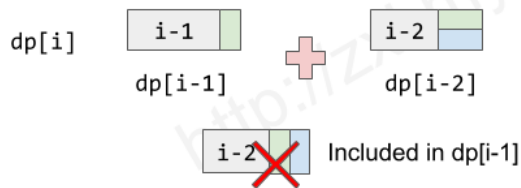
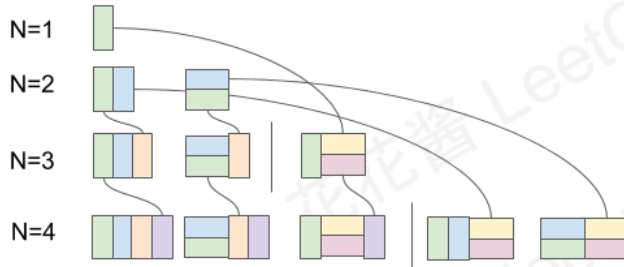


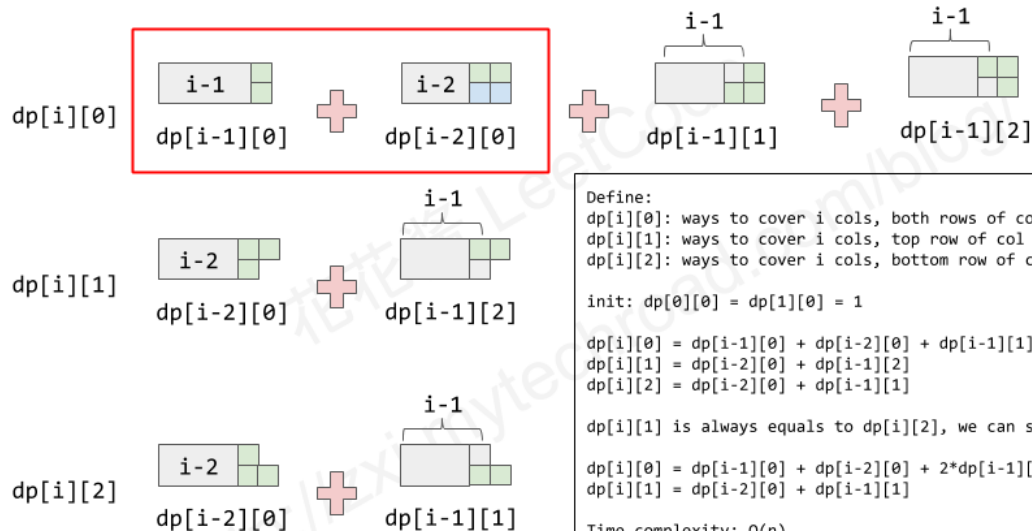
A simpler problem:

How many ways that we can cover a  $N \times 2$  board using one type of domino ( $1 \times 2$ ).



Define:  $dp[i]$ : ways to cover  $i$  cols  
 init:  $dp[0] = dp[1] = 1$   
 $dp[i] = dp[i-1] + dp[i-2]$  Fibonacci sequence!  
 ans:  $dp[n]$   
 Time complexity:  $O(n)$   
 Space complexity:  $O(n) \rightarrow O(1)$

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Define:  
 $dp[i][0]$ : ways to cover  $i$  cols, both rows of col  $i$  are covered  
 $dp[i][1]$ : ways to cover  $i$  cols, top row of col  $i$  is covered  
 $dp[i][2]$ : ways to cover  $i$  cols, bottom row of col  $i$  is covered  
 init:  $dp[0][0] = dp[1][0] = 1$   
 $dp[i][0] = dp[i-1][0] + dp[i-2][0] + dp[i-1][1] + dp[i-1][2]$   
 $dp[i][1] = dp[i-2][0] + dp[i-1][2]$   
 $dp[i][2] = dp[i-2][0] + dp[i-1][1]$   
 $dp[i][1]$  is always equals to  $dp[i][2]$ , we can simplify  
 $dp[i][0] = dp[i-1][0] + dp[i-2][0] + 2 * dp[i-1][1]$   
 $dp[i][1] = dp[i-2][0] + dp[i-1][1]$   
 Time complexity:  $O(n)$   
 Space complexity:  $O(n) \rightarrow O(1)$

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