Intro to RNN

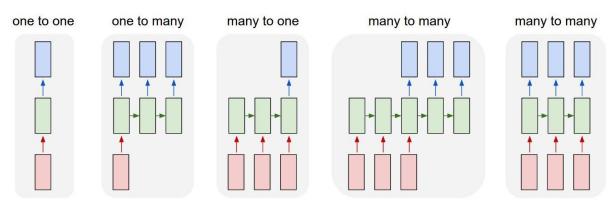
Web Clip

Import Libraries

```
import numpy as np
import torch
import torch.nn as nn
import torch.optim as optim
from torch.utils.data import Dataset, DataLoader
```

Types of RNNs

RNNs are mainly used in case of sequential data such as time series or NLP. There are multiple different types of RNNs which are used for different applications.



Different types of RNNs [Image [2]]

For Time Series -

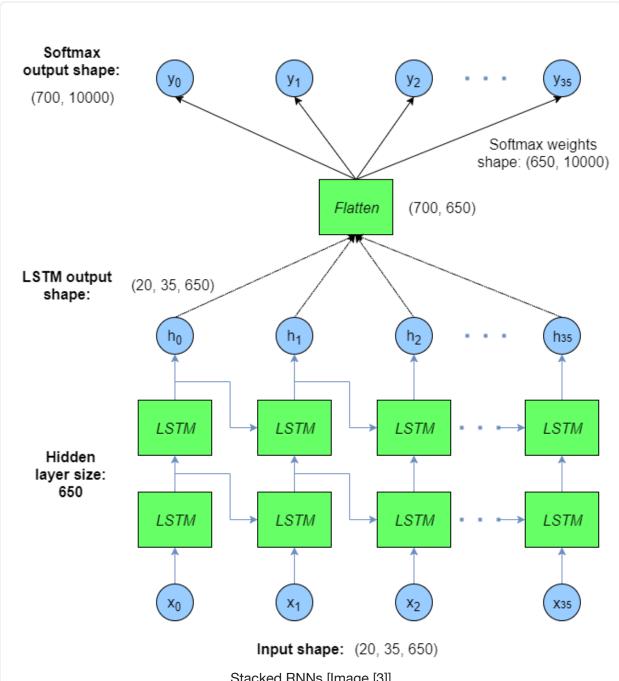
- Forecasting many-to-many or many-to-one
- Classification many-to-one

For NLP -

- Text Classification: many-to-one
- Text Generation: many-to-many
- Machine Translation: many-to-many
- Named Entity Recognition: many-to-many
- Image Captioning: one-to-many

Stacked RNNs

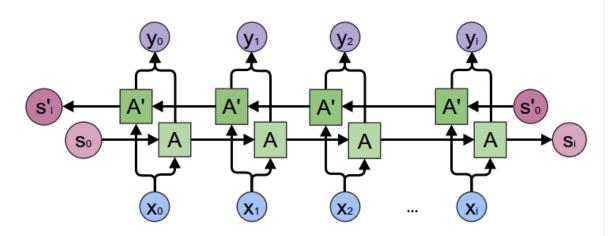
We often stack RNNs together for better performance.



Stacked RNNs [Image [3]]

Bidirectional RNN

Bidirectional RNN is essentially using 2 RNNs where the input sequence is fed in the normal order to 1 RNN and in reverse to the other RNN.



Bidirectional RNNs [Image [4]]

Input Data

Here the data is:

We divide it into 4 batches of sequence length = 5.

Batch Size = 4

Sequence Length = 5

Input Size = 1 (Since, only one dimension)

In our case, we're looking at 5 (seq_len) previous value to predict the next 2 values.

Vanilla RNN

```
# Number of features used as input. (Number of columns)
INPUT_SIZE = 1

# Number of previous time stamps taken into account.
SEQ_LENGTH = 5

# Number of features in last hidden state ie. number of output time—
# steps to predict.See image below for more clarity.
HIDDEN_SIZE = 2

# Number of stacked rnn layers.
NUM_LAYERS = 1

# We have total of 20 rows in our input.
# We divide the input into 4 batches where each batch has only 1
```

row. Each row corresponds to a sequence of length 5.
BATCH_SIZE = 4

Input

torch.nn.RNN has two inputs - input and h_0 ie. the input sequence and the hidden-layer at t=0. If we don't initialize the hidden layer, it will be autoinitiliased by PyTorch to be all zeros.

