

LECTURER: Nghia Duong-Trung

MACHINE LEARNING

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TOPIC OUTLINE

Introduction to Machine Learning

1

Clustering

2

Regression

3

Support Vector Machines

4

Decision Trees

5

Genetic Algorithm

6

UNIT 4

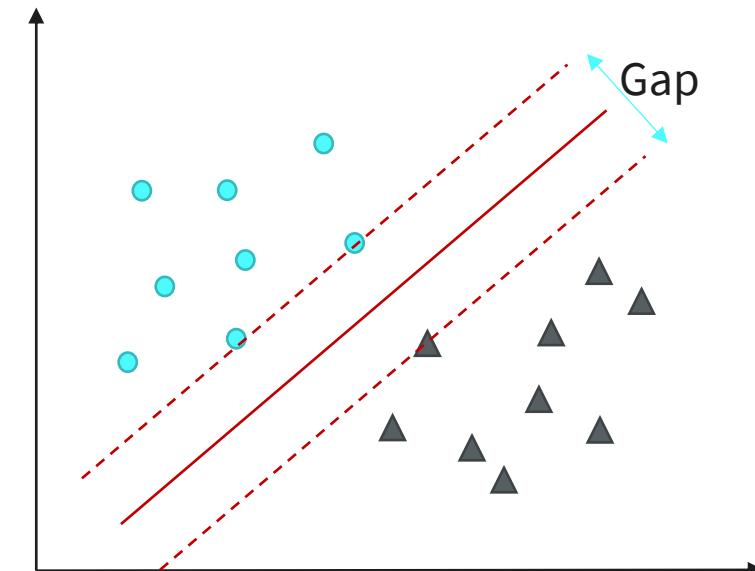
SUPPORT VECTOR MACHINES



- Know the definitions and terms used for Support Vector Machines (SVM)
- Comprehend common applications of SVM
- Understand different methods for SVM classifier and regressor
- Implement SVM methods in Python

INTRODUCTION

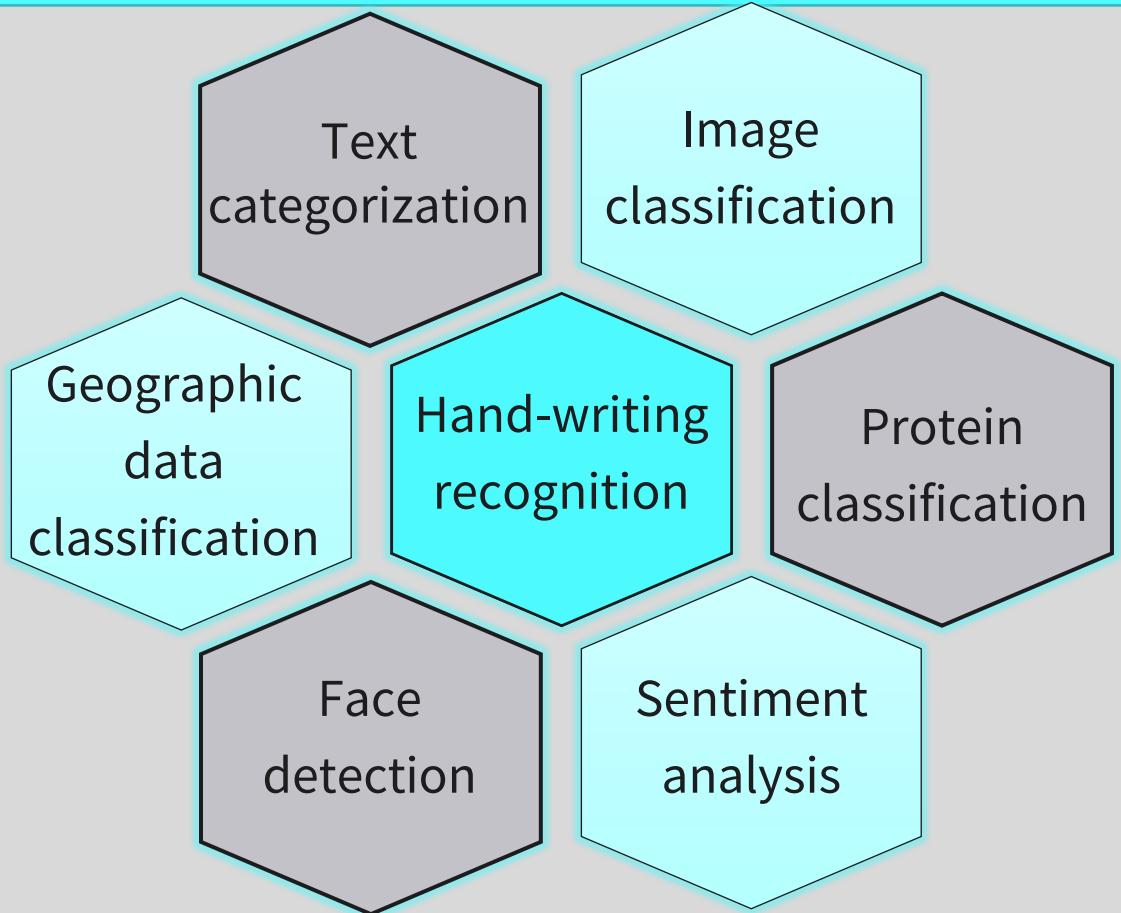
- Support vector machine (SVM) is a **mathematical** model within the class of **supervised** learning for:
 - accurate classification & prediction
 - both continuous & categorical data
 - both linear & non-linear problems
 - high efficiency & effectivity



