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Poetry of Programming

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These notes are being written for the MAT245 course at Akita International University in Japan. The content is not complete and stable yet, but each version is meant to be consistent and thus usable for self-study. Comments are welcome! When reporting errors please specify the version number. The latest version can be downloaded from https://egri-nagy.github.io/popbook/

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As science and technology advance, their fundamental ideas get simpler and better explained. Similarly, computer programming has also become more accessible. Being a software engineer is still as back-breaking as it ever was, but now the thrills of problem solving by instructing computers can be experienced with a little effort.

Here we aim to introduce the ideas of programming in a pure and minimal way. We focus more on conversations with a computer and less on the tools required for software engineering. Hence the language choice: the functional core of Clojure in its interactive command line REPL (read-eval-print-loop). Clojure is from the Lisp family of programming languages. It is an ideal first language with a "cheeky" character: it realizes many programming concepts with ridiculously simple constructs.

"THE PROCESS of preparing programs for a digital computer is especially attractive, not only because it can be economically and scientifically rewarding, but also because it can be an aesthetic experience much like composing poetry or music." – the first sentence of the *Art of Computer Programming* by Donald E. Knuth [5].

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What is programming?

How to instruct computers to do something? How to ask them questions? Computers solve problems in an extremely precise manner, therefore any tasks given to them should also be specified with thorough exactness. Work done by computers has a simple general form: based on input information we would like get the desired output. This observation makes our question more specific. What is the most rigorous way of defining input-output pairs? The mathematical language of functions is the primary form of talking to computers in a programming situation. One way or the other, all programming languages are about using, defining, transforming and composing functions. We specify a function and give its input values, then the computer figures out the value of the function. We say that we call a function and the computer evaluates the function with the given arguments. It is a simplifying view, but roughly this is how the game of programming is played.

Programming is also about writing text. Text interpreted and executed by computers, and – an often neglected aspect – text read by human beings. Thus, written code is also a way of communication between humans. Natural language is used not just for everyday communication, but for expressing personality, emotions and beauty. Similarly, beyond the mundane tasks of application development and maintenance, programming languages can express ideas, ingenuity, wisdom, wit and beauty. Here we aim to develop the ability of appreciating the beauty in written code. Slight difference from poetry is that reading text is not enough. The joy of coding can only be experienced by doing it.

There are three levels of understanding of procedural knowledge, i.e. knowing how to do things.

- 1. Seeing someone else doing it, listening to an explanation.
- 2. Doing it.
- 3. Explaining it to someone else.

Replace 'someone else' by 'computer' in the last item, and you will

"A computational process is indeed much like a sorcerer's idea of a spirit. It cannot be seen or touched. It is not composed of matter at all. However, it is very real. It can perform intellectual work. It can answer questions. It can affect the world by disbursing money at a bank or by controlling a robot arm in a factory. The programs we use to conjure processes are like a sorcerer's spells. They are carefully composed from symbolic expressions in arcane and esoteric programming languages that prescribe the tasks we want our processes to perform." - the auspicious beginning of legendary MIT programming textbook, colloquially known as SICP [1].

see why writing computer programs is an efficient way of understanding the world around us. Writing code for problem solving requires the ability of pulling things apart and rebuild them from primitive building blocks.

Learning a programming language is like learning a foreign language, but easier and faster than that. The 'grammar', the syntax is less complex, and 'meaning', the semantics, is aimed to be unambiguous. So learning a programming language is easy, while learning a natural language is more difficult. Exactly the opposite what people would think.

The purpose of this essay formed tutorial is to give a lightning-fast introduction to the core Clojure language. By reading and rereading this text and by trying out the examples one should gain enough knowledge to tackle programming puzzles in the style of https://4clojure.com. The imagined reader is someone who may not become a professional software developer, but do not want to miss out on this intellectual adventure (for instance, modern Liberal Arts students). People with some programming experience may find the exposition peculiar if not revolting. The code examples are chosen for maximizing the speed of worldview expansion. This may not coincide with the best practices and accepted idioms for writing efficient and readable code. It is assumed, that the reader will acquire good taste by writing and reading code, and not by merely reading a tutorial text.

What is the purpose, benefit of learning programming? Beyond the oft-repeated usefulness of programming due to the pervasiveness of computing, *learning to code will teach you how to think clearly and efficiently*. And this will be helpful in whatever profession/field you will be working in.

WARNING!!! This text is dense. It introduces at least one new concept in each example. Reading without trying out the examples will have little effect. Copy-pasting is also discouraged, since it does not really contribute to the learning process. Play in the REPL!



http://clojure.org/

Function composition first

Programming computers can be done by using functions. But what exactly are functions? We assume at least some vague memories of functions from school, like $f(x) = 4x^2 + 2x - 4$. A function takes a value and produces another value. In this example the input value is a number, for example x = 1, in which case f produces the output f(1) = 2, since $4 \cdot 1^2 + 2 \cdot 1 - 4 = 4 + 2 - 4 = 2$. Almost all examples of functions in high school math take numbers and produce numbers. This is a very limited usage of the function concept. In general, the input of a function can be anything, text or some composite piece of information; and the same is true for the output.

What is a function in general? Metaphorically, a function is a machine that can produce outputs from input values. We expect that a machine produces *valid outputs for all meaningful input values*. Thus, the sets of possible inputs and outputs are part of the definition of a function. We also expect that we get the *same output for a particular input all the time* (with the notable exception of probabilistic functions).

It is one thing that we can ask a computer to evaluate a function already available, and it is another thing one to produce a function which is needed for our purpose. This is the difference between being a *user* and a *programmer*. There are basically two ways of constructing new functions:

- 1. Creating new functions by composing existing ones.
- 2. Writing new functions.

Our first goal is to understand function composition as quickly as possible. Composition is in the sense of putting LEGO bricks together.

List notation for functions

For the sake of precision, we need to develop a new notation for functions, which is more suitable for computers. For a function f(x), the input variable is x is also called the *argument* of the function. For

The mathematical definition of a function is just the precise description of the machine metaphor in the language of set theory and mathematical logic. Also, the set of inputs *X* is called the *domain*, while the set of possible outputs is called the *codomain*.

A function $f: X \to Y$ is a subset of the direct product (ordered pairs)

$$X\times Y=\{(x,y)\,|\,x\in X,y\in Y\}$$

such that

- 1. $\forall x \in X, \exists y \in Y : (x,y) \in f$,
- **2.** $\forall x \in X, \forall y_1, y_2 \in Y$:

$$(x, y_1) \in f$$
 and $(x, y_2) \in f \Longrightarrow y_1 = y_2$,

i.e. for each $x \in X$, there is at least and at most one, therefore exactly one ordered pair (x,y) in f.

the computer we write (f x) instead of f(x). The function symbol f jumps behind the parenthesis but keeps a bit of distance from its argument. There can be more than one arguments, for example (g x y z) has three arguments. Even there are functions with no arguments, simply written as (h). All that matters that functions are written as a *list* denoted by parentheses. The first element is the function, the following ones are arguments. By convention, we also call this list of a function and its arguments a *function call*. One can think of this as grammar rule, a minimal syntax: **functions and its input arguments are written as a list of symbols between opening and closing parens, i.e. round brackets** '(' and ')'.

In algebra we also write y = f(x). So where is y? That is the computer's answer. The process of coming up with an answer is *function* evaluation. We can think of the computer as a machine that has a penchant for computing functions. An opening paren triggers this habit, and the first symbol, the name of the function, determines what to do with the rest of the list. The first element of a list is expected to be the name of a function, the rest of the list contains input data items for the function. The default behaviour is to compute the function. So, in order to get answers for computational problems we have to construct functions whose values are the solutions. This is the essence of functional programming.

The simplest function: identity

What is the simplest function? The function that does nothing, f(x) = x. Given the input it just returns it back. In elementary mathematics we rarely talk about more than three functions, so the symbols f, g, h are often enough. In programming we define tons of functions, so naming them is quite an issue (some say the biggest). It is thus important to give functions nice names. We call the simplest function identity.

```
(identity 42)
42
```

It works for numbers as expected. Same for text, but we have to put the sequence of letters and other symbols into double quotes. We will use a more technical term for textual data items, they are *strings*. Numbers and strings are examples of *data literals*. They are values that we write explicitly into the code or the REPL, as opposed to computing them. In other words, they evaluate to themselves. Data literals are literally just data.

```
(identity "Hello World!")
"Hello World!"
```

A precise mathematical theory for describing functions is *lambda-calculus* [3]. Luckily, here we can proceed without learning that formalism. But it nicely explains the λ symbol in the logo.

These are snippets of conversations with the computer. You enter the function call (the first line), then the answer appears below. Instead of writing an essay or book, which will be read by someone else later, we have this interactive, question-answer style communication.

