

**ARISTOTLE UNIVERSITY OF THESSALONIKI**  
**FACULTY OF SCIENCES**  
**SCHOOL OF INFORMATICS**



**Title...**

*A dissertation submitted to the School of Informatics of the Aristotle University of Thessaloniki  
in fulfillment of the requirements for the degree of doctor of philosophy  
by*

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Thessaloniki, 202x



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## ΠΕΡΙΛΗΨΗ

Σκοπός της παρούσας πτυχιακής εργασίας είναι η παρουσίαση και υλοποίηση του αλγορίθμου του Gauss Elimination modulo 2 ...

Λέξεις Κλειδιά. Γραμμική άλγεβρα, Γραμμικά Συστήματα, ..., CUDA, C

## ABSTRACT

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**Key Words.** Linear Algebra, Linear Systems, ..., CUDA, C

## Acknowledgements

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## Abreviations

AES	:	Advanced Encryption Standard
AKS	:	Agrawal - Kayal - Saxena
CBC	:	Cipher Block Chaining
CCA	:	Chosen Ciphertext Attack
CPA	:	Chosen Plaintext Attack
CRC	:	Cyclic Redundancy Check

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# CHAPTER 1

## INTRODUCTION

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### 1.1 a

...

#### 1.1.1 b

...

# CHAPTER 2

## GAUSS REDUCTION

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### 2.1 Linear Systems

$$\begin{cases} x_1 = 2r + s - t \\ x_2 = r \\ x_3 = -2s + 2t \\ x_4 = s \\ x_5 = t \end{cases}$$

$$\begin{cases} a_{11}x_1 + \cdots + a_{1n}x_n = b_1 \\ \vdots \\ a_{k1}x_1 + \cdots + a_{kn}x_n = b_k \\ \vdots \\ a_{n1}x_1 + \cdots + a_{nn}x_n = b_n \end{cases}$$

$$A_{m,n} = \begin{pmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m,1} & a_{m,2} & \cdots & a_{m,n} \end{pmatrix}$$

### 2.2 Linear Systems II

# CHAPTER 3

## GAUSS REDUCTION - SINGLE CORE CASE

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### 3.1 Algorithms in L<sub>A</sub>T<sub>E</sub>X

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**Algorithm 3.1.0.1 :** *Multiplication of Karatsuba*

**input.**  $a, b$  integers

**output.**  $a \cdot b$

```

1 def karatsuba(a, b)
2   if  $a < 100$  or  $b < 100$  then
3     | return  $a \cdot b$ 
4   end
5    $m = \max(\log_{10}(a), \log_{10}(b))$ 
6    $m_2 = \text{floor}(m/2)$ 
7    $high(a) =$  take the first  $m_2$  decimal digits of  $a$ 
8    $low(a) =$  take the last  $m_2$  decimal digits of  $a$ 
9    $high(b) =$  take the first  $m_2$  decimal digits of  $b$ 
10  ...
11  ...
12  print  $(z_2 \cdot 10^{2m_2} + (z_1 - z_2 - z_0) \cdot 10^{m_2} + z_0$ 
```

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**Algorithm 3.1.0.2 : Enumeration algorithm**

Είσοδος. An ordered basis  $\mathcal{B} = \{\mathbf{b}_1, \dots, \mathbf{b}_n\} \subset \mathbb{Z}^m$  of the lattice  $\mathcal{L}(\mathcal{B})$  and a positive real number  $R$ .

Έξοδος. All the vectors  $\mathbf{x} \in \mu \epsilon \|\mathbf{x}\| \leq R$ .

01. Compute  $\{\mu_{ij}\}$  and  $B_i = \|\mathbf{b}_i^*\|^2$
02.  $\mathbf{x} = (x_i) \leftarrow \mathbf{0}_n, \mathbf{c} = (c_i) \leftarrow \mathbf{0}_n, \mathbf{e} = (e_i) \leftarrow \mathbf{0}_n, sumli \leftarrow 0, S = \emptyset, i \leftarrow 1$
03. **While**  $i \leq n$
04.      $c_i \leftarrow -\sum_{j=i+1}^n x_j \mu_{ji}$
05.     ...
  
19. **return**  $S$

# CHAPTER 4

## SOMETHING

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# Appendix

**A title-1**

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**B title-2**

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