An example of SVM

INTRODUCTION

SVM applications



SVM methods

**CLASSIFICATION
HARD MARGIN**

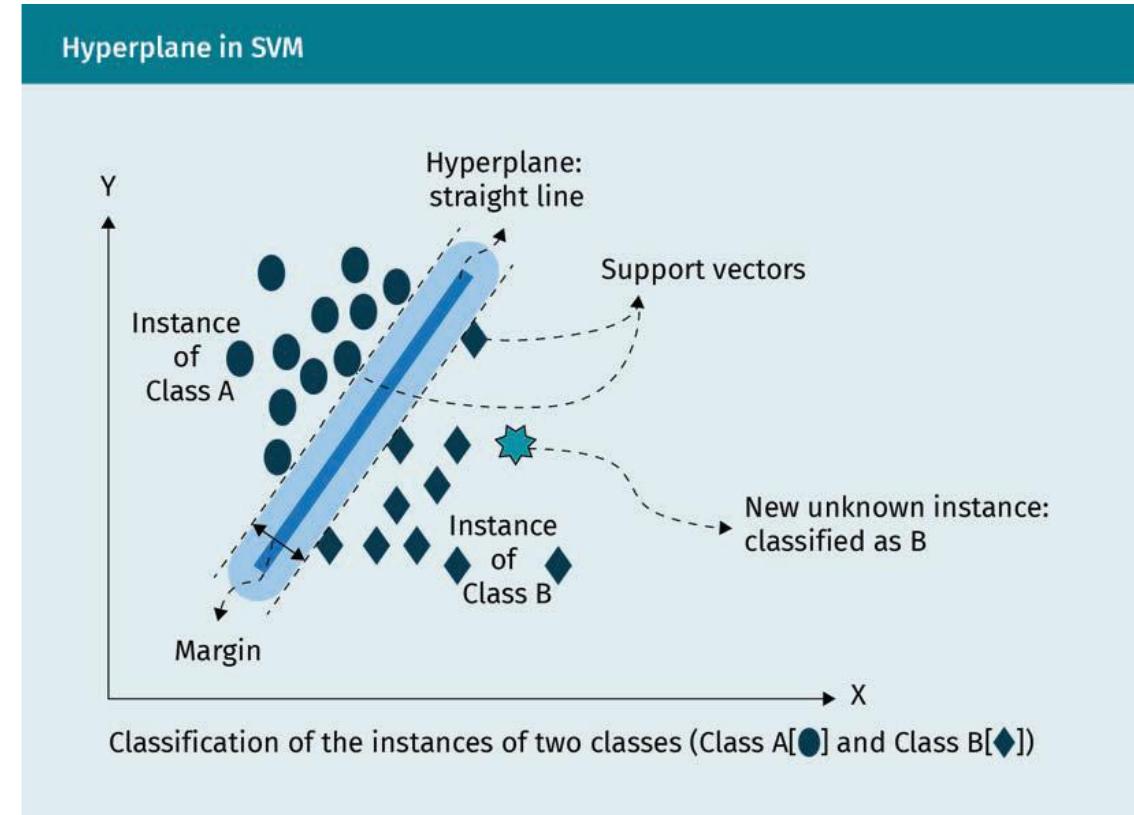
**CLASSIFICATION
SOFT MARGIN
PRIMAL FORM**

