

String matching

Data Structures and Algorithms for Computational Linguistics III
(ISCL-BA-07)

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Finding patterns in a string

- Finding a pattern in a larger text is a common problem in many applications
- Typical example is searching in a text editor or word processor
- There are many more:
 - DNA sequencing / bioinformatics
 - Plagiarism detection
 - Search engines / information retrieval
 - Spell checking
 - ...

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Introduction, motivation Brute force Rabin-Karp FPM KMP Edit-Distance

Types of problems

- The efficiency and usability of algorithms depend on some properties of the problem
- Typical applications are based on finding multiple occurrences of a single pattern in a text, where the pattern is much shorter than the text
- The efficiency of the algorithms may depend on the
 - relative size of the pattern
 - expected number of repetitions
 - size of the alphabet
 - whether the pattern is used once or many times
- Another related problem is searching for multiple patterns at once
- In some cases, fuzzy / approximate search may be required
- In some applications, preprocessing (indexing) the text to be searched may be beneficial

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Problem definition

and some terminology

text: A A T A G A C G G C T A G C A A

pattern: A G C A C

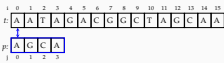
- We want to find all occurrences of pattern p (length m) in text t (length n)
- The characters in both t and p are from an alphabet Σ , in the example $\Sigma = \{A, C, G, T\}$
- The size of the alphabet (q) is often an important factor
- p occurs in t with shift s if $p[0 : m] = t[s : s + m]$, we have a match at $s = 3$ in the example
- A string x is a prefix of string y , if $y = xw$ for a possibly empty string w
- A string x is a suffix of string y , if $y = wx$ for a possibly empty string w

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Brute-force string search



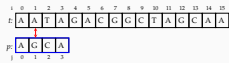
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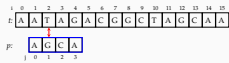
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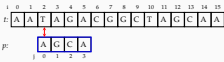
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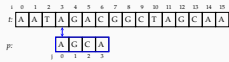
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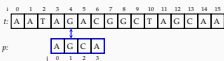
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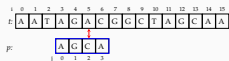
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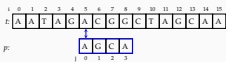


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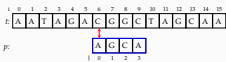
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Brute-force string search



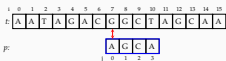
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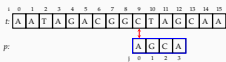
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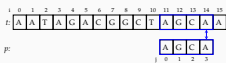
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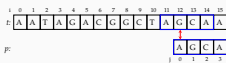
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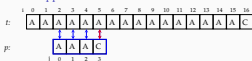
Brute-force approach: worst case



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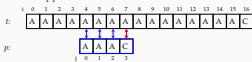
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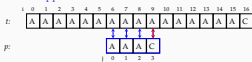
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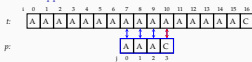
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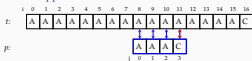
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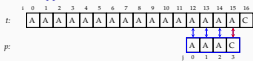
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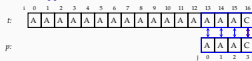
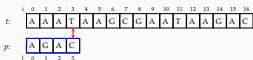
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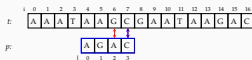
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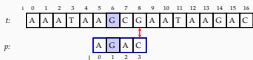
Brute-force approach: worst case

Boyer-Moore algorithm
slightly simplified version

- The main idea is to start comparing from the end of p
- If $t[i]$ does not occur in p, shift m steps
- Otherwise, align the last occurrence of $t[i]$ in p with $t[i]$

Boyer-Moore algorithm
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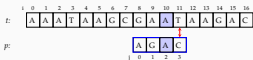
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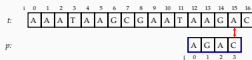
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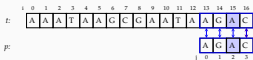
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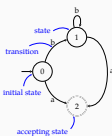
Boyer-Moore algorithm
implementation and analysis

- On average, the algorithm performs better than brute-force
- In worst case the complexity of the algorithm is $O(nm)$, example:
 $t = \text{aaa} \dots \text{a}$, $p = \text{baaa} \dots \text{a}$
- Faster versions exist ($O(n + m + q)$)

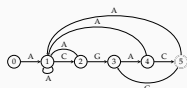
```
last = {}
for j in range(m):
    last[p[j]] = j
i, j = m-1, m-1
while i <= n:
    if T[i] == p[j]:
        return i
    else:
        k = last.get(T[i], -1)
        i += m - min(j, k+1)
        j = m-1
return None
```

A quick introduction to FSA

- Another efficient way to search a string is building a finite state automaton for the pattern
- An FSA is a directed graph where edges have labels
- One of the states is the *initial state*
- Some states are accepting states
- We will study FSA more in-depth soon



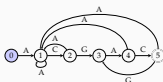
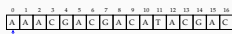
An FSA for the pattern ACGAC



