## Chalmers | GÖTEBORGS UNIVERSITET

2019-01-19

Examiner: Thomas Hallgren, hallgren@chalmers.se, D&IT, Answering questions at approx 10.00 (or by phone 031 772 1941)

## Functional Programming TDA 452, DIT 143

2019-01-19 8:30 - 12:30 Lindholmen-salar  $031\ 772\ 1941$ 

• There are 5 questions with maximum 8+8+12+8+4=40 points. Grading:

Chalmers: 3 = 20–26 points, 4 = 27–33 points , 5 = 34–40 points GU: G = 20–33 points, VG = 34–40 points

- Results: latest approximately 10 days.
- Permitted materials:
  - Dictionary
- Please read the following guidelines carefully:
  - Read through all Questions before you start working on the answers.
  - Begin each Question on a new sheet.
  - Write clearly; unreadable = wrong!
  - For each part Question, if your solution consists of more than a few lines of Haskell code, use your common sense to decide whether to include a short comment to explain your solution.
  - You can use any of the standard Haskell functions listed at the back of this exam document.
  - Full points are given to solutions which are short, elegant, and correct. Fewer
    points may be given to solutions which are unnecessarily complicated or unstructured.
  - You are encouraged to use the solution to an earlier part of a Question to help solve a later part even if you did not succeed in solving the earlier part.

1. (8 points) For each of the following definitions, give the most general type, or write "No type" if the definition is not correct in Haskell.

```
fa x = "Hello, "++x
fb (x:y) = (x,y)
fc x y z = x<=y && y<=z
fd = map . map
```

- 2. (8 points)
  - (a) (3 points) Define a function subsequences that computes all the subsequences of a list, i.e. all the list you get by keeping *some* of the elements in the list (including none of the elements and all of the elements).

```
subsequences :: [a] -> [[a]]
```

The elements within each subsequence should appear in the same order as in the argument list, but it doesn't matter in which order the subsequences appear, i.e. it could be the shortest subsequence first, the longest subsequence first, or some other order. Examples:

```
subsequences [1] == [[],[1]]
subsequences [1,2] == [[],[1],[2],[1,2]]
subsequences "abc" == ["abc","ab","ac","a","bc","b","c",""]
```

(b) (3 points) Define a function isSubsequenceOf that checks if one list is a subsequence of another list.

```
isSubsequenceOf :: Eq a => [a] -> [a] -> Bool
```

Examples:

```
"" 'isSubsequenceOf' "abc" == True
"a" 'isSubsequenceOf' "" == False
"a" 'isSubsequenceOf' "abc" == True
"ac" 'isSubsequenceOf' "abc" == True
"ad" 'isSubsequenceOf' "abc" == False
"cb" 'isSubsequenceOf' "abc" == False
```

(c) (2 points) Write a property that can be used with QuickCheck to test that all the subsequences returned by subsequences really are subsequences of the argument list.

3. (12 points) Consider the following function definitions:

```
checkEqn :: Equation -> Bool
checkEqn (Eqn e1 e2) = eval e1 == eval e2

eval :: Expr -> Int
eval (Num x) = x
eval (Op op e1 e2) = evalOp op (eval e1) (eval e2)

evalOp :: Oper -> Int -> Int -> Int
evalOp Add = (+)
evalOp Sub = (-)
evalOp Mul = (*)
```

- (a) (3 points) Give the data type definitions needed for the above function definitions to be correct.
- (b) (3 points) Define a QuickCheck test data generator

```
rExpr :: Int -> Gen Expr
```

such that rExpr n generates random expressions containing n operators. For the numbers in the expressions, use random ones from the sequence 1, 2 ... 10.

(c) (3 points) Define a function

```
exprs :: [Int] -> [Expr]
```

that generates all expressions that contain the given numbers in the given order. Examples:

```
exprs [1] == [Num 1]
exprs [1,2] ==
        [Op Add (Num 1) (Num 2), Op Sub (Num 1) (Num 2), -- 1+2, 1-2
        Op Mul (Num 1) (Num 2)] -- 1*2,
```

(d) (3 points) Define a function

```
equations :: [Int] -> [Equation]
```

that generates *all* equations that are true and contain the given numbers in the given order. Examples:

Hints: (i) Generating a list of expressions with list comprehensions is very similar to generating a random expression with the Gen monad and the do notation. (ii) A helper function that generates pairs of expressions can be useful in both exprs and equations.

