

CE-1901-11 - Dr. Durant - Quiz 6
Fall 2016, Week 7 Quiz

1. (4 points) Simplification and implementation: $F(abcd) = \sum_m(0, 1, 3, 5, 7, 9, 11, 13, 15) + d(12, 14)$

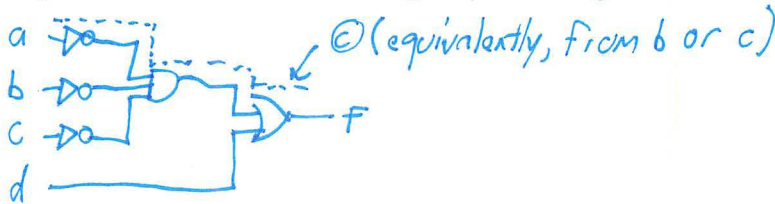
- a. (2 points) **Draw** the K-map and use it to **derive** a simplified SOP expression taking advantage of these don't cares.

ab \ cd	00	01	11	10
00	* 1	1	1	
01		1	1	
11		1	1	
10	X	1	1*	X

$$F = \bar{a}\bar{b}\bar{c} + d = \overline{a+b+c} + d$$

answer

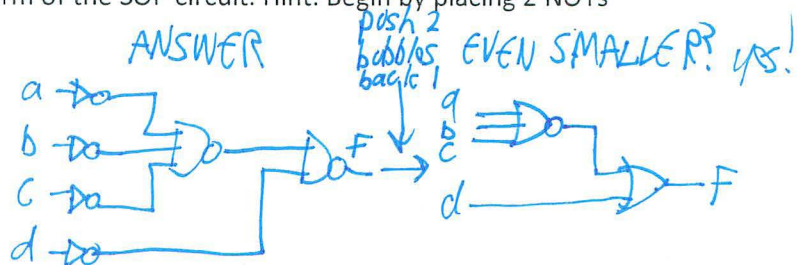
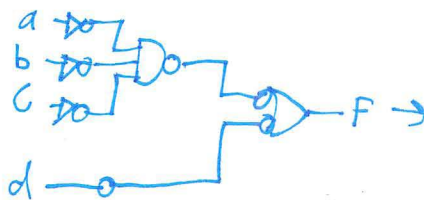
- b. (1 point) **Draw** the SOP schematic using NOT-AND-OR gates.



- c. (1 point) **What** path of gates is involved in the propagation delay (critical path) of this circuit? (illustrate in part b)
- d. (0.5 point) **How** many CMOS transistors does this require? Show your calculations.

3 NOT	6
1 AND3	8
1 OR2	6
	<u>20</u>

- e. (1 point) **Draw** the NOT-NAND-NAND form of the SOP circuit. Hint: Begin by placing 2 NOTs in series on each input to the OR.



- f. (0.5 point) **How** many CMOS transistors does this require? Show your calculations.

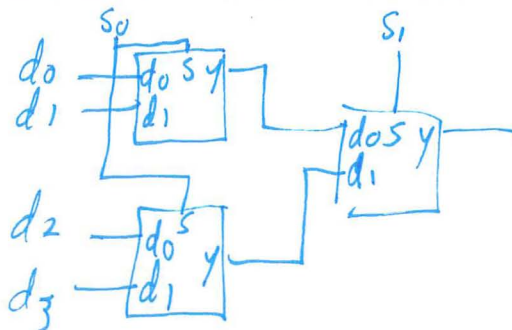
4 NOT	8	NOR-OR	1 NOR3	6
1 NAND3	6	opt	1 OR2	6
1 NAND2	4			<u>12</u>
	<u>16</u>			

2. (3 points) MUXes

- a. (1 point) **Write** the logic equation for the 4:1 MUX, $y = f(s_{1..0}, d_{0..3})$. Remember that there is a product term for each of the data terms; this product term checks all values of s to make sure they match the term's corresponding s -minterm.