We give the function a traditional geek greeting in a string and it simply gives it back. No surprise, no excitement. So let's do something unusual.

```
(identity identity)
#<core$identity clojure.core$identity@1804686d>
```

Whoa! What's that? We asked for trouble, and we got it. Something scary came up from deep inside the system. It looks like some sort of internal representation of the identity function. We revealed the true identity of identity!

Poking the guts of the system is not our purpose here, so we will not pursue this investigation any further. However, what happened offers a remarkable insight. Functions can take functions as arguments. While identity does this only as a contrived case, we will see that there are functions designed to take other functions as arguments and return functions as well. This is a big deal, this is what makes functional programming functional.

Growing and shrinking numbers: inc dec

Let's pretend we don't have the numbers (except zero), so we need to construct them. In mathematics, in order to build the set of natural numbers $\mathbb{N} = \{0,1,2,3,\ldots\}$, we need only two things: zero and the function f(x) = x + 1. Thus, 1 = f(0), 2 = f(f(0)), 3 = f(f(f(0))), and so on. In Clojure this function is called inc, as an abbreviation for incrementation.

```
(inc 0)
1
```

How can we do bigger numbers? Just like in math, nesting the function, using our slightly different notation.

```
(inc (inc (inc 0)))
3
```

Observe, that when a value is expected, we can simply call another function, since functions produce values. So in the general scheme of (f x), the argument x can be replaced by something like (g y). For (f (g y)) Clojure will evaluate (g y) first, then the value will be fed into f. **Function calls can be nested.** By the way, we can also construct negative numbers by dec.

```
(dec 0)
-1
```

And no worries, we have all the numbers in Clojure.

Other computers may give slightly different answer, as this internal representation of functions is system-dependent.

Let's say, we have a faulty keyboard. The digit keys do not work, except zero. Therefore, we do not have a way to enter numbers. Not a realistic scenario, but in foundational investigations in mathematics it is a very important tool (see Peano axioms).

'Nesting' in computing means that some object can contain some other object of the same kind. In other words, information is represented in a hierarchical manner.

Composition: comp

Nesting function calls has the unwanted effect of parentheses piling up. We can spare them by a simple trick. Instead of nesting the function calls, we can combine the functions first then apply the composite function to the argument. In mathematics we write

$$f \circ g(x) = f(g(x)),$$

```
while in CLOJURE
((comp f g) x)
means
(f (g x)).
```

Note the order, the rightmost function in the composition gets executed first.

We can compose arbitrary number of functions.

```
((comp inc inc inc) 0)
4
```

If f(x) = x + 1, then we would write this with function composition \circ in algebra as $(f \circ f \circ f \circ f)(0)$ instead of f(f(f(f(0)))). The calculated value is the same, but the two solutions are different, in a – let's say – ontological, metaphysical sense. In the composition case a new entity, a new function is created.

We can compose different functions, if the output of one function can be eaten by the other function. This is true for inc and dec since they expect and produce numbers.

```
((comp inc dec) 1)
1
```

Here we create a function that takes a number, decrements it, then increments the result. This is of course just a very roundabout way of saying that we want the identity function for numbers.

The general identity function can also be produced by comp. Given no arguments, it exactly returns that.

```
((comp) 19)
19
```

Consequently, comp works for a single argument as well. Given a function, it composes the function with the identity function, so (comp inc) is very much like inc.

The importance of the identity function becomes obvious on the level of abstract algebra: it is the neutral element of functions under composition. What this means for everyday programming is that we have sensible defaults. While most of the time we want to compose two or more functions, nothing bad happens if we try that with less.

Arithmetic done with functions

Computers, before they did anything else, performed arithmetic calculations. We do not usually think about arithmetic calculations in terms of applying functions, we just simply add, subtract, multiply and divide numbers. This is an inconsistency on our side. It is better to get rid of it, so we will write arithmetic calculations as function applications.

The basic operations: + - * /

Addition is the simplest algebraic operation. Here it is in LISPY style.

```
(+ 2 3)
5
```

Very unusual after writing 2 + 3 for many years, but there are numerous benefits. First of all, when adding more than two numbers together, we do not need to repeat the + symbol.

```
(+ 1 2 3 4)
10
```

A function can have different number of arguments, from zero to many. Surprisingly, we can do addition and multiplication with less than two arguments.

```
(+ 17)
17
(+)
0
(*)
1
```

When there is no argument, + and * are constant functions. The default values they give come from abstract algebra (additive and multiplicative identities, neutral elements). For subtraction and division both (-) and (/) complain about not having arguments. But their one argument versions do rely on the default values.

```
(- 1)
-1
(/ 2)
1/2
```

Yes, CLOJURE can do rational numbers (but CLOJURESCRIPT has a weaker host, so it cannot).

Another benefit of the function notation is that there is no need for precedence rules. What is the value of $2+3\cdot 4$? Well, it depends. There are two possibilities $(2+3)\cdot 4=20$, and $2+(3\cdot 4)=14$. So we have to put the parens or agree that multiplication has to be done first. In Lisp the problem is non-existent.

```
(+ 2 (* 3 4))
14
(* 4 (+ 2 3))
20
```

The price to pay: unusual notation; the gain: no ambiguity.

We can also use numbers with decimal fractions, but they are 'contagious'. Once they appear in an arithmetic expression, the result turns into a decimal number as well.

```
(* 2 (+ 1 2 3.45))
12.9
(/ 0.7 2)
0.35
```

Being a hosted language means that inner workings of the language are written in a different language. For CLOJURE the host is JAVA, for CLOJURESCRIPT it is JAVASCRIPT. This also explains why the error messages look so strange (or familiar): they come from the underlying host.

Asking yes-or-no questions: predicates

The simplest type of questions are where the answer is yes or no. These are called *predicates* in mathematics, and the computer says true and false instead of yes and no. It is a nice habit to name predicates ending with a question mark.

```
(zero? 0)
true
(zero? 1)
false
(neg? -1)
true
(pos? -1)
false
```

Some predicates are so obvious that they don't even need a question mark to signal their nature. We could say smaller? but we got used to < in mathematics, and the latter is lot easier to type.

```
(< 0 1)
true
(= 1 1)
true
(= 0 1)
false</pre>
```

We can check the equality of more than two things in one go.

```
(= 1 (dec 2) (inc 0) (/ 7 7) (+ 3 -2))
true
```

Similarly, we can conveniently check whether the arguments are strictly increasing or non-decreasing.

It's not exactly a top achievement that the computer can tell that zero is smaller than one. This is just for demonstrating the way of asking the questions. The real usage of predicates will be clear when will use symbols that can mean a wide range of values. Much like in math, 3 < 4 is a fact, but x < 4 is an expression that depends on x, and divides the set of real numbers into two sets (solutions and non-solutions).

```
(< 1 2 3 4 5 6)
true
(< 1 2 2 3)
false
(<= 1 2 3 4 5 5)
true</pre>
```

The nature of things: types

Things can be classified according to their nature, based on what they are. Forty-two is a number, comp is a function. In computing these classes are called *types*.

```
(number? 42)
true
(number? comp)
false
(fn? 42)
false
(fn? comp)
true
```

There are further distinctions for numbers, roughly following the types of numbers we have in mathematics.

```
(integer? 3)
true
(rational? (/ 1 2))
true
```

However, there are some subtle differences from the mathematical classification of numbers. Numbers with decimal fractions have a different representation, bit more complicated then storing integer numbers. They are called *floating point* numbers. So 3 is the same as 3.0, but their types are different.

```
(integer? 3)
true
(float? 3)
false
(integer? 3.0)
false
(float? 3.0)
true
```

CLOJURE is strongly and dynamically typed, meaning that every data item has a well-defined type which is checked when the program is running. So, you don't need to type types (no pun intended).

Strings

In elementary mathematics we mainly deal with functions that take numbers and produce numbers. As a departure from that, we introduce functions that work with textual information.

