

Package ‘decisionSupport’

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Type Package

Title Quantitative Support of Decision Making under Uncertainty

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Description Supporting the quantitative analysis of binary welfare based decision making processes using Monte Carlo simulations. Decision support is given on two levels: (i) The actual decision level is to choose between two alternatives under probabilistic uncertainty. This package calculates the optimal decision based on maximizing expected welfare. (ii) The meta decision level is to allocate resources to reduce the uncertainty in the underlying decision problem, i.e to increase the current information to improve the actual decision making process. This problem is dealt with using the Value of Information Analysis (VIA). The Expected Value of Information (EVI) for arbitrary prospective estimates can be calculated as well as Individual and Clustered Expected Value of Perfect Information (EVPI). The probabilistic calculations are done via Monte Carlo simulations. This Monte Carlo functionality can be used on its own.

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 'random.R'
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 'rtnorm90ci.R'
 'rdist90ci_exact.R'
 'estimate1d.R'
 'estimate.R'
 'mcSimulation.R'
 'welfareDecisionAnalysis.R'
 'eviSimulation.R'
 'individualEvpSimulation.R'
 'estimate_read_csv_old.R'
 'uncertaintyAnalysis.R'
 'decisionSupport-package.R'
 'globalNames2data.frameNames.R'
 'plsr.mcSimulation.R'

VignetteBuilder knitr

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as.data.frame.mcSimulation
<i>Coerce to a Data Frame.</i>

Description

Functions to check if an object is a data frame, or coerce it if possible.

Usage

```
## S3 method for class 'mcSimulation'
as.data.frame(x, row.names = NULL, optional = FALSE,
  ..., stringsAsFactors = default.stringsAsFactors())
```

Arguments

x	An object of class mcSimulation.
row.names	NULL or a character vector giving the row names for the data frame. Missing values are not allowed.
optional	logical. If TRUE, setting row names and converting column names (to syntactic names: see make.names) is optional.
...	additional arguments to be passed to or from methods.
stringsAsFactors	logical: should the character vector be converted to a factor?

See Also

[as.data.frame](#)

corMat	<i>Return the Correlation Matrix of x.</i>
--------	--

Description

Return the correlation matrix of x.

Usage

```
corMat(rho)
```

Arguments

rho a distribution.

corMat.estimate	<i>Return the correlation matrix of an estimate object.</i>
-----------------	---

Description

This function returns the full correlation matrix of an [estimate](#) object.

Usage

```
## S3 method for class 'estimate'  
corMat(rho)
```

Arguments

rho an [estimate](#) object.

See Also

[estimate](#), [row.names.estimate](#), [names.estimate](#)

Description

The decisionSupport package supports the quantitative analysis of welfare based decision making processes using Monte Carlo simulations. This is an important part of the Applied Information Economics (AIE) approach developed in Hubbard (2014). These decision making processes can be categorized into two levels of decision making:

1. The actual problem of interest of a policy maker which we call the *underlying welfare based decision* on how to influence an ecological-economic system based on a particular information on the system available to the decision maker and
2. the *meta decision* on how to allocate resources to reduce the uncertainty in the underlying decision problem, i.e to increase the current information to improve the underlying decision making process.

The first problem, i.e. the underlying problem, is the problem of choosing the decision which maximizes expected welfare. The welfare function can be interpreted as a von Neumann-Morgenstern utility function. Whereas, the second problem, i.e. the meta decision problem, is dealt with using the *Value of Information Analysis (VIA)*. Value of Information Analysis seeks to assign a value to a certain reduction in uncertainty or, equivalently, increase in information. Uncertainty is dealt with in a probabilistic manner. Probabilities are transformed via Monte Carlo simulations.

Details

The functionality of this package is subdivided into three main parts: (i) the welfare based analysis of the underlying decision, (ii) the meta decision of reducing uncertainty and (iii) the Monte Carlo simulation for the transformation of probabilities and calculation of expectation values. Furthermore, there is a wrapper function around these three parts which aims at providing an easy-to-use interface.

Welfare based Analysis of the Underlying Decision Problem:

Welfare Decision Analysis: Implementation: [welfareDecisionAnalysis](#)

Utility Functions: Implementation: ToDo

The Meta Decision of Reducing Uncertainty: The meta decision of how to allocate resources for uncertainty reduction can be analyzed with this package in two different ways: via (i) Expected Value of Information Analysis or (ii) via Partial Least Squares (PLS) analysis and Variable Importance in Projection (VIP).

Expected Value of Information (EVI): Implementation: [eviSimulation](#), [individualEvpSimulation](#)

Partial Least Squares (PLS) analysis and Variable Importance in Projection (VIP): Implementation: ToDo

Solving the Practical Problem of Calculating Expectation Values by Monte Carlo Simulation:

Estimates: Implementation: [estimate](#)

Multivariate Random Number Generation: Implementation: [random.estimate](#)

Monte Carlo Simulation: Implementation: [mcSimulation](#)

Uncertainty Analysis: A wrapper function: Implementation: [uncertaintyAnalysis](#)

Package Options

ToDo

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References

Hubbard, Douglas W., *How to Measure Anything? - Finding the Value of "Intangibles" in Business*, John Wiley & Sons, Hoboken, New Jersey, 2014, 3rd Ed, <http://www.howtomeasureanything.com/>.

Hugh Gravelle and Ray Rees, *Microeconomics*, Pearson Education Limited, 3rd edition, 2004.

See Also

[welfareDecisionAnalysis](#), [eviSimulation](#), [mcSimulation](#)

estimate

*Create a multivariate estimate object.***Description**

`estimate` creates an object of class `estimate`. The concept of an estimate is extended from the 1-dimensional (cf. `estimate1d`) to the multivariate case. This includes the description of correlations between the different variables. An estimate of an n-dimensional variable is at minimum defined by each component being a 1-dimensional estimate. This means, that for each component, at minimum, the type of its univariate parametric distribution, its 5% - and 95% quantiles must be provided. Optionally, the individual median and the correlations between the components can be supplied.

`as.estimate` tries to coerce a set of objects and transform them to class `estimate`.

Usage

```
estimate(distribution, lower, upper, ..., correlation_matrix = NULL)
```

```
as.estimate(..., correlation_matrix = NULL)
```

Arguments

<code>distribution</code>	character vector: defining the types of the univariate parametric distributions.
<code>lower</code>	numeric vector: lower bounds of the 90% confidence intervals, i.e the 5%-quantiles of this estimates components.
<code>upper</code>	numeric vector: upper bounds of the 90% confidence intervals, i.e the 95%-quantiles of this estimates components.
<code>...</code>	in <code>estimate</code> : optional arguments that can be coerced to a data frame comprising further columns of the estimate (for details cf. below). in <code>as.estimate</code> : arguments that can be coerced to a data frame comprising the base of the estimate. Mandatory columns are <code>distribution</code> , <code>lower</code> and <code>upper</code> .
<code>correlation_matrix</code>	numeric matrix: containing the correlations of the variables (optional).

Details

It must hold that `lower <= upper` for every component of the estimate.

The structure of the input arguments:

Mandatory input columns::

Column	R-type	Explanation
<code>distribution</code>	character vector	Distribution types of all components
<code>lower</code>	numeric vector	5%-quantiles of all components
<code>upper</code>	numeric vector	95%-quantiles of all components

Optional input elements:: The optional parameters in ... provide additional characteristics of the estimate. Frequent optional elements are:

Column	R-type	Explanation
variable	character vector	Variable names
median	cf. below	50%-quantiles of the estimate
method	character vector	Methods for calculation of components distribution parameters

The median column: If supplied as input, any component of median can be either NA, numeric (and not NA) or the character string "mean". If it equals "mean" it is set to `rowMeans(cbind(lower, upper))` of this component; if it is numeric it must hold that `lower <= median <= upper` for this component. In case that no element median is provided, the default is `median=rep(NA, length(distribution))`.

The parameters in ... provide the base information of an estimate.

The structure of the estimate base information (mandatory): Mandatory columns:

Column name	R-type	Explanation
distribution	character	Distribution types
variable	character	Variable names

Value

An object of class `estimate` which is a list with components `base` and `correlation_matrix`:

`$base` is a [data.frame](#) with mandatory columns:

Mandatory column	R-type	Explanation
distribution	character vector	Distribution types
lower	numeric vector	5%-quantiles
median	numeric vector	50%-quantiles or NA
upper	numeric vector	95%-quantiles

The `row.names` are the names of the variables. Each row has the properties of an [estimate1d](#). Note that the median is a mandatory element of an estimate, although it is not necessary as input. If a component of median is numeric and not NA it holds that: `lower <= median <= upper`. In any case an estimate object has the property `any(lower <= upper)`.