**CLASSIFICATION
SOFT MARGIN
DUAL FORM**

**REGRESSION
(SVR)**

Definition

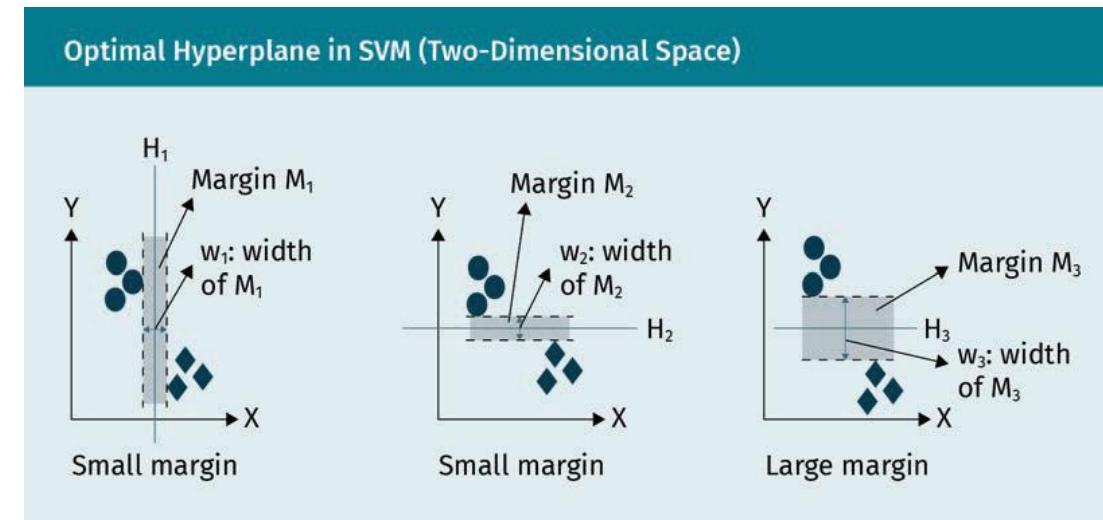
- **Hyperplane:** a separating boundary that help to classify the points
- **Margin:** the boundary gap between two point-sets
- **Support vectors:** the points that determine the margin



An example of SVM

SVM algorithm:

- The separating hyperplane is detected (learned) by **maximizing the margin** width
- The margin width is measured based on the **perpendicular distance** from the separating hyperplane to the support vectors
- Large margin ensures good **generalization**
- This method is **memory efficient**, as it uses only a subset of training points (support vectors)



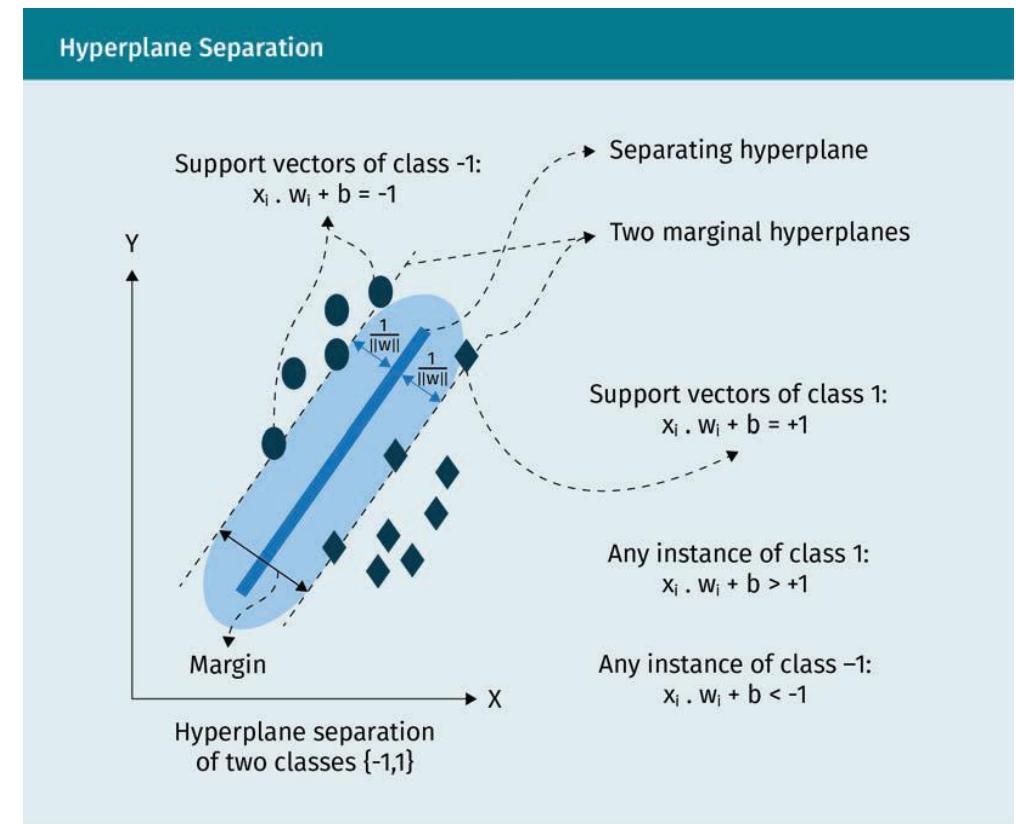
Optimization of Hyperplane in SVM

SVM classifier with **Hard Margin**:

