Linear Regression

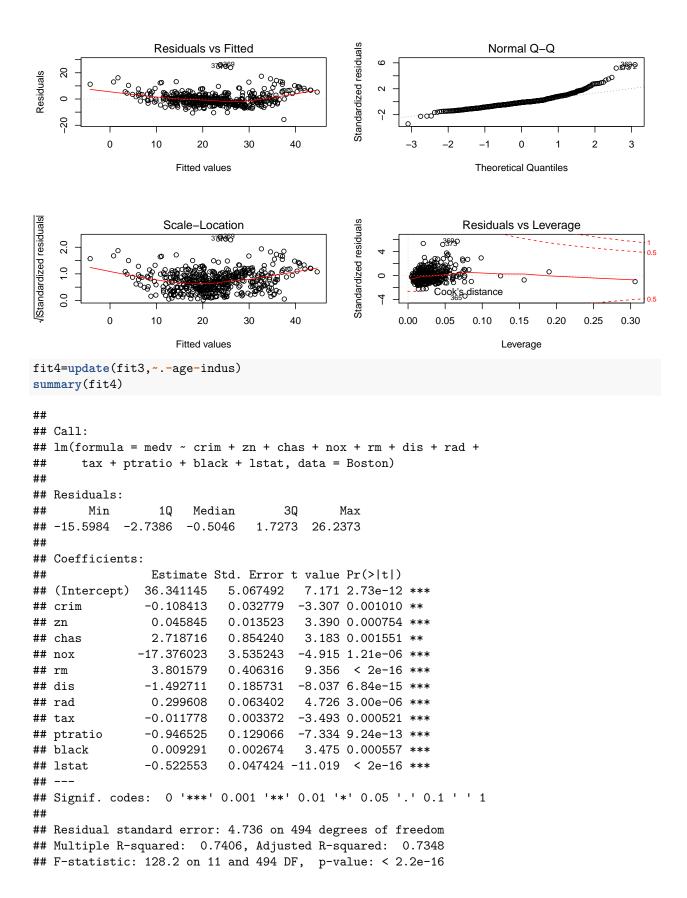
Pramod Duvvuri 4/10/2019

```
# Load libraries
library(MASS)
library(ISLR)
### Simple linear regression
names (Boston)
## [1] "crim"
                  "zn"
                            "indus"
                                      "chas"
                                                                    "age"
                                                "nox"
                                                          "rm"
## [8] "dis"
                  "rad"
                            "tax"
                                      "ptratio" "black"
                                                                    "medv"
                                                          "lstat"
?Boston
plot(medv~lstat,Boston)
fit1=lm(medv~lstat,data=Boston)
fit1
##
## Call:
## lm(formula = medv ~ lstat, data = Boston)
## Coefficients:
## (Intercept)
                     lstat
        34.55
                     -0.95
summary(fit1)
##
## lm(formula = medv ~ lstat, data = Boston)
##
## Residuals:
       Min
               1Q Median
                               3Q
                                      Max
## -15.168 -3.990 -1.318 2.034 24.500
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 34.55384
                          0.56263 61.41 <2e-16 ***
## lstat
              -0.95005
                          0.03873 -24.53 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.216 on 504 degrees of freedom
## Multiple R-squared: 0.5441, Adjusted R-squared: 0.5432
## F-statistic: 601.6 on 1 and 504 DF, p-value: < 2.2e-16
```