- Start at state 0, switch states based on the input
- All unspecified transitions go to state 0
- When at the accepting state, announce success

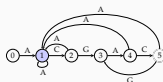
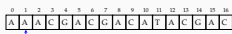
FSA pattern matching

demonstration



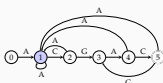
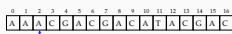
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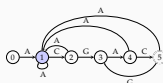
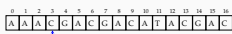
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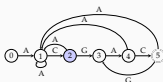
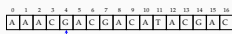
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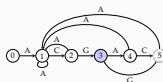
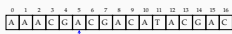
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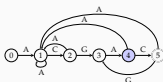
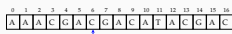
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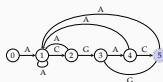
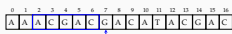
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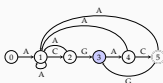
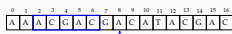
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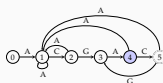
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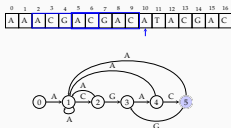
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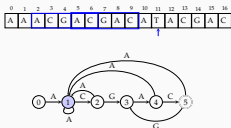
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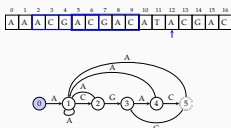
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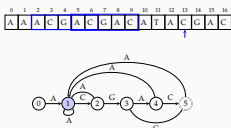
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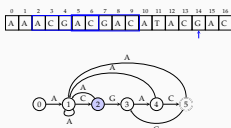
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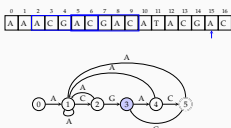
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demonstration



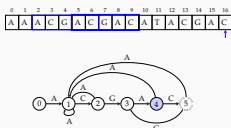
FSA pattern matching

demonstration



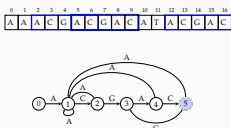
FSA pattern matching

demonstration



FSA pattern matching

demonstration



FSA for string matching

how to build the automaton

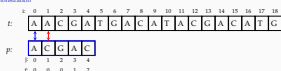
- An FSA results in $O(n)$ time matching, however, we need to first build the automaton
- At any state of the automaton, we want to know which state to go for the failing matches
- Given substring s recognized by a state and a non-matching input symbol a , we want to find the longest prefix of s such that it is also a suffix of sa
- A naive attempt results in $O(qm^3)$ time for building the automaton (where q is the size of the alphabet m is the length of the pattern)
- If stored in a matrix, the space requirement is $O(qm)$
- Better (faster) algorithms exist for construction these automaton (we will cover some later in this course)

Knuth-Morris-Pratt (KMP) algorithm

- The KMP algorithm is probably the most popular algorithm for string matching
- The idea is similar to the FSA approach: on failure, continue comparing from the longest matched prefix so far
- However, we rely on a simpler data structure (a function/table that tells us where to back up)
- Construction of the table is also faster

KMP algorithm

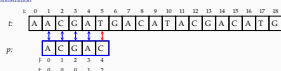
demonstration



- In case of a match, increment both i and j
- On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t[i]$ based on a function f
- $f[j-1]$ tells which j value to resume the comparisons from

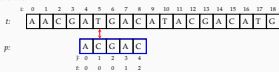
KMP algorithm

demonstration



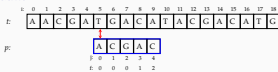
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KMP algorithm demonstration



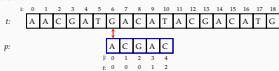
- In case of a match, increment both i and j
- On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t[i]$ based on a function f
- $f[j] - 1$ tells which j value to resume the comparisons from

KMP algorithm demonstration



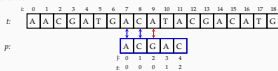
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KMP algorithm demonstration



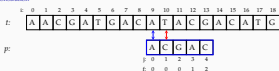
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KMP algorithm demonstration



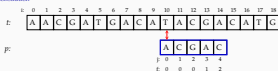
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KMP algorithm demonstration



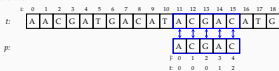
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KMP algorithm demonstration



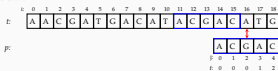
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KMP algorithm demonstration



- In case of a match, increment both i and j
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KMP algorithm demonstration



- In case of a match, increment both i and j
- On failure, or at the end of the pattern, decide which new $p[j]$ compare with $t[i]$ based on a function f
- $f[j] - 1$ tells which j value to resume the comparisons from

Complexity of the KMP algorithm

- In the while loop, we either increase i , or shift the comparison
- As a result, the loop runs at most $2n$ times, complexity is $O(n)$

```

i, j = 0, 0
while i < n:
    if T[i] == P[j]:
        if j == m - 1:
            return i - m + 1
        else:
            i += 1
            j += 1
    elif j > 0:
        j = f[k - 1]
    else:
        j = 1
    j += 1
return None

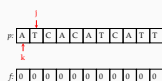
```