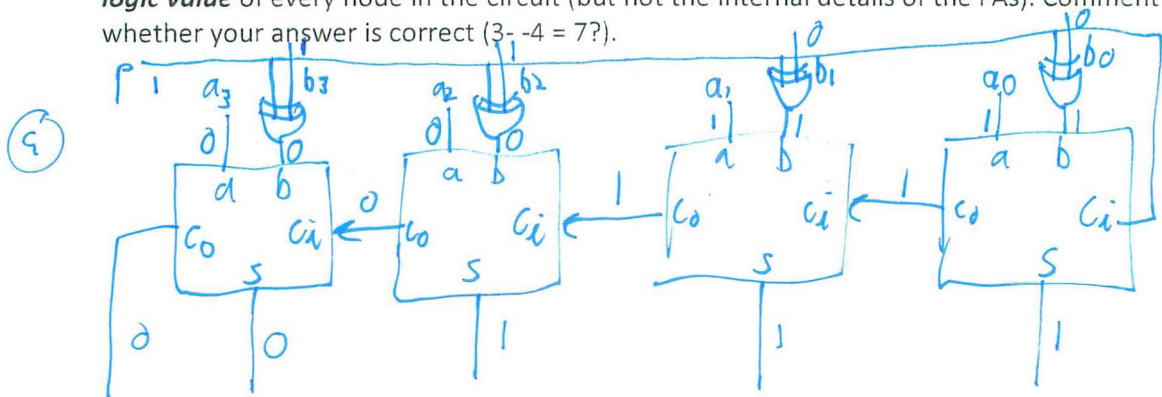
$$y = \bar{s}_1 \bar{s}_0 d_0 + \bar{s}_1 s_0 d_1 + s_1 \bar{s}_0 d_2 + s_1 s_0 d_3$$

- b. (2 points) Using a block diagram **show** how a 4:1 MUX can be made from 3, 2:1 MUXes.



3. (3 points) Subtraction

- a. (2 points) **Draw** the block diagram for the 4-bit ripple-carry adder-subtractor (RCAS4). Use full adder (FA) blocks. **Hint:** You need a "sub"tract input and 4 XOR2 gates.
- b. (1 point) **Label** the inputs to your RCAS3 so that it is subtracting $B = -4$ from $A = 3$. **Show the logic value** of every node in the circuit (but not the internal details of the FAs). Comment on whether your answer is correct ($3 - -4 = 7$?).

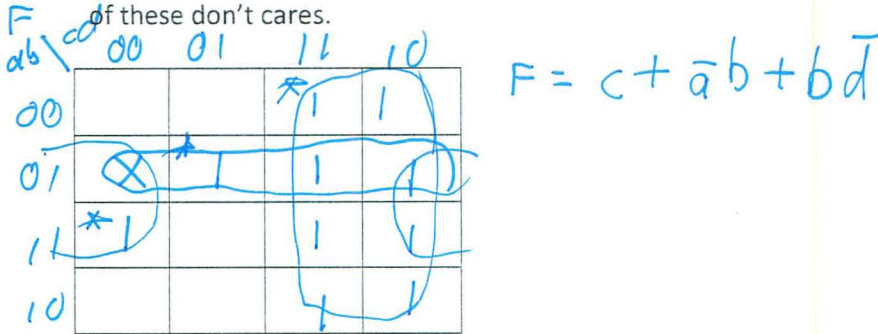


answer = $0111_2 = 7_{10}$ ✓

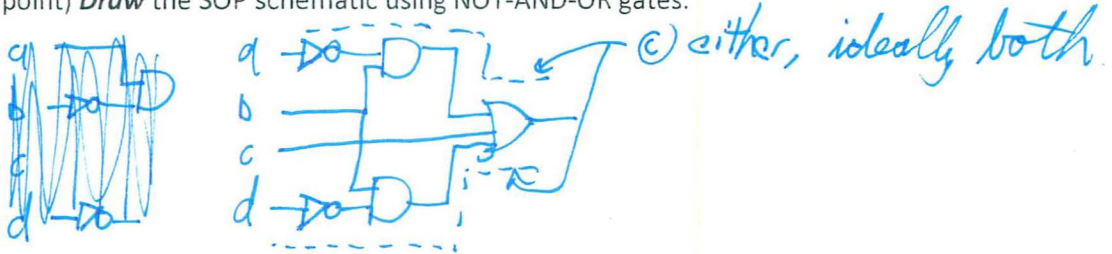
-4: $0100 \neq 4$
 $1011 \in \mathbb{N}$
 $\boxed{1100} \leftarrow +1$
 \uparrow
 -4

CE-1901-12 – Dr. Durant – Quiz 6
Fall 2016, Week 7 Quiz

1. (4 points) Simplification and implementation: $F(abcd) = \sum_m(2, 3, 5, 6, 7, 10, 11, 12, 14, 15) + d(4)$
a. (2 points) **Draw** the K-map and use it to **derive** a simplified SOP expression taking advantage of these don't cares.



- b. (1 point) **Draw** the SOP schematic using NOT-AND-OR gates.



- c. (1 point) **What** path of gates is involved in the propagation delay (critical path) of this circuit? (illustrate in part b)

- d. (0.5 point) **How** many CMOS transistors does this require? Show your calculations.

2 NOT	4
2 AND2	12
1 OR3	8
	24

- e. (1 point) **Draw** the NOT-NAND-NAND form of the SOP circuit. Hint: Begin by placing 2 NOTs in series on each input to the OR.



