



Machine Learning and Statistical Methods for Time Series Analysis

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Elastic

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@prelertsteve

Agenda

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Introduction

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Machine Learning Overview

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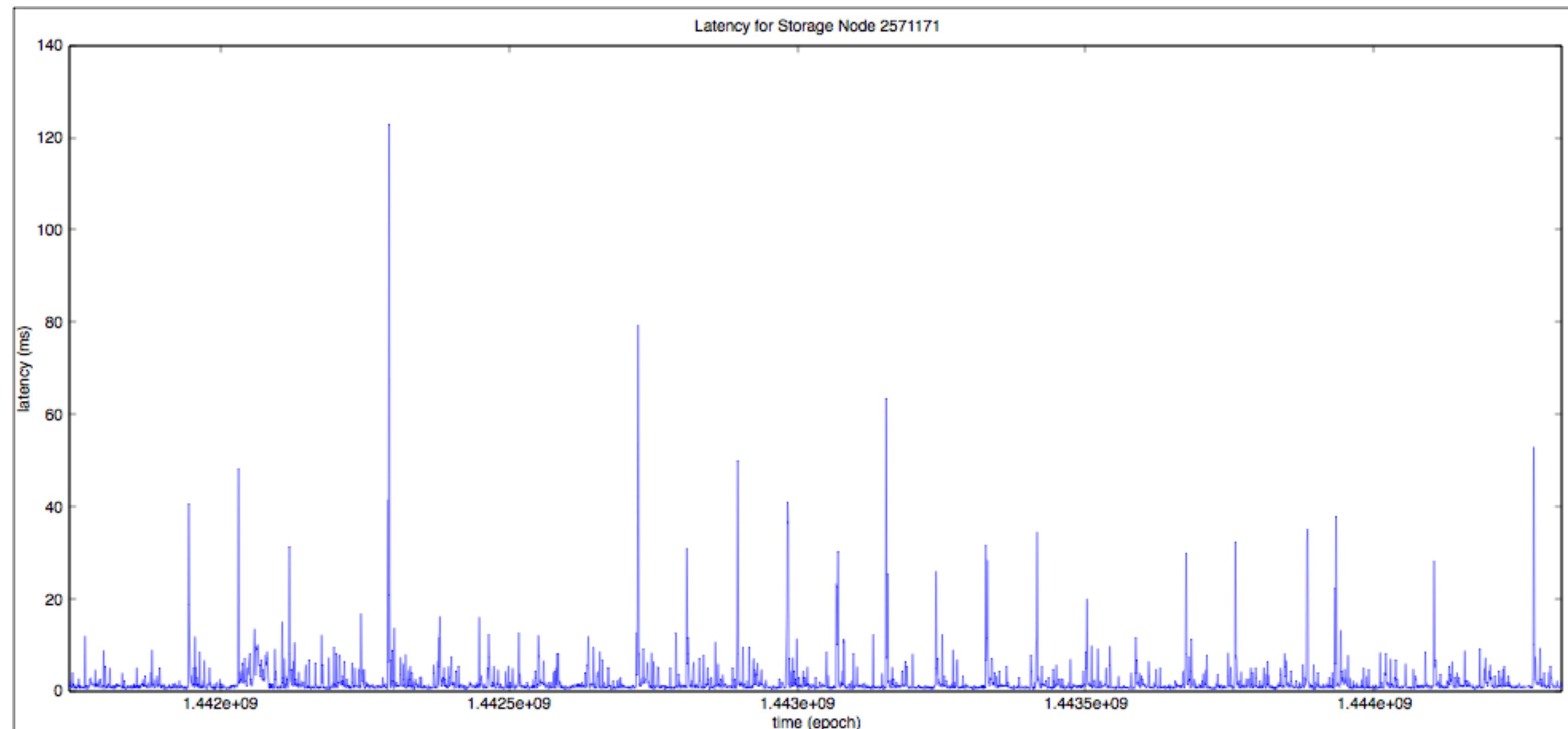
Time Series Anomaly Detection

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Demo

Introduction

- Problem Overview and Technology Background
- Problem Examples



Machine Learning Overview

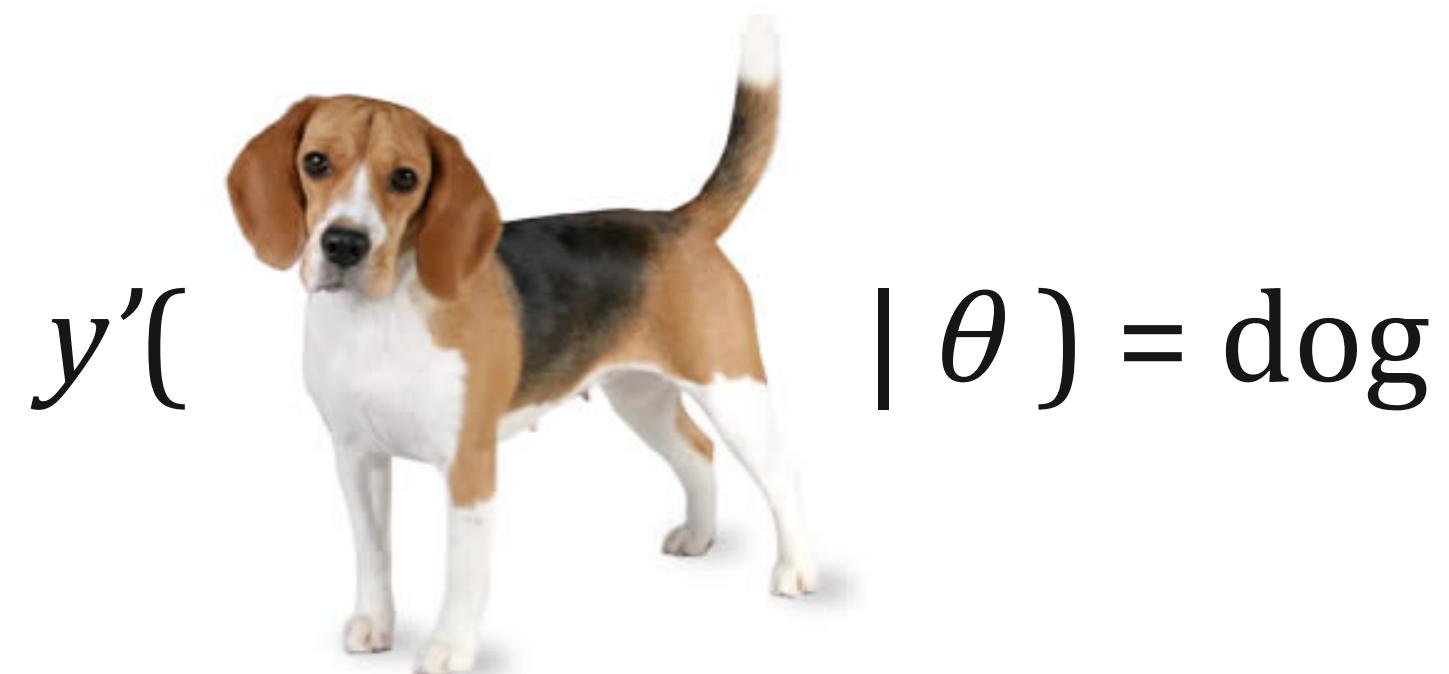
Supervised Machine Learning

Given (Input, Output) pairs, i.e. (x, y)



$y'($

$| \theta) = \text{cat}$



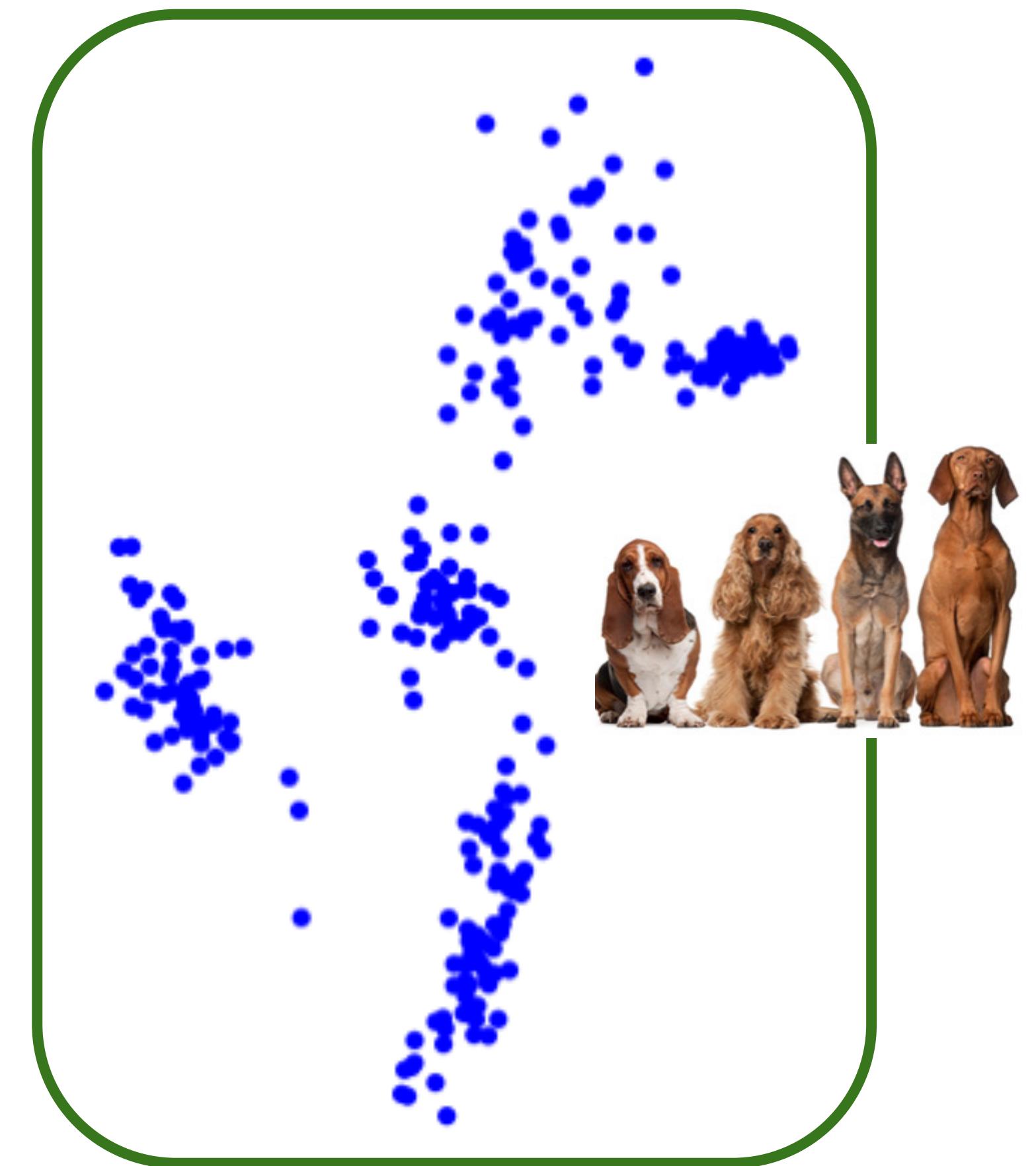
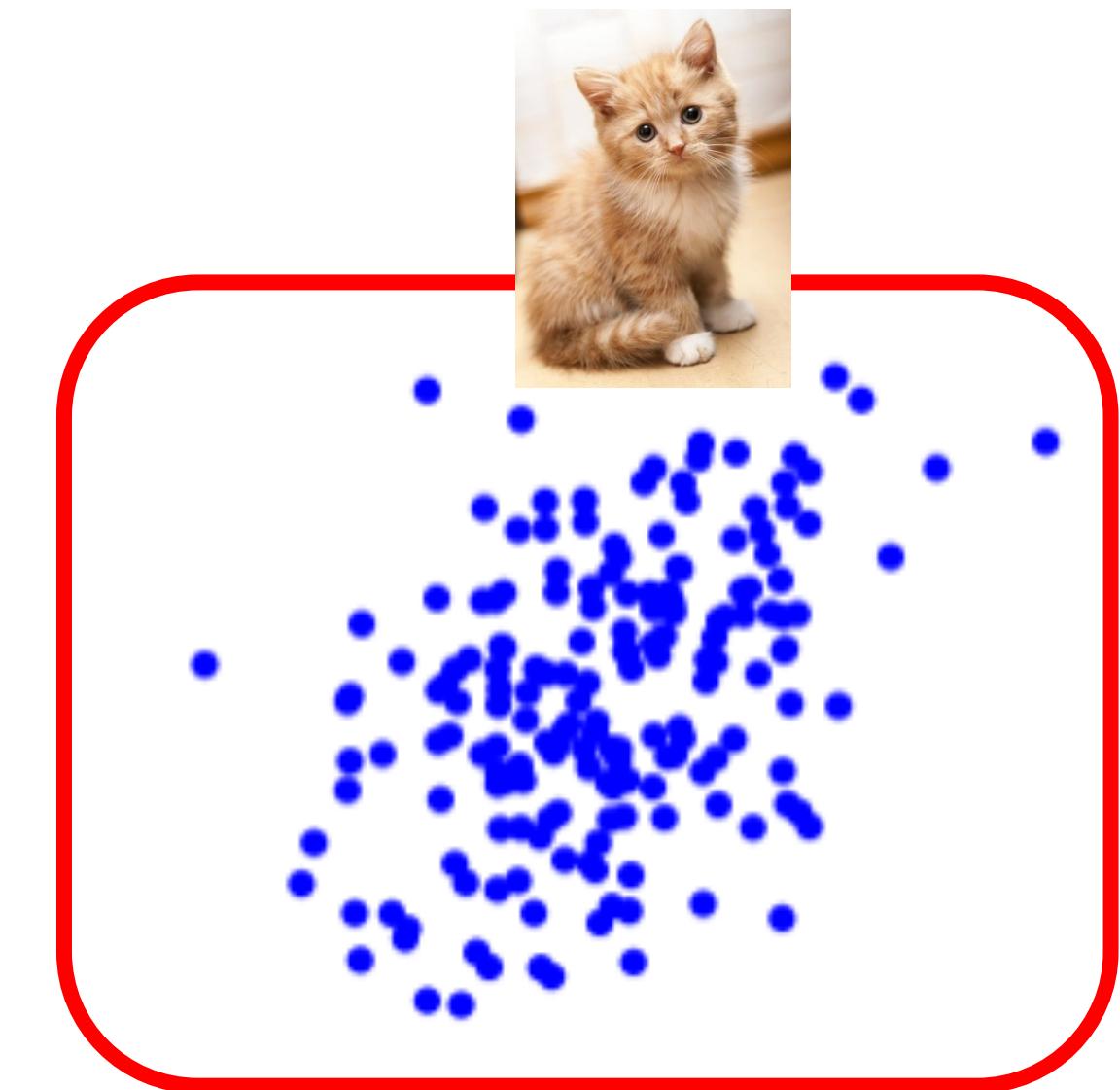
$y'($

Learn θ by minimizing measure of prediction error, i.e. $\|y - y'(x | \theta)\|$.