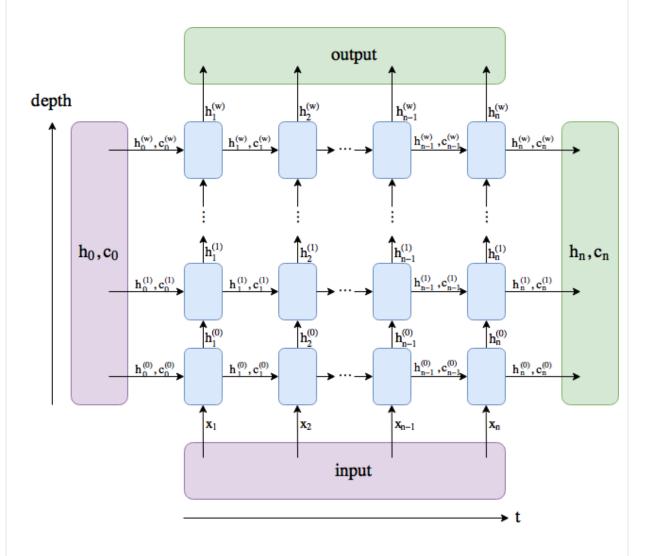
- input is the sequence which is fed into the network. It should be of size (seq_len, batch, input_size). If batch_first=True, the input size is (batch, seq_len, input_size).
- h_0 is the initial hidden state of the network. It is of the size (num_layers * num_directions, batch, input_size) where num_layers is the number of stacked RNNs. num_directions = 2 for bidirectional RNNs and 1 otherwise.

Output

torch.nn.RNN has two outputs - out and hidden.

- out is the output of the RNN from all timesteps from the last RNN layer. It is of the size (seq_len, batch, num_directions * hidden_size). If batch_first=True, the output size is (batch, seq_len, num_directions * hidden_size).
- h_n is the hidden value from the last time-step of all RNN layers. It is of
 the size (num_layers * num_directions, batch, hidden_size). h_n is
 unaffected by batch first=True. Github Issue.

The following diagram explains it more clearly. Here the batch=1. The diagram is for an LSTM which as two hidden parameters (h, c). RNN and GRU both have only h.



RNN input and output [Image [5] credits]

To reiterate —

out is the output of the RNN from all timesteps from the last RNN
layer.

h n is the hidden value from the last time-step of all RNN layers.

```
# Initialize the RNN.
rnn = nn.RNN(input_size=INPUT_SIZE, hidden_size=HIDDEN_SIZE,
num_layers = 1, batch_first=True)

# input size : (batch, seq_len, input_size)
inputs = data.view(BATCH_SIZE, SEQ_LENGTH, INPUT_SIZE)

# out shape = (batch, seq_len, num_directions * hidden_size)
# h_n shape = (num_layers * num_directions, batch,
hidden_size)
out, h_n = rnn(inputs)

input shape = [4, 5, 1]
out shape = [4, 5, 2]
h_n shape = [1, 4, 2]
```

In the **input** We have 4 batches as our output because we set the BATCH_SIZE=4. Each batch contains 5 rows because out SEQ_LENGTH = 5. We are using only a single feature as input INPUT_SIZE = 1.

In the **out**, we get values from all 4 batches where number of time-steps (seq_len) is 5 and the number of predictions are 2. For each batch, we're predicting 2 outputs.