First terminology. In computing letters are called *characters*, and words and sentences are called *strings*. This is not just arbitrary naming, it's more like abstraction, by being a more general concept, we can cover more things: characters are not just letters, but numerical digits, punctuation marks, other signs, whitespaces and control characters. A character is a symbolic unit of information. In Clo-Jure characters are denoted by a starting backslash.

```
(char? \a)
true
(char? \8)
true
(char? 8)
false
```

Strings are sequences of characters. The sequence can be empty, or just a few characters long, or a whole novel. They are denoted by double quotes.

```
(string? "tumbleweed")
true
(string? "")
true
(string? "Alice: How long is forever?")
true
```

Strings and characters are different things. This is easy to see as strings tend to have more than one character, but the edge case of a string consisting of a single character might be confusing.

```
(= \a "a")
false
```

Similarly, a number and a sequence of characters (digits) are of different *types* of data. Therefore, they are not equal even if in some sense, for us, they represent the same quantity.

```
(= 42 "42")
false
```

This also shows a fundamental fact: anything can be represented as text, therefore as strings. We can create strings from anything by using the str function. It takes arbitrary number of arguments, converts each arguments into a string, then joins them into one string.

```
(str \a \b \c \space \1 2 (inc 2))
"abc 123"
```

Before we introduce other string functions, it makes sense to do a technical step to avoid typing much. For example, there is a function called upper-case that given a string returns another with the same letters but all capital. This function's full name is clojure.string/upper-case. It's rather long and it would be tedious and unreadable to type it often. After entering

```
(require '[clojure.string :as string])
```

we can use advanced string functions easily.

```
(string/upper-case "old pond frog leaps in water's sound")
"OLD POND FROG LEAPS IN WATER'S SOUND"
(string/capitalize "i forgot.")
"I forgot."
(string/capitalize (str/lower-case "DO NOT SHOUT!"))
"Do not shout!"
```

Much of string processing is about dealing with parts of strings (substrings).

```
(string/ends-with? "banana" "na")
true
(string/starts-with? "apple" "pp")
false
```

A powerful way of transforming strings is by replacing substrings.

```
(string/replace "Banana and mango." "an" "um")
"Bumuma umd mumgo."
```

What happens here is that string functions live in a different *namespace*, which is like being in a folder. We just give a more convenient access to that folder. Other programming languages might say that we load a library. Organizing your software properly into namespaces, modules, libraries is a very important part of software engineering, but it will not be discussed here.

The most advanced way of dealing with strings is using *regular expressions*, which is sort of a mini language itself.

List, the most fundamental collection

Programmer's life would be quite easy if there were only scalar values, like numbers. These are like the atoms of data. However, the world is more complicated than that, so the data describing everything around us comes in bigger chunks. *Data structures* are combinations of scalar data and other data structures. Simple scalar data items are the 'atoms', while compound data structures are the 'molecules' of the world of information.

Creating lists

Lists are the most fundamental data structures in Lisp-like languages. They are simple a bunch of items in a sequence inside a pair of parentheses. Looks familiar? Sure! We have been using them from the beginning. Function calls are represented as a list. Given a list, Clojure will try to call the first element as a function with the remaining elements as arguments. It is so eager to evaluate, that if we just want to have a plain list of numbers, then we need to tell Clojure explicitly to stand back and not to try to evaluate the list as a function call. We have to quote the list. Otherwise, we get an error message saying that a number is not a function.

```
'(1 2 3)
(1 2 3)
```

The apostrophe is just a shorthand notation. The full form of quoting looks like a function call.

```
(quote (1 2 3))
(1 2 3)
```

However, if you have the suspicion that quoting is not really a function call (since the argument is not evaluated), then you are right. It is a *special form*.

Alternatively, we can use the list function that takes arbitrary number of elements and put them together in a list.

The name LISP stands for LISt Processing.

This is the code-as-data philosophy of Lisp. The technical term is *homoiconicity*, the same-representation-ness in ancient Greek. The upshot is that programs can work on lists, and programs are written as lists, so programs can work on themselves.

For now it is enough to know that the purpose of special forms is to do things that are not function calls.

```
(list (* 6 7) (inc 100) (/ 9 3))
(42 101 3)
```

We can also construct a bigger list by combining an element and a list.

```
(cons 0 (list 1 2 3))
(0 1 2 3)
```

Here we called the cons function with a number 0 and a list (1 2 3) freshly created by list,



and it returned a longer list containing \emptyset as well, attached to the beginning of the list.



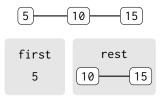
There is no restriction on what sort of elements you can have in a list.

```
(cons "a string!" (list 1 2 3))
("a string!" 1 2 3)
```

The structure of lists

How about if we want to dismantle a list? That can be done along the same scheme: we separate the first element and the rest of the list.

```
(first '(5 10 15))
5
(rest '(5 10 15))
(10 15)
```



The name of nothing: nil

Now, a tricky question. What is the first element of the empty list? Well, it's nothing. But remember, the computer needs precision, we have to be exact even when we talk about nothing. Therefore nothing, the void, the vacuum, the nonexistent, the empty, the oblivion is called nil.

Lists prefer to connect to elements in the front. The first element is the most accessible one, for all the other we have to walk through the sequence.

Historically these functions first and rest were called car and cdr referring to memory locations in the IBM 704 computer, in the late 1950s. And continued to be called like that long after those machines disappeared. Sometimes it is nice to break with the tradition.

```
(first ())
nil
```

Note that the empty list needs no quoting, since there is no danger to take the first element as a function. Only nothing is nothing, everything else is something.

```
(nil? 0)
false
(nil? ())
false
(nil? false)
false
(nil? nil)
true
```

What is the rest of the empty list? We agreed that rest will return a list no matter what. Also, we cannot produce a non-empty list from thin air. That leaves only one choice.

```
(rest ())
()
```

Size of a list

We can ask for the number of elements contained in a list.

```
(count '("a" \b 1.2))
3
```

There is a predicate for deciding whether a list is empty or not.

```
(empty? ())
true
(empty? '(1 2))
false
```

If empty was not available, how can we test for emptiness? We could use the size of the list. For example, (zero? (count '(1 2))).

Concatenation

We can build lists by using other lists as building blocks, by connecting them in a given order.

```
(concat '(1 2) '(3 4))
(1 2 3 4)
(concat '(3 4) '(1 2) '(5 6))
(3 4 1 2 5 6)
```

concat can take arbitrary many arguments, including one and zero.

```
(concat '(\a \b c))
(\a \b \c)
(concat)
()
```

Concatenating a single list is just that list. Concatenating nothing is just another way to produce the empty list.

reverse and last

Here are two self-explanatory functions for lists.

```
(reverse '(1 2 3 4))
(4 3 2 1)
(last '(5 6 7))
7
```

But what if only reverse was available. Could we somehow get the last element of the list without last? The last element is the same as the first of the reversed list. We have first, so simple function composition works.

```
((comp first reverse) '(5 6 7))
7
```

This is a recurring theme in the learning process. Pretend that some existing function is not available, then write it.

Vector, sequential collection that is also a function

Vectors are sequences of some elements enclosed within square brackets. On the surface they very much look like lists, but with a different delimiter. We'll see later that differences between lists and vectors are fundamental. We can create a vector the short way as a data literal

Using other delimiters beyond parentheses is a great innovation of CLOJURE.

```
[1 2 "three"]
```

or the long way, by using the vector function

```
(vector 1 2 "three")
[1 2 "three"]
```

or we can turn another collection (here a list) into a vector.

```
(vec '(1 2 "three"))
[1 2 "three"]
```

Even just on the surface, vectors are great because we don't need to quote them. A vector is not a list so no one tries to evaluate it as a function call. So whenever we want to write down a sequence of elements, we'd better use vectors. The differences between lists and vectors are lot deeper than this. In a list we can access its elements one-by-one, walking through its structure by first and rest. If we want to get the last, we have to visit each element. Vectors are more accessible. They are *indexed*, meaning that each element has an associated integer number starting with 0. For instance, the vector ["a" "b" "c"] can be visualized as a lookup table.

It is like a function that produces elements for index numbers. Indeed!

```
(["a" "b" "c"] 0)
"a"
(["a" "b" "c"] 2)
"c"
```

In mathematics we say the vector is a map from \mathbb{N} , the set of natural numbers to a set of objects (the things we can store in a vector).

Now this is something that really widens the concept of a function! A data structure that doubles as a function. Yet another example of data-as-code. A weird puzzle:

```
((comp ["a" "b" "c"] [2 1 0]) 0)
"c"
```

Why?

There is of course a more pedestrian way to get the values from a vector. We can just ask for the *n*th element.

```
(nth ["foo" "bar"] 0)
"foo"
(nth ["foo" "bar"] 1)
"bar"
```

Accessing the elements of vectors is not as forgiving as first, rest for lists. Using an index goes beyond the elements in the lists results in an error.

Constructing a bigger vector can be done by conjoining an element.

```
(conj [11 13 17] 19)
[11 13 17 19]
```

Vectors like to connect at the end and it is easy to see why. Connecting anywhere else would mess up previous associations. Note that the order of the arguments for conj reflects this, just as in cons for lists.

Making memories

The difficulty of talking to a mathematician lies in the continuous demand for defining all the terms. 'What exactly do you mean by that?' – the oft-repeated question asks about the meaning attached to words. Same for the computer, everything has to be defined. For instance, (+ x 1) has no meaning unless x is defined. Luckily, we can attach meaning to x. We just call this process differently: *symbol binding*. This can be done in two ways, one permanent and one temporary.