- Only suitable for **Linearly Separable** data
- A separating hyperplane (i.e., decision function $f(x)=0$) can be detected **without training errors**
- For a dataset of multiple features:

$$f(x) = \sum_{i=1}^n w_i \cdot x_i - b$$

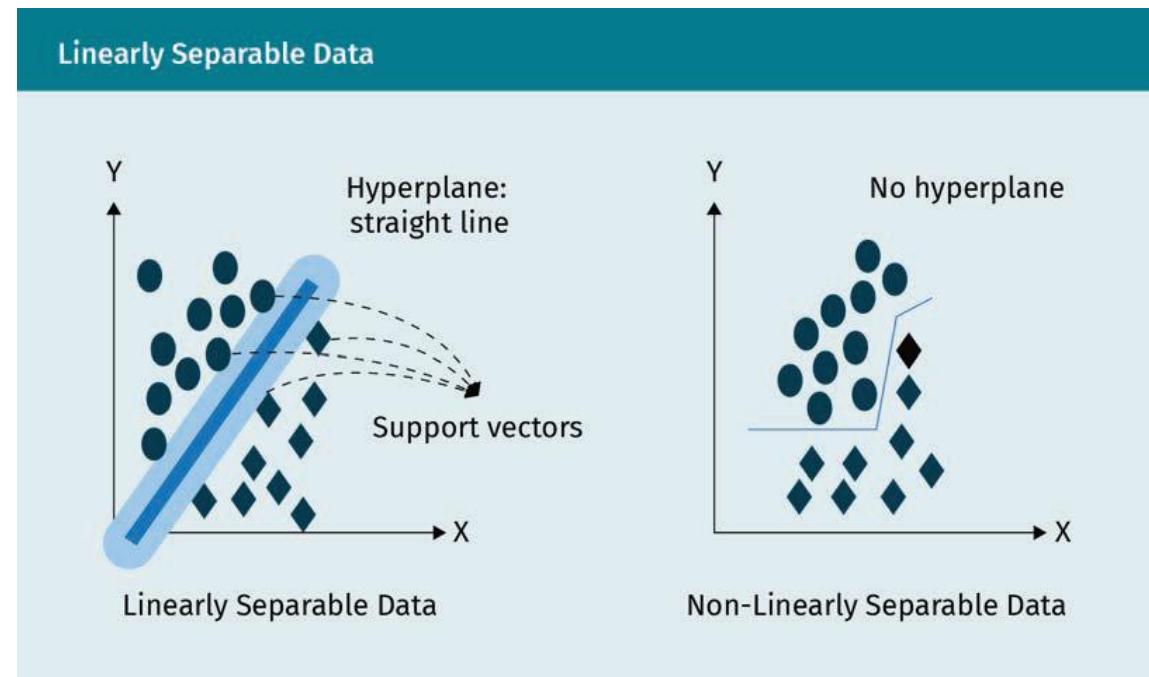
- Optimization problem: **Minimize** $\{\|w\|\}$
- Hard margin is **Sensitive** to outliers



An example of SVM with hard margin for classification

SVM classifier with Soft Margin:

- An **extension** of Hard Margin SVM for **nonlinearly** separable data
- Allow SVM to make a certain number of **mistakes** and keep the margin as wide as possible



An example of linearly and non-linearly separable data

SVM classifier with **Soft Margin**:

— Primal Form:

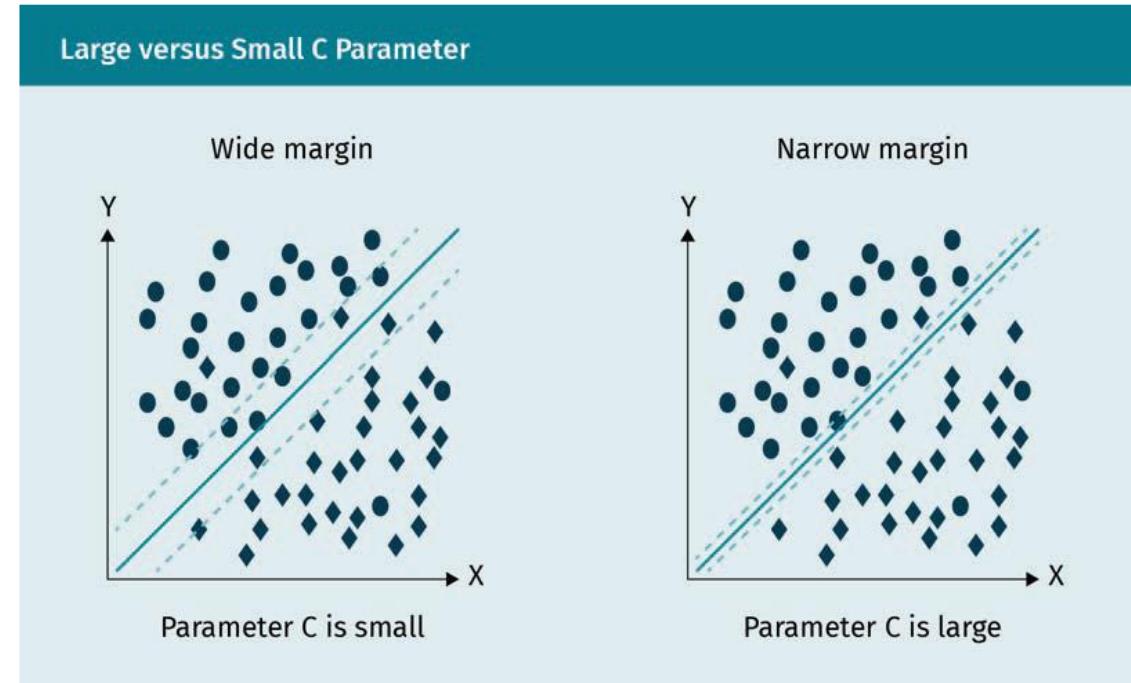
- The data are **almost** linearly separable
- Some data points can lie **inside** the margin area
- Optimization problem:

$$\text{Minimize } \frac{C}{n} \sum_{i=1}^n \xi_i + \|w\|^2$$

Where:

C – trade-off parameter

ξ_i - slack error



An application of SVM with Soft Margin/Primal form for classification

SVM classifier with **Soft Margin**:

- **Dual Form:**
 - an **adjusted form** from primal form
 - uses a **Lagrangian multiplier** α in defining weight vector:

$$\mathbf{w} = \sum_{j=1}^n \alpha_j y_j \mathbf{x}_j$$

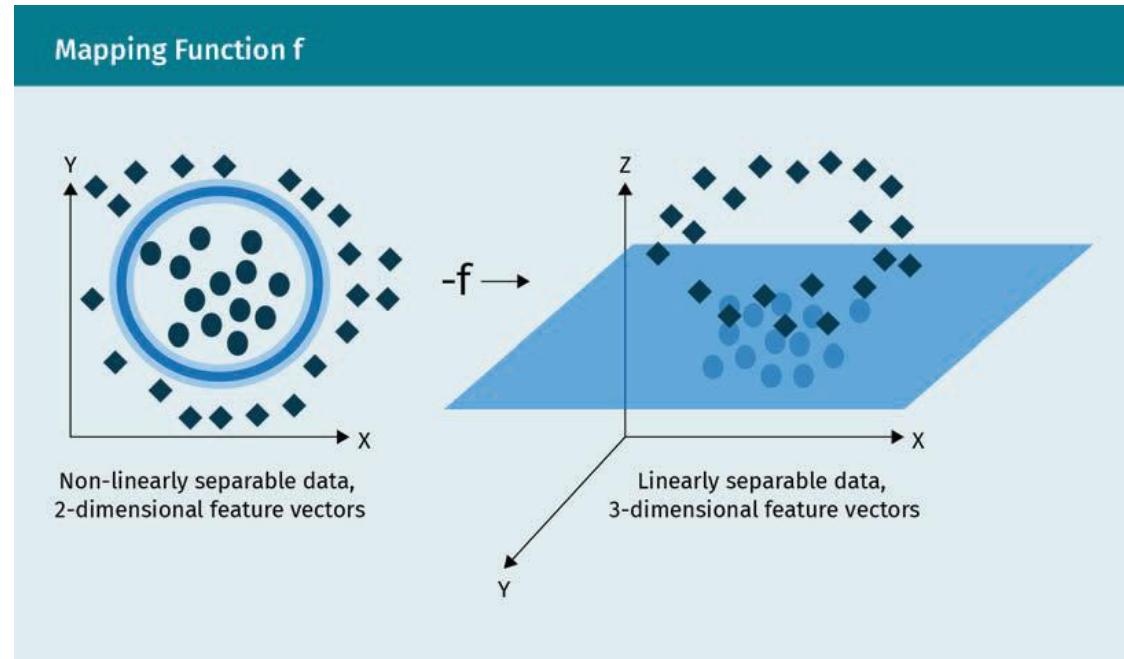
- Optimization problem: **Maximize** quadratic function:

$$Q(\alpha_i) = \sum_{i=1}^n \alpha_i - \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n \alpha_i \alpha_j (\mathbf{x}_i \cdot \mathbf{x}_j) y_i y_j$$

- Dual form is preferred when data has a **huge dimension**, and the **kernel trick** is needed to reduce the computational cost

Transformation

- **Real-life datasets** are usually not linearly separable
- The non-linearly separable data can be transformed to linearly separable data by **adding a new dimension** of the feature space
- **Problems:** Overfitting & high computational cost