`$correlation_matrix` is a symmetric matrix with row and column names being the subset of the variables supplied in base which are correlated. Its elements are the corresponding correlations.

See Also

[estimate1d](#), [random.estimate](#), [row.names.estimate](#), [names.estimate](#), [corMat](#), [estimate_read_csv](#) and [estimate_write_csv](#).

estimate1d	Create a 1-dimensional estimate object.
------------	---

Description

estimate1d creates an object of class estimate1d. The estimate of a one dimensional variable is at minimum defined by the type of a univariate parametric distribution, the 5% - and 95% quantiles. Optionally, the median can be supplied.

as.estimate1d tries to transform an object to class estimate1d.

Usage

```
estimate1d(distribution, lower, upper, ...)
```

```
as.estimate1d(x, ...)
```

Arguments

distribution	character: A character string that defines the type of the univariate parametric distribution.
lower	numeric: lower bound of the 90% confidence intervall, i.e the 5%-quantile of this estimate.
upper	numeric: upper bound of the 90% confidence intervall, i.e the 95%-quantile of this estimate.
...	arguments that can be coerced to a list comprising further elements of the 1-d estimate (for details cf. below). Each element must be atomic and of length 1 (1-d property).
x	an object to be transformed to class estimate1d.

Details

It must hold that `lower <= upper`.

The structure of the input arguments:

Mandatory input elements::

Argument	R-type	Explanation
distribution	character	Distribution type of the estimate
lower	numeric	5%-quantile of the estimate
upper	numeric	95%-quantile of the estimate

Optional input elements:: The optional parameters in ... provide additional characteristics of the 1-d estimate. Frequent optional elements are:

Argument	R-type	Explanation
variable	character	Variable name

median	cf. below	50%-quantile of the estimate
method	character	Method for calculation of distribution parameters

The median: If supplied as input, median can be either NULL, numeric or the character string "mean". If it is NA it is set to NULL; if it equals "mean" it is set to `mean(c(lower, upper))`; if it is numeric it must hold that `lower <= median <= upper`. In case that no element median is provided, the default is median=NULL.

Value

An object of class `estimate1d` and list with at least (!) the elements:

Element	R-type	Explanation
distribution	character	Distribution type of the estimate
lower	numeric	5%-quantile of the estimate
median	numeric or NULL	50%-quantile of the estimate
upper	numeric	95%-quantile of the estimate

Note that the median is a mandatory element of an `estimate1d`, although it is not necessary as input. If median is numeric it holds that: `lower <= median <= upper`. In any case an `estimate1d` object has the property `lower <= upper`.

See Also

[random.estimate1d](#)

<code>estimate_read_csv</code>	<i>Read an Estimate from CSV - File.</i>
--------------------------------	--

Description

This function reads an [estimate](#) from the specified csv files. In this context, an estimate of a variable is defined by its distribution type, its 90%-confidence interval `[lower, upper]` and its correlation to other variables. #ToDo: Implement characterization of distribution by mean and sd. Eventually, also by other quantiles.

Usage

```
estimate_read_csv(fileName, strip.white = TRUE, ...)
```

Arguments

fileName	Name of the file containing the base information of the estimate that should be read.
strip.white	logical. Allows the stripping of leading and trailing white space from unquoted character fields (numeric fields are always stripped). See scan for further details (including the exact meaning of 'white space'), remembering that the columns may include the row names.

... Further parameters to be passed to [read.csv](#).

Details

An estimate might consists of uncorrelated and correlated variables. This is reflected in the input file structure, which is described in the following.

Value

An object of type [estimate](#).

CSV input file structures

The estimate is read from one or two csv files: the basic csv file which is mandatory and the correlation csv file which is optional. The basic csv file contains the definition of the distribution of all variables ignoring potential correlations. The correlation csv file only defines correlations.

The structure of the basic input file (mandatory): File name structure: <basic-filename>.csv
Mandatory columns:

Column name	R-type	Explanation
lower	numeric	ToDo
upper	numeric	ToDo
distribution	character	ToDo
variable	character	ToDo

Optional columns:

Column name	R-type	Explanation
description	character	ToDo
median	numeric	ToDo
start	integer	ToDo
end	integer	ToDo
indicator	logical	ToDo

Columns without names are ignored. Rows where the variable field is empty are also dropped.

The structure of the correlation file (optional): File name structure: <basic-filename>_cor.csv
Columns and rows are named by the corresponding variables. Only those variables need to be present which are correlated with others. The element ["rowname", "columnname"] contains the correlation between the variables rowname and columnname. Uncorrelated elements can be left empty, i.e. as NA, or defined as 0. The element ["name", "name"] has to be set to 1. The matrix must be given in symmetric form.

See Also

[estimate_write_csv](#), [read.csv](#), [estimate](#)

estimate_read_csv_old *Read an Estimate from CSV - File (depreciated standard).*

Description

This function reads an [estimate](#) from the specified csv files. In this context, an estimate of a variable is defined by its distribution type, its 90%-confidence interval [lower, upper] and its correlation to other variables. #ToDo: Implement characterization of distribution by mean and sd. Eventually, also by other quantiles.

Usage

```
estimate_read_csv_old(fileName, strip.white = TRUE, ...)
```

Arguments

fileName	Name of the file containing the base information of the estimate that should be read.
strip.white	logical. Allows the stripping of leading and trailing white space from unquoted character fields (numeric fields are always stripped). See scan for further details (including the exact meaning of 'white space'), remembering that the columns may include the row names.
...	Further parameters to be passed to read.csv .

Details

An estimate might consists of uncorrelated and correlated variables. This is reflected in the input file structure, which is described in the following.

Value

An object of type [estimate](#).

CSV input file structures

The estimate is read from one or two csv files: the basic csv file which is mandatory and the correlation csv file which is optional. The basic csv file contains the definition of the distribution of all variables ignoring potential correlations. The correlation csv file only defines correlations.

The structure of the basic input file (mandatory): File name structure: <basic-filename>.csv
Mandatory columns:

Column name	R-type	Explanation
lower	numeric	ToDo
upper	numeric	ToDo
distribution	character	ToDo
variable	character	ToDo

Optional columns:

Column name	R-type	Explanation
description	character	ToDo
median	numeric	ToDo
start	integer	ToDo
end	integer	ToDo
indicator	logical	ToDo

Columns without names are ignored. Rows where the variable field is empty are also dropped.

The structure of the correlation file (optional): File name structure: <basic-filename>.csv_correlations.csv
#ToDo

See Also

[estimate_read_csv](#), [read.csv](#), [estimate](#)

estimate_write_csv	<i>Write an Estimate to CSV - File.</i>
--------------------	---

Description

This function writes an [estimate](#) to the specified csv file(s).

Usage

```
estimate_write_csv(estimate, fileName, varNamesAsColumn = TRUE,
  quote = FALSE, ...)
```

Arguments

estimate	Estimate object to write to file fileName.
fileName	character. Output file name which must end with .csv.
varNamesAsColumn	logical; If TRUE the variable names will be written as a separate column, otherwise as row names.
quote	a logical value (TRUE or FALSE) or a numeric vector. If TRUE, any character or factor columns will be surrounded by double quotes. If a numeric vector, its elements are taken as the indices of columns to quote. In both cases, row and column names are quoted if they are written. If FALSE, nothing is quoted. Parameter is passed on to write.csv .
...	Further parameters to be passed to write.csv .

Value

An object of type [estimate](#).

See Also

[estimate_read_csv](#), [estimate](#), [write_csv](#)

 eviSimulation

Expected Value of Information (EVI) Simulation.

Description

The Expected Value of Information (EVI) is calculated based on a Monte Carlo simulation of the values of two different decision alternatives.

Usage

```
eviSimulation(model, currentEstimate, prospectiveEstimate, numberOfSimulations,
              functionSyntax = "data.frameNames")
```

Arguments

model	either a function or a list with two functions: <code>list(p1,p2)</code> . In the first case the function is the net benefit of project approval vs. the status quo. In the second case the element p1 is the function valuing the first project and the element p2 valuing the second project.
currentEstimate	estimate object describing the distribution of the input variables as currently estimated.
prospectiveEstimate	estimate object describing the prospective distribution of the input variables which could hypothetically achieved by collecting more information, viz. improving the measurement.
numberOfSimulations	integer; number of simulations to be used in the underlying Monte Carlo analysis
functionSyntax	function character; function syntax used in the model function(s).

