Name ANNIS

## EE3032 - Dr. Durant - Quiz 6 Winter 2019-2020, Week 6

Recall that the convolution integral is  $y(t) = \int_{-\infty}^{\infty} x(\tau)h(t-\tau)d\tau$ .

Recall that the transfer function can be found by  $H(\omega) = \int_{-\infty}^{\infty} h(t)e^{-j\omega t}dt$ .

- 1. (2 points) Given  $H(\omega) = T \operatorname{sinc}(\omega T/2) \exp(-j\omega T/2)$  and parameter T = 0.1 s, calculate H and present it in polar form for 8, 10, and 12 Hz sinusoidal inputs. Recall that, in general,  $H(\omega)$  is a complex number.
- 2. (2 points) Let the system input  $x(t) = 50 \sin(2\pi \times 8t + 30^\circ)$ . Calculate the (steady-state, sinusoidal) output using transfer function theory. Hint: having H in polar form will be useful.
- 3. (2 points) Now, consider a new system, where  $h(t) = \delta(t+2) \delta(t-2)$ . Describe in words how the output of this system relates to the input by taking advantage of the properties of the  $\delta$  convolved with another function.
- 4. (2 points) Consider h(t) and explain why the system is BIBO stable.
- 5. (2 points) Calculate  $H(\omega)$  for this system.

$$0 = 2\pi f = 2\pi \left[ \frac{\partial}{\partial t} \right] = 0.12$$

$$H(w) = T \sin \left( \frac{wT}{2} \right) e^{-j \frac{wT}{2}} = 0.1 \sin \left( 2\pi \left[ 0.4 \ 0.5 \ 0.6 \right] \right) e^{-j 2\pi \left[ 0.4 \ 0.5 \ 0.6 \right]}$$

$$= \left[ 0.02341 - 0.8\pi \ 0 - 0.61564 - 1.2\pi \right]$$

(2) 
$$f=8Hz$$
, so we  $H=0.02342-0.8\pi$  From #1.  
 $y(x)=50.0.0234$  ain  $(2\pi 8t +30^{\circ}-0.8\pi)$   
 $=1.17$  pin  $(2\pi 8t -\frac{19}{10}\pi)=1.17$  pin  $(2\pi 8t -114^{\circ})$ 

- 3) The system outputs a time, -advanced copy of the signal 2p before the input arrives. It also adds the to an inverted a time -delayed copy of the input 2p after it arrives.
- (4) 5/h(+)/dt = 2< 00 .. BIBO otable

(5) 
$$H(w) = S[S(t+2) - S(t-2)] e^{-jut} dt = e^{-jw^2} - e^{-ju\cdot 2} = e^{-j2w}$$

Correction: Divide by j $\omega$  due to integral, simplify:  $2 \sin(2\omega)/\omega = 4 \sin(2\omega)$ .