Unsupervised Machine Learning

Aren't told the outputs

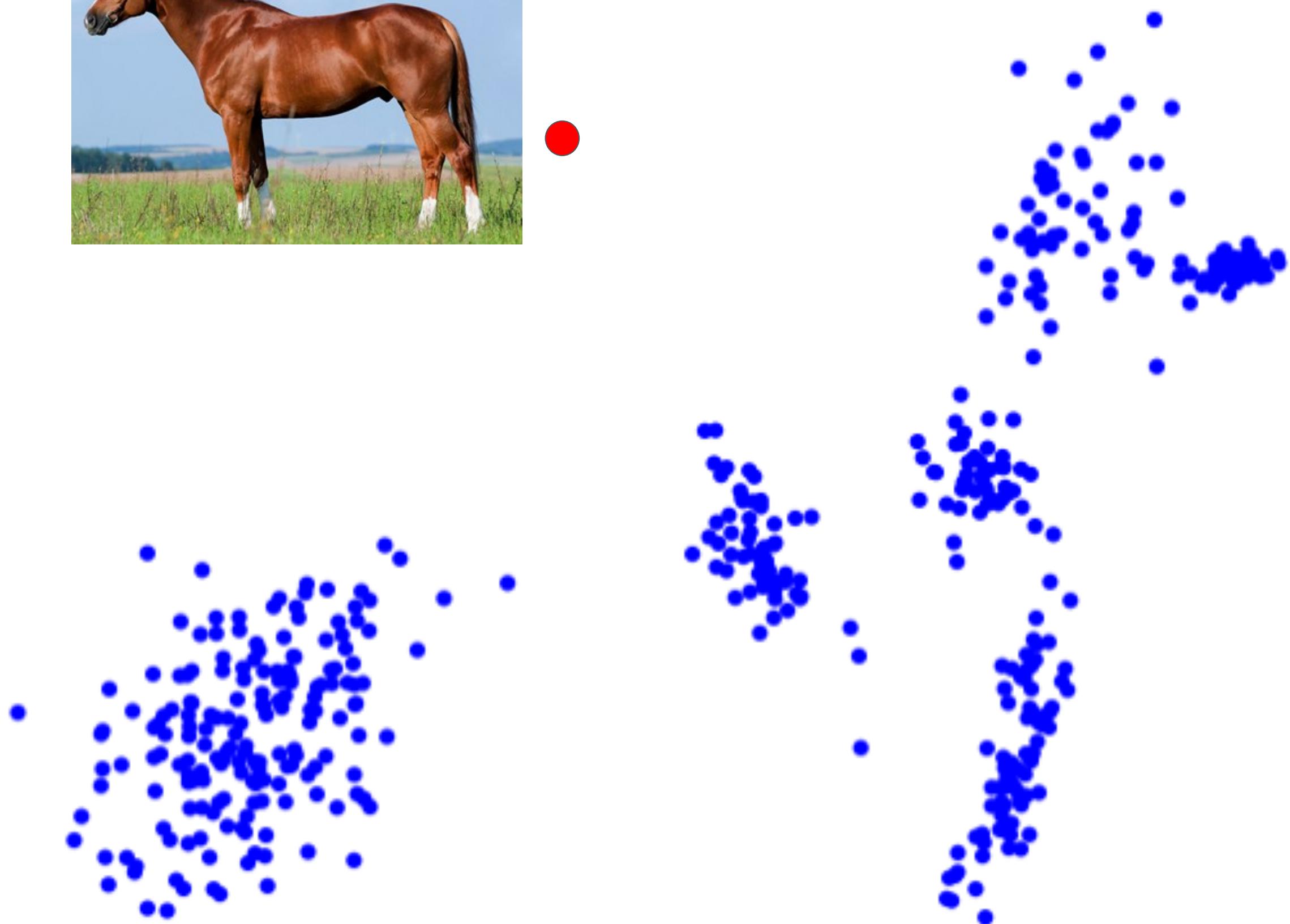
What objective does it make sense to target in this case?



Anomaly Detection

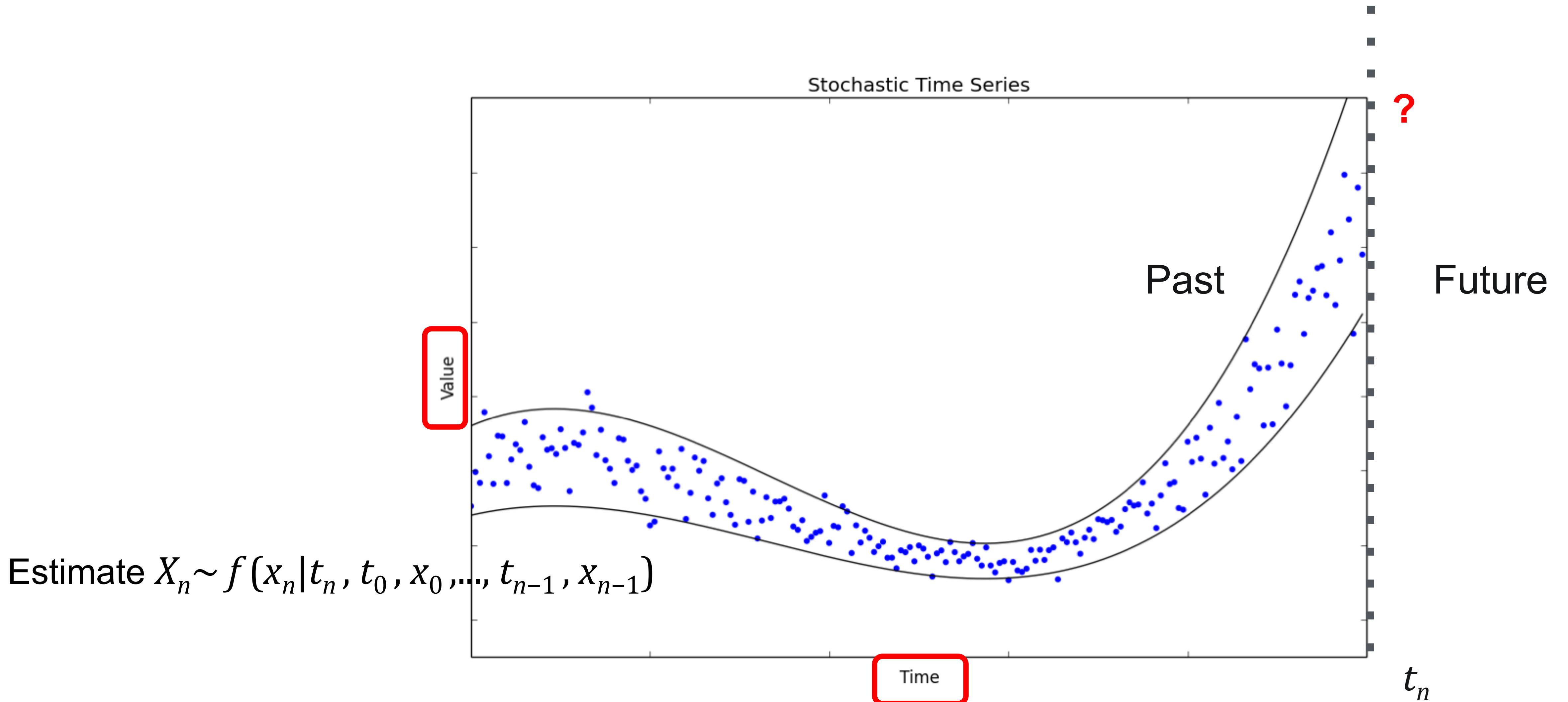
This is useful for anomaly detection

*“ values which don’t fit the model
are the things of interest ”*



Time Series Anomaly Detection

Time Series Anomaly Detection

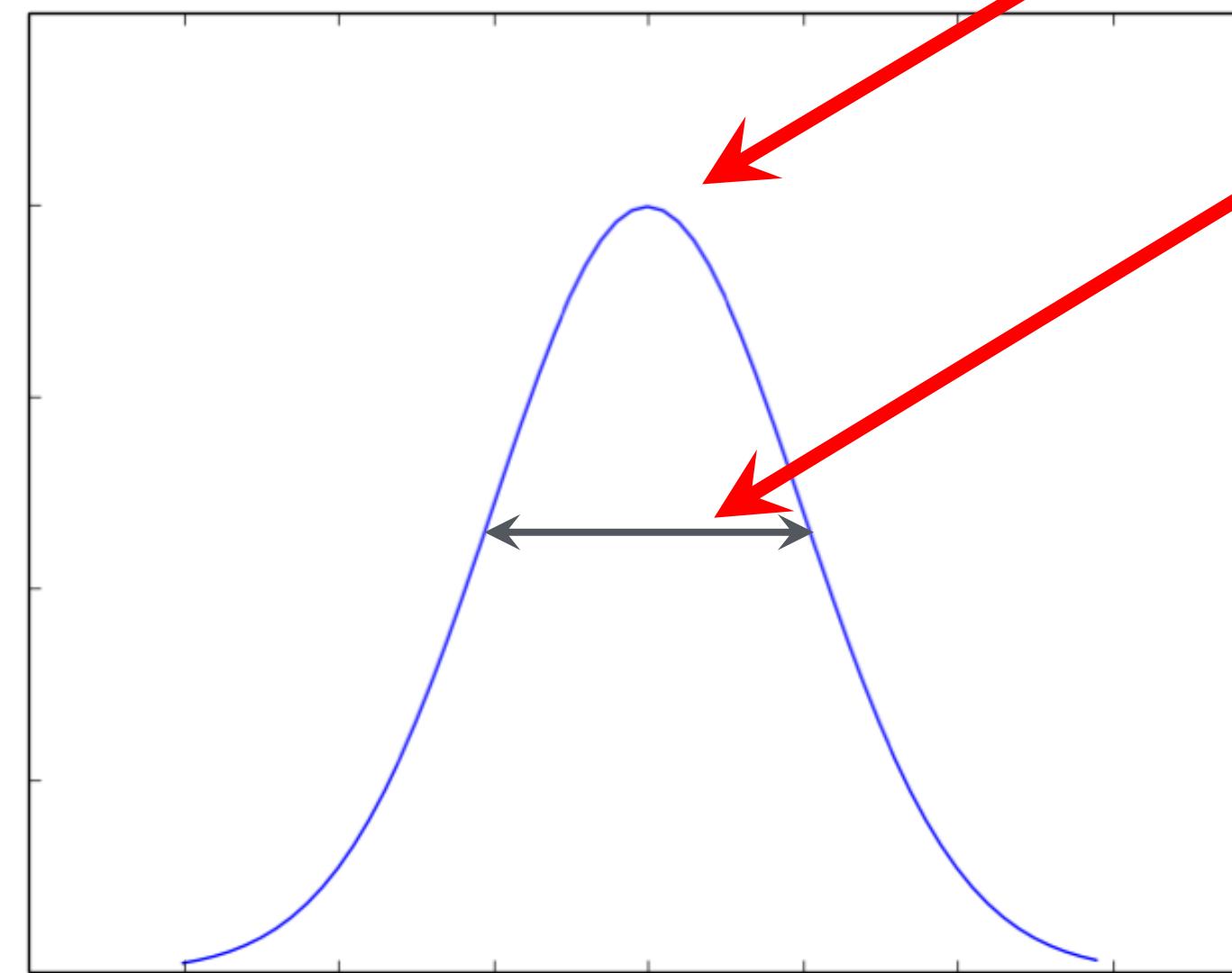


Time Series Anomaly Detection

Break problem down

$$f(x_n | t_n, t_0, x_0, \dots, t_{n-1}, x_{n-1}) = f'(x_n | \theta_0(w_0(t_n) \odot x), \dots, \theta_m(w_m(t_n) \odot x))$$