Details

This principle is along the line described in Hubbard (2014). The Expected Value of Information is the decrease in the EOL for an information improvement from the current estimate (I_{current}) to a better prospective (or hypothetical) information ($I_{\text{prospective}}$): $\text{EVI} := \text{EOL}(I_{\text{current}}) - \text{EOL}(I_{\text{prospective}})$. Thus, the EVI depends on the model for valuing a decision, the current information, i.e. the current estimate, and the specification of a hypothetical improvement in information, i.e. a prospective estimate.

Value

An object of class `eviSimulation` with the following elements:

current	welfareDecisionAnalysis object for currentEstimate
prospective	welfareDecisionAnalysis object for prospectiveEstimate
evi	Expected Value of Information (EVI) of gained by the prospective estimate w.r.t. the current estimate

See Also

[welfareDecisionAnalysis](#), [mcSimulation](#), [estimate](#)

Examples

```
#####
# Example 1 Only one prospective estimate:
#####
numberOfSimulations=10000
# Create the estimate object:
variable=c("revenue","costs")
distribution=c("posnorm","posnorm")
lower=c(10000, 5000)
upper=c(100000, 50000)
currentEstimate<-as.estimate(variable, distribution, lower, upper)
prospectiveEstimate<-currentEstimate
revenueConst<-mean(c(currentEstimate$base["revenue","lower"],
                     currentEstimate$base["revenue","upper"]))
#prospectiveEstimate$base["revenue",]<-data.frame(distribution="const",
#
#                                     lower=revenueConst,
#                                     upper=revenueConst,
#                                     row.names="revenue",
#                                     stringsAsFactors=FALSE)
prospectiveEstimate$base["revenue","distribution"]<-"const"
prospectiveEstimate$base["revenue","lower"]<-revenueConst
prospectiveEstimate$base["revenue","upper"]<-revenueConst
# (a) Define the model function without name for the return value:
profit<-function(x){
  x$revenue-x$costs
}

# Calculate the Expected Value of Information:
eviSimulationResult<-eviSimulation(model=profit,
                                   currentEstimate=currentEstimate,
                                   prospectiveEstimate=prospectiveEstimate,
                                   numberOfSimulations=numberOfSimulations,
                                   functionSyntax="data.frameNames")

# Show the simulation results:
print(summary(eviSimulationResult))
#####
# (b) Define the model function with a name for the return value:
profit<-function(x){
  list(Profit=x$revenue-x$costs)
}
# Calculate the Expected Value of Information:
eviSimulationResult<-eviSimulation(model=profit,
                                   currentEstimate=currentEstimate,
                                   prospectiveEstimate=prospectiveEstimate,
                                   numberOfSimulations=numberOfSimulations,
                                   functionSyntax="data.frameNames")

# Show the simulation results:
print(summary((eviSimulationResult)))
```

```
#####
# (c) Two decision variables:
decisionModel<-function(x){
  list(Profit=x$revenue-x$costs,
       Costs=-x$costs)
}
# Calculate the Expected Value of Information:
eviSimulationResult<-eviSimulation(model=decisionModel,
                                   currentEstimate=currentEstimate,
                                   prospectiveEstimate=prospectiveEstimate,
                                   numberOfSimulations=numberOfSimulations,
                                   functionSyntax="data.frameNames")

# Show the simulation results:
print(summary((eviSimulationResult)))
#####
# Example 2 A list of prospective estimates:
#####
numberOfSimulations=10000
# Define the model function with a name for the return value:
profit<-function(x){
  list(Profit=x$revenue-x$costs)
}
# Create the estimate object:
variable=c("revenue","costs")
distribution=c("posnorm","posnorm")
lower=c(10000, 5000)
upper=c(100000, 50000)
currentEstimate<-as.estimate(variable, distribution, lower, upper)
perfectInformationRevenue<-currentEstimate
revenueConst<-mean(c(currentEstimate$base["revenue","lower"],
                    currentEstimate$base["revenue","upper"]))
#perfectInformationRevenue$base["revenue",]<-data.frame(distribution="const",
#
#                                     lower=revenueConst,
#                                     upper=revenueConst,
#                                     row.names="revenue",
#                                     stringsAsFactors=FALSE)
perfectInformationRevenue$base["revenue","distribution"]<-"const"
perfectInformationRevenue$base["revenue","lower"]<-revenueConst
perfectInformationRevenue$base["revenue","upper"]<-revenueConst

# (a) A list with one element
prospectiveEstimate<-list(perfectInformationRevenue=perfectInformationRevenue)
# Calculate the Expected Value of Information:
eviSimulationResult<-eviSimulation(model=profit,
                                   currentEstimate=currentEstimate,
                                   prospectiveEstimate=prospectiveEstimate,
                                   numberOfSimulations=numberOfSimulations,
                                   functionSyntax="data.frameNames")

# Show the simulation results:
print(summary(eviSimulationResult))
#####
# (b) A list with two elements
perfectInformationCosts<-currentEstimate
```



```

costsConst<-mean(c(currentEstimate$base["costs","lower"],
                  currentEstimate$base["costs","upper"]))
#perfectInformationCosts$base["costs",]<-data.frame(distribution="const",
#
#                  lower=costsConst,
#                  upper=costsConst,
#                  row.names="costs",
#                  stringsAsFactors=FALSE)
perfectInformationCosts$base["costs","distribution"]<-"const"
perfectInformationCosts$base["costs","lower"]<-costsConst
perfectInformationCosts$base["costs","upper"]<-costsConst
prospectiveEstimate<-list(perfectInformationRevenue=perfectInformationRevenue,
                          perfectInformationCosts=perfectInformationCosts)
# Calculate the Expected Value of Information:
eviSimulationResult<-eviSimulation(model=profit,
                                   currentEstimate=currentEstimate,
                                   prospectiveEstimate=prospectiveEstimate,
                                   numberOfSimulations=numberOfSimulations,
                                   functionSyntax="data.frameNames")

# Show the simulation results:
print(summary(eviSimulationResult))
#####
# Example 3 A list of prospective estimates and two decision variables:
#####
numberOfSimulations=10000
# Create the current estimate object:
variable=c("revenue","costs")
distribution=c("posnorm","posnorm")
lower=c(10000, 5000)
upper=c(100000, 50000)
currentEstimate<-as.estimate(variable, distribution, lower, upper)
# Create a list of two prospective estimates:
perfectInformationRevenue<-currentEstimate
revenueConst<-mean(c(currentEstimate$base["revenue","lower"],
                    currentEstimate$base["revenue","upper"]))
#perfectInformationRevenue$base["revenue",]<-data.frame(distribution="const",
#
#                  lower=revenueConst,
#                  upper=revenueConst,
#                  row.names="revenue",
#                  stringsAsFactors=FALSE)
perfectInformationRevenue$base["revenue","distribution"]<-"const"
perfectInformationRevenue$base["revenue","lower"]<-revenueConst
perfectInformationRevenue$base["revenue","upper"]<-revenueConst
perfectInformationCosts<-currentEstimate
costsConst<-mean(c(currentEstimate$base["costs","lower"],currentEstimate$base["costs","upper"]))
#perfectInformationCosts$base["costs",]<-data.frame(distribution="const",
#
#                  lower=costsConst,
#                  upper=costsConst,
#                  row.names="costs",
#                  stringsAsFactors=FALSE)
perfectInformationCosts$base["costs","distribution"]<-"const"
perfectInformationCosts$base["costs","lower"]<-costsConst
perfectInformationCosts$base["costs","upper"]<-costsConst
prospectiveEstimate<-list(perfectInformationRevenue=perfectInformationRevenue,

```

```

                                perfectInformationCosts=perfectInformationCosts)
# Define the model function with two decision variables:
decisionModel<-function(x){
  list(Profit=x$revenue-x$costs,
       Costs=-x$costs)
}
# Calculate the Expected Value of Information:
eviSimulationResult<-eviSimulation(model=decisionModel,
                                   currentEstimate=currentEstimate,
                                   prospectiveEstimate=prospectiveEstimate,
                                   numberOfSimulations=numberOfSimulations,
                                   functionSyntax="data.frameNames")

# Show the simulation results:
print(sort(summary(eviSimulationResult)),decreasing=TRUE,along="Profit")

```

```
globalNames2data.frameNames
```

Transform model function variable names: global to data.frame names.

Description

The variable names of a function are transformed from global variable names to data.frame names of the form x\$<globalName>.

Usage

```
globalNames2data.frameNames(modelFunction, globalNames)
```

Arguments

modelFunction	a function which body contains global variables. The function must not contain any arguments.
globalNames	a character vector containing the names of the global variables that shall be transformed.

Details

The input function must be of the form:

```

modelFunction<-function(){
  ...
  <expression with variable1>
  ...
}

```

Value

The transformed function which is of the form:

```
function(x){
  ...
  <expression with x$variable1>
  ...
}
```

Warning

If there are local functions within the function modelFunction defined, which arguments have identical names to any of the globalNames the function fails!