In the h_n , we get values from each of the 4 batches of the last time-step of the single RNN layer.

```
print('Input: ', inputs.shape, 'n', inputs)
print('nOutput: ', out.shape, 'n', out)
print('nHidden: ', h_n.shape, 'n', h_n)
```

```
torch.Size([4, 5, 1])
 tensor([[[ 1.],
          [ 2.],
          [3.],
          [ 4.],
          [5.]],
        [[6.],
          [7.],
          [8.],
          [ 9.],
          [10.]
        [[11.],
          [12.],
          [13.],
          [14.],
          [15.]],
        [[16.],
          [17.],
          [18.],
          [19.],
          [20.]]])
         torch.Size([4, 5, 2])
Output:
 tensor([[[-0.0819,
                       0.8100],
          [-0.4311,
                      0.9332],
          [-0.3162,
                      0.9748],
          [-0.3979,
                     0.9875],
          [-0.3675,
                      0.9944]],
        [-0.1081,
                      0.9953],
          [-0.5145,
                      0.9986],
          [-0.3269,
                      0.9995],
          [-0.4254,
                      0.9997],
          [-0.3820]
                     0.9999]],
        [-0.1342,
                      0.9999],
          [-0.5245,
                      1.0000],
          [-0.3458]
                      1.0000],
          [-0.4382,
                      1.0000],
```

```
[-0.1601,
                   1.0000],
         [-0.5328]
                   1.0000],
         [-0.3648,
                   1.0000],
         [-0.4506]
                   1.0000],
                   1.0000]]], grad fn=<TransposeBackward1>)
         [-0.4143,
Hidden: torch.Size([1, 4, 2])
tensor([[[-0.3675, 0.9944],
         [-0.3820,
                   0.9999],
         [-0.3982, 1.0000],
         [-0.4143, 1.0000]]], grad_fn=<StackBackward>)
```

In the output above, notice the last row in each batch of $\[Omega]$ out is present in h_n .

- out is the output value at all time-steps of the last RNN layer for each batch.
- h_n is the hidden value at the last time-step of all RNN layers for each batch.

Stacked RNN

If I change the num_layers = 3, we will have 3 RNN layers stacked next to each other. See how the out, and h_n tensors change in the example below.

We now have 3 batches in the h_n tensor. The last batch contains the endrows of each batch in the out tensor.

```
# Initialize the RNN.
rnn = nn.RNN(input_size=INPUT_SIZE, hidden_size=HIDDEN_SIZE,
num_layers = 3, batch_first=True)
```

```
# input size : (batch_size , seq_len, input_size)
inputs = data.view(BATCH_SIZE, SEQ_LENGTH, INPUT_SIZE)

# out shape = (batch, seq_len, num_directions * hidden_size)
# h_n shape = (num_layers * num_directions, batch,
hidden_size)
out, h_n = rnn(inputs)

input shape = [4, 5, 1]

out shape = [4, 5, 2]
h_n shape = [3, 4, 2]
```

In the **input**, We have 4 batches as our output because we set the BATCH_SIZE=4. Each batch contains 5 rows because out SEQ_LENGTH = 5. We are using only a single feature as input INPUT_SIZE = 1.

In the **out**, we get values from all 4 batches where number of time-steps (seq_len) is 5 and the number of predictions are 2. For each batch, we're predicting 2 outputs.

In the $\,h_n$, we get values from each of the 4 batches of the last time-steps of the 3 stacked RNN layers.

```
[ 3.],
          [ 4.],
          [5.]],
         [[6.],
          [7.],
          [8.],
          [ 9.],
          [10.]],
         [[11.],
          [12.],
          [13.],
          [14.],
          [15.]],
         [[16.],
          [17.],
          [18.],
           [19.],
          [20.]]])
         torch.Size([4, 5, 2])
Output:
 tensor([[[ 0.3144, -0.7527],
          [-0.0597, -0.6038],
[ 0.0896, -0.7646],
          [ 0.0608, -0.6358],
[ 0.1084, -0.6783]],
         [[0.4442, -0.6350],
          [0.0949, -0.3948],
          [0.2715, -0.5962],
          [0.1819, -0.4580],
          [0.2529, -0.5213]],
         [[0.4907, -0.5688],
          [0.1671, -0.2976],
          [ 0.3462, -0.4922], [ 0.2388, -0.3768],
          [0.3078, -0.4418]
         [[0.5041, -0.5466],
          [0.1883, -0.2675],
```

```
[0.3684, -0.4576],
         [0.2572, -0.3502],
         [ 0.3238, -0.4167]]], grad_fn=<TransposeBackward1>)
Hidden: torch.Size([3, 4, 2])
tensor([[[-0.6480, -0.4044],
         [-0.8912, -0.7801],
         [-0.9808, -0.9366],
         [-0.9975, -0.9836]
        [[-0.7848, -0.0118],
         [-0.8707, -0.1721],
         [-0.8955, -0.2411]
         [-0.9016, -0.2605]],
        [[0.1084, -0.6783],
         [0.2529, -0.5213],
         [0.3078, -0.4418],
         [ 0.3238, -0.4167]]], grad_fn=<StackBackward>)
```