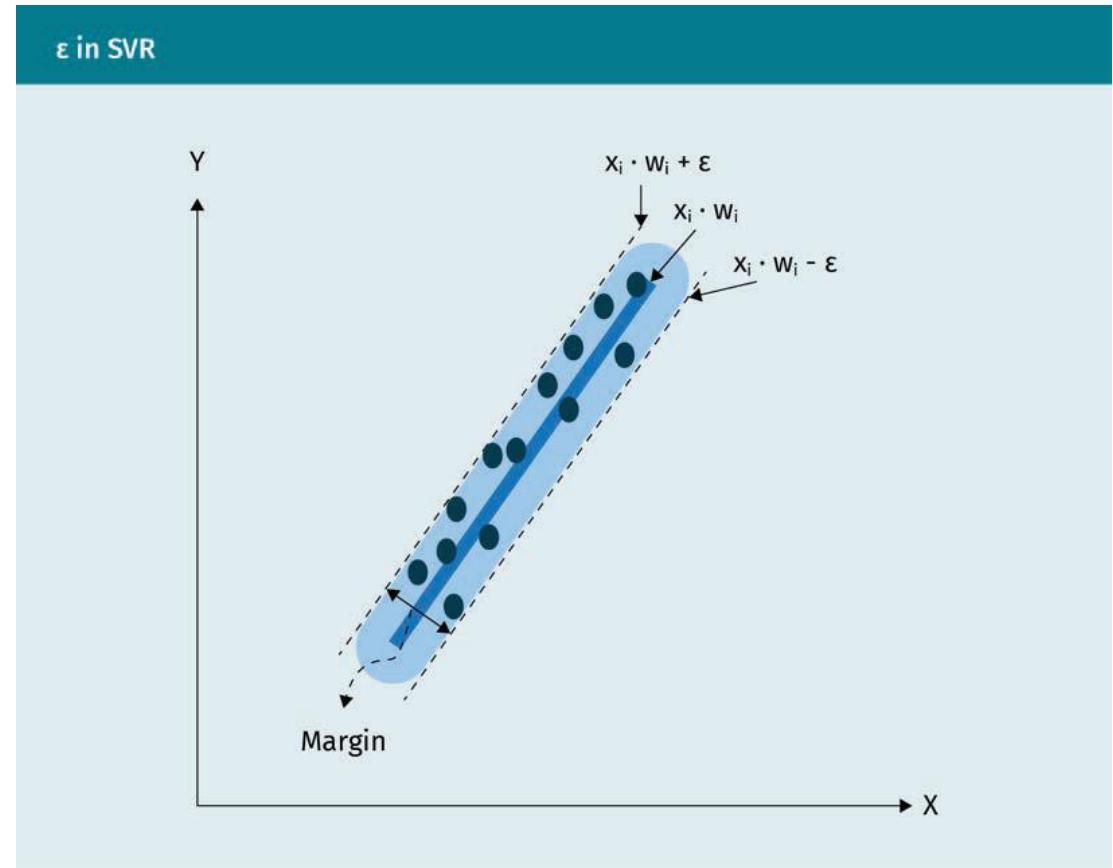
An example of Transformation from non-linearly to linearly separable data

4.3 SVM FOR REGRESSION (SVR)

SVM Regression (SVR): a version of the SVM classifier

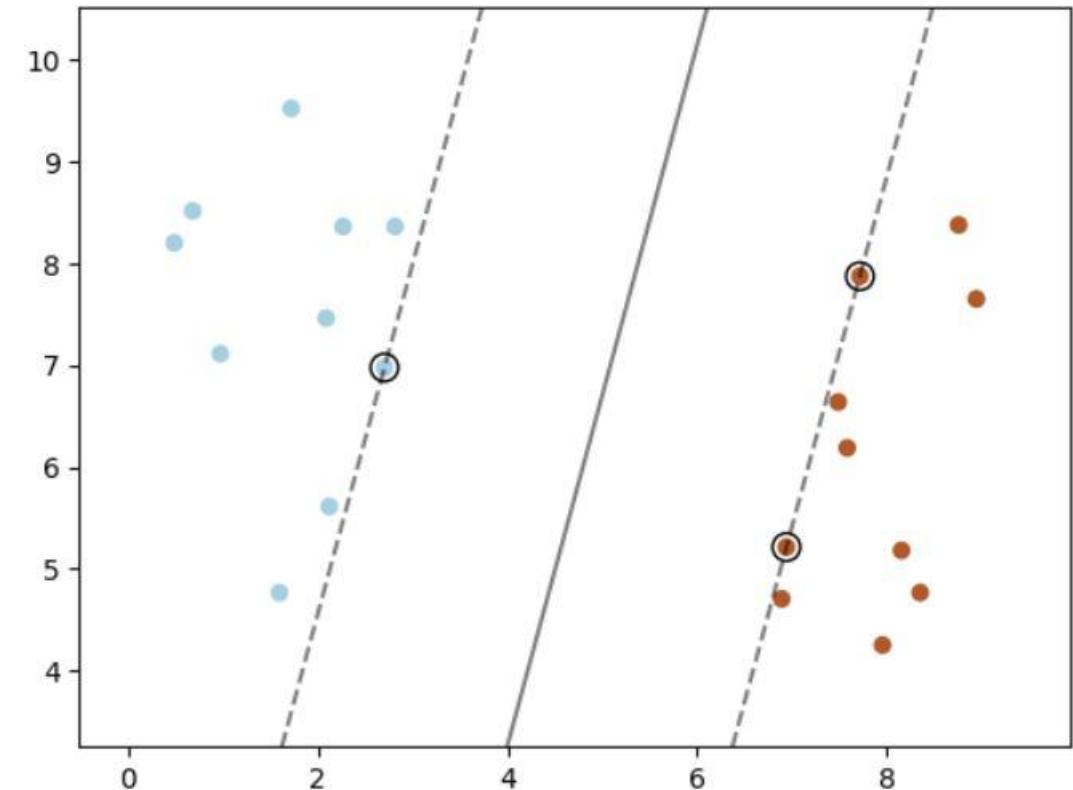
- SVR **predicts** numerical output values with some deviation (**epsilon error ϵ**)
- Objective function: **Minimize** the model coefficient **w** and introduce the cost C (**trade-off** parameter) and two slack variables ξ_i, ξ_i^* :