See Also

[mcSimulation](#), [estimate](#)

Examples

```
profit1<-function(){
  list(Profit=revenue-costs)
}
profit2<-globalNames2data.frameNames(modelFunction=profit1, globalNames=c("revenue", "costs"))
print(profit2)
is.function(profit2)
profit2(data.frame("revenue"=10, "costs"=2))
```

hist.mcSimulation

Plot Histogram of results of a Monte Carlo Simulation

Description

This function plots the histograms of the results of [mcSimulation](#).

Usage

```
## S3 method for class 'mcSimulation'
hist(x, breaks = 100, col = NULL, xlab = NULL,
     main = paste("Histogram of ", xlab), ..., colorQuantile = c("GREY",
     "YELLOW", "ORANGE", "DARK GREEN", "ORANGE", "YELLOW", "GREY"),
     colorProbability = c(1, 0.95, 0.75, 0.55, 0.45, 0.25, 0.05),
     resultName = NULL)
```

Arguments

x	An object of class <code>mcSimulation</code> .
breaks	one of: <ul style="list-style-type: none"> • a vector giving the breakpoints between histogram cells, • a function to compute the vector of breakpoints, • a single number giving the number of cells for the histogram, • a character string naming an algorithm to compute the number of cells (see ‘Details’), • a function to compute the number of cells. <p>In the last three cases the number is a suggestion only; the breakpoints will be set to <code>pretty</code> values. If <code>breaks</code> is a function, the <code>x</code> vector is supplied to it as the only argument.</p>
col	a colour to be used to fill the bars. The default of <code>NULL</code> yields unfilled bars.
xlab	character; x label of the histogram. If it is not provided, i.e. equals <code>NULL</code> the name of the chosen variable by argument <code>resultName</code> is used.
main	character; main title of the histogram.
...	Further arguments to be passed to <code>hist</code> .
colorQuantile	character vector encoding the color of the quantiles defined in argument <code>colorProbability</code> .
colorProbability	numeric vector; defines the quantiles that shall be distinguished by the colors chosen in argument <code>colorQuantile</code> . Must be of the same length as <code>colorQuantile</code> .
resultName	character; indicating the name of the component of the simulation function (<code>model_function</code>) which results histogram shall be generated. If <code>model_function</code> is single valued, no name needs to be supplied. Otherwise, one valid name has to be specified. Defaults to <code>NULL</code> .

Value

an object of class "histogram". For details see `hist`.

See Also

`mcSimulation`, `hist`. For a list of colors available in R see `colors`.

individualEvpSimulation

Individual Expected Value of Perfect Information Simulation

Description

The Individual Expected Value of Perfect Information (Individual EVPI) is calculated based on a Monte Carlo simulation of the values of two different decision alternatives.

Usage

```
individualEvpSimulation(model, currentEstimate,
  perfectProspectiveNames = row.names(currentEstimate),
  perfectProspectiveValues = colMeans(random(rho = currentEstimate, n =
    numberOfSimulations)[, perfectProspectiveNames]), numberOfSimulations,
  functionSyntax = "data.frameNames")
```

Arguments

model either a function or a list with two functions: `list(p1,p2)`. In the first case the function is the net benefit of project approval vs. the status quo. In the second case the element `p1` is the function valuing the first project and the element `p2` valuing the second project.

currentEstimate **estimate** object describing the distribution of the input variables as currently estimated.

perfectProspectiveNames character vector; input variable names that are assumed to be known perfectly with prospective information.

perfectProspectiveValues numeric vector of the same length as `perfectProspectiveNames` with the corresponding values assumed to be known perfectly.

numberOfSimulations integer; number of simulations to be used in the underlying Monte Carlo analysis

functionSyntax function character; function syntax used in the model function(s).

Details

This principle is along the line described in Hubbard (2014). The Expected Value of Information is the decrease in the EOL for an information improvement from the current estimate (I_{current}) to a better prospective (or hypothetical) information ($I_{\text{prospective}}$): $\text{EVI} := \text{EOL}(I_{\text{current}}) - \text{EOL}(I_{\text{prospective}})$. If one variables under $I_{\text{prospective}}$ is assumed to be known with certainty the EVI is called the Individual Expected Value of Perfect Information (Individual EVPI). More precisely, if one assumes under $I_{\text{prospective}}$ to perfectly know (x_1, \dots, x_k) to equal (a_1, \dots, a_k) then one can specify the notation as Individual EVPI[$x_i = a_i$]. Summarizing, the Individual EVPI depends on the model for valuing a decision, the current information, i.e. the current estimate, and the specification of the variable that is assumed to be known with certainty, viz. the improvement in information, i.e. a prospective estimate.

Value

An object of class `eviSimulation` with the following elements:

current	welfareDecisionAnalysis object for <code>currentEstimate</code>
prospective	welfareDecisionAnalysis object for <code>prospectiveEstimate</code>
evi	Expected Value of Information (EVI) of gained by the prospective estimate w.r.t. the current estimate

See Also

[eviSimulation](#), [welfareDecisionAnalysis](#), [mcSimulation](#), [estimate](#)

Examples

```
# Number of simulations:
n=100000
# Create the current estimate from text:
estimateText<-"variable, distribution, lower, upper
               revenue1, posnorm,      100,   1000
               revenue2, posnorm,      50,   2000
               costs1,   posnorm,      50,   2000
               costs2,   posnorm,     100,   1000"
currentEstimate<-as.estimate(read.csv(header=TRUE, text=estimateText,
                                     strip.white=TRUE, stringsAsFactors=FALSE))

# The model function:
profitModel <- function(x){
  list(Profit=x$revenue1 + x$revenue2 - x$costs1 - x$costs2)
}
# Calculate the Individual EVPI:
individualEvpiResult<-individualEvpiSimulation(model=profitModel,
                                              currentEstimate=currentEstimate,
                                              numberOfSimulations=n,
                                              functionSyntax="data.frameNames")

# Show the simulation results:
print(sort(summary(individualEvpiResult)),decreasing=TRUE,along="Profit")
```

mcSimulation

Perform a Monte Carlo Simulation.

Description

This method solves the following problem. Given a multivariate random variable $x = (x_1, \dots, x_k)$ with joint probability distribution P , i.e.

$$x \sim P.$$

Then the continuous function

$$f : R^k \rightarrow R^l, y = f(x)$$

defines another random variable with distribution

$$y \sim f(P).$$

Given a probability density ρ of x that defines P the problem is the determination of the probability density ϕ that defines $f(P)$. This method samples the probability density ϕ of y by Monte Carlo simulation.

Usage

```
mcSimulation(estimate, model_function, ..., numberOfSimulations,
             randomMethod = "calculate", functionSyntax = "data.frameNames")
```

Arguments

estimate	Filename or estimate object representing the joint probability distribution of the input variables.
model_function	A numeric function; The function that describes the value of a certain project.
...	Optional arguments of model_function.
numberOfSimulations	The number of Monte Carlo simulations to be run.
randomMethod	character. The method to be used to sample the distribution representing the input estimate.
functionSyntax	character. The syntax which has to be used to implement the model function. Possible values are globalNames, data.frameNames or matrixNames. Details are given below.

Details

If functionSyntax="globalNames", the variable names used in the definition of model_function have to be defined globally. model_function has to be of the form function(x,varnames). If functionSyntax="data.frameNames", the model function is constructed, e.g. like this:

```
profit<-function(x){      x[["revenue"]]-x[["costs"]]      }   or like this:
profit<-function(x){      x$revenue-x$costs      }   If functionSyntax="matrixNames",
the model function is constructed, e.g. like this:
profit<-function(x){      x[, "revenue"]-x[, "costs"]      }
```

Value

An object of class mcSimulation.

```
phi  an l-variate probability distribution
x    a dataframe containing the sampled  $x$ - values
y    a dataframe containing the simulated  $y$ - values
```

See Also

[print.mcSimulation](#), [summary.mcSimulation](#), [hist.mcSimulation](#), [estimate](#), [random.estimate](#)

Examples

```
#####
# Example 1 (Creating the estimate from the command line):
#####
# Create the estimate object:
variable=c("revenue","costs")
distribution=c("norm","norm")
lower=c(10000, 5000)
upper=c(100000, 50000)
costBenefitEstimate<-as.estimate(variable, distribution, lower, upper)
# (a) Define the model function without name for the return value:
profit1<-function(x){
```



```

                                numberOfSimulations=100000,
                                functionSyntax="data.frameNames")
# Show the simulation results:
print(summary(predictionProfit2))
hist(predictionProfit2)

```

names.estimate	<i>Return the column names of an estimate object.</i>
----------------	---

Description

This function returns the column names of an [estimate](#) object which is identical to `names(x$base)`.