Bidirectional RNN

For Bidirectional RNN, we set the bidirectional=True.

```
rnn = nn.RNN(input_size=INPUT_SIZE, hidden_size=HIDDEN_SIZE,
batch_first=True, num_layers = 1, bidirectional = True)

# input size : (batch_size , seq_len, input_size)
inputs = data.view(BATCH_SIZE, SEQ_LENGTH, INPUT_SIZE)

# out shape = (batch, seq_len, num_directions * hidden_size)
# h_n shape = (num_layers * num_directions, batch,
hidden_size)
out, h_n = rnn(inputs)
```

```
input shape = [4, 5, 1]
out shape = [4, 5, 4]
h_n shape = [2, 4, 2]
```

In the **input** We have 4 batches as our output because we set the BATCH_SIZE=4. Each batch contains 5 rows because out SEQ_LENGTH = 5. We are using only a single feature as input INPUT_SIZE = 1.

In the **out**, we get values from all 4 batches where number of time-steps (seq_len) is 5 and the number of predictions are 2. For each batch, we're predicting 2 outputs. Since, it's a bidirectional RNN, we get 2 sets of predictions. Hence, the shape is [4, 5, 4] and not [4, 5, 2] (which we observed in the case of a unidirectional RNN above).

In the h_n, we get values from each of the 4 batches of the last time-steps of the single RNN layers. Since, it's a bidirectional RNN, we get 2 sets of predictions. Hence, the shape is [2, 4, 2] and not [1, 4, 2] (which we observed in the case of a unidirectional RNN above).

[7.],

```
[8.],
         [ 9.],
         [10.]],
        [[11.],
         [12.],
         [13.],
         [14.],
         [15.]],
        [[16.],
         [17.],
         [18.],
         [19.],
         [20.]])
         torch.Size([4, 5, 4])
Output:
                      0.4086,
 tensor([[[ 0.2184,
                               0.6418, -0.1677,
         L-0.0222, -0.0095,
                              0.8794, -0.4927,
         [-0.6716, -0.2802,
                              0.9585, -0.7248,
                              0.9846, -0.8646],
         [-0.9387, -0.4152,
         [-0.9841, -0.6164,
                              0.9789, -0.9192],
        [[-0.9813, -0.8829,
                              0.9979, -0.9721,
         [-0.9986, -0.8902,
                              0.9992, -0.9877,
         [-0.9995, -0.9449,
                              0.9997, -0.9946,
         [-0.9998, -0.9729,
                              0.9999, -0.9977],
         [-0.9999, -0.9868]
                              0.9998, -0.9987],
        [-0.9999, -0.9968]
                              1.0000, -0.9996],
         [-1.0000, -0.9969,
                              1.0000, -0.9998],
         [-1.0000, -0.9985,
                              1.0000, -0.9999],
         [-1.0000, -0.9993,
                              1.0000, -1.0000],
         [-1.0000, -0.9997,
                              1.0000, -1.0000]],
        [[-1.0000, -0.9999,
                              1.0000, -1.0000],
                              1.0000, -1.0000],
         [-1.0000, -0.9999,
         [-1.0000, -1.0000,
                              1.0000, -1.0000,
                              1.0000, -1.0000],
         [-1.0000, -1.0000,
                              1.0000, -1.0000]]], grad_fn=
         [-1.0000, -1.0000,
<TransposeBackward1>)
Hidden:
         torch.Size([2, 4, 2])
```

Let us now try to understand the output in a little more detail. According to the docs, to separate the directions (forward and backward), we can do the following -

- out.view(seq_len, batch, num_directions, hidden_size) with forward and backward being direction 0 and 1 respectively. Keep in mind that if you used batch_first=True, then it would be out.view(batch, seq_len, num_directions, hidden_size).
- h_n.view(num_layers, num_directions, batch, hidden_size) with forward and backward being direction 0 and 1 respectively.