$$\frac{1}{2} \|w\|^2 + C \sum_{i=1}^n |\xi_i + \xi_i^*|$$



3.4 SVM WITH PYTHON

```
# SVM classifier with linear kernel
import matplotlib.pyplot as plt
from sklearn import svm
from sklearn.datasets import make_blobs
from sklearn.inspection import DecisionBoundaryDisplay
# we create 20 separable points
X, y = make_blobs(n_samples=20, centers=2, random_state=20)
# fit the model, don't regularize for illustration purposes
clf = svm.SVC(kernel="linear", C=1000)
clf.fit(X, y)
plt.scatter(X[:, 0], X[:, 1], c=y, s=30, cmap=plt.cm.Paired)
# plot the decision function
ax = plt.gca()
DecisionBoundaryDisplay.from_estimator(clf, X, plot_method="contour",
    colors="k", levels=[-1, 0, 1], alpha=0.5, linestyles=["--", "-", "--"], ax=ax,)
# plot support vectors
ax.scatter(clf.support_vectors_[:, 0], clf.support_vectors_[:, 1],
    s=100, linewidth=1, facecolors="none", edgecolors="k", )
plt.show()
```

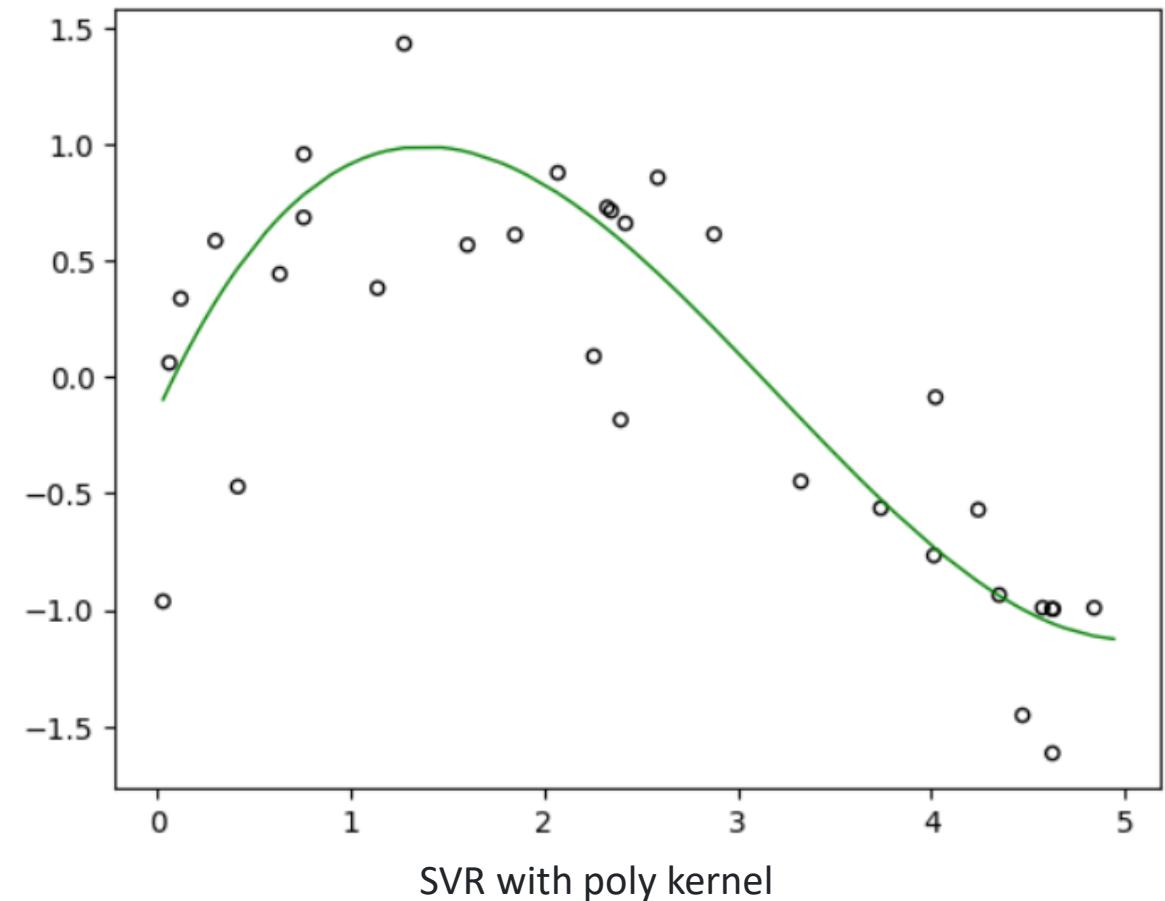


Maximum margin separating hyperplane within a two-class separable dataset using SVM classifier

