

```
function s = machin0(m)
%MACHIN Calculate decimals of pi with Machin's formula
%   MACHIN(M) gives a string with pi truncated to M decimals
%   using Machin's formula:  $\pi = 16*\text{acot}(5) - 4*\text{acot}(239)$ 

%   Author: Jonas Lundgren <splinefit@gmail.com> 2008

if nargin < 1, m = 50; end
base = 1e15;
n = ceil(m/15) + 1;

% Machin's formula
x = xacot(5,16,n,base) - xacot(239,4,n,base);

% Canonical form
carry = 0;
for k = n+1:-1:1
    xk = x(k) + carry;
    carry = floor(xk/base);
    x(k) = xk - carry*base;
end

% Write string
s = sprintf('%15.0f',x(2:n));
s(isspace(s)) = '0';
s = ['3.', s(1:m)];

%-----
function y = xacot(a,c,n,base)
% Calculate C*ACOT(A) to N digits in base BASE

b = a*a;
m = floor(n*log(base)/log(b));
```

```
x = [c; zeros(n,1)];           % x = c
y = 0;                         % y = 0
for k = m:-1:0
    y = xdiv(x,2*k+1,base) - xdiv(y,b,base);   % y = c/✓
(2*k+1) - y/b
end
y = xdiv(y,a,base);           % y = y/a
```

```
%-----
```

```
function x = xdiv(x,a,base)
% Calculate X/A to N digits in base BASE
```

```
r = 0;
t = floor(base/a);
u = base - a*t;
for k = 1:numel(x)
    v = x(k) + r*u;
    q = floor(v/a);
    x(k) = q + r*t;
    r = v - a*q;
end
```