Long term memories

With def we can permanently associate a name with a value. Though seemingly follows the syntax of function call, def is another special form.

```
(def x 2)
```

So, x now refers to a value, which is its meaning.

Once defined, we can use the name x, and it will evaluate to its bound value. Wherever we want to use 2, we can write x instead. The computer will know what we are talking about.

```
(+ x 1)
3
```

In technical language, we call the words with meaning used in CLOJURE *symbols*. The symbols can be just single letters, or a sequence of letters mixed with numbers and some other signs like ?,-,_, etc.. We can also tell CLOJURE to stop figuring out the attached meaning. If we quote a symbol, we get the symbol back.

```
'x
x
```

We don't display how the REPL reports successful definitions. It varies for different REPLs.

Where are these definitions stored? It is called the *environment*, and it is the memory where every well-formed expressions in the REPL gets its meaning from. This can be thought of as long-term memory. This metaphor gives a hint why that redefining memories is not a good idea.

Since both symbols and strings are just sequences of characters, it is very important to distinguish them. The string "x" is a data literal, just a piece of data that evaluates to itself. The symbol x is a name for something else, for example a piece of data or a function. It can also be undefined. Note that quoting symbols and the double quotes for strings are different.

```
(symbol? 'x)
true
(symbol? "x")
false
(string? 'x)
false
(string? "x")
true
```

Short term memories

Often we want to store the results of partial computations, in order to save work. Instead of

```
(+ (* 2 (+ 6 7))
(/ 3 (+ 6 7))
(- 2 (+ 6 7)))
198/13
```

we could do

computing (+ 6 7) only once, not three times. However, this 'pollutes the environment' by leaving r defined. We only want r to have some meaning until we evaluate the expression. let lets us do that.

Here the input spreads over several lines. This is no problem, CLOJUREWILL no that you are not finished when you hit ENTER, since opening parens are not closed yet. When the expression is finished, it will acknowledge that by evaluating it.

The temporary bindings are given in a vector. There can be more bindings, but they should come in pairs: symbol first followed by a value to bind to. The bindings are only valid in the inside let. Yes, this is another special form.

The bindings are done in order, so we can use a binding immediately to define another one.

```
(let [x 1
        y (inc x)
        z (+ x y)]
    (str "x: " x " y: " y " z: " z))
"x: 1 y: 2 z: 3"
```

Defining functions

In a more traditional introduction to programming, defining functions would be the second step, right after the arithmetic operators. In Cloure we have many ways of combining functions and the associative data structures also behave as functions, thus the issue is less urgent. But this does not diminish the significance of crafting functions.

One way to think about functions is that they are great time-saving tools. Same as in algebra, we use a single letter to denote a multitude of choices of things, there most notably numbers. For example, when talking about square numbers, I can mention a few: $5 \cdot 5 = 5^2 = 25$, $11 \cdot 11 = 11^2 = 121$. I can also refer to all square numbers by writing $x \cdot x = x^2$ when x is any natural number. Same happens in programming. We can do concrete calculations,

```
(* 2 2)
4
(* 12 12)
144
```

but soon we would get tired of typing the numbers twice. Alternatively, we can forget about the concrete numerical values, replacing them by a symbol, for instance x. This x is a hole to be filled later. Thus, we get an *abstract expression* (* x x), but in itself this does not make sense, since what is x? We need to attach some meaning to it. For instance, after (def x 2) the expression (* x x) evaluates to 4; after (def x 12) to 144. So far so good, but there are two major problems with this approach. First, we have to be very disciplined by using the symbols: the symbol in the definition has to match the symbol in the abstract expression. Second, we make permanent changes to the environment by attaching meanings to symbols. This may seem harmless first, but in practice the effects could render interacting with the computer totally useless. Imagine two abstract expressions using the same symbol, but expecting different meanings – recipe for disaster.

There is of course a better mechanism for making the abstract ex-

The official term for a 'hole' in an abstract expression is *free variable*.

Humans are really bad at administration. If we have to write the same thing at two different places, sooner or later we will write something else and get genuinely surprised by inconsistent results. pression reusable, and that is the same as creating functions. We plug the whole by saying that it is the input to the function. We need to say that a value for x will be supplied later in the abstract expression by writing (fn [x] (* x x)). By squinting at this, it looks like a let statement, except there is no value bound to x. Where does the meaning come from? Well, this is a function, so whoever calls it will provide the meaning for x.

```
((fn [x] (* x x)) 2)
4
((fn [x] (* x x)) 12)
144
```

In all these examples we create a function, apply it to some argument(s) and throw it away. Coming up with good names for functions is often mentioned as the single most difficult problem in software engineering. So, it is nice to have the option of not naming them when they are short and self-explaining.

Of course, we can make memories, where the value attached to a symbol is a function. We can make a definition (def square (fn [x] (* x x))), but this comes up so often so there is a shortened way to define named functions.

```
(defn square
  [x]
  (* x x))
```

The special form defn reads as 'define function'. The name of the newly defined function is square. The following vector contains the input parameter of the function (here just a single x); then finally comes the *body* of the function: an abstract arithmetic expression. After this function definition, we can calculate square numbers in an elegant way.

```
(square 2)
4
(square 12)
144
```

When the square function is called with number 2, the function's input parameter x is bound to 2, so evaluating its body gives 4. One can think of as substituting a concrete value into x. Important to note, that this assignment is temporary, just valid for the function call. So even if x is defined in the environment, it has no effect on the function's value.

The official term is *lambda function* for anonymous, throw-away functions. Again, see the CLOJURE logo.

```
(def x 3)

(square 10)
100
x
3
```

There is a *global* x and a *local* in the function. The function has its own little environment.

The real great thing about functions, that after writing them we can forget about their details. They are indistinguishable from Clojure's own functions. Therefore, we can use this newly defined function as many times I want, no restrictions.

It is concievable that a function does not have an input argument.

```
(defn greetings
[]
"Hello world!")
```

There is no input to depend on to have different output values, so this is a *constant* function. (greetings) will always evaluate to "Hello world!". Also, the function body is quite simple, just a string literal.

There can be more arguments.

```
(defn rectangle-circumference
  [a b]
  (* 2 (+ a b)))

(rectangle-circumference 3 2)
10
```

Lambda function shorthand notation

Anonymous functions save us from the burden of naming them, but we still need to do some naming. We have to give names to the inputs of the function. Luckily this can be avoided as well.

```
(map #(* % %) [1 2 3 4 5])
(1 4 9 16 25)
```

The hashmark indicates a function literal and the % symbol refers to the argument of the function. If there are more arguments then numbering can be used % or %1 for the first argument, %2 for the second, and so on.

Manual function calls

Given a bag of apples, before eating the fruits we need to unpack them. A bag is one thing, containing several items, here the apples. Removing the container, the paper bag for example, is an essential step.

Removing the packaging is something we need to do in programming as well. There is a clear distinction between a function taking n arguments and another taking a list with n elements. For the latter there is only one argument. For instance, addition expects a bunch of numbers and it would not work with a list or a vector. So, (+ [10 11 12]) gives an error message, since the + function expects numbers and doesn't know what to do with a vector. The numbers are packaged in a vector, + cannot 'eat' them.

The apply function can feed the elements of a collection properly as arguments to a given function. In general,

```
(apply f [x y z])
evaluates to
  (f x y z)
```

which is just calling the function f with arguments coming from the collection.

Here is how apply helps in calculating the sum of numbers in a vector.

```
(apply + [10 11 12])
33
```

The functions max and min take multiple arguments and return the biggest one of them. If we call them with a single argument, they just return that.

```
(max 5)
5
```

There is nothing to compare. Same happens when we call it with a collection.

```
(max [22 11 33])
[22 11 33]
```

This may not be the answer we are looking for. If we want to find the maximal element of the vector, we need to use apply.

```
(apply max [22 11 44 33])
44
```

Similarly, the function str converts its arguments into strings and concatenates them into one big string.

```
(str [\h \e \l \l \o])
"[\\h \\e \\l \\l \\o]"
```

The answer is correct, str turns the vector into a string, but it may not be what we expect. If we want to turn a sequence of characters into a string, then we need to use apply.

```
(apply str [\h \e \l \l \o])
"hello"
```

apply accepts multiple arguments, but only the last argument will be treated as a collection containing more arguments.

```
(apply str "Hello" " " [1 2 3] " " [\w \o \r \l \d \!])
"Hello [1 2 3] world!"
```

Why is it called apply? If the purpose is unpacking collections, then why choosing a name that clashes with the 'applying a function' expression? The answer is simple, because it is really function application. It is somewhat manual: apply takes a function and a collection of arguments and applies that function to the arguments. This process is automatically triggered by the opening paren, but we can also do it explicitly. The same argument as above, just backwards: the automatic function application (f x y z) can also be written as (apply f [x y z]).

