, the operation can be decided by using a map object type with the comparison result as the key and the operation as the value, seen in Listing 3.11.

Finally, to simplify dealing with signed operations, an object type with all possible sign pairs can be used to determine whether to invoke addition or subtraction, as seen in Listing 3.12.

Addition and Subtraction

#### **Listing 3.10** Floating point addition

```
type AddFloatNumber<</pre>
A extends FloatNumber,
B extends FloatNumber
> = PadFloat<A, B> extends [
  FloatNumber<infer IntA, infer FracA>,
  FloatNumber<infer IntB, infer FracB>
? AddArr<FracA, FracB> extends [
    infer FracResult extends Digit[],
    infer FracCarry extends boolean
  ? AddArr<IntA, IntB> extends [
      infer IntResult extends Digit[],
      infer IntCarry extends boolean
    ? IntCarry extends true
      ? FracCarry extends true
        ? AddFloatNumber<
            FloatNumber<[1, ...IntResult], FracResult>,
            FloatNumber<[1], []>
        : FloatNumber<[1, ...IntResult], FracResult>
      : FracCarry extends true
      ? AddFloatNumber<
          FloatNumber<IntResult, FracResult>,
          FloatNumber<[1], []>
      : FloatNumber<IntResult, FracResult>
    : never
  : never
: never
```

#### **Listing 3.11** Subtraction switching

```
type SubOperatorSwitch<A extends FloatNumber, B extends FloatNumber> = {
   [-1]: SignFloatNumber<"-", SubFloatNumber<B, A>>
   [0]: SignFloatNumber<"+", FloatNumber<[0], []>>
   [1]: SignFloatNumber<"+", SubFloatNumber<A, B>>
}[CompareAbsNumbers<A, B>]
```

#### ■ Listing 3.12 Signed number addition and subtraction

```
type AddSignFloatNumber<
    A extends SignFloatNumber,
    B extends SignFloatNumber
> = {
    "+": {
        "+": SignFloatNumber<"+", AddFloatNumber<A["float"], B["float"]>>
        "-": SubOperatorSwitch<A["float"], B["float"]>
    }
    "-": {
        "+": SubOperatorSwitch<B["float"], A["float"]>
        "-": SignFloatNumber<"-", AddFloatNumber<A["float"], B["float"]>>
    }
}[A["sign"]][B["sign"]]
```

Addition and Subtraction

#### Listing 3.13 Addition algorithm

```
type AddWithCarry<</pre>
  Left extends number,
  Right extends number,
  Carry extends boolean
  > = Carry extends true
  ? AddMapCarry[Left][1] extends [
      infer LeftTmp extends number,
      infer LeftCarry extends boolean
    ? AddWithCarry<LeftTmp, Right, false> extends [
        infer Result extends number,
        infer RightCarry extends boolean
      ? [Result, Or<LeftCarry, RightCarry>]
      : never
    : never
  : AddMapCarry[Left][Right]
type AddArr<</pre>
  A extends number[],
  B extends number[],
 Tmp extends [number[], boolean] = [[], false]
> = [A, B, Tmp] extends [
  [...infer ARest extends number[], infer ARight extends number],
  [...infer BRest extends number[], infer BRight extends number],
  [infer Result extends number[], infer Carry extends boolean]
]
  ? AddWithCarry<ARight, BRight, Carry> extends [
      infer Digit extends number,
      infer Carry extends boolean
    ? AddArr<ARest, BRest, [[Digit, ...Result], Carry]>
    : never
  : Tmp
export type AddInt<A extends Digit[], B extends Digit[]> = PadStartEqually
> extends [infer PA extends Digit[], infer PB extends Digit[]]
  ? AddArr<PA, PB> extends [
      infer Rest extends Digit[],
      infer Carry extends boolean
    ? Carry extends true
      ? [1, ...Rest]
      : Rest
    : never
  : never
```

#### 3.3 Multiplication

A naive implementation of the multiplication algorithm can be created by repeatably adding the multiplicand when numbers are represented by tuple length, as seen in Listing 3.14. Multiply generic type has two mandatory type parameters: A and B representing the multiplicand and multiplier respectively. The optional type parameter Left is used to track how many iterations are left before the recursion terminates. This method is considered ineffective, as the number of recursion calls is proportional to the size of the multiplicand, and the method can easily reach the instantiation depth limit with large multiplicands.

