Name Aswers

EE3032 - Dr. Durant - Quiz 5 Winter 2019-2020, Week 5

Recall that the convolution integral is $y(t) = \int_{-\infty}^{\infty} x(\tau)h(t-\tau)d\tau$ and that convolution is commutative.

2 points
1. Circle those of the following system properties that are necessary for an impulse response to exist and, therefore, for convolution to apply Linear Time-invariant, Causal, BIBO stable

2. Let h(t) be an impulse response that has non-zero values only between t=0 and 5 s. Let x(t) be a system input that has non-zero values only between t=-2 and 7 s.

a. Using the width property, calculate when the output may have non-zero values.

b. Explain why the system is or is not causal.

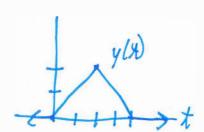
 $G \longrightarrow C^{-2}, 7]$

(b) Causal system (5 h(t)=0 4t<0
"For all"

3. (5 points) Let x(t) = h(t) = u(t) - u(t-2). Calculate y(t) using convolution. You may use any combination of the graphical and analytical approaches. Show your work and fill in your final answer in the blanks below.

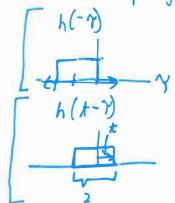
$$y(t) = \begin{cases} 0, t \le 0 \\ \frac{1}{4}, 0 \le t \le 2 \\ \frac{4-1}{4}, 2 \le t \le 4 \end{cases}$$

$$\{0, t \ge 4\}$$



x(+)=L(x)

Width proporty: CO, 2] + CO, 2] = [O, 4] : y(x)=0 \ t < 0 \ t < 4 h(-7)



Partial, incleasing overlap For OSXS2 y(t) = Area of overlap rectargle = width × height = wed th x (height h x height x) = t. (1.1) = +

Partial, decreasing overlop For 2= x= 14

$$y(x) = \text{area } q \left(x(h) \cdot h(t-\gamma) \right)$$

= $w_1 d_1 h \times H_{21} g_1 d_2 =$
= $\int_{t-2}^{2} |\cdot| d\gamma = 2 - (t-2) = 4 - t$

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% EE3032 Winter 2019-20 Quiz 4 Problem/
3 Solution
dt = 0.01;
t = -1:dt:3;
x = zeros(size(t));
x(t)=0 & t<=2) = 1;
h = x;
y = dt*conv(x,h);
ty = (2*t(1)):dt:(2*t(end)); % width/
property
plot(t,x, t,h, ty,y)
legend('x(t)', 'h(t)', 'y(t)')
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