+ assumption

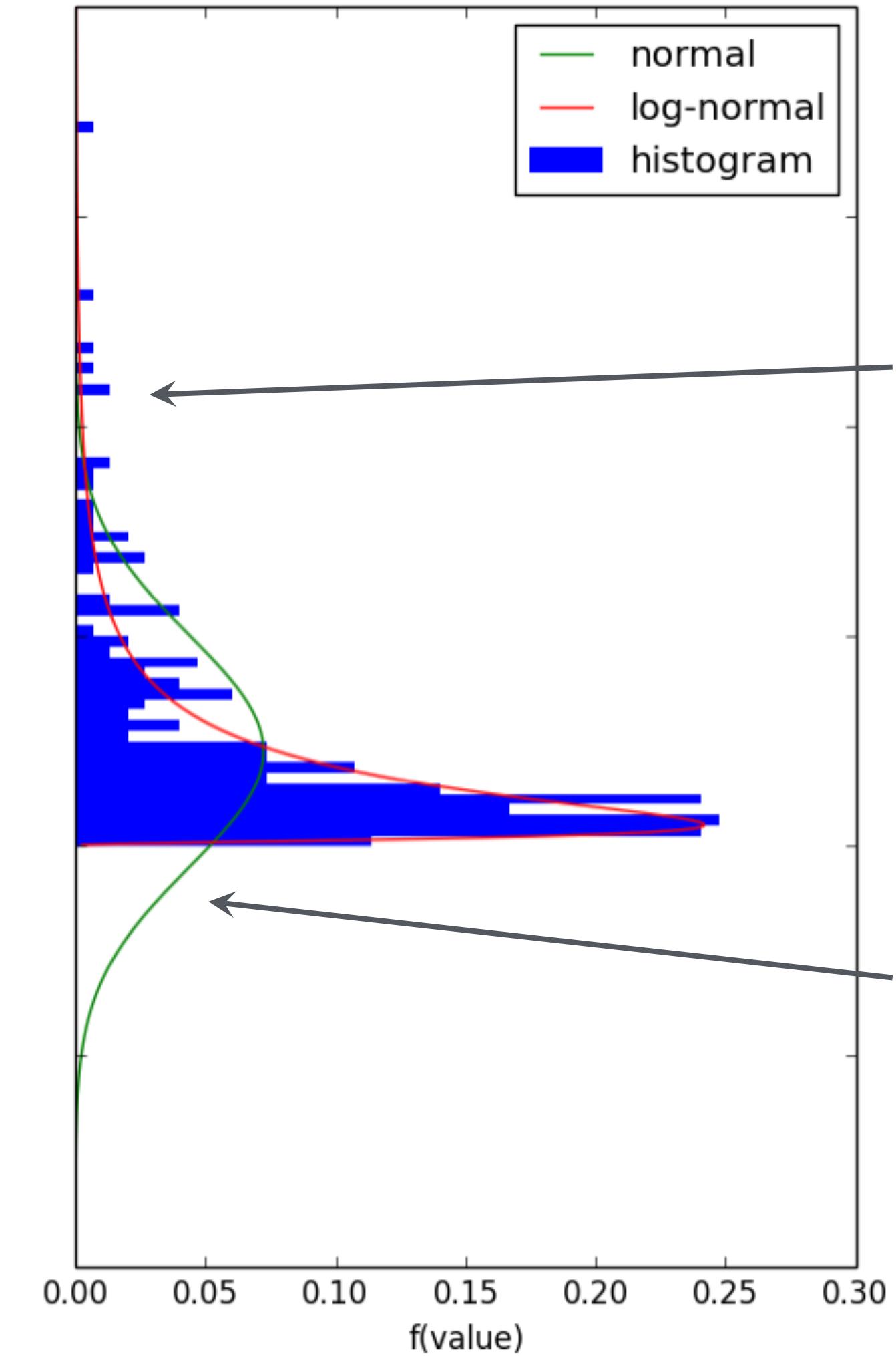
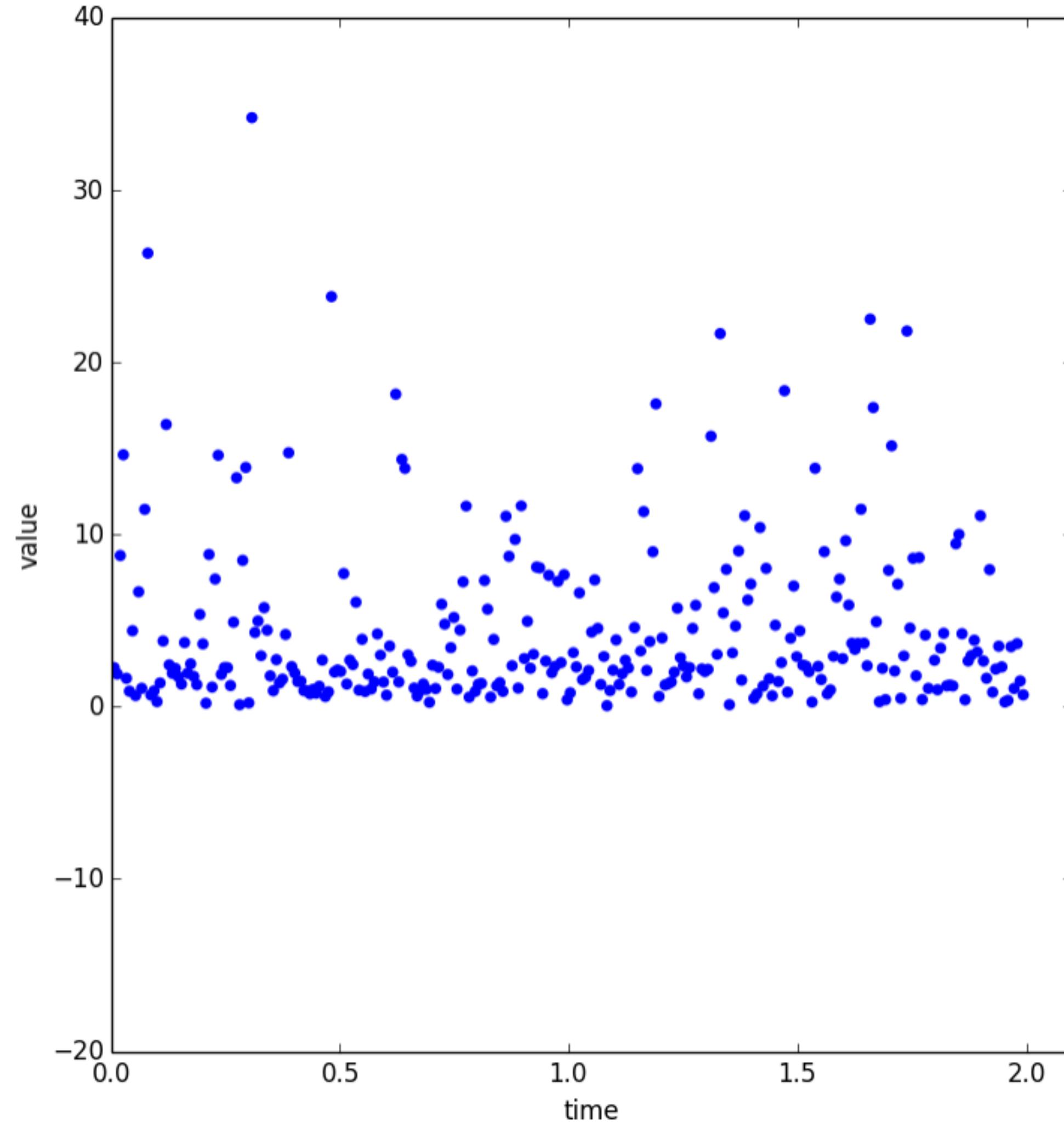


mean

“variance”

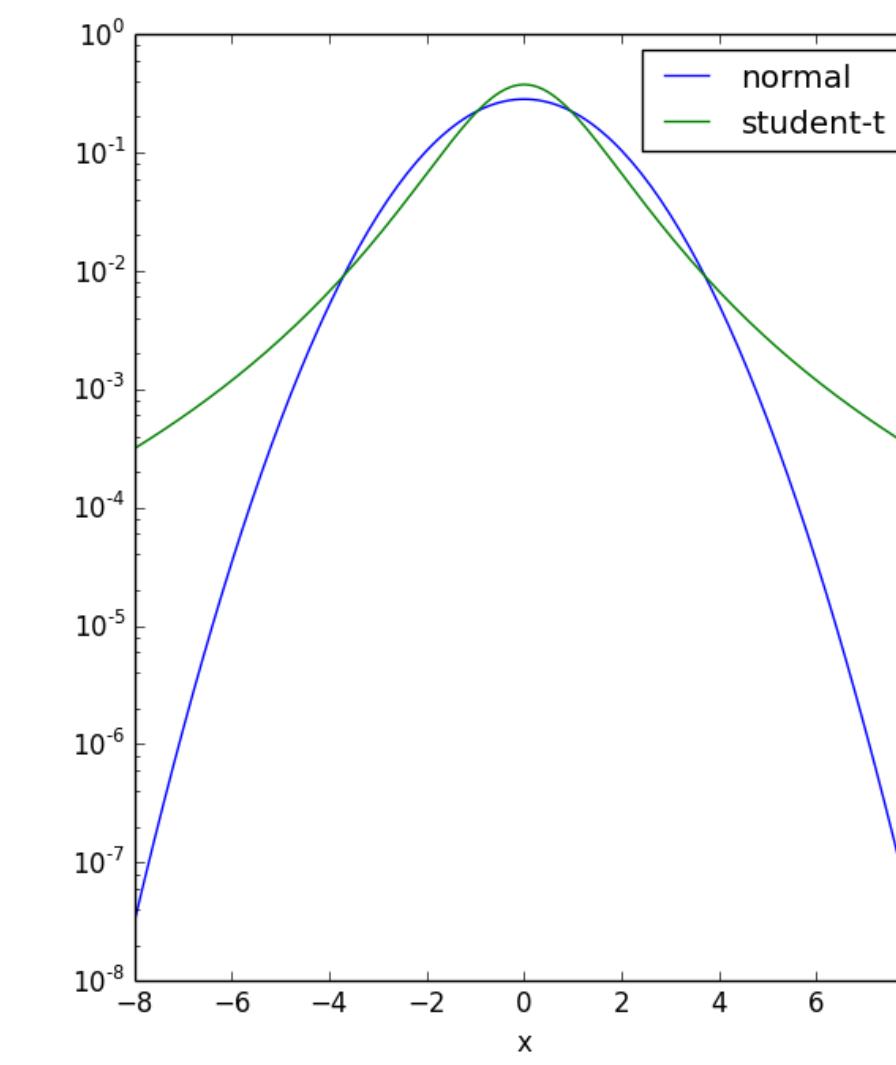
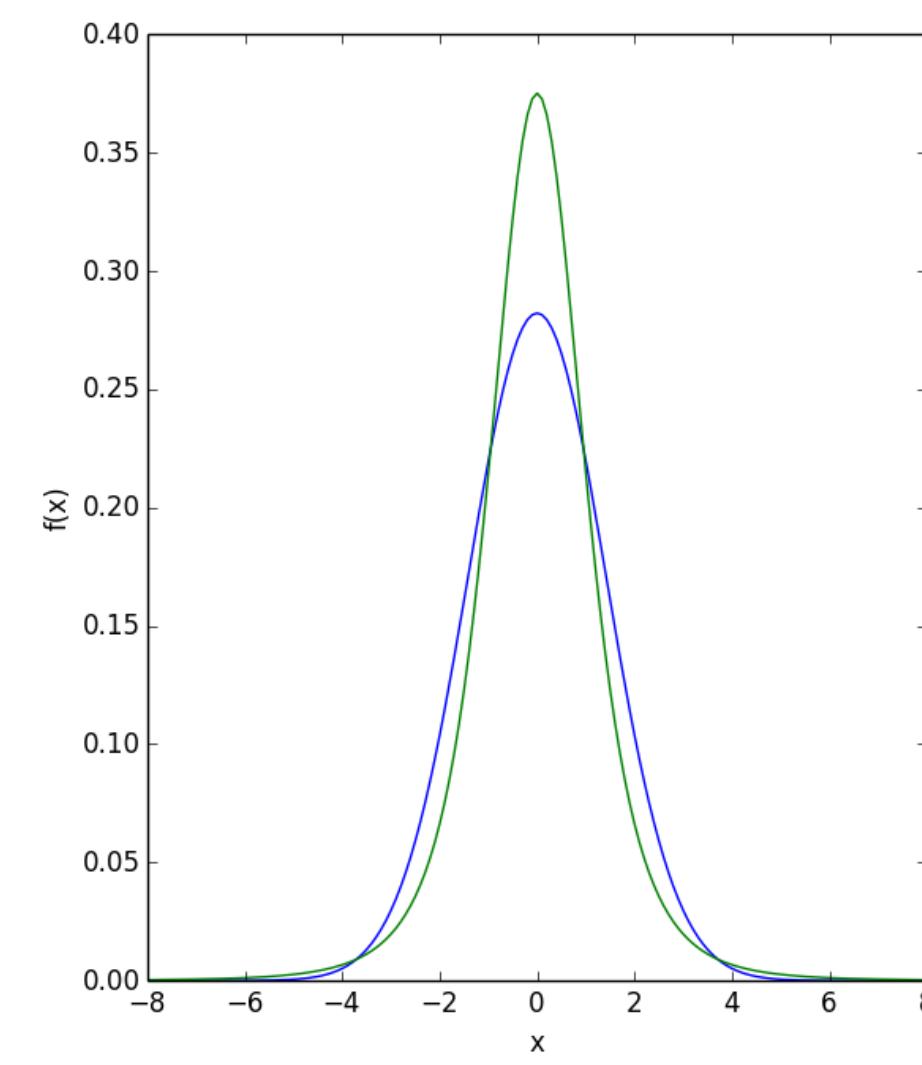
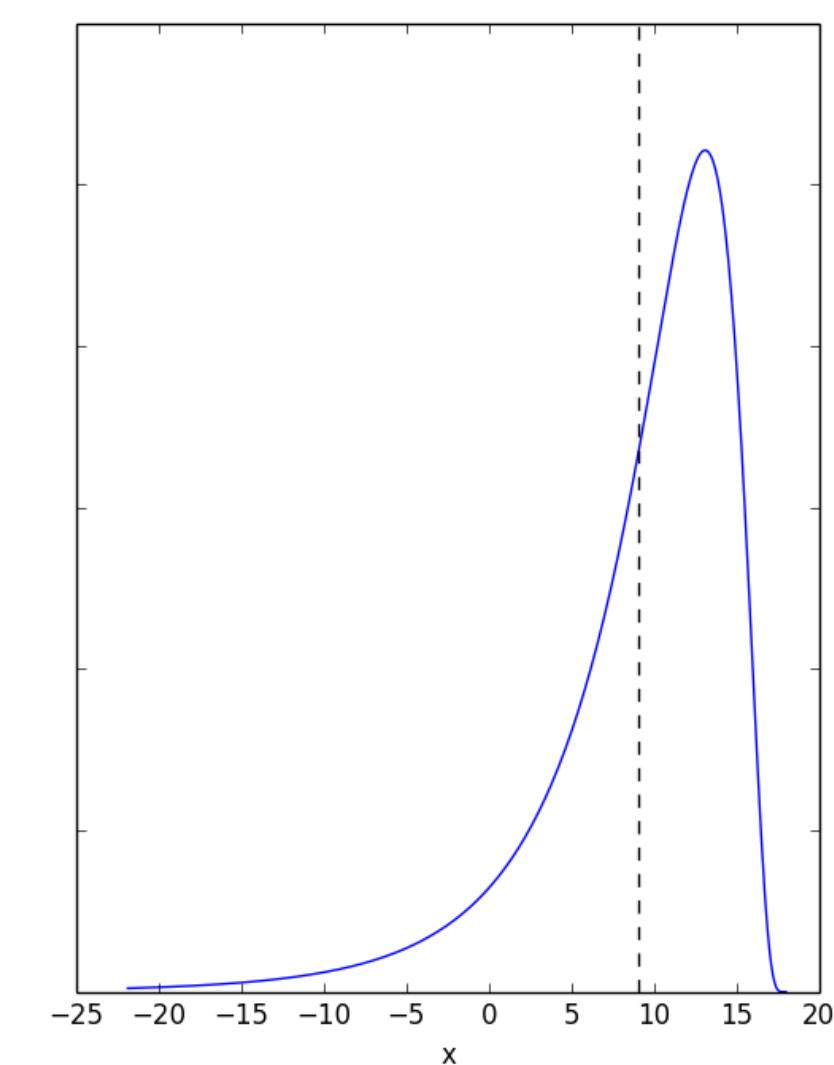
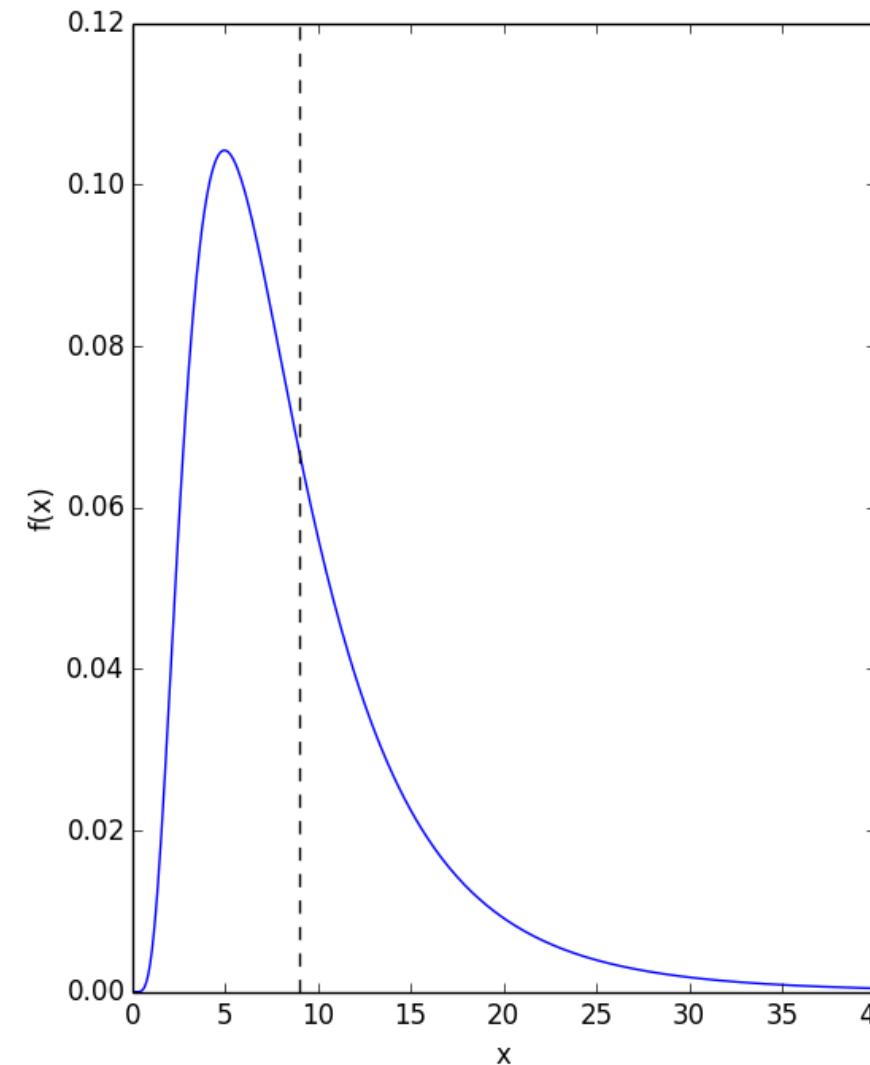
$$f(x_n) = 1/\sqrt{2\pi}\sigma \exp(-1/2\sigma^2(x_n - m)^2)$$