#### Listing 3.14 Naive multiplication algorithm

```
type Multiply<
  A extends number,
  B extends number,
  Left extends number = B
> = Left extends 0 ? 0 : Multiply<Add<A, B>, B, Subtract<B>>
```

Because of this reason, the library implements the long multiplication method instead. Similarly to the addition and subtraction algorithm, a two-dimensional lookup object type is used to obtain the resulting multiplication digit and the appropriate carry number. First, MultiplyInt will iterate on multiplier digits from right to left and multiply each digit with the multiplicand by invoking the MultiplySingleInt generic type. The result of each multiplication, appropriately offset with zeroes to account for the position of the digit in the multiplier, is then added together to obtain the final result. An example can be seen in Listing 3.15.

#### **Listing 3.15** Long multiplication

With the core building block for integer multiplication, extending the algorithm to floating-point numbers and signed numbers is straightforward.

The MultiplyFloat generic type, as seen in Listing 3.16, converts the floating point number to an integer by concatenating the integer part of a number with the fractional part, preserving the precision, number of digits in the fractional part, as the length of a tuple. The precision

Division 31

is encoded as a tuple because the precision of the multiplication is the sum of the multiplicand and multiplier precisions. This can be done by spreading the tuples representing the precisions instead of calling expensive per-digit addition recursive types.

#### **Listing 3.16** Float multiplication

The result of the integer multiplication is then converted back to a floating-point number by shifting the integer part right, as seen in Listing 3.17. This is done by iteratively taking the elements from the tuple representing the precision, acting as a counter, and prepending the rightmost digit of the integer part to the fractional part. The recursion terminates when the precision tuple is empty.

#### Listing 3.17 Conversion of an integer number back to a fractional number

```
type Compress<
   Count extends Array<0>,
   Left extends Digit[],
   Right extends Digit[] = []
> = Count extends [0, ...infer RestCount extends 0[]]
   ? Left extends [...infer LeftRest extends Digit[], infer End extends Digit]
        ? Compress<RestCount, LeftRest, [End, ...Right]>
        : Compress<RestCount, Left, [0, ...Right]>
        : [Left, Right]
```

#### 3.4 Division

- Eucledian division for each digit
- Long division
- Bypass infinite recursion checks by creating a new type instance via infer

#### 3.5 Other operations

- **Exponentiation** Exponentiation by squaring (Complexity  $O(n^2) \log(n)$ )
- Comparison operators Lookup table, compare by digit
- Round, Floor, Ceil, Truncate use object representations
- Root Newton's method

#### 3.6 Statement parser & evaluator

- Architecture of parser: lexer, parser, evaluator
- Decision why we are not evaluating directly in the parser reduce the number of type instantiations
- Mention alternative algorithms (Shunting-yard algorithm, Pratt parser) and the decision why
  parser is a better solution create a more generic parser implementation which is easier to
  extend
- Description of the math grammar, how we ensure operator precedence and left/right-associativity
- Mention creating a custom code generator for detecting valid strings of a LL(1) grammar
- Namespaces and default types instead of enums
- Behavior of never type and the need to create a custom error type (duck typing)

#### 3.7 Higher kinded types

- TypeScript does not support Higher Kinded Types (essentially passing a generic type as a type parameter of an another generic type)
- There is a workaround to simulate HKTs using an intersection of interfaces and inheritance
- Adapter for HOTScript

## Testing and release management

#### 4.1 Developer experience

By using tsserver, we can see and verify the types representing a symbol during development, by hovering on top of a symbol. This does provide some useful feedback during development but does require significant context switching with the mouse pointer, especially when switching back and forth from implementation to testing. There are various plugins for editors, that are able to display the inferred types in a different manner. One such key plugin used thoroughly during development is vscode-twoslash-plugins [41], which allows inserting a // ^? comment to display the inferred type of an expression right in the editor.

TODO: Add a screenshot of the vscode-twoslash-plugins in action

- Testing with eslint
- \$ExpectType and twoslash operator
- Testing with vitest and ExpectType

### 4.2 Testing with eslint

#### TODO: Describe \$ExpectType

To remedy the issue, we are using eslint together with @typescript-eslint/parser as the source code parser and eslint-plugin-expect-type plugin to create unit tests for each of the math methods.