Usage

```
## S3 method for class 'estimate'
names(x)
```

Arguments

`x` an [estimate](#) object.

See Also

[estimate](#), [row.names.estimate](#), [corMat.estimate](#)

paramtnormci_fit	<i>Fit parameters of truncated normal distribution based on a confidence interval.</i>
------------------	--

Description

This function fits the distribution parameters, i.e. mean and sd, of a truncated normal distribution from an arbitrary confidence interval and, facultatively, the median.

Usage

```
paramtnormci_fit(p, ci, median = mean(ci), lowerTrunc = -Inf,
  upperTrunc = Inf, relativeTolerance = 0.05, fitMethod = "Nelder-Mead",
  ...)
```

Arguments

<code>p</code>	numeric 2-dimensional vector; probabilities of upper and lower bound of the corresponding confidence interval.
<code>ci</code>	numeric 2-dimensional vector; lower, i.e <code>ci[[1]]</code> , and upper bound, i.e <code>ci[[2]]</code> , of the confidence interval.
<code>median</code>	if <code>NULL</code> : truncated normal is fitted only to lower and upper value of the confidence interval; if <code>numeric</code> : truncated normal is fitted on the confidence interval and the median simultaneously. For details cf. below.
<code>lowerTrunc</code>	numeric; lower truncation point of the distribution ($\geq -\text{Inf}$).
<code>upperTrunc</code>	numeric; upper truncation point of the distribution ($\leq \text{Inf}$).
<code>relativeTolerance</code>	numeric; the relative tolerance level of deviation of the generated probability levels from the specified confidence interval. If the relative deviation is greater than <code>relativeTolerance</code> a warning is given.
<code>fitMethod</code>	optimization method used in constrOptim .
<code>...</code>	further parameters to be passed to constrOptim .

Details

For details of the truncated normal distribution see [tnorm](#).

The cumulative distribution of a truncated normal $F_{\mu,\sigma}(x)$ gives the probability that a sampled value is less than x . This is equivalent to saying that for the vector of quantiles $q = (q_{p_1}, \dots, q_{p_k})$ at the corresponding probabilities $p = (p_1, \dots, p_k)$ it holds that

$$p_i = F_{\mu,\sigma}(q_{p_i}), \quad i = 1, \dots, k$$

In the case of arbitrary postulated quantiles this system of equations might not have a solution in μ and σ . A least squares fit leads to an approximate solution:

$$\sum_{i=1}^k (p_i - F_{\mu,\sigma}(q_{p_i}))^2 = \min$$

defines the parameters μ and σ of the underlying normal distribution. This method solves this minimization problem for two cases:

1. `ci[[1]] < median < ci[[2]]`: The parameters are fitted on the lower and upper value of the confidence interval and the median, formally:
 $k = 3$
 $p_1 = p[[1]], p_2 = 0.5$ and $p_3 = p[[2]]$;
 $q_{p_1} = ci[[1]], q_{0.5} = median$ and $q_{p_3} = ci[[2]]$
2. `median=NULL`: The parameters are fitted on the lower and upper value of the confidence interval only, formally:
 $k = 2$
 $p_1 = p[[1]], p_2 = p[[2]]$;
 $q_{p_1} = ci[[1]], q_{p_2} = ci[[2]]$

The $(p[[2]] - p[[1]])$ - confidence interval must be symmetric in the sense that $p[[1]] + p[[2]] = 1$.

Value

A list with elements mean and sd, i.e. the parameters of the underlying normal distribution.

See Also

[tnorm](#), [constrOptim](#)

paramtnormci_numeric	<i>Return parameters of truncated normal distribution based on a confidence interval.</i>
----------------------	---

Description

This function calculates the distribution parameters, i.e. mean and sd, of a truncated normal distribution from an arbitrary confidence interval.

Usage

```
paramtnormci_numeric(p, ci, lowerTrunc = -Inf, upperTrunc = Inf,
  relativeTolerance = 0.05, rootMethod = "probability", ...)
```

Arguments

p	numeric 2-dimensional vector; probabilities of lower and upper bound of the corresponding confidence interval.
ci	numeric 2-dimensional vector; lower, i.e ci[[1]], and upper bound, i.e ci[[2]], of the confidence interval.
lowerTrunc	numeric; lower truncation point of the distribution ($\geq -\text{Inf}$).
upperTrunc	numeric; upper truncation point of the distribution ($\leq \text{Inf}$).
relativeTolerance	numeric; the relative tolerance level of deviation of the generated confidence interval from the specified interval. If this deviation is greater than relativeTolerance a warning is given.
rootMethod	character; if = "probability" the equation defining the parameters mean and sd is the difference between calculated and given probabilities of the confidence interval; if = "quantile" the equation defining the parameters is the difference between calculated and given upper and lower value of the confidence interval.
...	Further parameters passed to nleqslv .

Details

For details of the truncated normal distribution see [tnorm](#).

Value

A list with elements mean and sd, i.e. the parameters of the underlying normal distribution.

See Also

[tnorm](#), [nleqslv](#)

plsr.mcSimulation	<i>Partial Least Squares Regression (PLSR) of Monte Carlo simulation results.</i>
-------------------	---

Description

Perform a Partial Least Squares Regression (PLSR) of Monte Carlo simulation results.

Usage

```
plsr.mcSimulation(object, resultName = NULL, variables.x = names(object$x),
  method = "oscorespls", scale = TRUE, ncomp = 2, ...)
```

Arguments

object	An object of class <code>mcSimulation</code> .
resultName	character; indicating the name of the component of the simulation function (<code>model_function</code>) which results histogram shall be generated. If <code>model_function</code> is single valued, no name needs to be supplied. Otherwise, one valid name has to be specified. Defaults to <code>NULL</code> .
variables.x	character or character vector; Names of the components of the input variables to the simulation function, i.e. the names of the variables in the input estimate which random sampling results shall be displayed. Defaults to all components.
method	the multivariate regression method to be used. If <code>"model.frame"</code> , the model frame is returned.
scale	numeric vector, or logical. If numeric vector, X is scaled by dividing each variable with the corresponding element of <code>scale</code> . If <code>scale</code> is <code>TRUE</code> , X is scaled by dividing each variable by its sample standard deviation. If cross-validation is selected, scaling by the standard deviation is done for every segment.
ncomp	the number of components to include in the model (see below).
...	further arguments to be passed to plsr .

Value

An object of class [mvr](#).

See Also

[mcSimulation](#), [plsr](#), [summary.mvr](#), [biplot.mvr](#), [coef.mvr](#), [plot.mvr](#),

print.mcSimulation	<i>Print Basic Results from Monte Carlo Simulation.</i>
--------------------	---

Description

This function prints basic results from Monte Carlo simulation and returns it invisible.

Usage

```
## S3 method for class 'mcSimulation'  
print(x, ...)
```

Arguments

x	An object of class mcSimulation.
...	Further arguments #ToDo

See Also

[mcSimulation](#)

print.summary.eviSimulation	<i>Print the Summarized EVI Simulation Results.</i>
-----------------------------	---

Description

This function prints the summary of of eviSimulation obtained by [summary.eviSimulation](#).

Usage

```
## S3 method for class 'summary.eviSimulation'  
print(x, ...)
```

Arguments

x	An object of class summary.eviSimulation.
...	Further arguments #ToDo

See Also

[eviSimulation](#)

```
print.summary.mcSimulation
```

Print the Summary of a Monte Carlo Simulation.

Description

This function prints the summary of of mcSimulation obtained by [summary.mcSimulation](#).

Usage

```
## S3 method for class 'summary.mcSimulation'  
print(x, ...)
```

Arguments

x	An object of class mcSimulation.
...	Further arguments #ToDo

See Also

[mcSimulation](#), [summary.mcSimulation](#)

```
print.summary.welfareDecisionAnalysis
```

Print the Summarized Decsion Analysis Results..

Description

This function prints the summary of of welfareDecisionAnalysis obtained by [summary.welfareDecisionAnalysis](#).

Usage

```
## S3 method for class 'summary.welfareDecisionAnalysis'  
print(x, ...)
```

Arguments

x	An object of class summary.welfareDecisionAnalysis.
...	Further arguments #ToDo

See Also

[welfareDecisionAnalysis](#)

random	<i>Quantiles based generic random number generation.</i>
--------	--

Description

This function generates random numbers for parametric distributions, parameters of which are determined by given quantiles.

The default method generates univariate random numbers specified by arbitrary quantiles.