Stationary Unimodal Example



Stationary Unimodal Summary

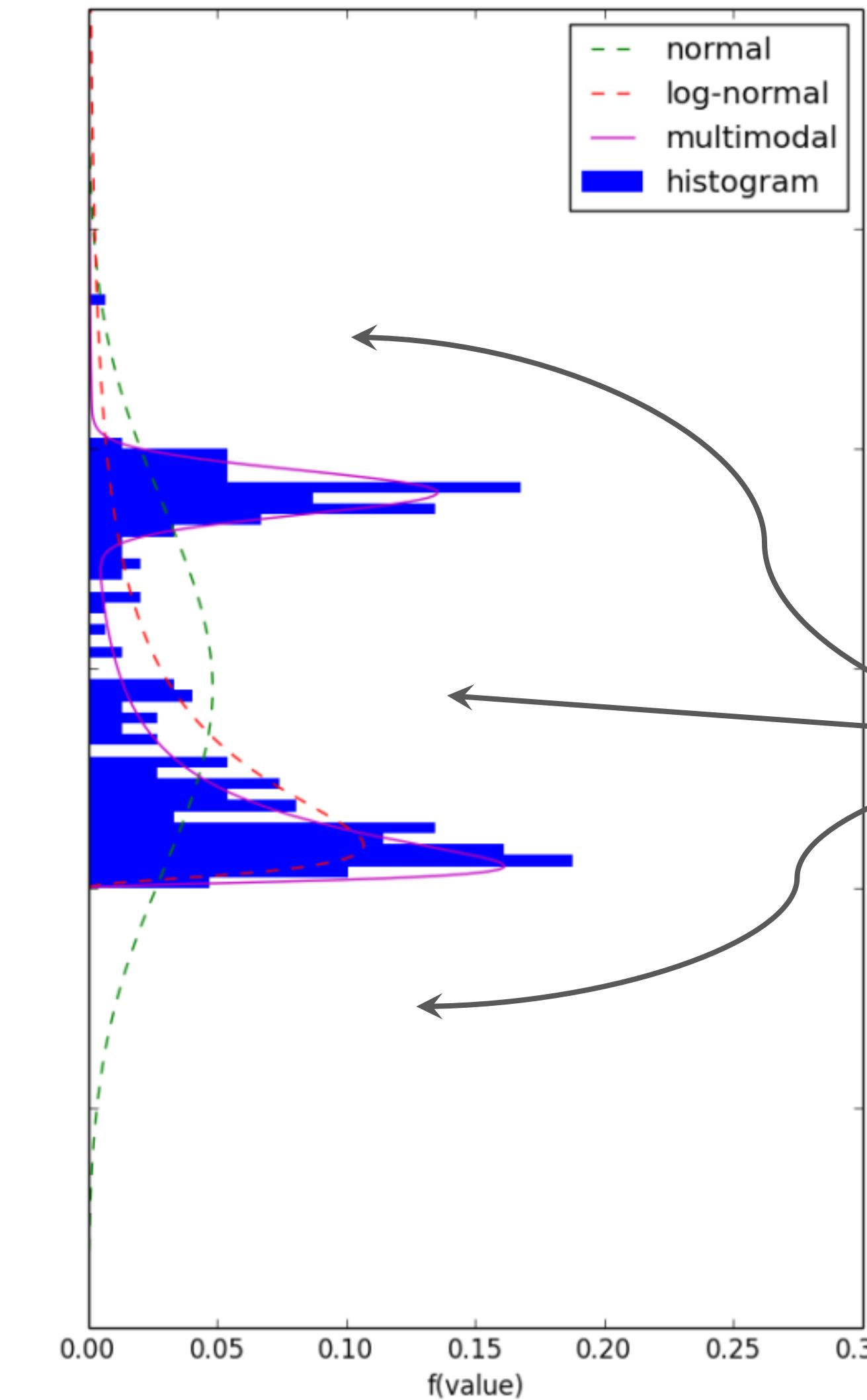
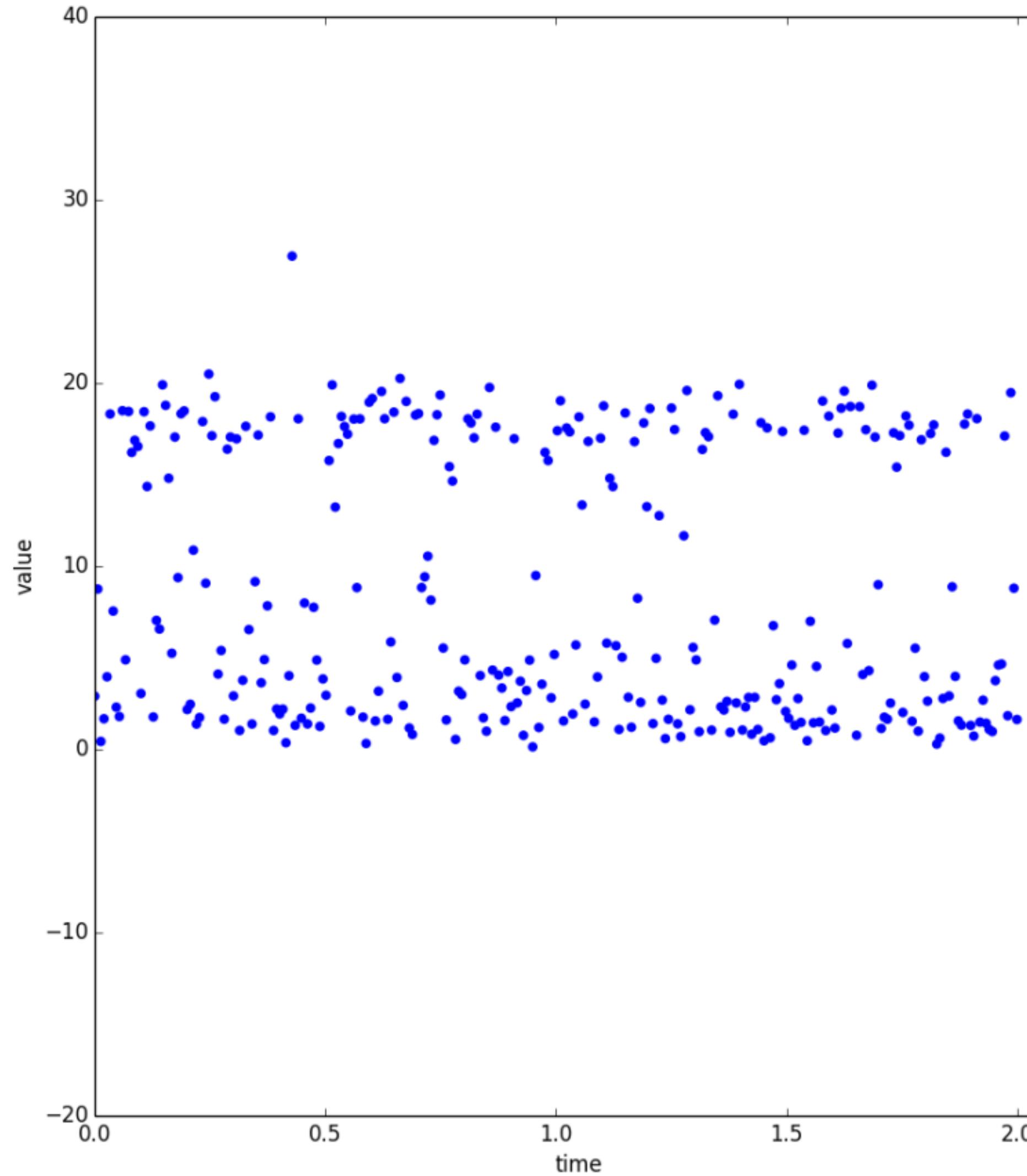
$$f'(x_n | \theta_0(w \odot x), \dots, \theta_m(w \odot x)) \quad [w]_i = 1 \text{ for all } i.$$



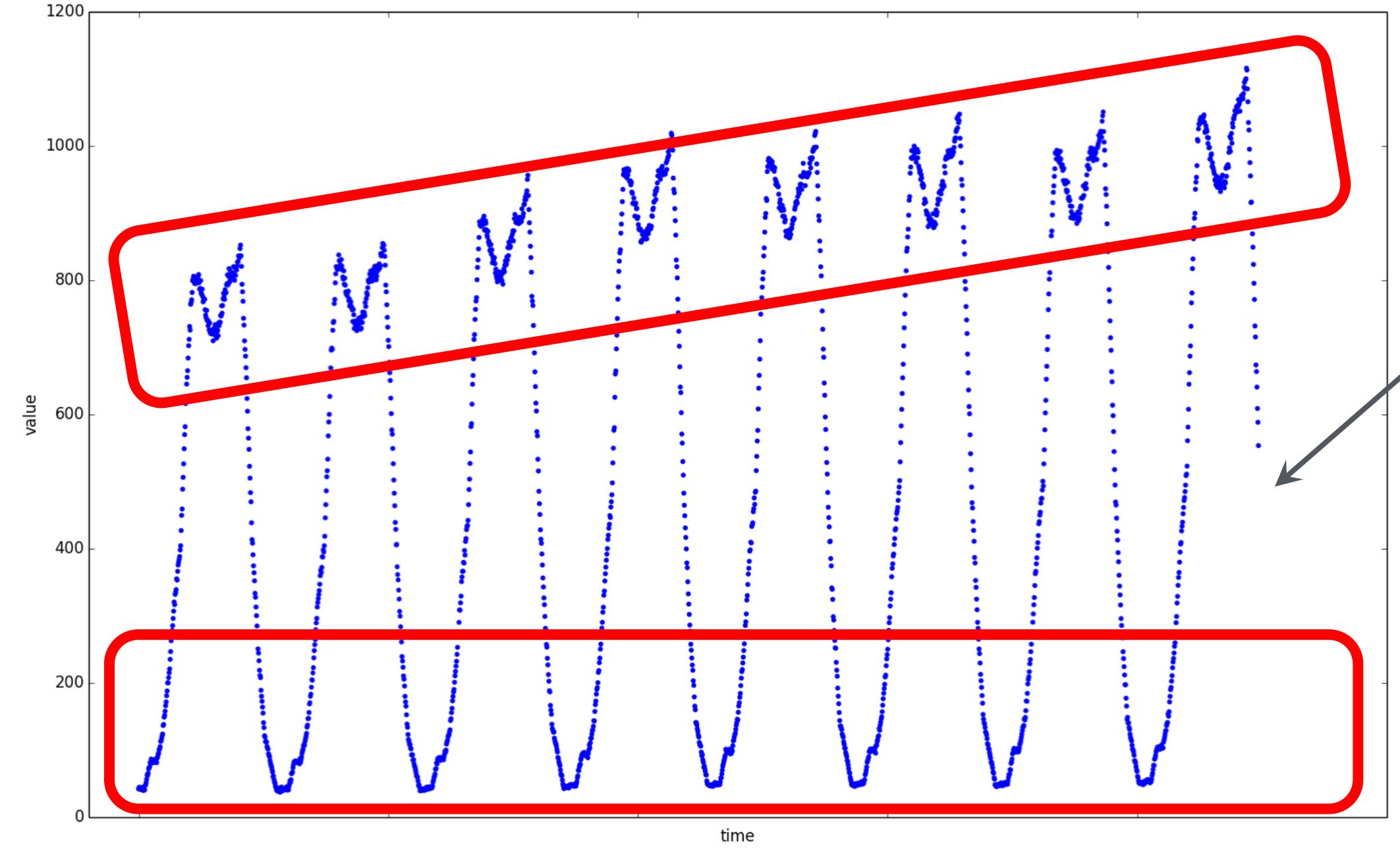
Skewness, heavy tails, etc = “Model Selection”.