- Developer experience
- Unit tests, integration tests (eslint, eslint-plugin-expect-type)
- Github Actions
- Changesets automatic release management

■ Comparison between existing TS math libraries

### Chapter 5

## Conclusion

- 5.1 Advantages and disadvantes of TS
- 5.2 Future work

36 Conclusion

## Appendix A

# Nějaká příloha

Sem přijde to, co nepatří do hlavní části.

38 Nějaká příloha

- JSWORLD CONFERENCE (director). Fred K. Schott Type-safety Is Eating the World [online]. 2023. [visited on 2023-03-25]. Available from: https://www.youtube.com/watch?v= DqYxbjTM2vw.
- 2. The State of JS 2022: Usage [online]. [visited on 2023-03-25]. Available from: https://2022.stateofjs.com/en-US/usage/.
- 3. Prisma/Prisma: Next-generation ORM for Node.Js & TypeScript PostgreSQL, MySQL, MariaDB, SQL Server, SQLite, MongoDB and CockroachDB [online]. [visited on 2023-03-25]. Available from: https://github.com/prisma.
- 4. MCDONNELL, Colin. Zod [online]. 2023. [visited on 2023-03-25]. Available from: https://github.com/colinhacks/zod.
- 5. tRPC [online]. tRPC, 2023. [visited on 2023-03-25]. Available from: https://github.com/trpc/trpc.
- 6. Stack Overflow Developer Survey 2022 [online]. Stack Overflow. [visited on 2023-01-29]. Available from: https://survey.stackoverflow.co/2022/?utm\_source=social-share&utm\_medium=social&utm\_campaign=dev-survey-2022.
- 7. FARD, Amin Milani; MESBAH, Ali. JSNOSE: Detecting JavaScript Code Smells. 2013 IEEE 13th International Working Conference on Source Code Analysis and Manipulation (SCAM) [online]. 2013, pp. 116–125 [visited on 2023-03-25]. ISBN 9781467357395. Available from DOI: 10.1109/SCAM.2013.6648192.
- 8. ECMAScript Proposal: Type Annotations [online]. Ecma TC39, 2023. [visited on 2023-01-29]. Available from: https://github.com/tc39/proposal-type-annotations.
- 9. Elm Delightful Language for Reliable Web Applications [online]. [visited on 2023-01-31]. Available from: https://elm-lang.org/.
- 10. The Elm Architecture · An Introduction to Elm [online]. [visited on 2023-01-31]. Available from: https://guide.elm-lang.org/architecture/.
- 11.  $Prior\ Art\ -\ Redux\ [online]$ . 2022-02-07. [visited on 2023-01-31]. Available from: https://redux.js.org/understanding/history-and-design/prior-art.

12. BuckleScript & Reason Rebranding [online]. ReScript Blog. [visited on 2023-01-29]. Available from: https://rescript-lang.org/blog/bucklescript-is-rebranding.

- 13. Efficient and Insightful Generalization [online]. [visited on 2023-02-12]. Available from: https://okmij.org/ftp/ML/generalization.html.
- 14.  $\it History ReScript$  [online]. 2022-02-12. [visited on 2023-02-12]. Available from: https://github.com/rescript-lang/rescript-compiler/blob/master/CREDITS.md.
- 15. Reconstructing TypeScript, Part 0: Intro and Background [online]. [visited on 2023-01-24]. Available from: https://jaked.org/blog/2021-09-07-Reconstructing-TypeScript-part-0.
- CHAUDHURI, Avik; VEKRIS, Panagiotis; GOLDMAN, Sam; ROCH, Marshall; LEVI, Gabriel. Fast and Precise Type Checking for JavaScript. Proceedings of the ACM on Programming Languages [online]. 2017, vol. 1, 48:1–48:30 [visited on 2023-01-29]. Available from DOI: 10.1145/3133872.
- 17. Flow [online]. Meta, 2023. [visited on 2023-01-29]. Available from: https://github.com/facebook/flow.
- 18. TypeScript Design Goals [online]. GitHub. [visited on 2023-01-29]. Available from: https://github.com/microsoft/TypeScript/wiki/TypeScript-Design-Goals.
- 19. TypeScript: JavaScript With Syntax For Types [online]. [visited on 2023-02-01]. Available from: https://www.typescriptlang.org/.
- 20. Documentation TypeScript for JavaScript Programmers [online]. [visited on 2023-01-14]. Available from: https://www.typescriptlang.org/docs/handbook/typescript-in-5-minutes.html.
- 21. Babel/Babel [online]. Babel, 2023. [visited on 2023-02-01]. Available from: https://github.com/babel/babel.
- 22. Esbuild An Extremely Fast Bundler for the Web [online]. [visited on 2023-02-01]. Available from: https://esbuild.github.io/.
- 23. SWC Rust-based Platform for the Web [online]. [visited on 2023-02-01]. Available from: https://swc.rs/.
- 24. Visual Studio Code Code Editing. Redefined [online]. [visited on 2023-02-01]. Available from: https://code.visualstudio.com/.
- 25. Octoverse 2022: The State of Open Source [online]. The State of the Octoverse. [visited on 2023-01-29]. Available from: https://octoverse.github.com/.
- 26. Standalone Server (Tsserver) [online]. GitHub. [visited on 2023-03-27]. Available from: https://github.com/microsoft/TypeScript/wiki/Standalone-Server-(tsserver).
- VANDERKAM, Dan. Effective TypeScript: 62 Specific Ways to Improve Your TypeScript.
   First edition. Beijing [China]; Sebastopol, CA: O'Reilly Media, 2019. ISBN 978-1-4920-5374-3.