Building the prefix/failure table

```

f = [0] * m
j, k = 1, 0
while j < m:
    if P[j] == P[k]:
        f[j] = k + 1
        j += 1
        k += 1
    elif k > 0:
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    else:
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```

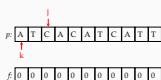


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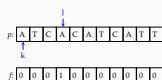


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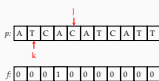


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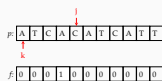


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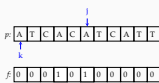


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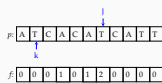


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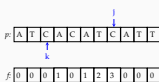


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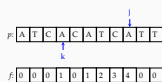


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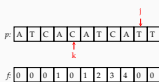


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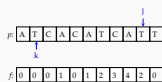


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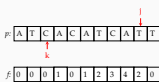


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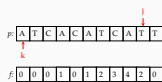


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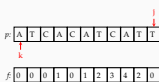


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    if P[j] == P[k]:
        f[j] = k + 1
        j += 1
    elif k > 0:
        k = f[k - 1]
    else:
        j += 1

```



Rabin-Karp algorithm

- Rabin-Karp string matching algorithm is another interesting algorithm
- The idea is instead of matching the string itself, matching the hash of it (based on a hash function)
- If a match found, we need to verify – the match may be because of a hash collision
- Otherwise, the algorithm makes a single comparison for each position in the text
- However, a hash should be computed for each position (with size m)
- Rolling hash functions avoid this complication

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 39

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 37

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 43

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 49

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 47

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 43

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Rabin-Karp string matching

demonstration with additive hashing

t: 7 1 3 6 7 4 3 8 5 7 9 4 3 9

h = 48

p: 4 3 8 5 7 9 4 3

h(p) = 43

- A rolling hash function changes the hash value only based on the item coming in and going out of the window
- To reduce collisions, better rolling-hash functions (e.g., polynomial hash functions) can also be used

Summary

- String matching is an important problem with wide range of applications
- The choice of algorithm largely depends on the problem
- We will revisit the problem on regular expressions and finite-state automata
- Reading: [goodrich2013](#)

Next:

- Algorithms on strings: edit distance / alignment
- Reading: [goodrich2013](#), [jurafsky2009](#)

Building the prefix/failure table

another example

```
f = [0] * m
j, k = 1, 0
while j < m:
    if P[j] == P[k]:
        f[j] = k + 1
        j += 1
        k += 1
    elif k > 0:
        k = f[k - 1]
    else:
        j += 1
```

t: A T A C G A T A C A T G C

p: A T A C G A T A C A T G C

f: 0 0 0 0 0 0 0 0 0 0 0 0 0 0

Building the prefix/failure table

another example

```
f = [0] * m
j, k = 1, 0
while j < m:
    if P[j] == P[k]:
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```

t: A T A C G A T A C A T G C

p: A T A C G A T A C A T G C

f: 0 0 1 0 0 0 0 0 0 0 0 0 0 0

Building the prefix/failure table

another example

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    else:
        j += 1
```

t: A T A C G A T A C A T G C

p: A T A C G A T A C A T G C

f: 0 0 1 0 1 0 0 0 0 0 0 0 0 0

Building the prefix/failure table

another example

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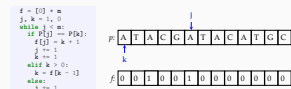
t: A T A C G A T A C A T G C

p: A T A C G A T A C A T G C

f: 0 0 1 0 1 0 0 0 0 0 0 0 0 0

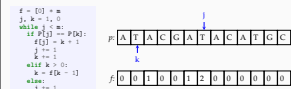
Building the prefix/failure table

another example



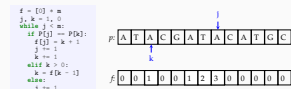
Building the prefix/failure table

another example



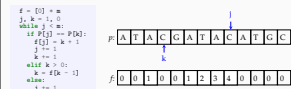
Building the prefix/failure table

another example



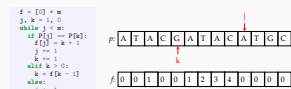
Building the prefix/failure table

another example



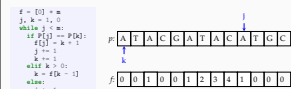
Building the prefix/failure table

another example



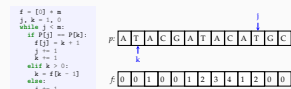
Building the prefix/failure table

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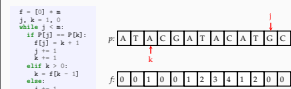
Building the prefix/failure table

another example



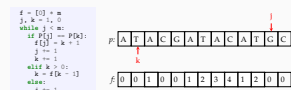
Building the prefix/failure table

another example



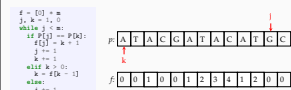
Building the prefix/failure table

another example



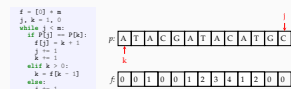
Building the prefix/failure table

another example



Building the prefix/failure table

another example



Acknowledgments, credits, references