BiRNN Separated out

Let's reshape the BiRNN output to separate out forward and backward values using out.view(batch, seq_len, num_directions, hidden_size).

```
out_reshaped = out.view(BATCH_SIZE, SEQ_LENGTH, 2,
HIDDEN_SIZE)
print("Shape of the output after directions are separated:
", out_reshaped.shape)
```

```
Shape of the output after directions are separated:
  torch.Size([4, 5, 2, 2])
The shape is now — (batch, seq_len, num_directions, hidden_size).
num directions is the 2nd dimension. To obtain forward and backward
outputs, we can do the following -
• out forward = (batch, seq_len, 0, hidden_size)
• out backward = (batch, seq_len, 1, hidden_size)
 out_forward = out_reshaped[:, :, 0, :]
 out_backward = out_reshaped[:, :, 1, :]
 print("Forward output: ", out_forward.shape, "n",
 out forward)
 print("nnBackward output: ", out_backward.shape, "n",
 out backward)
 Forward output: torch.Size([4, 5, 2])
  tensor([[[ 0.2184, 0.4086],
          [-0.0222, -0.0095],
          [-0.6716, -0.2802],
          [-0.9387, -0.4152],
          [-0.9841, -0.6164]
         [[-0.9813, -0.8829],
          [-0.9986, -0.8902],
          [-0.9995, -0.9449],
          [-0.9998, -0.9729],
```

```
[-0.9999, -0.9868]],
        [[-0.9999, -0.9968],
         [-1.0000, -0.9969],
         [-1.0000, -0.9985],
         [-1.0000, -0.9993],
         [-1.0000, -0.9997]
        [[-1.0000, -0.9999],
         [-1.0000, -0.9999],
         [-1.0000, -1.0000],
         [-1.0000, -1.0000],
         [-1.0000, -1.0000]]], grad_fn=<SliceBackward>)
Backward output: torch.Size([4, 5, 2])
tensor([[[ 0.6418, -0.1677],
         [0.8794, -0.4927],
         [0.9585, -0.7248],
         [0.9846, -0.8646],
         [0.9789, -0.9192]
        [[0.9979, -0.9721],
         [0.9992, -0.9877],
         [0.9997, -0.9946],
         [0.9999, -0.9977],
         [0.9998, -0.9987]],
        [[1.0000, -0.9996],
         [1.0000, -0.9998],
         [1.0000, -0.9999],
         [1.0000, -1.0000],
         [1.0000, -1.0000]],
        [[1.0000, -1.0000],
         [1.0000, -1.0000],
         [1.0000, -1.0000],
         [1.0000, -1.0000],
         [ 1.0000, -1.0000]]], grad_fn=<SliceBackward>)
```

```
Let's reshape the BiRNN hidden to separate out forward and backward
values using h_n.view(num_layers, num_directions, batch, hidden_size).
  h_n_reshaped = h_n.view(1, 2, BATCH_SIZE, HIDDEN_SIZE)
  print("Shape of the hidden after directions are separated:
  ", h_n_reshaped.shape)
  Shape of the hidden after directions are separated:
  torch.Size([1, 2, 4, 2])
The shape is now — (num_layers, num_directions, batch, hidden_size).
num_directions is the 1st dimension. To obtain forward and backward
hidden, we can do the following -
 • hidden forward = (num_layers, 0, batch, hidden_size)

    hidden backward = (num_layers, 1, batch, hidden_size)

  h n forward = h n reshaped[:, 0, :, :]
  h_n_backward = h_n_reshaped[:, 1, :, :]
  print("Forward h_n: ", h_n_forward.shape, "n", h_n_forward)
 print("nnBackward h_n: ", h_n_backward.shape, "n",
  h n backward)
  Forward h n: torch.Size([1, 4, 2])
  tensor([[[-0.9841, -0.6164],
          [-0.9999, -0.9868],
          [-1.0000, -0.9997],
```

Stacked Bidirectional RNN

For a Stacked Bidirectional RNN, we set the bidirectional=True and num layers = 3.

```
rnn = nn.RNN(input_size=INPUT_SIZE, hidden_size=HIDDEN_SIZE,
batch_first=True, num_layers = 3, bidirectional = True)

# input size : (batch_size , seq_len, input_size)
inputs = data.view(BATCH_SIZE, SEQ_LENGTH, INPUT_SIZE)

# out shape = (batch, seq_len, num_directions * hidden_size)
# h_n shape = (num_layers * num_directions, batch,
hidden_size)
out, h_n = rnn(inputs)

input shape = [4, 5, 1]
out shape = [4, 5, 4]
h_n shape = [6, 4, 2]
```

In the **input** We have 4 batches as our output because we set the BATCH_SIZE=4. Each batch contains 5 rows because out SEQ_LENGTH = 5. We are using only a single feature as input INPUT SIZE = 1.