Non-parametrics: don’t want to assign “mass” at all data points.

Stationary Multimodal Example

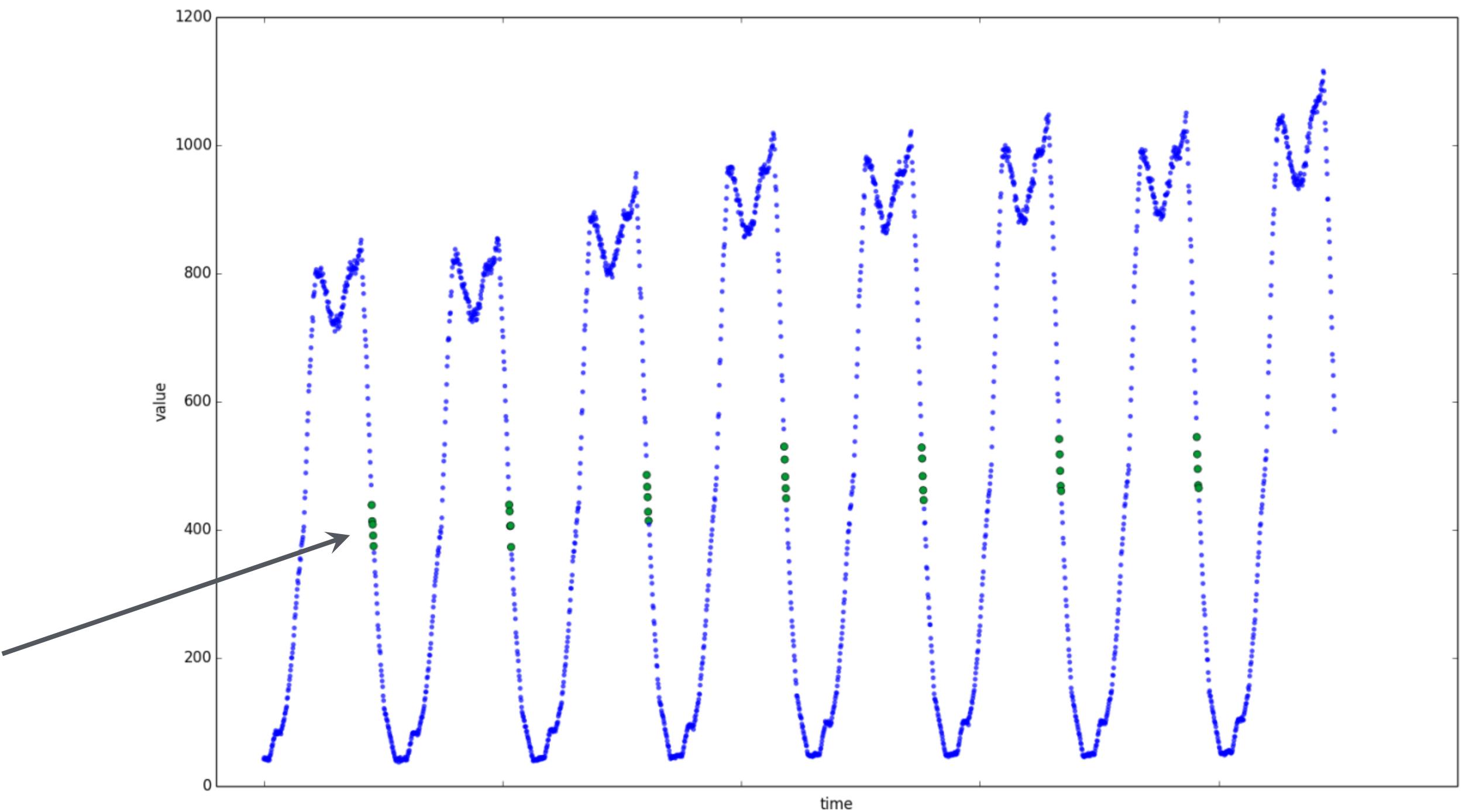


Seasonality Example

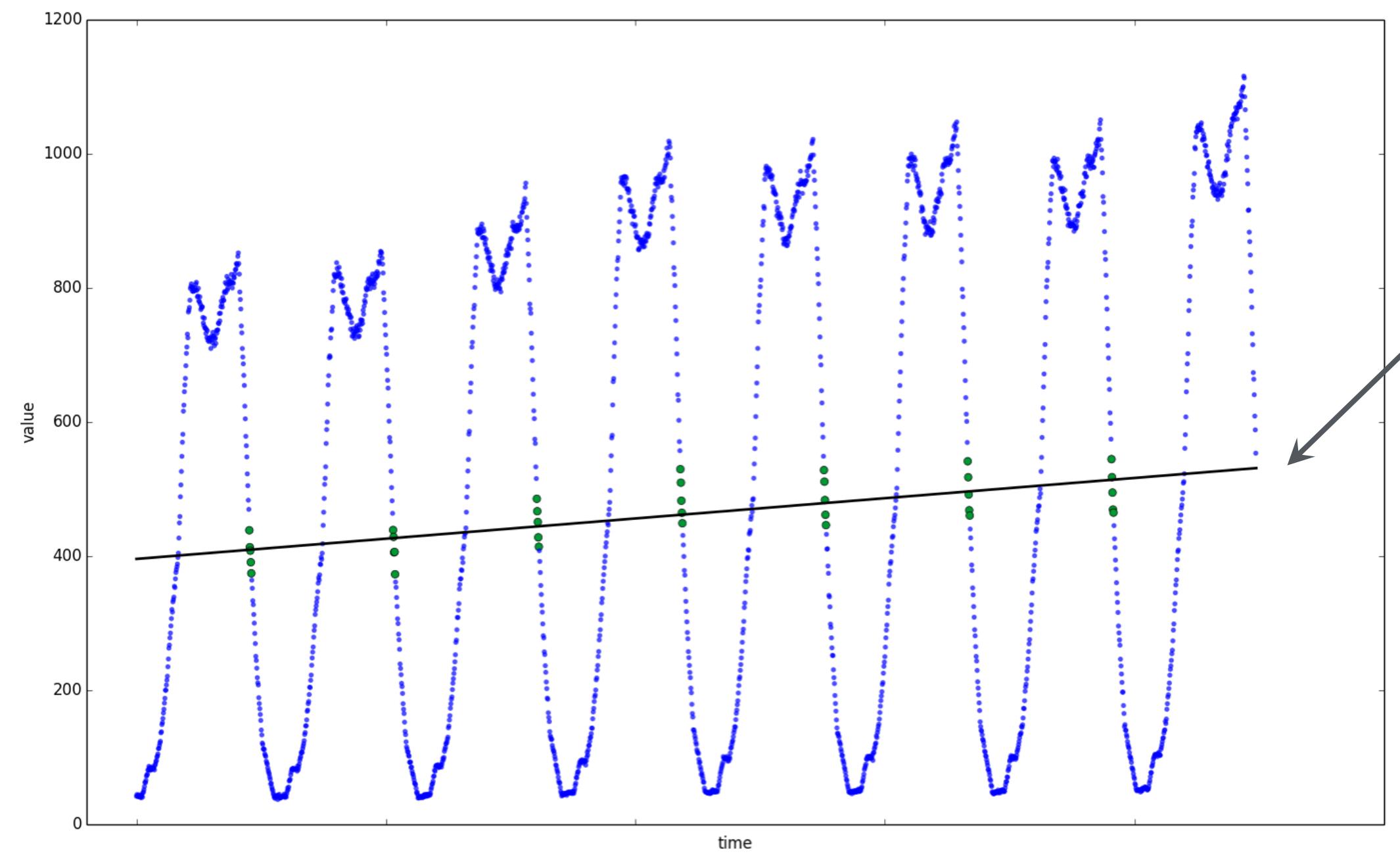


Subset of historical points relevant

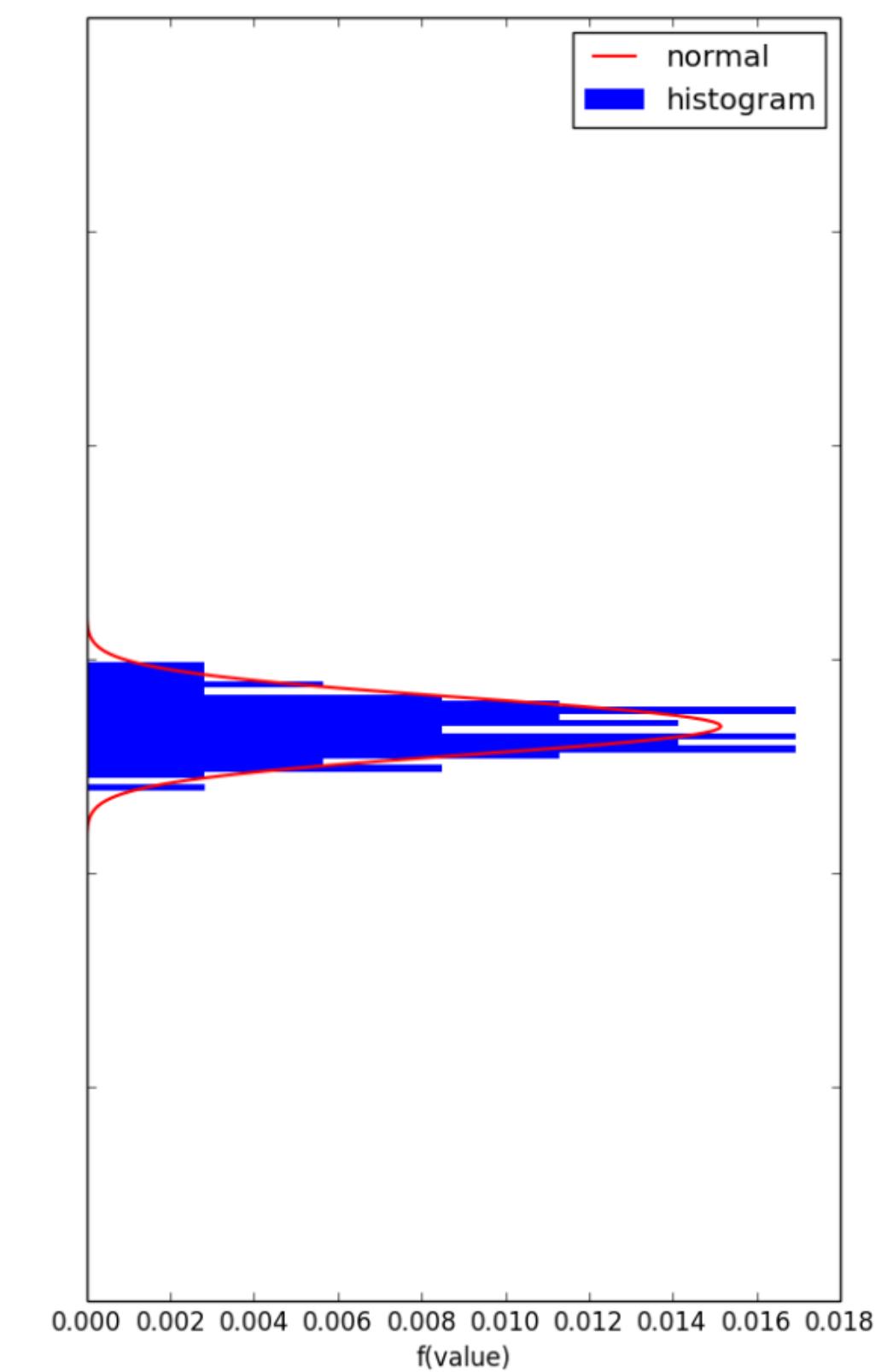
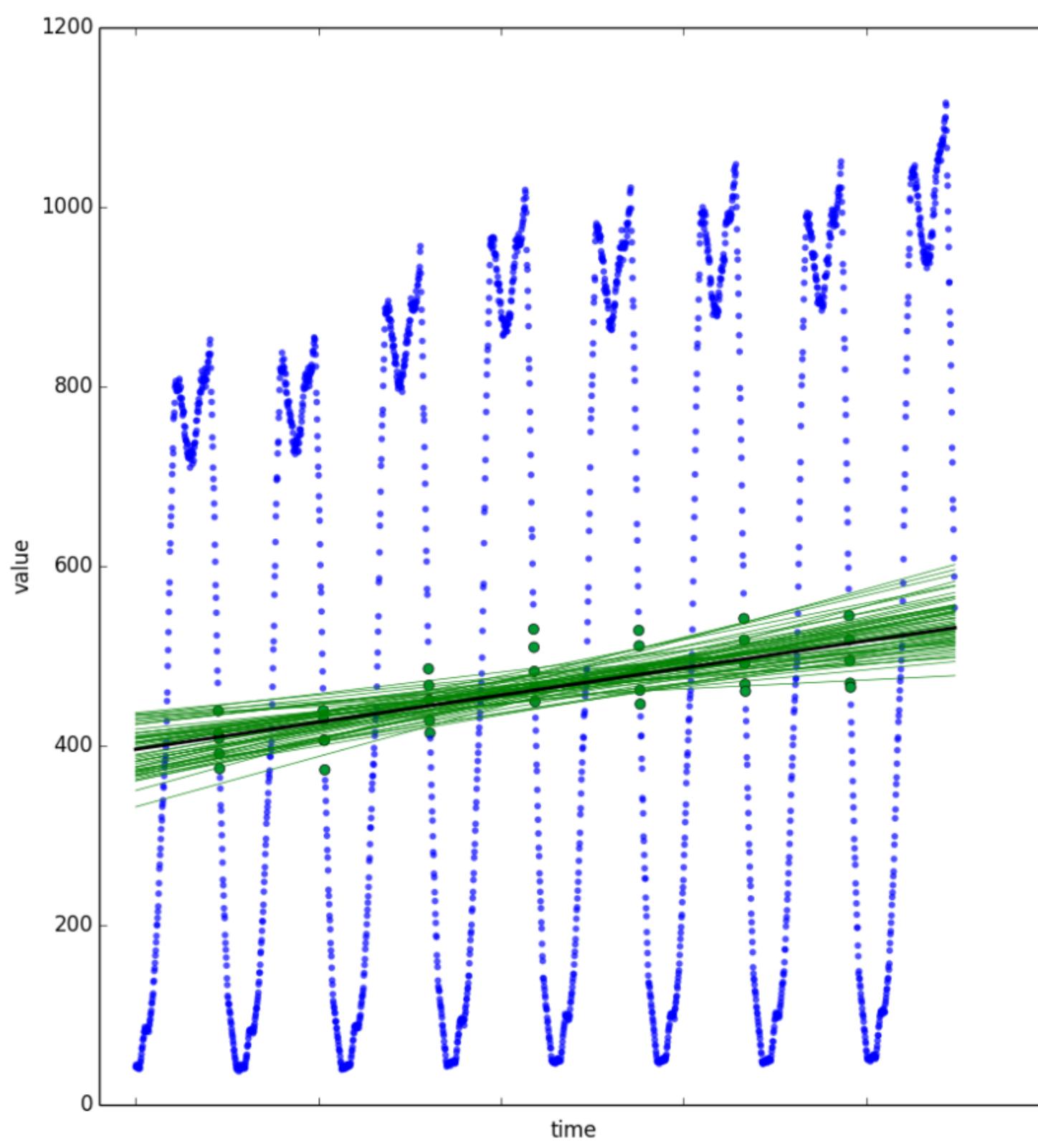
Want to predict the next value