28. Documentation - Declaration Merging [online]. [visited on 2023-04-10]. Available from: https://www.typescriptlang.org/docs/handbook/declaration-merging.html#module-augmentation.

- 29. *Performance* [online]. GitHub. [visited on 2023-04-02]. Available from: https://github.com/microsoft/TypeScript/wiki/Performance.
- 30. Documentation Everyday Types [online]. [visited on 2023-03-27]. Available from: https://www.typescriptlang.org/docs/handbook/2/everyday-types.html.
- 31. The Top Types 'any' and 'unknown' in TypeScript [online]. [visited on 2023-03-26]. Available from: https://2ality.com/2020/06/any-unknown-typescript.html.
- 32. Type Inference for Higher-Order, Generic Curried Function Breaks down When the Function Is Applied to Another Generic Function · Issue #49312 · Microsoft/TypeScript [online]. GitHub. [visited on 2023-03-28]. Available from: https://github.com/microsoft/TypeScript/issues/49312.
- 33. ROSENWASSER, Daniel. *Announcing TypeScript 4.7* [online]. TypeScript, 2022-05-24. [visited on 2023-03-29]. Available from: https://devblogs.microsoft.com/typescript/announcing-typescript-4-7/.
- 34. ROSENWASSER, Daniel. *Announcing TypeScript 4.1* [online]. TypeScript, 2020-11-19. [visited on 2023-03-29]. Available from: https://devblogs.microsoft.com/typescript/announcing-typescript-4-1/.
- 35. Implementation of Checker.Ts [online]. Microsoft, 2023. [visited on 2023-03-31]. Available from: https://github.com/microsoft/TypeScript/blob/55867271933d603f6c29b8eb7399960a71e96ccc/src/compiler/checker.ts.
- 36. Documentation Template Literal Types [online]. [visited on 2023-04-02]. Available from: https://www.typescriptlang.org/docs/handbook/2/template-literal-types.html.
- 37. Type-Challenges/Type-Challenges [online]. Type Challenges, 2023. [visited on 2023-04-02]. Available from: https://github.com/type-challenges/type-challenges.
- 38. SORHUS, Sindre. *Sindresorhus/Type-Fest* [online]. 2023. [visited on 2023-04-02]. Available from: https://github.com/sindresorhus/type-fest.
- 39. KAWAYILINLIN. kawayiLinLin/Typescript-Lodash [online]. 2023. [visited on 2023-01-15]. Available from: https://github.com/kawayiLinLin/typescript-lodash.
- 40. ARIEL. *Type Level Arithmetic* [online]. 2023. [visited on 2023-01-15]. Available from: https://github.com/arielhs/ts-arithmetic.
- 41. THEROX, Orta. *Vscode-Twoslash-Queries* [online]. 2023. [visited on 2023-03-26]. Available from: https://github.com/orta/vscode-twoslash-queries.

## Obsah přiloženého média

ı	readme.txt	stručný popis obsahu média
	exe	adresář se spustitelnou formou implementace
	_ src	
	impl	zdrojové kódy implementace
	thesis	zdrojové kódy implementace zdrojová forma práce ve formátu L <sup>A</sup> T <sub>E</sub> X
	text	text práce
	thesis.pd	ftext práce ve formátu PDF