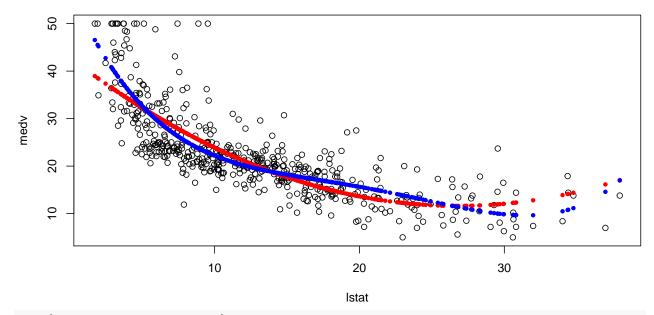
```
abline(fit1,col="red")
          യ അാറ്റ് താ
                      0
    9
    30
medv
                                                00
    20
                                                                                        0
    10
                                                                                      0
                            10
                                                                      30
                                                 20
                                                Istat
names(fit1)
  [1] "coefficients" "residuals"
                                         "effects"
                                                         "rank"
   [5] "fitted.values" "assign"
                                         "qr"
                                                         "df.residual"
  [9] "xlevels"
                                         "terms"
                                                         "model"
                         "call"
confint(fit1)
##
                   2.5 %
                             97.5 %
## (Intercept) 33.448457 35.6592247
## lstat
               -1.026148 -0.8739505
predict(fit1,data.frame(lstat=c(5,10,15)),interval="confidence")
##
          fit
                   lwr
## 1 29.80359 29.00741 30.59978
## 2 25.05335 24.47413 25.63256
## 3 20.30310 19.73159 20.87461
### Multiple linear regression
fit2=lm(medv~lstat+age,data=Boston)
summary(fit2)
##
## Call:
## lm(formula = medv ~ lstat + age, data = Boston)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                        Max
## -15.981 -3.978 -1.283
                             1.968 23.158
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 33.22276
                           0.73085 45.458 < 2e-16 ***
                           0.04819 -21.416 < 2e-16 ***
## lstat
               -1.03207
                                    2.826 0.00491 **
## age
               0.03454
                           0.01223
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.173 on 503 degrees of freedom
## Multiple R-squared: 0.5513, Adjusted R-squared: 0.5495
## F-statistic: 309 on 2 and 503 DF, p-value: < 2.2e-16
fit3=lm(medv~.,Boston)
summary(fit3)
##
## Call:
## lm(formula = medv ~ ., data = Boston)
## Residuals:
      Min
##
               1Q Median
                              3Q
                                     Max
## -15.595 -2.730 -0.518
                          1.777 26.199
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.646e+01 5.103e+00
                                    7.144 3.28e-12 ***
             -1.080e-01 3.286e-02 -3.287 0.001087 **
## crim
## zn
              4.642e-02 1.373e-02 3.382 0.000778 ***
## indus
              2.056e-02 6.150e-02 0.334 0.738288
## chas
              2.687e+00 8.616e-01 3.118 0.001925 **
              -1.777e+01 3.820e+00 -4.651 4.25e-06 ***
## nox
## rm
              3.810e+00 4.179e-01 9.116 < 2e-16 ***
## age
              6.922e-04 1.321e-02 0.052 0.958229
## dis
              -1.476e+00 1.995e-01 -7.398 6.01e-13 ***
## rad
              3.060e-01 6.635e-02
                                    4.613 5.07e-06 ***
## tax
              -1.233e-02 3.760e-03 -3.280 0.001112 **
## ptratio
              -9.527e-01 1.308e-01 -7.283 1.31e-12 ***
              9.312e-03 2.686e-03 3.467 0.000573 ***
## black
## lstat
              -5.248e-01 5.072e-02 -10.347 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.745 on 492 degrees of freedom
## Multiple R-squared: 0.7406, Adjusted R-squared: 0.7338
## F-statistic: 108.1 on 13 and 492 DF, p-value: < 2.2e-16
par(mfrow=c(2,2))
```

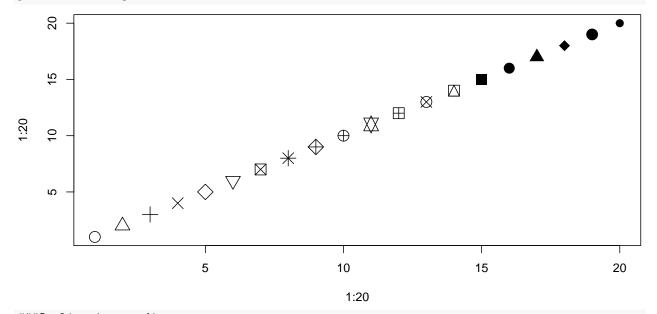
plot(fit3)



```
### Nonlinear terms and Interactions
fit5=lm(medv~lstat*age,Boston)
summary(fit5)
##
## Call:
## lm(formula = medv ~ lstat * age, data = Boston)
## Residuals:
##
               1Q Median
      Min
                               3Q
                                      Max
## -15.806 -4.045 -1.333
                            2.085
                                   27.552
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 36.0885359 1.4698355 24.553 < 2e-16 ***
              -1.3921168  0.1674555  -8.313  8.78e-16 ***
## lstat
## age
              -0.0007209 0.0198792 -0.036
                                              0.9711
## lstat:age
               0.0041560 0.0018518
                                      2.244
                                              0.0252 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.149 on 502 degrees of freedom
## Multiple R-squared: 0.5557, Adjusted R-squared: 0.5531
## F-statistic: 209.3 on 3 and 502 DF, p-value: < 2.2e-16
fit6=lm(medv~lstat +I(lstat^2),Boston); summary(fit6)
##
## Call:
## lm(formula = medv ~ lstat + I(lstat^2), data = Boston)
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -15.2834 -3.8313 -0.5295 2.3095 25.4148
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 42.862007 0.872084
                                   49.15
              -2.332821
## lstat
                          0.123803 -18.84
                                             <2e-16 ***
## I(lstat^2)
              0.043547
                          0.003745
                                    11.63
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 5.524 on 503 degrees of freedom
## Multiple R-squared: 0.6407, Adjusted R-squared: 0.6393
## F-statistic: 448.5 on 2 and 503 DF, p-value: < 2.2e-16
attach (Boston)
par(mfrow=c(1,1))
plot(medv~lstat)
points(lstat,fitted(fit6),col="red",pch=20)
fit7=lm(medv~poly(lstat,4))
points(lstat,fitted(fit7),col="blue",pch=20)
```



plot(1:20,1:20,pch=1:20,cex=2)



