In a calculus course I TA'd once I noticed a very common mistake was to carry a derivative into the operand of a log function, like for $x(t)$,

$$(\ln x)' = \ln x' \tag{*}$$

I thought it would make an interesting problem to find such an $x(t)$ for which (*) holds.