Usage

```
random(rho, n, method, relativeTolerance, ...)
```

```
## Default S3 method:
```

```
random(rho = list(distribution = "norm", probabilities =
  c(0.05, 0.95), quantiles = c(qnorm(0.05), qnorm(0.95))), n, method = "fit",
  relativeTolerance = 0.05, ...)
```

Arguments

rho	list Distribution to be randomly sampled. The list elements are distribution, probabilities and quantiles. For details cf. below.
n	integer Number of observations to be generated
method	character Particular method to be used for random number generation. Currently only method <code>rdistq_fit{fit}</code> is implemented which is the default.
relativeTolerance	numeric; the relative tolerance level of deviation of the generated confidence interval from the specified interval. If this deviation is greater than <code>relativeTolerance</code> a warning is given.
...	Optional arguments to be passed to the particular random number generating function, i.e. <code>rdistq_fit</code> .

Details

The distribution family is determined by `rho[["distribution"]]`. For the possibilities cf. `rdistq_fit`. `rho[["probabilities"]]` and `[[rho"quantiles"]]` are numeric vectors of the same length. The first defines the probabilities of the quantiles, the second defines the quantiles values which determine the parametric distribution.

Value

A numeric vector of length `n` containing the generated random numbers.

Methods (by class)

- default: Univariate random number generation.

See Also[rdistq_fit](#)**Examples**

```

x<-random(n=10000)
hist(x,breaks=100)
mean(x)
sd(x)

rho<-list(distribution="norm",
          probabilities=c(0.05,0.4,0.8),
          quantiles=c(-4, 20, 100))
x<-random(rho=rho, n=10000, tolConv=0.01)
hist(x,breaks=100)
quantile(x,p=rho[["probabilities"]])

```

random.estimate

*Generate Random Numbers for an Estimate.***Description**

This function generates random numbers for general multivariate distributions that are defined as an [estimate](#).

Usage

```

## S3 method for class 'estimate'
random(rho, n, method = "calculate",
       relativeTolerance = 0.05, ...)

```

Arguments

rho	estimate object; Multivariate distribution to be randomly sampled.
n	Number of generated observations
method	Particular method to be used for random number generation.
relativeTolerance	numeric; the relative tolerance level of deviation of the generated confidence interval from the specified interval. If this deviation is greater than relativeTolerance a warning is given.
...	Optional arguments to be passed to the particular random number generating function.

Details

Generation of uncorrelated components: Implementation: [random.estimate1d](#)

Generation of correlated components: Implementation: [rmvnorm90ci_exact](#)

See Also

[estimate](#), [random.estimate1d](#), [random](#)

Examples

```
variable=c("revenue","costs")
distribution=c("norm","norm")
lower=c(10000, 5000)
upper=c(100000, 50000)
estimateObject<-as.estimate(variable, distribution, lower, upper)
x<-random(rho=estimateObject, n=10000)
apply(X=x, MARGIN=2, FUN=quantile, probs=c(0.05, 0.95))
cor(x)
colnames(x)
summary(x)
hist(x[, "revenue"])
hist(x[, "costs"])
```

random.estimate1d	<i>Generate univariate random numbers defined by a 1-d estimate.</i>
-------------------	--

Description

This function generates random numbers for univariate parametric distributions, which parameters are determined by a one dimensional estimate ([estimate1d](#)).

Usage

```
## S3 method for class 'estimate1d'
random(rho, n, method = "calculate",
       relativeTolerance = 0.05, ...)
```

Arguments

rho	estimate1d: Univariate distribution to be randomly sampled.
n	integer: Number of observations to be generated
method	character: Particular method to be used for random number generation. It can be either "calculate" (the default) or "fit". Details below.
relativeTolerance	numeric: the relative tolerance level of deviation of the generated confidence interval from the specified interval. If this deviation is greater than relativeTolerance a warning is given.
...	Optional arguments to be passed to the particular random number generating function (cf. below).

Details

`rho[["distribution"]]`: The following table shows the available distributions and the implemented generation method:

<code>rho[["distribution"]]</code>	Distribution Name	method
<code>"const"</code>	Deterministic case	not applicable
<code>"norm"</code>	Normal	calculate , fit
<code>"posnorm"</code>	Positive normal	calculate , fit
<code>"tnorm_0_1"</code>	0-1-truncated normal	calculate , fit
<code>"beta"</code>	Beta	fit
<code>"cauchy"</code>	Cauchy	fit
<code>"logis"</code>	Logistic	fit
<code>"t"</code>	Student t	fit
<code>"chisq"</code>	Central Chi-Squared	fit
<code>"chisqnc"</code>	Non-central Chi-Squared	fit
<code>"exp"</code>	Exponential	fit
<code>"f"</code>	Central F	fit
<code>"gamma"</code>	Gamma with scale=1/rate	fit
<code>"lnorm"</code>	Log Normal	calculate , fit
<code>"unif"</code>	Uniform	calculate , fit
<code>"weibull"</code>	Weibull	fit
<code>"triang"</code>	Triangular	fit
<code>"gompertz"</code>	Gompertz	fit
<code>"pert"</code>	(Modified) PERT	fit

For `distribution="const"` the argument `method` is obsolete, as a constant is neither fitted nor calculated.

`rho[["method"]]` If supplied, i.e. `!is.null(rho[["method"]])`, this value overwrites the function argument `method`.

`method` This parameter defines, how the parameters of the distribution to be sample are derived from `rho[["lower"]]`, `rho[["upper"]]` and possibly `rho[["median"]]`. Possibilities are `"calculate"` (the default) or `"fit"`:

`method="calculate"` The parameters are calculated if possible using the exact (analytical) formula or, otherwise, numerically. This calculation of the distribution parameters is independent of `rho[["median"]]` being supplied or not. For the implemented distributions, it only depends on `rho[["lower"]]` and `rho[["upper"]]`. However, if it is supplied, i.e. `is.numeric(rho[["median"]])`, a check is performed, if the relative deviation of the generated median from `rho[["median"]]` is greater than `relativeTolerance`. In this case a warning is given.

`method="fit"` The parameters are obtained by fitting the distribution on the supplied quantiles. Given that `rho[["median"]]==NULL` the distribution is fitted only to lower and upper and a warning is given; due to the used numerical procedure, the calculated parameters might define a distribution which strongly deviates from the intended one. There is larger control on the shape of the distribution to be generated by supplying the estimate of the median. If `is.numeric(rho[["median"]])` the distribution is fitted to lower, upper and median.

... For passing further parameters to the function which generates the random numbers, cf. the above table and follow the link in the column `method`.

See Also

`estimate1d`; For method="calculate": `rdist90ci_exact`; for method="fit": `rdistq_fit`; for both methods: `rposnorm90ci` and `rtnorm_0_1_90ci`. For the default method: `random`.

Examples

```
# Generate log normal distributed random numbers:
x<-random(estimate1d("lnorm",50,100), n=100000)
quantile(x, probs=c(0.05, 0.95))
hist(x, breaks=100)
```

<code>rdist90ci_exact</code>	<i>90%-confidence interval based univariate random number generation (by exact parameter calculation).</i>
------------------------------	--

Description

This function generates random numbers for a set of univariate parametric distributions from given 90% confidence interval. Internally, this is achieved by exact, i.e. analytic, calculation of the parameters for the individual distribution from the given 90% confidence interval.

Usage

```
rdist90ci_exact(distribution, n, lower, upper)
```

Arguments

<code>distribution</code>	character; A character string that defines the univariate distribution to be randomly sampled. For possible options cf. section Details.
<code>n</code>	Number of generated observations.
<code>lower</code>	numeric; lower bound of the 90% confidence intervall.
<code>upper</code>	numeric; upper bound of the 90% confidence intervall.

Details

The follwing table shows the available distributions and their identification (option: `distribution`) as a character string:

distribution	Distribution Name	Requirements
"const"	Deterministic case	lower == upper
"norm"	Normal	lower < upper
"lnorm"	Log Normal	0 < lower < upper
"unif"	Uniform	lower < upper

Parameter formulae: We use the notation: l =lower and u =upper; Φ is the cummulative distribution function of the standard normal distribution and Φ^{-1} its inverse, which is the quantile

function of the standard normal distribution.

distribution="norm": The formulae for μ and σ , viz. the mean and standard deviation, respectively, of the normal distribution are $\mu = \frac{l+u}{2}$ and $\sigma = \frac{\mu-l}{\Phi^{-1}(0.95)}$.

distribution="unif": For the minimum a and maximum b of the uniform distribution $U_{[a,b]}$ it holds that $a = l - 0.05(u - l)$ and $b = u + 0.05(u - l)$.

distribution="lnorm": The density of the log normal distribution is $f(x) = \frac{1}{\sqrt{2\pi\sigma x}} \exp(-\frac{(\ln(x)-\mu)^2}{2\sigma^2})$ for $x > 0$ and $f(x) = 0$ otherwise. Its parameters are determined by the confidence interval via $\mu = \frac{\ln(l)+\ln(u)}{2}$ and $\sigma = \frac{1}{\Phi^{-1}(0.95)}(\mu - \ln(l))$. Note the correspondence to the formula for the normal distribution.