Seasonality Example



Best fit OLS



Seasonality Summary

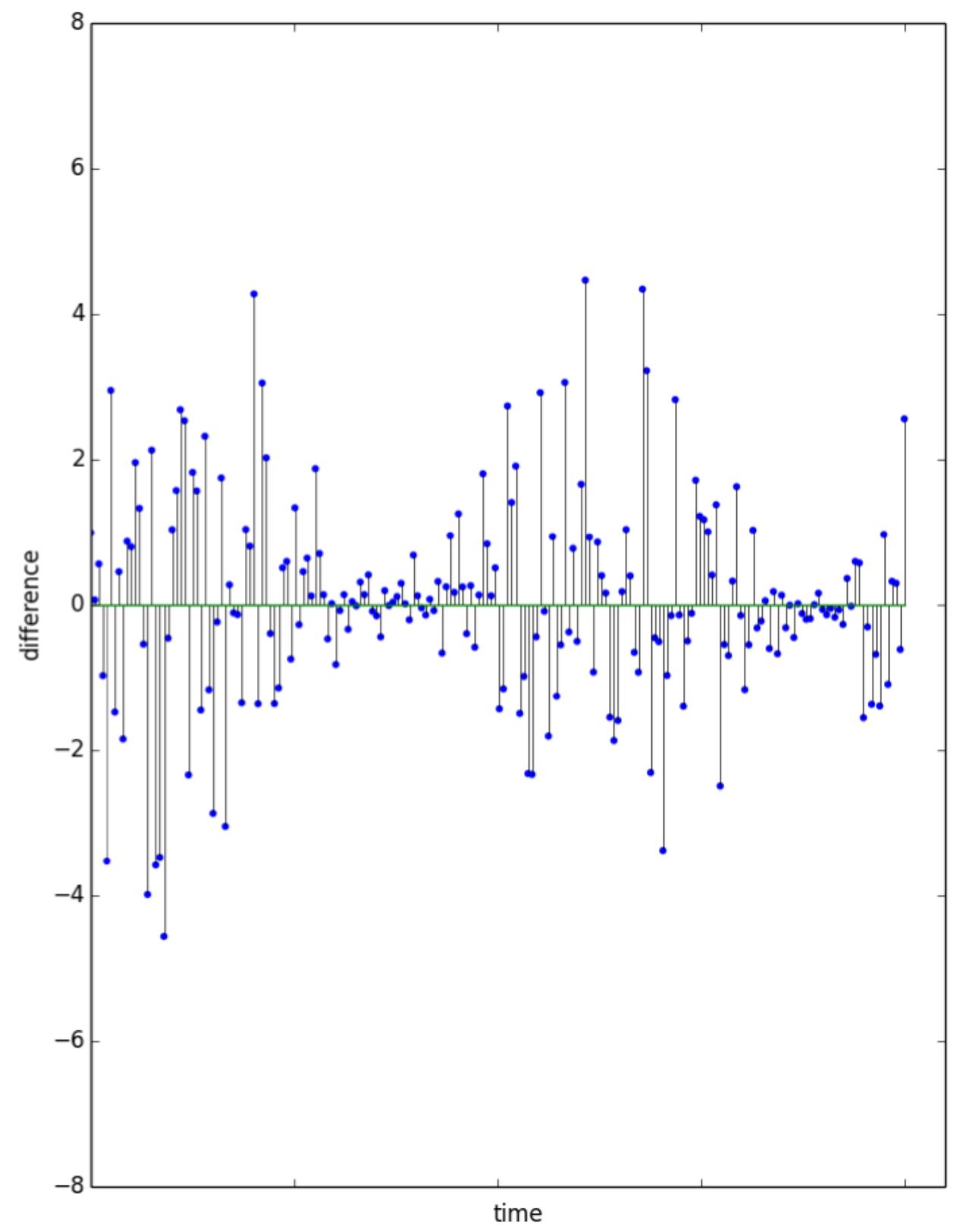
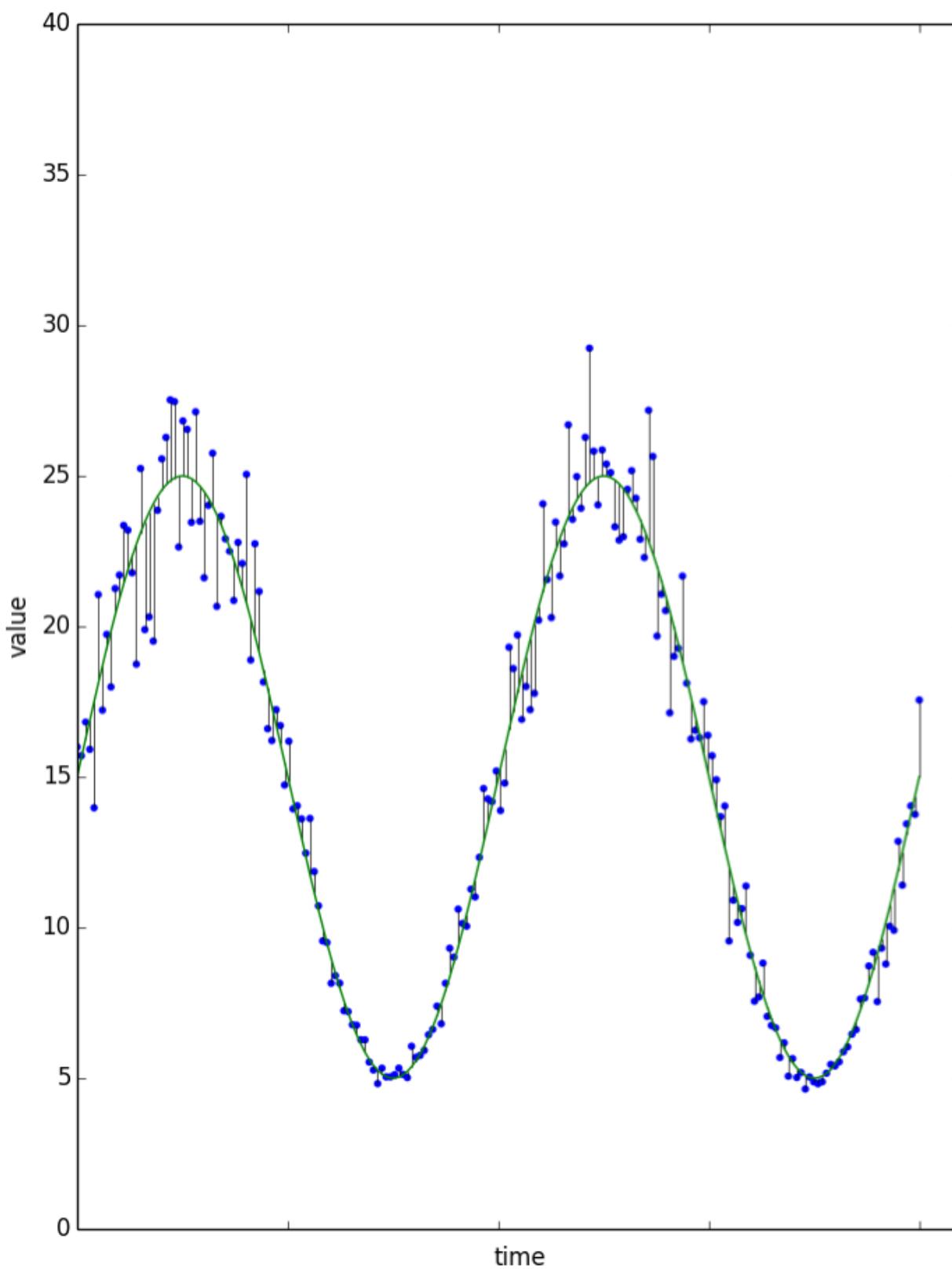
Data pattern repeated *regularly in time*.

$$f'(x_n | \theta_0(w(t_n) \odot x), \dots, \theta_m(w(t_n) \odot x))$$

$$[w(t)]_k = \sum_i 1\{t_k \in [t-iT-\varepsilon, t-iT+\varepsilon]\}$$

Period is T and interval $\varepsilon \ll T$

Not just the mean changes...



What is an Anomaly?

One way to think about what is an anomaly is
“what should I draw to someone’s attention”.

Thought experiment...

200
200
200
200
200
200
200

•
•
•
•
501

•
•
•
•
200
200

status.txt

68.225.64.230
82.66.9.59
6.221.126.97
98.170.142.103
65.219.248.175
42.58.77.167
119.154.198.125
•
•
•
•
•
•
9.7.144.83
68.173.20.5
9.138.147.109
103.16.218.43
31.100.56.29

IP.txt

What is an Anomaly?

A definition for anomalousness

“ The chance of making a draw of a value which is equal or less likely ”

Generalizes to any density function

200
200
200
200
200
200
200
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.
.
501
.
.
.
200
200

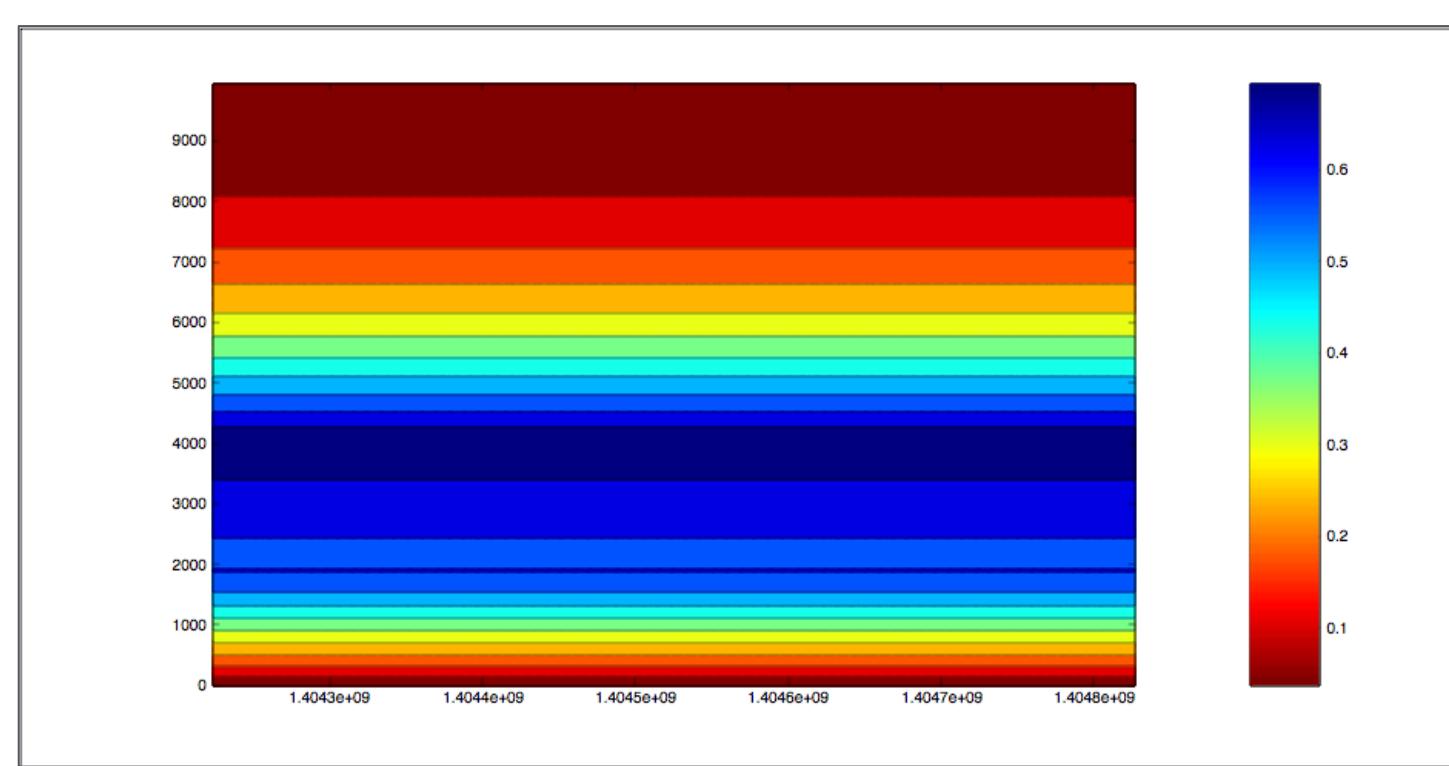
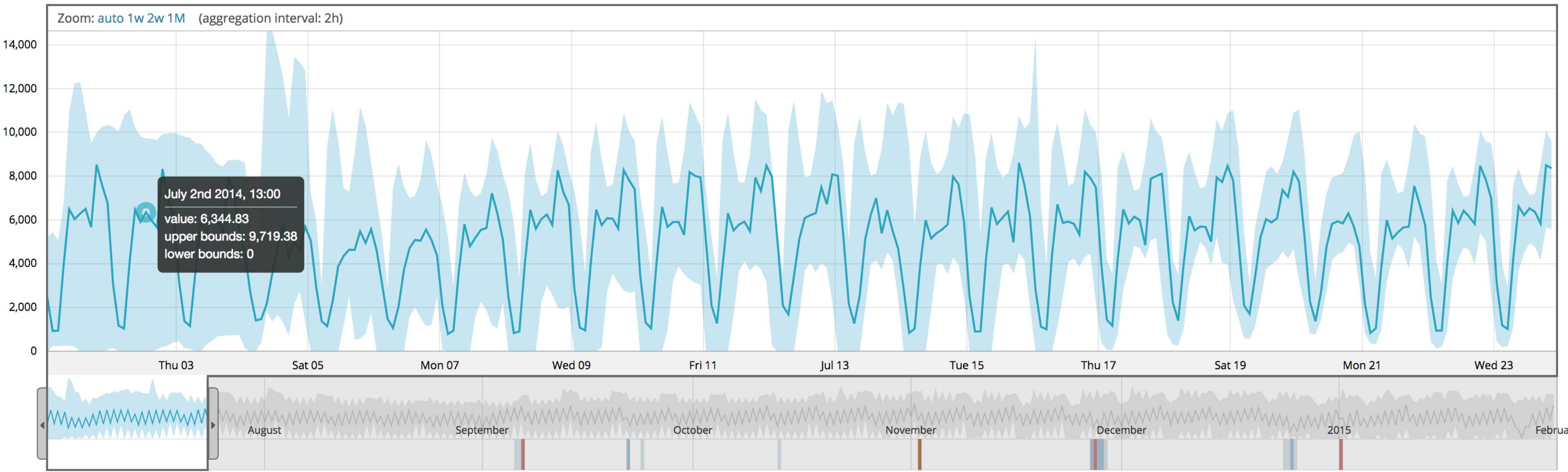
status.txt