###Qualitative predictors

fix(Carseats)

names(Carseats)

[1] "Sales" "CompPrice" "Income" "Advertising" "Population"
[6] "Price" "ShelveLoc" "Age" "Education" "Urban"
[11] "US"

summary(Carseats)

Sales ${\tt CompPrice}$ Income Advertising : 0.000 : 77 : 21.00 Min. : 0.000 ## Min. Min. Min. 1st Qu.: 5.390 1st Qu.:115 1st Qu.: 42.75 ## 1st Qu.: 0.000 Median : 7.490 Median:125 Median : 69.00 Median : 5.000 : 7.496 Mean : 68.66 ## Mean Mean :125 Mean : 6.635 3rd Qu.: 9.320 3rd Qu.:135 3rd Qu.: 91.00 3rd Qu.:12.000

```
:16.270
                    Max.
                           :175
                                 Max.
                                        :120.00
                                                  Max.
                                                         :29.000
   Max.
##
                                                    Age
     Population
                      Price
                                   ShelveLoc
                         : 24.0
         : 10.0
                   Min.
                                  Bad
                                        : 96
                                               Min.
                                                     :25.00
   1st Qu.:139.0
                   1st Qu.:100.0
                                  Good : 85
                                               1st Qu.:39.75
##
  Median :272.0
                 Median :117.0
                                  Medium:219
                                               Median :54.50
  Mean
          :264.8
                         :115.8
##
                 Mean
                                               Mean
                                                     :53.32
   3rd Qu.:398.5
                   3rd Qu.:131.0
                                               3rd Qu.:66.00
##
  \mathtt{Max}.
          :509.0 Max.
                          :191.0
                                               Max.
                                                     :80.00
##
     Education
                  Urban
                              US
## Min.
          :10.0
                  No :118
                           No :142
## 1st Qu.:12.0
                 Yes:282
                          Yes:258
## Median :14.0
## Mean
          :13.9
## 3rd Qu.:16.0
## Max.
          :18.0
fit1=lm(Sales~.+Income:Advertising+Age:Price,Carseats)
summary(fit1)
##
## Call:
## lm(formula = Sales ~ . + Income:Advertising + Age:Price, data = Carseats)
## Residuals:
               1Q Median
                               3Q
      Min
                                     Max
## -2.9208 -0.7503 0.0177 0.6754 3.3413
##
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                      6.5755654 1.0087470
                                           6.519 2.22e-10 ***
## CompPrice
                      0.0929371 0.0041183 22.567 < 2e-16 ***
## Income
                      0.0108940 0.0026044
                                           4.183 3.57e-05 ***
## Advertising
                      0.0702462 0.0226091
                                            3.107 0.002030 **
## Population
                      0.0001592 0.0003679
                                            0.433 0.665330
## Price
                     -0.1008064  0.0074399  -13.549  < 2e-16 ***
## ShelveLocGood
                      4.8486762 0.1528378 31.724 < 2e-16 ***
## ShelveLocMedium
                      1.9532620 0.1257682 15.531 < 2e-16 ***
## Age
                     ## Education
                     -0.0208525 0.0196131 -1.063 0.288361
## UrbanYes
                     0.1401597 0.1124019
                                           1.247 0.213171
## USYes
                     -0.1575571 0.1489234
                                          -1.058 0.290729
## Income: Advertising 0.0007510 0.0002784
                                            2.698 0.007290 **
## Price:Age
                     0.0001068 0.0001333
                                            0.801 0.423812
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.011 on 386 degrees of freedom
## Multiple R-squared: 0.8761, Adjusted R-squared: 0.8719
## F-statistic:
                210 on 13 and 386 DF, p-value: < 2.2e-16
contrasts(Carseats$ShelveLoc)
##
         Good Medium
## Bad
            0
                   0
## Good
            1
```

```
## Medium
             0
###Writing R functions
regplot=function(x,y){
  fit=lm(y-x)
  plot(x,y)
  abline(fit,col="red")
attach(Carseats)
regplot(Price,Sales)
    15
                        0
                         0
          0
    10
                      0 0
                               00
                             0 0
    2
                                                                           0
                                                                                       0 0
    0
                      50
                                              100
                                                                     150
                                                  Х
regplot=function(x,y,...){
  fit=lm(y~x)
  plot(x,y,...)
  abline(fit,col="red")
regplot(Price, Sales, xlab="Price", ylab="Sales", col="blue", pch=20)
    15
    10
    2
    0
                       50
                                              100
                                                                     150
                                                 Price
```