4. (8 points) Consider the following data type for trees where the leaves contain one type of values and the internal nodes contain another type of values:

```
data Tree a b = Leaf a | Node b (Tree a b) (Tree a b)
```

(a) (3 points) Define a function that corresponds to map for lists:

```
mapTree :: (a1->a2) -> (b1->b2) -> Tree a1 b1 -> Tree a2 b2
```

(b) (2 points) Define a function that "folds" a tree which has functions in the internal nodes. (So unlike foldr for lists, the function used to combine values is not given as an extra argument.)

```
foldTree :: Tree a (a->a->a) -> a
```

(c) (3 points) Reimplement eval from Question 3 by first converting an Expr to a Tree Int Oper, then using mapTree and foldTree.

5. (4 points) Write a function that reads lines of text form a number of files and outputs all the lines sorted.

```
sortFiles :: [FilePath] -> IO ()
```

Example: sortFiles ["A.txt","B.txt"]

A.txt	B.txt	Output
PHP	Lisp	С
Haskell	C	Erlang
Python	Java	Haskell
Erlang		Java
		Lisp
		PHP
		Python

In addition to the functions listed at the back of this exam, the following library function might be useful:

```
-- Functions to output text putStr, putStrLn :: String -> IO ()
```

-- readFile reads the contents of a file readFile :: FilePath -> IO String

-- File names are strings. type FilePath = String

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:: (Eq a) => a -> lookup key [] = M---.
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all
                                                                                                                                                                                  and
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     drop n (_:xs)
                                                                                   elem x
                                                                                                                                                                                                                                                                                            unlines, unwords :: [String] -> String -- unlines ["apa","bepa","cepa"]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      dropWhile dropWhile
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 splitAt n xs
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     take _ []
take n (x:xs)
                       lookup key ((x,y):xys)
                                                                         notElem x
                                                                                              elem, notElem
                                                                                                                                           any, all
                                                                                                                                                                                              and, or
                                                                                                                                                                                                                                                              -- unwords ["apa","bepa","cepa"]
-- == "apa bepa cepa"
                                                                                                                                                                                                                                                                                                                                                                      -- lines "apa\nbepa\ncepa\n"
                                                                                                                                                                                                                                                                                                                                                                                   lines, words
                                                                                                                                                                                                                                                                                                                                                                                                          span p as = (takeWhile p as, dropWhile p as)
                                                                                                                                                                                                                                                                                                                                                                                                                     span :: (a -> Bool) -> [a] -> ([a], [a])
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            drop n
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          tails xs
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                                                                                                                      ם ם
otherwise
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                                                                                                                                                                                                                                                                                                                                  == ["apa","bepa","cepa"]
                                                                                                                                                                                                                                                                                                                                                         == ["apa","bepa","cepa"]
             key == x
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                                                                                                                                                                                                                                                                                 == "apa\nbepa\ncepa"
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                                                                                                                                                                                                                                                          "apa bepa cepa"
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= foldl (fliv
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                                                                                                                                                                                              :: [Bool] -> Bool
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lookup key xys
           Just y
                                                                                              (Eq a) => a ->
                                                                                   any (== x)
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                                                                         all (/= x)
                                                                                                                      and . map p
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K
                                                                                                                                               (a -> Bool) -> [a] ->
                                                                                                                                                                      foldr (||) False
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                                                                                                                                                                                   foldr (&&) True
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                                                                                                                                  . map p
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= (take n xs, drop n xs)
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= []
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     drop (n-1) xs
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                                               [(a,b)] -> Maybe b
                                                                                             [a]
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                                                                                                                                                                                  partition
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      minimum (x:xs) =
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                                                                       groupBy eq (x:xs) =
                                                                                   groupBy _
                                                                                                                                                                      partition p xs =
                                                                                                                                                                                                                                                                                               intersect xs
                                                                                                                                                                                                                                                                                                                                   union
                                                                                                                                                                                                                                                                                                                                                                                                                      delete y (x:xs)
                                                                                                                                                                                                                                                                                                                                                                                                                                              delete
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              drzun
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    zipWith _
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              zipWith z (a:as) (b:bs)
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isPrefixOf (x:xs) (y:ys) =
                                                                                                                                                                                                                                     transpose
                                                                                                                                                                                                                                                                      intersperse
                                                                                                                                                                                                                                                                                                           intersect
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          zipWith
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      foldr (\(a,b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     (sx:xs)
                                                                                                                                                                                                                                                                                                                                   xs ys