68.225.64.230
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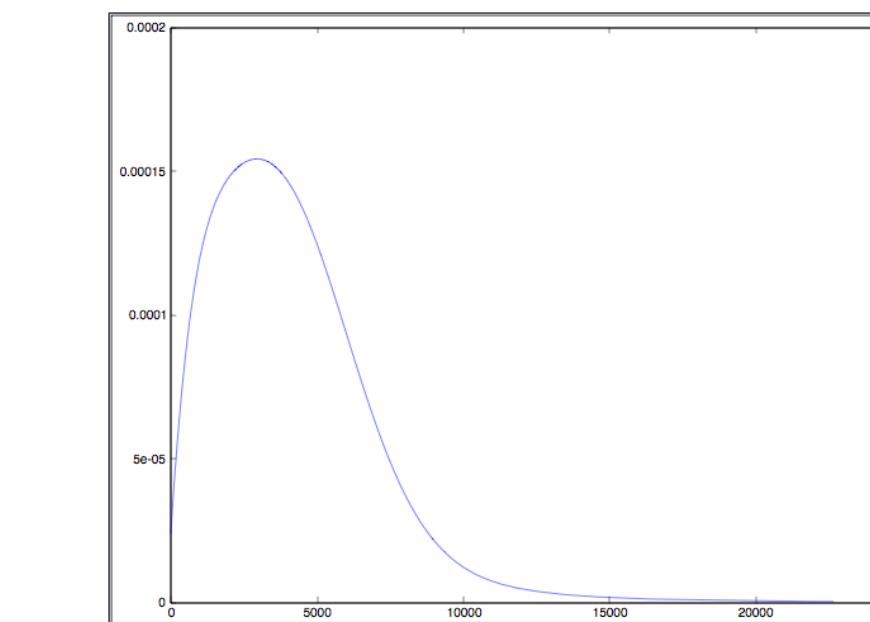
IP.txt

Demo

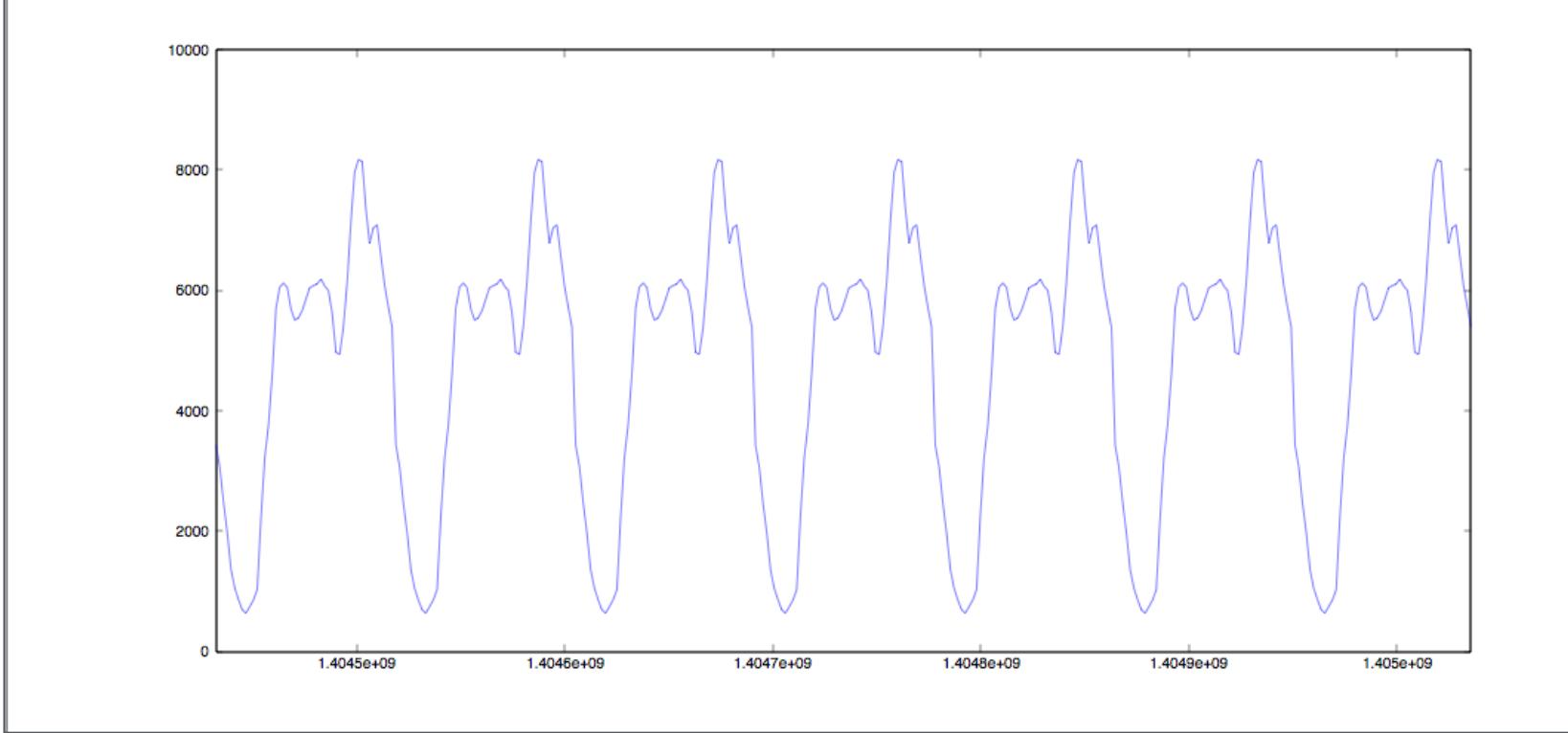
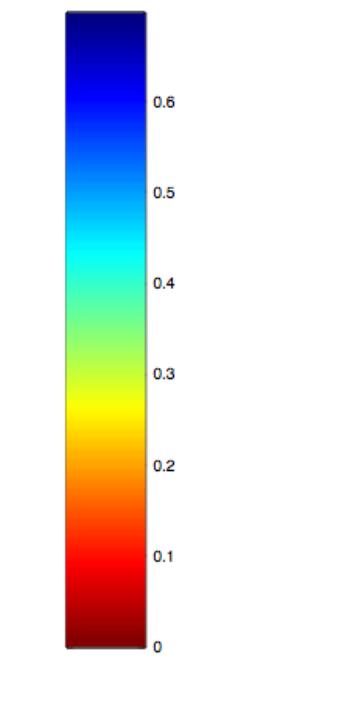
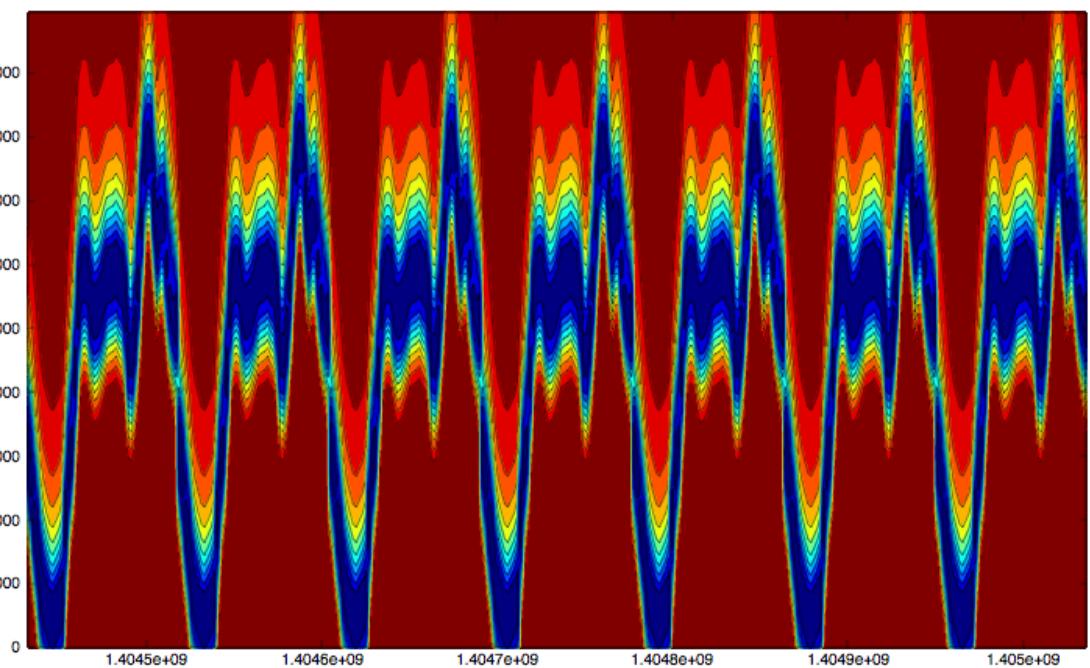
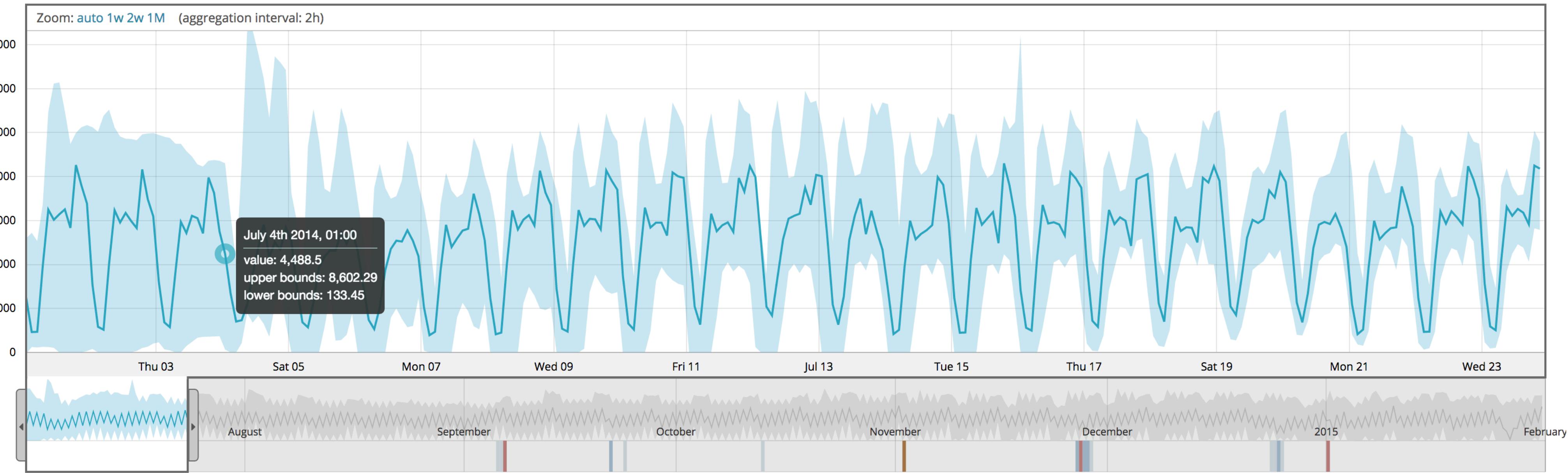
NYC Yellow Taxi Data



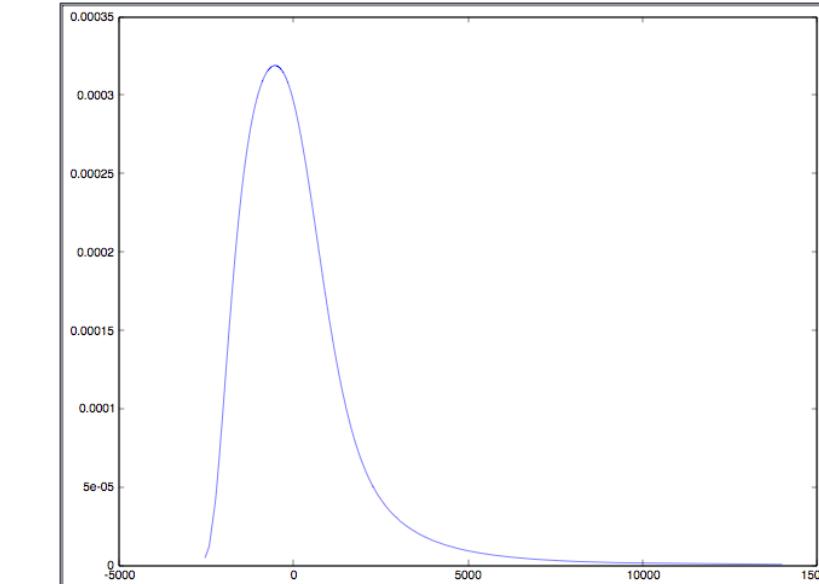
one-of-n:
samples 27.08807
weight 0.6127408 gamma mean = 3997.926 sd = 3057.266
weight 0.1349328 log-normal mean = 4312.742 sd = 4397.683
weight 1 normal mean = 3998.194 sd = 2459.595