Collection unpacking is just a special use case of apply, though probably the most accessible one.

Why the extra backslashes? Backslash is used to indicate characters, so if we want to have backslash as a character, we need to 'backslash' it.

Lazy sequences of numbers

We often need to produce an ascending list of numbers, therefore this task is automated. The range function can produce numbers starting from zero up to a limit.

```
(range 13)
(0 1 2 3 4 5 6 7 8 9 10 11 12)
```

The limit is not included in the result, so (range 0) is a synonym for the empty list.

When two arguments are given to range, they are interpreted as the start of the sequence and the end of the sequence.

```
(range 1 10)
(1 2 3 4 5 6 7 8 9)
```

The third argument can change the step, which defaults to one. We can get produce the even and odd single digit numbers.

```
(range 0 10 2)
(0 2 4 6 8)
(range 1 10 2)
(1 3 5 7 9)
```

range is not limited to integer numbers.

```
(range 1.1 4.2 0.5)
(1.1 1.6 2.1 2.6 3.1 3.6 4.1)
```

Up to this point range gave nothing surprising. But what happens when we give no argument at all? The start point defaults to zero, but what is the limit? Well, there is no limit, or as mathematicians would say, infinity is the limit. Without arguments, range returns the list of all natural numbers. The following definition is valid,

```
(def natural-numbers (range))
```

and the binding is done immediately. The computer now has \mathbb{N} , the infinite set of natural numbers bound to the symbol natural-numbers.

How is this possible? How can we fit infinitely many numbers into the machine that has finite memory? Being *lazy* is the solution. Not doing anything until the last minute, unless explicitly asked. If we force the REPL to print natural-numbers, it will sooner or later produce some error message complaining about memory not being sufficient enough.

What is the purpose then? It is useful not to set artificial limits to computations. We can do computations on demand, so we can deal with arbitrary big instances of a problem, memory permitting of course, but without doing any administration to change limits. Laziness is a crucial idea, its usefulness will become apparent later. For now, let's see how we can deal with an 'infinite list'. We can take the first five elements.

```
(take 5 natural-numbers)
(0 1 2 3 4)
```

We can also take the second five elements by dropping the first five first (still producing a lazy infinite list).

```
(take 5 (drop 5 natural-numbers))
(5 6 7 8 9)
```

When we don't know how many elements are needed, we can make it the taking and dropping more flexible by giving a predicate.

```
(take-while neg? '(-2 -1 0 1 2))
(-2 -1)
(drop-while neg? '(-2 -1 0 1 2))
(0 1 2)
```

take-while collects the elements from the original sequence as long as the predicate returns true when applied to the elements and stops when it gets false; drop-while discards elements as long as the condition is satisfied, then returns the rest.

It is a good idea to try this. One has to know how to stop a computer program when it goes rogue.

Functional collection transformation

As a recurring activity pattern, we often need to do the same operation on the elements of a collection. As a real life example one can mention peeling oranges. We do the same thing to all oranges, we peel them. In programming we say that we *transform* the elements of a collection. In functional programming this is automated. If you want to call the same function for all elements of a collection, we don't need to bother with doing it one by one. We just *map* a function across the elements of a collection:

```
(map f [x y z])
will evaluate to
  ((f x) (f y) (f z))
```

The archetypal example appears in every functional programming introduction.

```
(map inc [1 2 3 4])
(2 3 4 5)
```

The result is constructed as ((inc 1) (inc 2) (inc 3) (inc 4)).

When processing a collection, the right way of thinking is to figure out how to deal with a single element of a collection, the rest is done by map. This means that we need to supply a function that takes an input, namely an element of the collection. Let's say we want to turn names into greetings. We have a collection to process:

```
["Curious George" "Shimajiro" "world"]
```

We have to give the way to transform an element of this vector. We take a string and append Hello in front and an exclamation mark at the end.

```
(defn hello-message
  [s]
  (str "Hello " s "!"))
```

Now we can use map to transform the whole collection.

```
(map hello-message ["Curious George" "Shimajiro" "world"])
("Hello Curious George!" "Hello Shimajiro!" "Hello world!")
```

The name 'map' may not be the most intuitive (it will also clash with hashmaps), but what would be a better term?

It is a good practice to use anonymous functions in a map call. However, for beginners this is a source of trouble. It is a good idea to write and test the function separately then give it to map, until one gains enough confidence to write functions on the fly.

Is map lazy?

```
(take 2 (map inc (range)))
(1 2)
```

Yes. Otherwise we would not be able to talk about transforming infinite collections.

Is map restricted to single-argument functions? No.

```
(map + [1 2 3] [40 50 60] [700 800 900])
(741 852 963)
```

It takes the first element from each supplied collection to make the arguments of the first call of the mapped function, then the second elements, and so on. Clearly, the supplied function should be able to take the right number of arguments.

Selecting things from sequences

Selecting things from a sequential collection is nicely automated. Imagine we have a vector full of all kinds of stuff, and we need to separate the elements by their nature, by their type. The function filter takes a predicate (a yes-or-no question) and a sequential collection as its second argument. Then it goes through the collection, applies the predicate to all of its elements, selects those that give a yes answer, and finally returns a newly built list of selected items. We can separate the elements by separating by their types.

```
(def v [-1 0 2 "two" 'foo 42 "42" -6])

(filter number? v)
(-1 0 2 42 -6)
(filter string? v)
("two" "42")
(filter symbol? v)
(foo)
```

Since filter also returns a collection, we can do filtering again on that to get some finer selection.

```
(filter even? (filter number? v))
(0 2 42 -6)
```

People seeing map and filter for the first time might have some problems distinguishing between the two. So it is instructive to put them side-by-side.

```
(map pos? [-2 0 1])
(false false true)
(filter pos? [-2 0 1])
(1)
```

If we map a predicate over a collection, we get a list of logical values. When filtering, based on the returned value of the predicate applied to an element, we decide whether we need to put the element into the result collection or not. The size of the result for map is the same

People coming from programming languages of the imperative style may ask 'Where is my for-loop?'. The short answer is that there is no need for them. Higher order functions like map and filter (and other constructs later) give the same functionality of going through a collection and doing something to the elements; with the added bonus that we don't have to fiddle with a loop variable.

as the input collection, for filter it can be the same size (predicate says true for all), smaller, or even zero, when there is no positive answer.

Sometimes we want to select the elements for which the predicate returns false.

```
(remove zero? (filter number? v))
(-1 2 42 -6)
```

The name of the function is a bit misleading, by immutability, no elements are removed from vector v. A new list is created for the numbers, leaving out zero.

Decision making – conditionals

When selecting elements from a sequence, we only need to supply a predicate function that describes the desired property. Then, the individual decisions for keeping or discarding elements is made for us implicitly by filter and remove. However, sometimes we want to do decisions ourselves explicitly, independent of collection processing. Without the ability of choosing between alternatives, we only have a fancy symbolic calculator. The simplest way of making a choice is the if-then-else form. We understand this very well as we use it in natural language. If *condition* is true, then we have the *consequent*, otherwise the *alternative*.

Here is a function calculating the absolute value of a number.

```
(fn [a]
(if (> a 0) a (- a)))
```

Is there a way to calculate the absolute value without if?

```
(fn [a]
(max a (- a)))
```

This only makes the decision invisible, done by max.

In an if form not all elements are evaluated. The condition after if is evaluated first. If true, then the consequent is evaluated and that is the value of the if form (and the alternative not evaluated at all - why bother if its value is not needed?). If the condition is false the alternative is evaluated, giving the value of the form. Therefore, if is a special form, not a function call.

Let's say we would like to calculate a + |b|, where $a, b \in \mathbb{R}$. With a and b bound to numerical values and using the definition of absolute value, the straightforward, 'prosaic' way to write the expression is

```
(if (> b 0)
  (+ a b)
  (- a b))
```

as we need to choose between two cases. There is a 'poetic' way as well, in a sense that we can express a deep truth with very few words.

Having conditionals is a decisive feature, as it was discovered by Charles Babbage in 1837. He switched from the Difference Engine project to the Analytical Engine, but never finished it. This probably delayed the birth of computers by a century.

```
((if (> b 0) + -) a b)
```

Here we emphasize that functions are first class citizens, they are treated as any other values.

For more complicated, non-binary decisions we use cond.

The condition consequent pairs are evaluated one-by-one in order. When a condition evaluates to logical true, the corresponding conseuent is returned. If no condition matches, nil is returned.