Value

A numeric vector of length n with the sampled values according to the chosen distribution.

In case of distribution="const", viz. the deterministic case, the function returns: rep(lower, n).

Examples

```
# Generate uniformly distributed random numbers:
lower=3
upper=6
hist(r<-rdist90ci_exact(distribution="unif", n=10000, lower=lower, upper=upper),breaks=100)
print(quantile(x=r, probs=c(0.05,0.95)))
print(summary(r))

# Generate log normal distributed random numbers:
hist(r<-rdist90ci_exact(distribution="lnorm", n=10000, lower=lower, upper=upper),breaks=100)
print(quantile(x=r, probs=c(0.05,0.95)))
print(summary(r))
```

rdistq_fit	<i>Quantiles based univariate random number generation (by parameter fitting).</i>
------------	--

Description

This function generates random numbers for a set of univariate parametric distributions from given quantiles. Internally, this is achieved by fitting the distribution function to the given quantiles.

Usage

```
rdistq_fit(distribution, n, percentiles = c(0.05, 0.5, 0.95), quantiles,
  relativeTolerance = 0.05, tolConv = 0.001, fit.weights = rep(1,
  length(percentiles)), verbosity = 1)
```

Arguments

distribution	A character string that defines the univariate distribution to be randomly sampled.
n	Number of generated observations.
percentiles	Numeric vector giving the percentiles.
quantiles	Numeric vector giving the quantiles.
relativeTolerance	numeric; the relative tolerance level of deviation of the generated individual percentiles from the specified percentiles. If any deviation is greater than relativeTolerance a warning is given.
tolConv	positive numerical value, the absolute convergence tolerance for reaching zero by fitting distributions get.norm.par will be shown.
fit.weights	numerical vector of the same length as a probabilities vector p containing positive values for weighting quantiles. By default all quantiles will be weighted by 1.
verbosity	integer; if 0 the function is silent; the larger the value the more verbose is the output information.

Details

The following table shows the available distributions and their identification (option: distribution) as a character string:

distribution	Distribution Name	length(quantiles)	Necessary Package
"norm"	Normal	>=2	
"beta"	Beta	>=2	
"cauchy"	Cauchy	>=2	
"logis"	Logistic	>=2	
"t"	Student t	>=1	
"chisq"	Central Chi-Squared	>=1	
"chisqnc"	Non-central Chi-Squared	>=2	
"exp"	Exponential	>=1	
"f"	Central F	>=2	
"gamma"	Gamma with scale=1/rate	>=2	
"lnorm"	Log Normal	>=2	
"unif"	Uniform	==2	
"weibull"	Weibull	>=2	
"triang"	Triangular	>=3	mc2d
"gompertz"	Gompertz	>=2	eha
"pert"	(Modified) PERT	>=4	mc2d
"tnorm"	Truncated Normal	>=4	msm

percentiles and quantiles must be of the same length. percentiles must be ≥ 0 and ≤ 1 .

The default for percentiles is 0.05, 0.5 and 0.95, so for the default, the quantiles argument should be a vector with 3 elements. If this is to be longer, the percentiles argument has to be adjusted to match the length of quantiles.

The fitting of the distribution parameters is done using [rriskFitdist.perc](#).

Value

A numeric vector of length n with the sampled values according to the chosen distribution.

See Also

[rriskFitdist.perc](#)

Examples

```
# Fit a log normal distribution to 3 quantiles:
percentiles<-c(0.05, 0.5, 0.95)
quantiles=c(1,3,15)
hist(r<-rdistq_fit(distribution="lnorm", n=10000, quantiles=quantiles),breaks=100)
print(quantile(x=r, probs=percentiles))
```

rmvnorm90ci_exact	<i>90%-confidence interval multivariate normal random number generation.</i>
-------------------	--

Description

This function generates normal distributed multivariate random numbers which parameters are determined by the 90%-confidence interval. The calculation of mean and sd is exact.

Usage

```
rmvnorm90ci_exact(n, lower, upper, correlationMatrix)
```

Arguments

n	integer Number of observations to be generated.
lower	numeric vector; lower bound of the 90% confidence intervall.
upper	numeric vector; upper bound of the 90% confidence intervall.
correlationMatrix	numeric symmetric matrix which is the correlation matrix of the multivariate normal distribution. In particular, all diagonal elements must be equal to 1.

See Also

[random](#), [rmvnorm](#)

row.names.estimate	<i>Return the variable names of an estimate object.</i>
--------------------	---

Description

This function returns the variable names of an [estimate](#) object which is identical to `row.names(x$base)`.

Usage

```
## S3 method for class 'estimate'
row.names(x)
```

Arguments

`x` an [estimate](#) object.

See Also

[estimate](#), [names.estimate](#), [corMat.estimate](#)

rtnorm90ci	<i>90%-confidence interval based truncated normal random number generation.</i>
------------	---

Description

`rtnorm90ci` generates truncated normal random numbers based on the 90% confidence interval calculating the distribution parameter numerically from the 90%-confidence interval or via a fit on the 90%-confidence interval. The fit might include the median or not.

`rposnorm90ci` generates positive normal random numbers based on the 90% confidence interval. It is a wrapper function for `rtnorm90ci`.

`rtnorm_0_1_90ci` generates normal random numbers truncated to $[0, 1]$ based on the 90% confidence interval. It is a wrapper function for `rtnorm90ci`.

Usage

```
rtnorm90ci(n, ci, median = mean(ci), lowerTrunc = -Inf, upperTrunc = Inf,
  method = "numeric", relativeTolerance = 0.05, ...)
```

```
rposnorm90ci(n, lower, median = mean(c(lower, upper)), upper,
  method = "numeric", relativeTolerance = 0.05, ...)
```

```
rtnorm_0_1_90ci(n, lower, median = mean(c(lower, upper)), upper,
  method = "numeric", relativeTolerance = 0.05, ...)
```


Arguments

n	Number of generated observations.
ci	numeric 2-dimensional vector; lower, i.e ci[[1]], and upper bound, i.e ci[[2]], of the 90%-confidence interval.
median	if NULL: truncated normal is fitted only to lower and upper value of the confidence interval; if numeric: truncated normal is fitted on the confidence interval and the median simultaneously. For details cf. below. This option is only relevant if method="fit".
lowerTrunc	numeric; lower truncation point of the distribution ($\geq -\text{Inf}$).
upperTrunc	numeric; upper truncation point of the distribution ($\leq \text{Inf}$).
method	method used to determine the parameters of the truncated normal; possible methods are "numeric" (the default) and "fit".
relativeTolerance	numeric; the relative tolerance level of deviation of the generated confidence interval from the specified interval. If this deviation is greater than relativeTolerance a warning is given.
...	further parameters to be passed to paramtnormci_numeric or paramtnormci_fit , respectively.
lower	numeric; lower bound of the 90% confidence interval.
upper	numeric; upper bound of the 90% confidence interval.

Details

method="numeric" is implemented by [paramtnormci_numeric](#) and method="fit" by [paramtnormci_fit](#).

Positive normal random number generation: a positive normal distribution is a truncated normal distribution with lower truncation point equal to zero and upper truncation is infinity. `rposnorm90ci` implements this as a wrapper function for `rtnorm90ci(n, c(lower,upper), median, lowerTrunc=0, upperTrunc=Inf,`

0-1-(truncated) normal random number generation: a 0-1-normal distribution is a truncated normal distribution with lower truncation point equal to zero and upper truncation equal to 1. `rtnorm_0_1_90ci` implements this as a wrapper function for `rtnorm90ci(n, c(lower,upper), median, lowerTrunc=0, upperTrunc=1, m`

See Also

For the implementation of method="numeric": [paramtnormci_numeric](#); for the implementation of method="fit": [paramtnormci_fit](#).

```
sort.summary.eviSimulation
```

Sort Summarized EVI Simulation Results..

Description

Sort summarized EVI simulation results according to their EVI.

Usage

```
## S3 method for class 'summary.eviSimulation'
sort(x, decreasing = TRUE, ...,
     along = row.names(x$summary$evi)[[1]])
```

Arguments

x	An object of class <code>summary.eviSimulation</code> .
decreasing	logical; if the evi should be sorted in decreasing order.
...	Further arguments <code>#ToDo</code>
along	character; the name of the valuation variable along which evi should be sorted.