- f. (0.5 point) **How** many CMOS transistors does this require? Show your calculations.

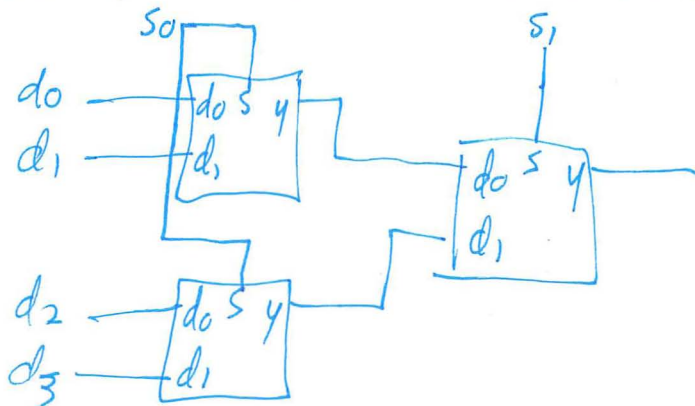
3 NOT	6
2 NAND2	8
1 NAND3	6
	20

2. (3 points) MUXes

- a. (1 point) **Write** the logic equation for the 4:1 MUX, $y = f(s_{1..0}, d_{0..3})$. Remember that there is a product term for each of the data terms; this product term checks all values of s to make sure they match the term's corresponding s -minterm.

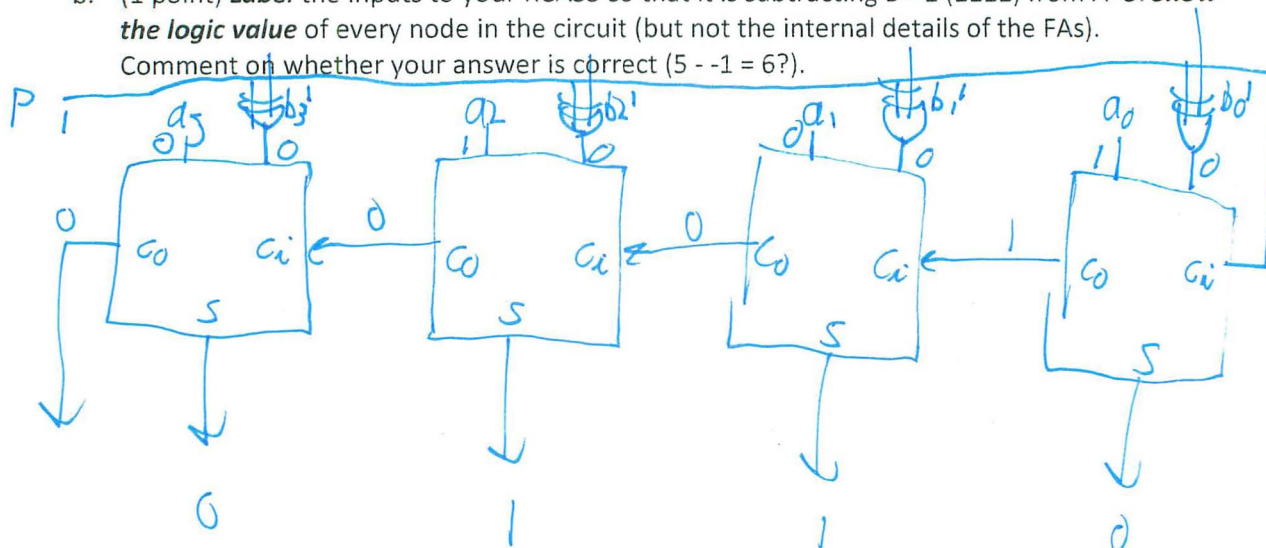
$$y = \bar{s}_1 \bar{s}_0 d_0 + \bar{s}_1 s_0 d_1 + s_1 \bar{s}_0 d_2 + s_1 s_0 d_3$$

- b. (2 points) Using a block diagram **show** how a 4:1 MUX can be made from 3, 2:1 MUXes.



3. (3 points) Subtraction

- a. (2 points) **Draw** the block diagram for the 4-bit ripple-carry adder-subtractor (RCAS4). **Use** full adder (FA) blocks. **Hint:** You need a "sub"tract input and 4 XOR2 gates.
- b. (1 point) **Label** the inputs to your RCAS3 so that it is subtracting $B = -1$ (1111) from $A = 5$. **Show the logic value** of every node in the circuit (but not the internal details of the FAs). Comment on whether your answer is correct ($5 - -1 = 6$?).



$$S = 0110_2 = 6_{10} \checkmark$$