3.4 SVM WITH PYTHON

```
# SVM regression with poly kernel
```

```
import numpy as np
from sklearn.svm import SVR
import matplotlib.pyplot as plt
X = np.sort(5 * np.random.rand(100, 1), axis=0)
y = np.sin(X).ravel()
# add noise to targets
y[::5] += 2 * (0.5 - np.random.rand(20))
svr = SVR(kernel="poly", C=100, gamma="auto", degree=3, epsilon=0.1,
coef0=1)
ax = plt.gca()
#plot regression curve
ax.plot(X,svr.fit(X, y).predict(X),color=model_color[ix],lw=1)
ax.scatter(X[svr.support_],y[svr.support_],facecolor="none",
edgecolor="k",s=20)
plt.show()
```



REVIEW STUDY GOALS



- Know the definitions and terms used for Support Vector Machines (SVM)
- Comprehend common applications of SVM
- Understand different methods for SVM classifier and regressor
- Implement SVM methods in Python

SESSION 4

TRANSFER TASK

TRANSFER TASKS

1. Create the dataset using the following code:

```
from sklearn.datasets import make_blobs  
X, y = make_blobs(n_samples=100, centers=2, random_state=12)
```

Implement SVM classifier using

- a) Poly kernel
- b) RBF kernel

TRANSFER TASKS

2. Create the dataset using the following code:

```
import numpy as np  
X = np.sort(5 * np.random.rand(100, 1), axis=0)  
y = np.sin(X).ravel()  
y[::5] += 2 * (0.5 - np.random.rand(20)) # adding noises
```

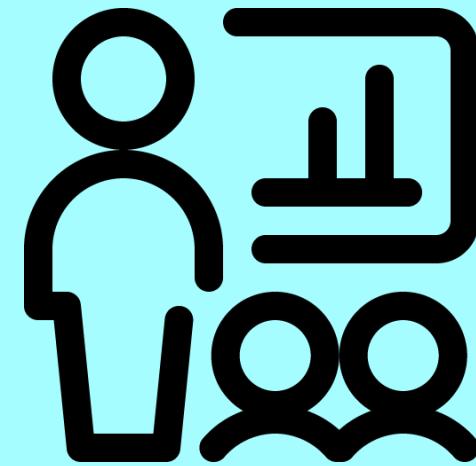
Implement SVM regression using

- a) linear kernel
- b) RBF kernel

TRANSFER TASK
PRESENTATION OF THE RESULTS

Please present your
results.

The results will be
discussed in plenary.





1. The idea of SVM classification is to find a hyperplane that _____ the margin between classes.?

- a) Removes
- b) Minimizes
- c) Maximizes
- d) None of these



2. What is/are true about kernel in SVM?

- (1): Kernel function maps low dimensional data to a high dimensional space.
 - (2): It's a similarity function.
-
- a) Neither option is correct
 - b) Options 1 and 2 are correct
 - c) Option 1 is correct
 - d) Option 2 is correct



3. The regularization parameter in the SVM cost function determines...

- a) ...the tradeoff between misclassification and simplicity of the model.
- b) ...the number of cross-validations to be made.
- c) ...the kernel to be used.
- d) None of the above.



4. If I am using all features of my dataset and I achieve 100% accuracy on my training set, but ~70% on testing set, what should I look out for?
- a) Underfitting
 - b) Nothing, the model is perfect.
 - c) Include more testing data
 - d) Overfitting



5. The constraint of the Support Vector Regression model is that the absolute error is _____ the value of error term epsilon.
- a) Less than or equal to
 - b) Not related to
 - c) Greater than
 - d) Exactly equal to



Solutions

1. c)
2. b)
3. a)
4. d)
5. a)

LIST OF SOURCES

Text:

- Schölkopf, B., & Smola, A. J. (2002). Learning with kernels: support vector machines, regularization, optimization, and beyond. *MIT Press*.
- Misra, R. (2019). Support Vector Machines – Soft Margin Formulation and Kernel Trick. <https://towardsdatascience.com/support-vector-machines-soft-margin-formulation-and-kernel-trick-4c9729dc8efe>
- Rajput, V. (2021). The Optimization Behind SVM: Primal and Dual Form. <https://medium.com/aiguys/the-optimization-behind-svm-primal-and-dual-form-5cca1b052f45>

Images:

File: Normdist_regression.png (2023)

Zöller (2022, p. 89)

Zöller (2022, p. 90)

Zöller (2022, p. 92)

Zöller (2022, p. 94)

Zöller (2022, p. 97)

Zöller (2022, p. 98)

Zöller (2022, p. 101)

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