Instead of true as the last condition, it is customary to use :else. This is not a special syntax, it is a keyword (used in hash-maps).

The logic of truthy and falsey



Figure 1: Falsey is nil and false, truthy is everything else.

How to express more complicated conditions? Just as in everyday language, we can negate statements, connect them with and or. However, what is considered to be true or false has a generalized meaning in Clojure. Both false and nil are treated as false, every other value is treated as true.

```
(if true "consequent" "alternative")
"consequent"
(if 0 "consequent" "alternative")
"consequent"
(if () "consequent" "alternative")
"consequent"
(if [] "consequent" "alternative")
"consequent"
(if + "consequent" "alternative")
"consequent"
(if nil "consequent" "alternative")
"alternative"
(if false "consequent" "alternative")
"alternative"
```

So logical expressions can be *truthy* or *falsey*. Note this does not turn nil into false, or 1 into true,

```
(true? 1)
false
(true? true)
true
(false? nil)
false
(false? false)
true
```

but in decision making situations we are quite liberal about what counts as truth. What are the benefits? The flexibility in expressing selections. For instance, we can easily filter out nils and falses from a collection.

```
(filter identity [1 2 nil \c "hello" nil false])
(1 2 \c "hello")
```

Truthiness is also good for the efficient evaluation of logical expressions. The special form and evaluates its arguments until it find a falsey one,

```
user=> (and (< 4 5) false (range))
false
user=> (and (= 1 (inc 0)) nil (range))
nil
```

note that the dangerous (range) is not evaluated at all; or if they are all truthy it returns the last.

```
(and (< 4 5) [] [1 2])
[1 2]
```

Short-circuit evaluation is the computer science term for trying to save work when making decisions.

The returned value may feel strange, but an if statement would interpret this as a yes. The form or does the opposite, it returns the first truthy, or the last falsey if they are all falsey.

```
(or nil false 1)
1
user=> (or false nil)
nil
```

Negation also accepts truthy and falsey values, and produces geniune true/false answers.

```
(not nil)
true
(not "hello")
false
```

Reducing a collection

Often we need to make a single value out of a collection. Or another collection, for that matter. Reducing is a very general operation, therefore it may be perplexing first. A visual image may help to get the idea. Imagine a child collecting pebbles on the seashore. Picking up stones with the right hand, while holding the already collected ones in the left palm, or in a small bucket hold in the left hand. Or the child can decide not to gather all pebbles, just the most beautiful one. For each newly picked up pebble, she compares it with the one held in the left hand, and decides which one to keep. In both cases, some result is accumulated in the left hand.

Let's see how to collect pebbles in CLOJURE, or rather keywords into vectors.

```
(reduce conj [1 2] [3 4 5])
[1 2 3 4 5]
```

Here we have an initial collection [:a :b] (the pebbles already in the bucket), and the keywords [:c :d :e] to be collected (the pebbles still on the beach). 'Putting a pebble into the bucket' is done by conjing them one by one to the existing collection. The fact that we only see the result may hinder understanding the reduction process. Luckily, it is possible to see the accumulation step-wise.

```
(reductions conj [1 2] [3 4 5])
([1 2] [1 2 3] [1 2 3 4] [1 2 3 4 5])
```

Reducing some elements into a new collection is such a common operator that there is a dedicated function for that. Roughly speaking into is just reduce conj.

```
(into [1 2] [3 4 5])
[1 2 3 4 5]
```

Now for finding the most beautiful pebble. This is the same type of problem as finding a maximal number from a collection of numbers.

map, filter and reduce form an expressive set of collection processing functions. All we need to do is to supply a function that can deal with a single element of a collection, the rest is automated.

```
(reduce max [1 2 1 3 2 5 4 6 1 2])
6
(reductions max [1 2 1 3 2 5 4 6 1 2])
(1 2 2 3 3 5 5 6 6 6)
```

Here we didn't specify the initial value of the reduction, the first value of the vector can serve as the initial value.

At this point it might be difficult to see the difference between apply and reduce, since in special cases they produce the same result.

```
(reduce + [1 2 3 4 5 6 7 8 9])
45
(apply + [1 2 3 4 5 6 7 8 9])
45
```

However, the shape of the process is different: apply yields (+ 1 2 3 4 5 6 7 8 9) while reduce will go through steps (+ 1 2) (+ 3 3) (+ 6 4) (+ 10 5) (+ 15 6) (+ 21 7) (+ 28 8) (+ 36 9). What happens is that reduction requires a function with 2 arguments, the so called *reducing function*. Its first argument is an *accumulator*, some data in which we collect the result of the computation. The second is an element from the collection being processed by reduce. Here is a simple example of a reducing lambda function: (fn [c _] (inc c)). This ignores its second argument, but whenever it gets a new one, it increments the counter. This can be used for re-implementing count.

The _ symbol is used for an argument that is not used in the body of the function. It is just a convention, the underscore is a symbol as good as any other. This emphasises that we don't need to process the elements when we just want to count them. Here is another example, where the collection is just used to provide the number of steps.

These are the first 17 of the so called Fibonacci numbers.

The general form of reduce is this.

The + function with multiple arguments will do reductions internally anyway, so ultimately they realize the same process.

Depending on the body of the reducing function (what compute-new-result is doing), the behaviour can be really versatile. The initial value is optional, in case it can be inferred from the collection.

Hash-maps

Association is a mental connection between things and ideas. The most common example is naming. We associate meaning to words, that are sequences of letters. When we have several associations together, we need hash-maps.

Another way to understand hash-maps is that after introducing vectors, we should do a powerful abstraction. A vector associates things, some *values* to numbers 0,1,2,3,..., to the so-called *indices*. We have index-value type pairings. This is useful for some things in an ordered sequence, but it is a very special association. What if the indices can be anything? What if we could map any value to any other? That's what *hash-maps* do. The name is unfortunate, since it describes how these associations are implemented, and not what they do. Lookup table might be a better name, but we are stuck with the old name. Still about terminology, we call the generalized indices *keys*.

Curly braces indicate a hash-map, and we simply write the key-value pairs inside.

```
{"answer" 42 "question" "?" 2 "two" "list" '(1 2) () '(3) }
{"answer" 42, "question "?", 2 "two", "list" (1 2), () (3)}
```

The computer politely puts commas after the each key-value pair. We can do that as well, but it is not necessary. We associate the string "answer" with the number 42, while the question itself is unknown, so the key "question" gets associated with "?". Then number 2 is connected to its English name, the word "list" is associated with a two-element list of numbers, then the empty list with a one-element list. The order of the key-value pairs is not guaranteed.

| "answer" | () | 2 | "question" | "list" |
|----------|-----|-------|------------|--------|
| 42 | (3) | "two" | "?" | (1 2) |

So anything can be used as keys and values. Even nothing is permissible as a key: {nil "nothing"} is a permissible map. But there is a type of keys, that is specially designed for hash-maps: *keywords*. They are symbols starting with a colon. So, what was the book you mentioned?

Yes, these associations are from an old science-fiction book.

A hash-map behaves like a small database. Here we store information about a book. You can look up values by giving keywords.

```
(book :author)
"Douglas Adams"
```

A database as a function?!? Yes, hash-maps can be used as functions with a key as the single argument. The result of the function call is the corresponding value, or nil if it is not in the map. There are more neat surprises.

```
(:author book)
"Douglas Adams"
```

Keywords also behave as functions! They look themselves up in a hash-map.

There is a manual way to look up a data item.

```
(get book :title)
"Hitch-hiker's guide to the galaxy"
(get book :price)
nil
```

Why is this useful? We can give a default value in case the key is not in the hash-map.

```
(get book :title "no information")
"Hitch-hiker's guide to the galaxy"
(get book :price "no information")
"no information"
```

There is an elegant way to create a hash-map when we have the keys and values in separate sequential collections, but matched up nicely. We can just 'zip' them together.

```
(zipmap (range 4) ["zero" "one" "two" "three"])
{0 "zero", 1 "one", 2 "two", 3 "three"}
```

There is also easy access to the keys and values separately.

```
(keys {:x 1 :y 11 :z 111})

(:x :y :z)

(vals {:x 1 :y 11 :z 111})

(1 11 111)
```

This is an all-time favorite sciencefiction novel with computers playing central roles. [2]

Hash-sets

Imagine a hash-map where keys are mapped to themselves. This doesn't make too much sense at first sight. If I have the element, why would I want to look it up in a hash-map? If the key is there, I get back the key, otherwise nil – truthy and falsey. Also, in a hash-map, keys cannot be duplicated (otherwise the output value of the lookup function would be ambiguous). These two give the behaviour of a *set* in the mathematical sense.

