

ARISTOTLE UNIVERSITY OF THESSALONIKI
FACULTY OF SCIENCES
SCHOOL OF INFORMATICS



Title...

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by*

Name

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Αριστοτέλειο Πανεπιστήμιο Θεσσαλονίκης
Σχολή Θετικών Επιστημών
Τμήμα Πληροφορικής

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This PhD dissertation was examined and approved by the following committee:

Members of the committee

aaa bbb (Supervisor) Professor, ... , Aristotle University of Thessaloniki.

aaa bbb Professor, ... , Aristotle University of Thessaloniki.

aaa bbb Professor, ... , Aristotle University of Thessaloniki.

aaa bbb Professor, ... , Aristotle University of Thessaloniki.

aaa bbb Professor, ... , Aristotle University of Thessaloniki.

aaa bbb Professor, ... , Aristotle University of Thessaloniki.

aaa bbb Professor, ... , Aristotle University of Thessaloniki.

ΠΕΡΙΛΗΨΗ

Σκοπός της παρούσας πτυχιακής εργασίας είναι η παρουσίαση και υλοποίηση του αλγορίθμου του Gauss Elimination modulo 2 ...

Λέξεις Κλειδιά. Γραμμική άλγεβρα, Γραμμικά Συστήματα, ..., CUDA, C

ABSTRACT

....

Key Words. Linear Algebra, Linear Systems, ..., CUDA, C

Acknowledgements

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Abbreviations

AES	:	Advanced Encryption Standard
AKS	:	Agrawal - Kayal - Saxena
CBC	:	Cipher Block Chaining
CCA	:	Chosen Ciphertext Attack
CPA	:	Chosen Plaintext Attack
CRC	:	Cyclic Redundancy Check

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CHAPTER 1

INTRODUCTION

.....

1.1 a

...

1.1.1 b

...

CHAPTER 2

GAUSS REDUCTION

2.1 Linear Systems

$$\begin{cases} x_1 = 2r + s - t \\ x_2 = r \\ x_3 = -2s + 2t \\ x_4 = s \\ x_5 = t \end{cases}$$

$$\begin{cases} a_{11}x_1 + \cdots + a_{1n}x_n = b_1 \\ \vdots \\ a_{k1}x_1 + \cdots + a_{kn}x_n = b_k \\ \vdots \\ a_{n1}x_1 + \cdots + a_{nn}x_n = b_n \end{cases}$$

$$A_{m,n} = \begin{pmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m,1} & a_{m,2} & \cdots & a_{m,n} \end{pmatrix}$$

2.2 Linear Systems II

CHAPTER 3

GAUSS REDUCTION - SINGLE CORE CASE

.....

3.1 Algorithms in L^AT_EX

Alogrithm 3.1.0.1 : *Multiplication of Karatsuba*

input. a, b integers

output. $a \cdot b$

```

1 def karatsuba(a, b)
2   if  $a < 100$  or  $b < 100$  then
3     | return  $a \cdot b$ 
4   end
5    $m = \max(\log_{10}(a), \log_{10}(b))$ 
6    $m_2 = \text{floor}(m/2)$ 
7    $high(a)$  = take the first  $m_2$  decimal digits of  $a$ 
8    $low(a)$  = take the last  $m_2$  decimal digits of  $a$ 
9    $high(b)$  = take the first  $m_2$  decimal digits of  $b$ 
10  ...
11  print  $(z_2 \cdot 10^{2m_2} + (z_1 - z_2 - z_0) \cdot 10^{m_2} + z_0)$ 
```

Alogrithm 3.1.0.2 : *Enumeration algorithm*

Εἰσόδος. An ordered basis $\mathcal{B} = \{\mathbf{b}_1, \dots, \mathbf{b}_n\} \subset \mathbb{Z}^m$ of the lattice $\mathcal{L}(\mathcal{B})$ and a positive real number R .

Ἐξόδος. All the vectors $\mathbf{x} \in \mu \in \|\mathbf{x}\| \leq R$.

```

01. Compute  $\{\mu_{ij}\}$  and  $B_i = \|\mathbf{b}_i^*\|^2$ 
02.  $\mathbf{x} = (x_i) \leftarrow \mathbf{0}_n, \mathbf{c} = (c_i) \leftarrow \mathbf{0}_n, \mathbf{e} = (\epsilon_i) \leftarrow \mathbf{0}_n, \text{sum}i \leftarrow 0, S = \emptyset, i \leftarrow 1$ 
03. While  $i \leq n$ 
04.    $c_i \leftarrow -\sum_{j=i+1}^n x_j \mu_{ji}$ 
05. ...

19. return S

```

CHAPTER 4

SOMETHING

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Appendix

A title-1

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B title-2

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