                                                                                                                                                                                                                                                                                                                                                                                                                                 y []
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group = groupBy (==)
                                        isPrefixOf :: Eq a => [a] -> [a] -> Bool
isPrefixOf [] _ = True
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    minimum [] = error "Prelude.minimum: empty list"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                maximum (x:xs) = foldl max x xs
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   maximum [] = error "Prelude.maximum: empty list"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          maximum, minimum :: (Ord a) => [a] -> a
                                                                                                                                                                    groupBy :: (a -> a -> Bool) -> [a] -> [[a]]
                                                                                                                                                                                                                                                                                                                                                                    transpose [[1,2,3],[4,5,6]]
== [[1,4],[2,5],[3,6]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                       tersperse :: a -> [a] -> [a]
intersperse 0 [1,2,3,4] == [1,0,2,0,
                                                                                                                                                                                                                                                                                (filter p xs, filter (not . p) xs)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if x == y then xs else x: delete y xs
                                                                                                                                                                                                                                                                                                                            :: (a -> Bool) -> [a] -> ([a],[a])
                                                                                                       where (ys,zs) =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ~(as,bs) -> (a:as,b:bs)) ([],[])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      :: Eq a => [a] -> [a] -> [a] = [ x | x <- xs, x 'elem' ys
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         П
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          II
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 :: [a] -> [b] -> [(a,b)]
= zipWith ( )
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 foldl min x xs
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                                                                                                                                                                                                                                                                                                                                                                                                              :: [[a]] -> [[a]]
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                                                                                                                                                     П
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           x : nub [ y | y \leftarrow xs,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         xs ++ (ys \\ xs)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   foldl (flip delete)
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    foldl (*) 1
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                                                                                                                              (x:ys):
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     بم
۷-
x == y
                     False
                                                                                                         span (eq x) xs
                                                                                                                              groupBy eq zs
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          0
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                                                                                                                                                                                                                                                                                                                                                                                                                                                         ,3,0,4]
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                                                                                                                              sized :: (Int -> Gen a) -> Gen a
                                                                                                                                                                                          vectorOf :: Int -> Gen a -> Gen [a]
                                                                                                                                                                                                                                                             listOf :: Gen a -> Gen [a]
                                                                                                                                                                                                                                                                                                                            elements :: [a] -> Gen a
                                                                                                                                                                                                                                                                                                                                                                                                                frequency :: [(Int, Gen a)] -> Gen a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              oneof :: [Gen a] -> Gen
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    choose :: Random a => (a, a) -> Gen a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      arbitrary :: Arbitrary a => Gen a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | |
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     chr :: Char -> Int
chr :: Int -> Char
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       digitToInt :: Char -> Int
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 -- toUpper 'a' == 'A'
-- toLower 'Z' == 'Z'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ŀ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sort
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               sort
                                                                                                       -- construct generators that depend on
                                                                                                                                                                                                                                                                                                                                                                      -- weighted random distribution.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         intToDigit :: Int -> Char
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             toUpper, toLower :: Char -> Char
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     type String = [Char]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    insert x (y:xs)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         insert x []
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              insert
                                                                                    the size parameter
                                                                                                                                                                        Generates a list of the given length
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               the generator for values of a type
                                                                                                                                                                                                                                                                                                     Generates one of the given values.
                                                                                                                                                                                                                                        Generates a list of random length.
                                                                                                                                                                                                                                                                                                                                                                                           Chooses from list of generators with
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inclusive range.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Generates a random element
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    digitToInt '8' == 8
                                                                                                                                                                                                                                                                                                                                                                                                                                                         Randomly uses one of the given generators
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          in class Arbitrary, used by quickCheck
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   from
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Signatures of some useful functions
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    intToDigit 3 == '3'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Test.QuickCheck
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given

&& isPrefixOf xs

ΣY

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isSuffixOf x y = reverse x 'isPrefixOf' reverse y
                                                                                                                                                                                                                                   isSuffixOf :: Eq a => [a] -> [a] -> Bool
functions on Char
                                                         if x <= y then x:y:xs</pre>
                                                                                               П
                                                                                                                 :: (Ord a) => a ->
                                                                                                                                                          = foldr insert []
                                                                                                                                                                          :: (Ord a) => [a] -> [a]
                                                                                               ×
                                                           else
                                                           y:insert x xs
                                                                                                                    [a] ->
                                                                                                                    [a]
```