Hash-sets can be defined as data literals by curly braces prefixed by a #.

```
(def numbers #{1 2 3})
```

As in mathematical sets, the order of the elements does not matter, and it is not guaranteed to retain the order of the definition.

```
numbers
#{1 3 2}
```

As with hash-maps, we can use get to do lookup and to have the possibility for a default answer in case the key is not in the hash-set and don't want to have nil as an answer, which is falsey.

```
(get numbers 2)
2
(get numbers 4)
nil
(get numbers 4 :not-an-element)
:not-an-element
```

Hash-sets are also functions of their keys.

```
(numbers 4)
nil
(numbers 3)
3
```

In case more civilized logic values are needed, contains? is a predicate function that decides whether a hash-set contains the given key or not.

This is a bit weird, it's like asking "What's the weather like tomorrow? If you don't know, just say sunny.". But often, handling nil would be quite a hassle.

```
(contains? numbers 6)
false
(contains? numbers 1)
true
```

Thanks to truthiness, sets can be used as predicate functions in filter.

```
(def fruits #{:apple :mango :pear :grape :banana :orange})
(def vegetables #{:cucumber :tomato :carrot :onion})
(def basket [:apple :apple :onion :carrot :grape])
(filter vegetables basket)
(:onion :carrot)
(filter fruits basket)
(:apple :apple :grape)
```

For creating hash-sets, we can directly supply the elements to hash-set,

```
(hash-set 3 2 1 2 3 1 1)
#{1 3 2}
(hash-set)
#{}
(hash-set "hello")
#{"hello"}
```

or we can turn a collection in a hash-set.

```
(set [13 17 17 19 23 19])
#{13 17 23 19}
(set (range 5))
#{0 1 4 3 2}
```

It is important to remember, that sets do not make any promise about keeping the order. All they do is just answering whether a key is contained or not. However, one can have sorted sets as well.

```
(sorted-set 13 17 17 19 23 19)
#{13 17 19 23}
```

The sequence abstraction

All the collections so far, namely lists, vectors, strings, hash-maps, hash-sets can be handled as sequences of elements. We can use the seq function to investigate how the collections are turned into logical sequences. Being a sequence is not a surprising property for lists and vectors, since they are sequential data structures anyway.

```
(seq '(1 2 3 4))
(1 2 3 4)
(seq [1 2 3 4])
(1 2 3 4)
```

Strings are also sequences, whose elements are characters.

```
(seq "hello")
(\h \e \l \l \o)
```

For hash-sets, the elements can be enumerated one-by-one, but it is important to note that there is no promise about the order of elements.

```
(seq #{:a :b :c})
(:c :b :a)
(seq #{1 2 3 5 8 13})
(1 13 3 2 5 8)
```

How about hash-maps? They don't really have single elements in them, rather contian pairs of elements. These key-value pairs van be represented by vectors. Accordingly, the sequence of a hash-map consists of key-value pairs in vectors.

```
(seq {:x 1, :s "foo", :c \x})
([:x 1] [:s "foo"] [:c \x])
```

So it seems that the right way to think about hash-maps that it is a collection that contains associations, treated as single things.

```
(count {:a 11, :b 13})
2
```

This also shows that there is no need to call seq explicitly. CLO-JURE takes care of turning the collections into sequences, whenever needed. This way, all the sequence functions like first, rest, first, second, last and the higher order sequence processing function like map, filter, etc. can work with all the above data structures.

What is the point? The sequence abstraction can be justified in different ways. From the students' perspective it is a big win, since one only needs to remember functions dealing with sequences, then working with other data structures can be done without learning anything new. The software engineer relishes the fact the same piece of code would work in many different situations, enabling *code reuse*.

Where is the catch? The behaviour of the same function can be different for different data structures. For example, the difference between cons and conj can be confusing. cons builds a sequence, always putting a new element in the front,

```
(cons 1 '(2 3))
(1 2 3)
(cons 1 [2 3])
(1 2 3)
```

while conj *conjoins* a new element in a way that is 'natural' for the collection, (front for lists, back for vectors)

```
(conj '(2 3) 1)
(1 2 3)
(conj [2 3] 1)
[2 3 1]
```

and it can take arbitrary many arguments.

```
(conj [2 3] 4 5 6)
[2 3 4 5 6]
```

Conjoining keeps the type of the collection.

```
(conj {:name "Arthur"} [:age 42])
{:name "Arthur", :age 42}
```

Beyond the different behaviours, performance can also be an issue. One can use nth on lists, but it will not be as efficient as on vectors, since Cloure has to hop through all the preceding elements.

Here the unmissable quote is: "It is better to have 100 functions operate on one data structure than to have 10 functions operate on 10 data structures.", by Alan J. Perlis in the foreword of SICP [1].

Immutability

Consider the following little conversation with the computer.

```
(def v [1 2 3])
v
(conj v 4)
[1 2 3 4]
```

Now the question is what is the current value of v? What does v evaluate to? If your answer is [1 2 3] (the correct one), then there is nothing to worry about. We associated the vector [1 2 3] with the symbol v, then we called the conj function with arguments v and 4, which returned the new combined vector [1 2 3 4], but the association of v has not changed.

However, if you say v is [1 2 3 4], then you must have some previous programming experience in a programming language with mutable data structures, and Clojure's *immutable* data structures can look a bit strange in the beginning. Both approaches have advantages and disadvantages, however if we run programs concurrently or in parallel then immutable data structures have a clear edge.

So what is the immutability exactly? Simple data items never change. 42 is 42 forever. I can add one to it, (inc 42) equals 43. Function create new values but do not touch their arguments. Naturally, 42 will not mutate into 43 just by applying the function f(x) = x + 1 to it. This is so obvious, that it feels a bit silly to mention it.

However, for composite data items immutability is less obvious. It makes perfect sense to add a new element to a vector, by changing it to a bigger one. However, in Cloure a new vector is created and the old one is retained. Well, it's better than that. It is also efficient: there is structural sharing between the old and the new vector. There is no unnecessary duplication of the data items stored in vectors.

This is exactly how version control systems work, e.g. GIT. They store only the difference between different versions of the documents.

Iteration

We often need to call a function *iteratively*, i.e. feeding the output back into the function. Let's consider a simple mathematical game. Given a positive integer, if it is even then half it (still a whole number), when it's odd multipply by 3 and add 1. What happens if you do the same with the result? Again and again. The function itself is easy to write.

```
(defn c [n]
  (if (even? n)
        (/ n 2)
        (inc (* 3 n))))
```

So we can try.

```
(c 1)
4
(c 4)
2
(c 2)
1
```

From 1 we get back to 1. From 8 we would go to 4, then again get back to 1. Is this the case for other numbers? Interesting problem but tedious to call the function again and again. So, let's automate! In algebraic notation, we want the sequence

```
n, c(n), c(c(n)), c(c(c(n))), \dots
```

we want to repeat the function *c*, calling it with the newly produced value. The function iterate does that exactly:

```
(iterate f x) produces the lazy list ( (f x) (f (f x)) (f (f (f x))) ... ), so in particular we can use the above function c
```

```
(iterate c 1)
```

In mathematics this is called the Collatz conjecture, and it is a particularly tough problem. We do not know at the time being whether for all numbers the process eventually returns to 1 or not.

But when you hit enter, no result. Seemingly. The computer evaluates c with argument 1, then takes the result as an argument of c, infinitely many times (at least until the computer's memory fills up). That's why it never returns a value. This is another example of dealing with something potentially infinite. The functions take and drop can tame infinite sequences of numbers, and they can do that to infinite sequence of function calls. We simpy ask to return the first few values of the infinite sequence.

```
(take 20 (iterate c 9))
(9 28 14 7 22 11 34 17 52 26 13 40 20 10 5 16 8 4 2 1)
```

We can also ask what is the sixth element of the sequence (indexed by 5)?

```
(first (drop 5 (iterate c 9)))
11
```

The range function called without arguments produces the infinite lazy list of natural numbers. Can we produce the same list without range? Yes, (iterate inc \emptyset).

Recursion

The simplest way of defining *recursion* is that a function calls itself. It may even look paradoxical, since we are defining something in terms of itself. The paradox disappears when we realize that when function calls itself it does it with arguments that somehow represent a smaller and easier to solve version of the problem. So recursion is a way of dividing a difficult problem into easier ones. For instance, when a problem is somehow given as a list we can naturally divide it into two parts: dealing with the first element, and dealing with the rest of the list. Recursive functions are list are the classical examples of functional programming.

Let's imagine count, a function for getting the size of a collection, is not available, so here is an implementation for lists.

```
(defn COUNT
  [1]
  (if (empty? 1)
      0
      (inc (COUNT (rest 1)))))
```

If the list is empty, then the function returns 0. This is the base case, where the recursion stops. Otherwise, it knocks off the first element of the list and calls itself for the rest of the list. This way it calculates the size of the list by adding one to the size of the list without the first element.