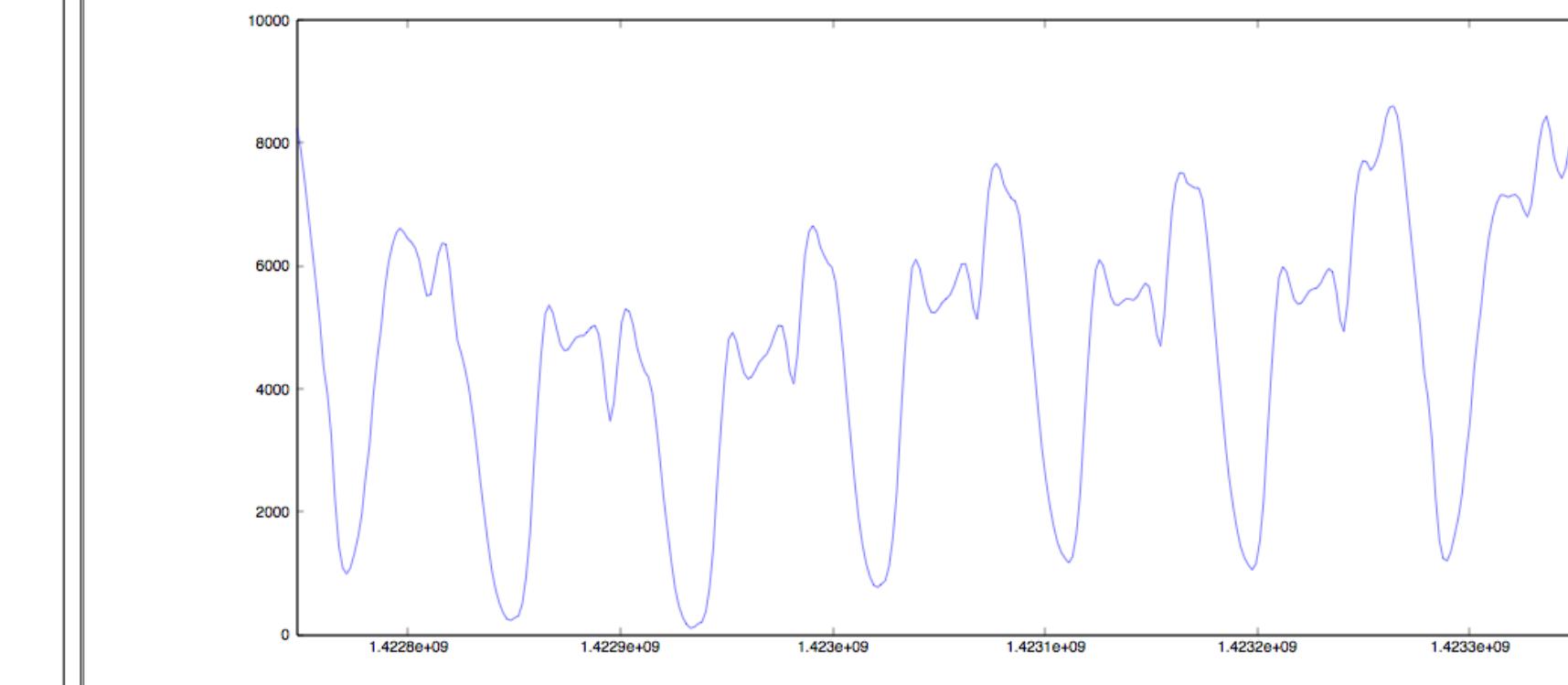
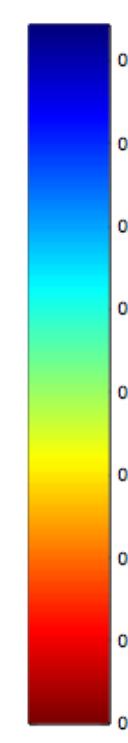
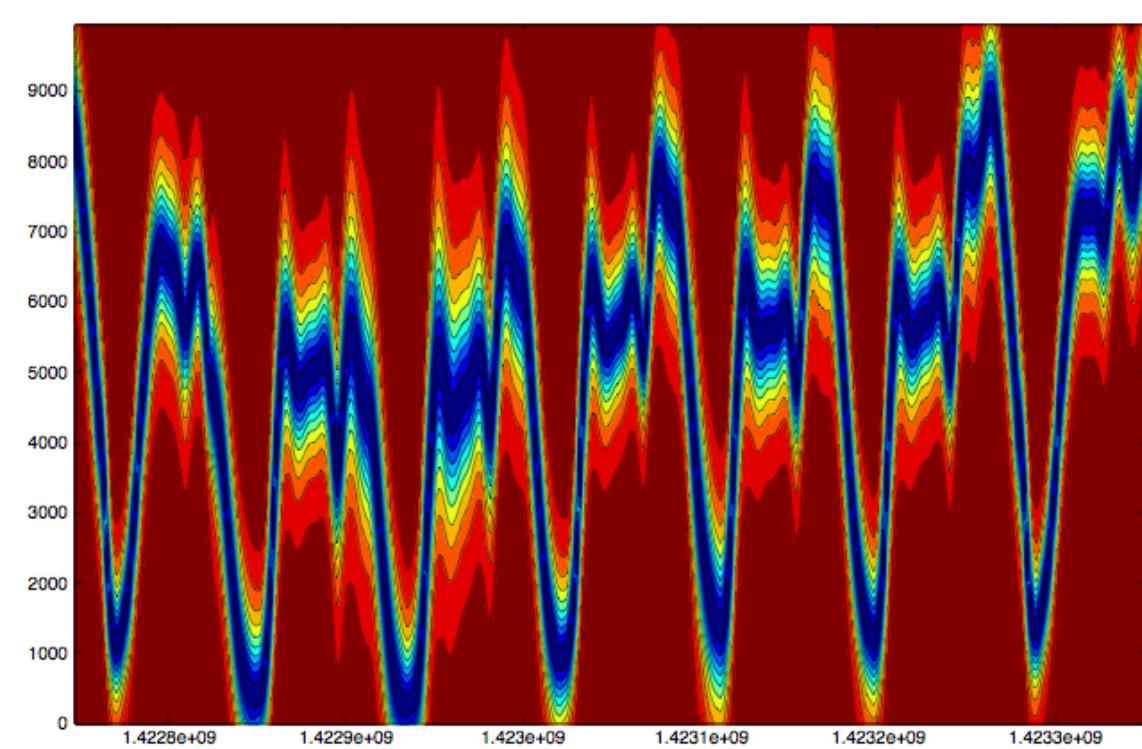
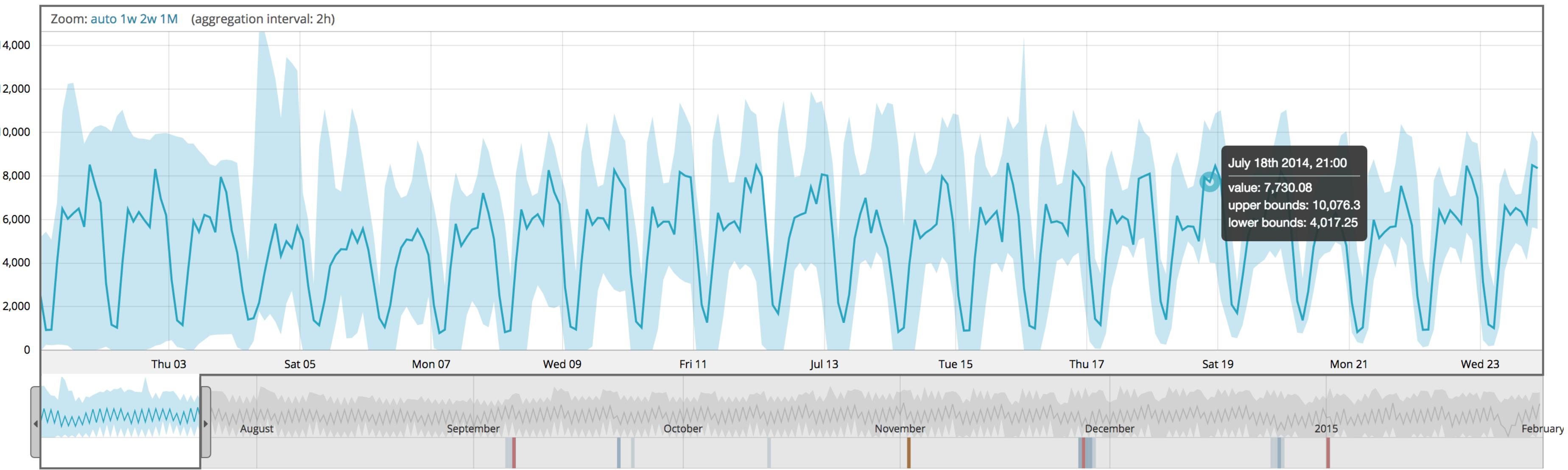
NYC Yellow Taxi Data



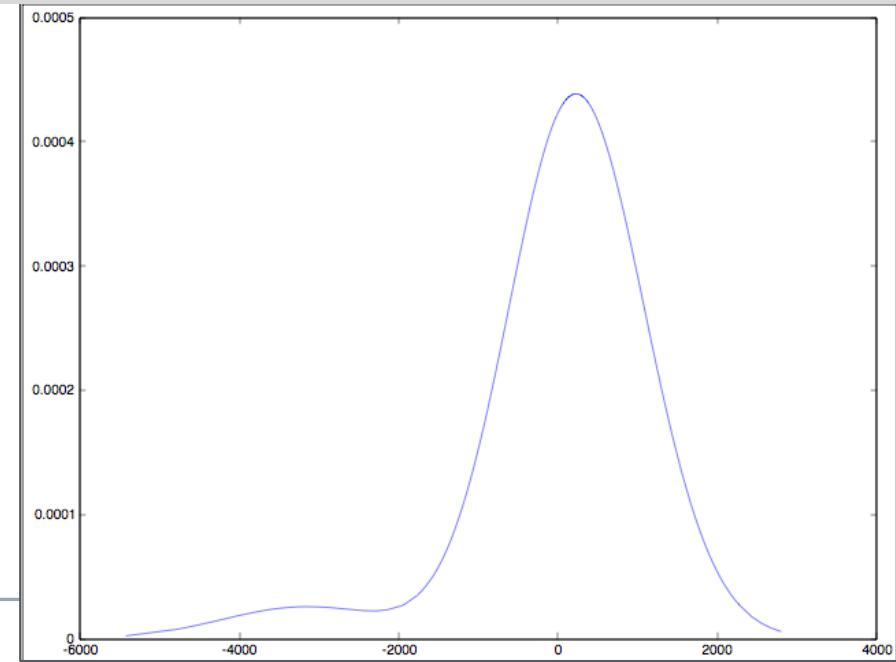
one-of-n:
samples 10.24265
weight 0.8721099 gamma mean = -11.0318 sd = 1326.766
weight 1 log-normal mean = 306.7829 sd = 2202.448
weight 0.7571213 normal mean = -11.5318 sd = 983.4198



NYC Yellow Taxi Data



```
one-of-n:  
# samples 2419.166  
weight 1 multimodal:  
weight 1 weight 0.06826681 one-of-n:  
weight 1 weight 0.06826681 # samples 165.1488  
weight 1 weight 0.2297682 gamma mean = -3130.213 sd = 1068.919  
weight 1 weight 0.06826681 weight 0.08569148 log-normal mean = -3128.735 sd = 1083.164  
weight 1 weight 0.06826681 weight 1 normal mean = -3130.713 sd = 1054.263  
weight 1 weight 0.9317332 one-of-n:  
weight 1 weight 0.9317332 # samples 2254.017  
weight 1 weight 0.9317332 weight 0.382987 gamma mean = 251.7118 sd = 849.5769  
weight 1 weight 0.9317332 weight 0.2192974 log-normal mean = 251.858 sd = 852.8664  
weight 1 weight 0.9317332 weight 1 normal mean = 251.2118 sd = 846.9203
```



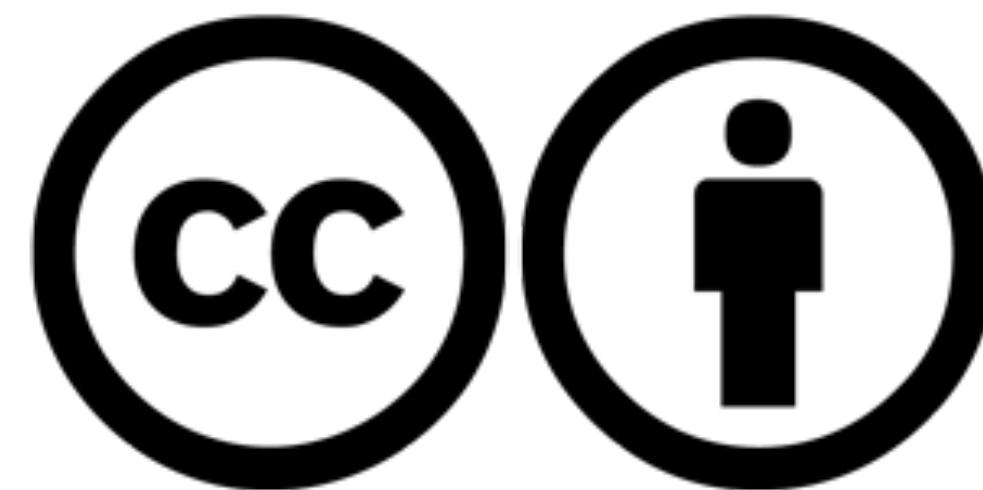
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