Value

An object of class `summary.eviSimulation`.

See Also

[eviSimulation](#), [summary.eviSimulation](#), [sort](#)

`summary.eviSimulation` *Summarize EVI Simulation Results*

Description

`summary.eviSimulation` produces result summaries of the results of Expected Value of Information (EVI) simulation obtained by the function [eviSimulation](#).

Usage

```
## S3 method for class 'eviSimulation'
summary(object, ..., digits = max(3,
  getOption("digits") - 3))
```

Arguments

object	An object of class <code>eviSimulation</code> .
...	Further arguments passed to summary.welfareDecisionAnalysis .
digits	how many significant digits are to be used for numeric and complex x. The default, NULL, uses getOption("digits") . This is a suggestion: enough decimal places will be used so that the smallest (in magnitude) number has this many significant digits, and also to satisfy <code>nsmall</code> . (For the interpretation for complex numbers see signif .)

Value

An object of class `summary.eviSimulation`.

See Also

[eviSimulation](#), [print.summary.eviSimulation](#), [summary.welfareDecisionAnalysis](#)

<code>summary.mcSimulation</code>	<i>Summarize Results from Monte Carlo Simulation.</i>
-----------------------------------	---

Description

A summary of the results of a Monte Carlo simulation obtained by the function `mcSimulation` is produced.

Usage

```
## S3 method for class 'mcSimulation'
summary(object, ..., digits = max(3,
  getOption("digits") - 3), variables.y = names(object$y), variables.x = if
  (classicView) names(object$x), classicView = FALSE, probs = c(0, 0.1,
  0.25, 0.5, 0.75, 0.9, 1))
```

Arguments

<code>object</code>	An object of class <code>mcSimulation</code> .
<code>...</code>	Further arguments passed to summary.data.frame (<code>classicView=TRUE</code>) or format (<code>classicView=FALSE</code>).
<code>digits</code>	how many significant digits are to be used for numeric and complex x. The default, <code>NULL</code> , uses getOption("digits") . This is a suggestion: enough decimal places will be used so that the smallest (in magnitude) number has this many significant digits, and also to satisfy <code>nsmall</code> . (For the interpretation for complex numbers see signif .)
<code>variables.y</code>	character or character vector; Names of the components of the simulation function (<code>model_function</code>) which results shall be displayed. Defaults to all components.
<code>variables.x</code>	character or character vector; Names of the components of the input variables to the simulation function, i.e. the names of the variables in the input estimate which random sampling results shall be displayed. Defaults to all components.
<code>classicView</code>	logical; if <code>TRUE</code> the results are summarized using <code>summary.data.frame</code> , if <code>FALSE</code> further output is produced and the quantile information can be chosen. Cf. section Value and argument <code>probs</code> . Default is <code>FALSE</code> .
<code>probs</code>	numeric vector of quantiles that shall be displayed if <code>classicView=FALSE</code> .

Value

An object of class `summary.mcSimulation`.

chance_loss
 chance_zero
 chance_gain

See Also

[mcSimulation](#), [print.summary.mcSimulation](#), [summary.data.frame](#)

summary.welfareDecisionAnalysis

Summarize Decsion Analysis Results.

Description

summary.welfareDecisionAnalysis produces result summaries of the results of decision analysis simulation obtained by the function [welfareDecisionAnalysis](#).

Usage

```
## S3 method for class 'welfareDecisionAnalysis'
summary(object, ..., digits = max(3,
  getOption("digits") - 3))
```

Arguments

object	An object of class welfareDecisionAnalysis.
...	Further arguments passed to format .
digits	how many significant digits are to be used for numeric and complex x. The default, NULL, uses getOption("digits") . This is a suggestion: enough decimal places will be used so that the smallest (in magnitude) number has this many significant digits, and also to satisfy nsmall. (For the interpretation for complex numbers see signif .)

Value

An object of class summary.welfareDecisionAnalysis.

See Also

[welfareDecisionAnalysis](#), [print.summary.welfareDecisionAnalysis](#), [format](#)

uncertaintyAnalysis *Uncertainty Analysis Wrapper Function.*

Description

This function performs a Monte Carlo simulation from input files and analyses the results via Partial Least Squares Regression (PLSR) and calculates the Variable Importance on Projection (VIP). Results are saved as plots.

Usage

```
uncertaintyAnalysis(inputFilePath, outputPath, modelFunction,
  numberOfSimulations, randomMethod = "calculate",
  functionSyntax = "globalNames", write_table = TRUE,
  plsVipAnalysis = TRUE, indicators = FALSE, log_scales = FALSE,
  oldInputStandard = FALSE, verbosity = 1)
```

Arguments

inputFilePath	Path to input csv file, which gives the input estimate .
outputPath	Path where the result plots and tables are saved.
modelFunction	The model function.
numberOfSimulations	The number of Monte Carlo simulations to be performed.
randomMethod	ToDo
functionSyntax	ToDo
write_table	logical: If the full Monte Carlo simulation results and PLSR results should be written to file.
plsVipAnalysis	logical: If PLSR-VIP analysis shall be performed.
indicators	logical: If indicator variables should be respected specially.
log_scales	logical: If the scales in the pls plots should be logarithmic.
oldInputStandard	logical: If the old input standard should be used (estimate_read_csv_old).
verbosity	integer: if 0 the function is silent; the larger the value the more verbose is output information.

See Also

[mcSimulation](#), [estimate](#), [estimate_read_csv](#), [pls.mcSimulation](#), [VIP](#)

welfareDecisionAnalysis

Analysis of the Underlying Welfare Based Decision Problem

Description

The optimal choice between two different opportunities is calculated. This decision is based on minimizing the Expected Net Loss (ENL).

Usage

```
welfareDecisionAnalysis(estimate, model, numberOfSimulations,
  functionSyntax = "data.frameNames")
```

Arguments

estimate	estimate object describing the distribution of the input variables.
model	either a function or a list with two functions: <code>list(p1,p2)</code> . In the first case the function is the net benefit of project approval vs. the status quo. In the second case the element p1 is the function valuing the first project and the element p2 valuing the second project.
numberOfSimulations	integer; number of simulations to be used in the underlying Monte Carlo analysis
functionSyntax	function character; function syntax used in the model function(s).

Details

This principle is along the line described in Hubbard (2014). The Expected Opportunity Loss (EOL) is defined as the Expected Net Loss (ENL) for the best decision. The best decision minimises the ENL. The EOL is always conditional on the available information (I): $EOL = ENL(I)$. Here, the available information is the supplied estimate. One can show that in the case of two alternatives, minimization of EOL is equivalent to maximization of the Expected Net Benefit.

Value

An object of class `welfareDecisionAnalysis` with the following elements:

enbPa	Expected Net Loss (ENL) in case of project approval (PA)
enbSq	Expected Net Loss (ENL) in case of status quo (SQ)
eol	Expected Opportunity Loss (EOL)
optimalChoice	The optimal choice, i.e. either project approval (PA) or the status quo (SQ)

See Also

[mcSimulation](#), [estimate](#), [summary.welfareDecisionAnalysis](#)

Examples

```
#####
# Example 1 (Creating the estimate from the command line):
#####
# Create the estimate object:
variable=c("revenue","costs")
distribution=c("posnorm","posnorm")
lower=c(10000, 5000)
upper=c(100000, 50000)
costBenefitEstimate<-as.estimate(variable, distribution, lower, upper)
# (a) Define the model function without name for the return value:
profit<-function(x){
  x$revenue-x$costs
}
# Perform the decision analysis:
myAnalysis<-welfareDecisionAnalysis(estimate=costBenefitEstimate,
                                   model=profit,
                                   numberOfSimulations=100000,
                                   functionSyntax="data.frameNames")

# Show the analysis results:
print(summary((myAnalysis)))
#####
# (b) Define the model function with a name for the return value:
profit<-function(x){
  list(Profit=x$revenue-x$costs)
}
# Perform the decision analysis:
myAnalysis<-welfareDecisionAnalysis(estimate=costBenefitEstimate,
                                   model=profit,
                                   numberOfSimulations=100000,
                                   functionSyntax="data.frameNames")

# Show the analysis results:
print(summary((myAnalysis)))
#####
# (c) Two decision variables:
decisionModel<-function(x){
  list(Profit=x$revenue-x$costs,
       Costs=-x$costs)
}
# Perform the decision analysis:
myAnalysis<-welfareDecisionAnalysis(estimate=costBenefitEstimate,
                                   model=decisionModel,
                                   numberOfSimulations=100000,
                                   functionSyntax="data.frameNames")

# Show the analysis results:
print(summary((myAnalysis)))
```


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