Another classic is the re-implementation of map, again dividing the work by first and rest.

Typically we use let bindings in functions, to get a better structuring of the computation to be done.

Self-reference is where things get interesting. Consider the sentence "This sentence is false."; it does not have a well-defined logical value. Beyond logical paradoxes, self-reference is often thought to be a key ingredient to consciousness. See for example [4].

Pretty, but not the most efficient way, in practice we will use reducing (folding).

We use uppercase name for the new implementation to avoid clashing with the existing count function.

Destructuring

Often there is a need for a systematic naming of elements in a collection.

How often do we get some collection as an argument of a function and then spend half of the body of the function to pull the collection apart? Destructuring handles this. Just like kicking the ball on the volley, we can give names to parts of the arguments before they land in the function.

For example, we a represent a line defined by two points by a vector of vectors and we would like to compute the slope of the line like (slope [[1 2] [2 4]]). So we define the function slope.

```
(defn slope
  [line]
  (/
    (- (first (first line)) (first (second line)))
    (- (second (first line)) (second (second line)))))
```

Here the coordinate information is extracted on demand, making the actual calculation obscure, littered with the retrieval. We can separate these two.

Now the computation is quite clear, it is basically the mathematical formula. However, we have a long list of bindings. Destructuring gets rid of this, by giving the 'shape' of the input data in the argument list.

```
(defn slope3

[[[x1 y1] [x2 y2]]]

(/ (- x1 x2) (- y1 y2)))
```

This may look like magic first, but it is actually just a simple automation. It is easy to reveal how it is done.

```
(destructure '[ [x y] [13 19]])
[vec__1246 [13 19]
x (clojure.core/nth vec__1246 0 nil)
y (clojure.core/nth vec__1246 1 nil)]
```

It does exactly the work we did not want to do manually. destructure produces a vector of bindings, that is given to let in a real destructuring situation.

destructure is very useful in figuring out what goes wrong in an unsuccessful and complex destructuring attempt.

Point-free style

We can create new functions by specifying what they do with their arguments, but we can also make new functions without mentioning those input values (points). There are several ways to do this:

- composing functions by comp,
- preloading arguments by partial,
- grouping functions to work on same input by juxt,
- negating logical output value by complement.

Nested function calls of the form (f (g (h x))) can be replaced by ((comp f g h) x).

```
(def negative-product (comp - *))
(negative-product 2 3)
-6
```

With partial we can create functions by preloading the first few arguments of a function with several inputs. In a sense we turn a general function into a more specific one.

```
(def ten-times (partial * 10))
(map ten-times [1 2 3])
(10 20 30)
```

When we want to apply several functions to same input, we can juxtapose them. (juxt f g h) is the function that produces [(f x)(g x)(h x)] when applied to x. It works functions that can take more arguments, but obviously they need to have the same number of inputs,

```
((juxt take drop) 3 [1 2 3 4 5 6])
[(1 2 3) (4 5 6)]
```

and juxt always returns the result in a vector.

One thing where juxt really shines is retrieving data items from a hash-map, more than one at the same time.

Combining these higher-order functions can be very expressive. Here is a one-liner function for segregating even and odd numbers.

```
(def sgr (juxt (partial filter even?) (partial filter odd?)))
(sgr (range 9))
[(0 2 4 6 8) (1 3 5 7)]
```

It's amazing how far one can get with point-free style. Here we define a function that counts the number of lowercase letters in a string.

```
(def count-if (comp count filter))
(def letters (set "abcdefghijklmnopqrstuvwxyz"))
(def count-lowercase (partial count-if letters))
(count-lowercase "aBbC10x")
3
```

It is debated how desirable is the point-free style in practice. Some say it is 'pointless', and readability can be a subjective issue.

Of course, the standard solution for this problem would use regular expressions.

for

```
(for [x [1 2 3]
y [:a :b]]
[x y])
([1 :a] [1 :b] [2 :a] [2 :b] [3 :a] [3 :b])
```

Changing the world – Side-effects

The functions we have seen so far were *pure* functions: the output depends only on the inputs. In order to understand what the function does, we don't need to check anything else. The history of previous function calls have no effect on the current call. This makes things very easy. Of course, the world is not like this. If you ask me now and tomorrow 'How are you?', you are not guaranteed to have the same answer. Similarly, we have 'functions' that are not pure.

```
(rand)
0.7811104824887901
(rand)
0.3589579594682847
(rand)
0.629147957095869
```

These are random numbers between 0 and 1. The function takes no arguments but it doesn't return the same value for each call. Something must be changing in the background.

println doseq Rather, they are pseudo-random numbers generated by an algorithm.

Etudes

One can learn the rules of chess or Go immediately. However, mastering them takes long time, playing many games. Same for programming. Learning the basic constructs of a programming language is a quick process. Understanding what reduce does is not that hard, but knowing when to use it and how to adapt the general mechanism to a particular problem require lot of practice. Like performing musicians, we need to go through exercises several times.

What is 42?

The task is simple. Write some code that somehow produces 42. The easiest way is to use a data literal 42. How about other ways? When you are not allowed to write down the number itself. By arithmetic operations,

```
(* 6 7)
(+ 40 2)
```

or by incrementing/decrementing,

```
(inc 41)
(dec 43)
```

or by counting a number of elements in a collection,

```
(count "012345678901234567890123456789012345678901")
```

the ASCII code of * is also 42,

```
(int \*)
```

n!

Writing a function to calculate n! (n factorial) is a common programming exercise for recursion. It is defined as the product of natural numbers from 1 up to n, with the special case of 0! = 1. Recursively,

but if someone is worried about the inefficiency of the recursive call then tail recursion is also possible.

The current value to be multiplied with is also passed on through the call, so the caller don't have to wait. However, there is no real need to be recursive, thus checking for the base case is not necessary.

```
(defn factorial [n]
  (reduce * (range 1 (inc n))))
```

Transposing a matrix

Considering matrix

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix},$$

we would like to calculate its transpose (swapping rows with columns)

$$A^T = \begin{bmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{bmatrix}.$$

Matrices can be represented as nested vectors.

```
(def A [[1 2] [3 4] [5 6]])
```

Without further ado, here is how to do the transpose.

```
(apply map vector A)
([1 3 5] [2 4 6])
```

If the result needs to be a vector as well, then mapv can replace map.

Functional Programming

What is functional programming? The computer is doing useful work by evaluating functions. When given a function and some input arguments it calculates the value of the function. If we have a problem to solve or a question to be answered, we need to bring into this form: function and input values.

Where do we get the inputs? That is the raw data we have in the beginning. Bits and pieces of information which we want to process to get some meaningful results. Certain data items that represent our question.

Where do we get the functions to call? There are four ways to get those.

- 1. **The built-in functions are already there.** The programming language comes with numerous general purpose functions. We can just start using them.
- Some data structures behave like functions. Vectors are functions
 from the set of valid indices to the corresponding content. Hashmaps are functions from keys to values. Hash-sets are functions
 from elements to truthy values.
- Higher order functions can create new functions. Some functions
 produce functions as their output values. Function composition is
 the prime example, but all point-free style functions belong to this
 category.
- 4. Writing new functions from scratch. We can define functions directly by sepcifying its arguments and its body, which is a bunch of function calls. Thus we still combine existing functions, but in a more manual way.

Calling only built-in functions, we can use the language as a calculator, and we are *users*. In case the desired functionality is not available, we need take the role of the *programmer*, and create new functions.

Functions can be found not just in the core language, but in external *libraries*. These are collections of useful functions, usually for solving some particular type of problems. In the 21st century, software development is more about finding the right library, than programming.

Bibliography

- [1] H. Abelson, G.J. Sussman, and J. Sussman. *Structure and Interpretation of Computer Programs*. Electrical engineering and computer science series. MIT Press, 1996. https://mitpress.mit.edu/sicp/, https://sicpebook.wordpress.com/, https://github.com/sarabander/sicp-pdf.
- [2] Douglas Adams. *The Hitchhiker's Guide to the Galaxy*. Pan Books, 1979.
- [3] J. Roger Hindley and Jonathan P. Seldin. *Lambda-Calculus and Combinators: An Introduction*. Cambridge University Press, New York, NY, USA, 2 edition, 2008.
- [4] D.R. Hofstadter. *Gödel, Escher, Bach. Anniversary Edition: An Eternal Golden Braid.* Basic Books. Basic Books, 1999.
- [5] Donald E. Knuth. *The Art of Computer Programming, Volume 1* (3rd Ed.): Fundamental Algorithms. Addison Wesley Longman Publishing Co., Inc., Redwood City, CA, USA, 1997.

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