In the **out**, we get values from all 4 batches where number of time-steps (seq_len) is 5 and the number of predictions are 2. For each batch, we're predicting 2 outputs. Since, it's a bidirectional RNN, we get 2 sets of predictions. Hence, the shape is [4, 5, 4] and not [4, 5, 2] (which we observed in the case of a stacked-unidirectional RNN above).

In the h_n , we get values from each of the 4 batches of the last time-steps of the single RNN layers. Since, it's a bidirectional RNN, we get 2 sets of predictions. Hence, the shape is [6, 4, 2] and not [3, 4, 2] (which we observed in the case of a stacked-unidirectional RNN above).

```
print('Input: ', inputs.shape, 'n', inputs)
print('nOutput: ', out.shape, 'n', out)
print('nHidden: ', h_n.shape, 'n', h_n)
Input: torch.Size([4, 5, 1])
 tensor([[[ 1.],
          [ 2.],
          [ 3.],
          [4.],
          [5.]],
         [[6.],
          [7.],
          [8.],
          [ 9.],
          [10.]],
         [[11.],
          [12.],
          [13.],
           [14.],
          [15.]],
```

[[16.],

```
[17.],
         [18.],
         [19.],
         [20.]])
        torch.Size([4, 5, 4])
Output:
tensor([[[-0.4175, -0.6278, -0.0101, -0.4025],
         [0.1271, -0.5579,
                             0.2162, -0.4832,
         [-0.2557, -0.6714, 0.3084, -0.4927],
         [0.0556, -0.6295, 0.3194, -0.4467],
                            0.3917, -0.6299]],
         [-0.1510, -0.6863,
        [[-0.4311, -0.6939, -0.2381, -0.6894],
         [0.1423, -0.5335, -0.0872, -0.6471],
                            0.0076, -0.6274],
         [-0.2943, -0.6468,
         [0.0392, -0.5691, 0.0595, -0.5576],
         [-0.2070, -0.6238, 0.2187, -0.6570]]
        [[-0.4458, -0.6581, -0.6259, -0.8299],
         [0.0999, -0.4501, -0.5715, -0.8090],
         [-0.3441, -0.5669, -0.4723, -0.7729],
         [-0.0133, -0.4705, -0.3131, -0.6745],
         [-0.2617, -0.5444, 0.0042, -0.6820]],
        [[-0.4556, -0.6330, -0.7035, -0.8531],
         [0.0780, -0.4118, -0.6690, -0.8358],
         [-0.3608, -0.5393, -0.5730, -0.7989],
         [-0.0285, -0.4442, -0.3958, -0.6973]
         [-0.2739, -0.5259, -0.0447, -0.6868]], grad fn=
<TransposeBackward1>)
Hidden: torch.Size([6, 4, 2])
tensor([[[ 0.9455, 0.5653],
         [0.9986, -0.1385],
         [1.0000, -0.7900],
         [1.0000, -0.9272]],
        [[0.1570]
                    0.2765],
         [0.9959,
                    0.9972],
         [ 1.0000,
                    1.0000],
                    1.0000]],
         [ 1.0000,
        [[-0.6463, 0.5301],
```

```
[-0.5393, 0.6556],
[-0.4089, 0.7277],
[-0.3732, 0.7372]],

[[ 0.0474, -0.5973],
[ 0.0082, -0.9715],
[-0.1373, -0.9681],
[-0.2362, -0.9658]],

[[-0.1510, -0.6863],
[-0.2070, -0.6238],
[-0.2617, -0.5444],
[-0.2739, -0.5259]],

[[-0.0101, -0.4025],
[-0.2381, -0.6894],
[-0.6259, -0.8299],
[-0.7035, -0.8531]]], grad_fn=<StackBackward>)
```

Let us now try to understand the output in a little more detail. According to the docs, to separate the directions (forward and backward), we can do the following -

- out.view(seq_len, batch, num_directions, hidden_size) with forward and backward being direction 0 and 1 respectively. Keep in mind that if you used batch_first=True, then it would be out.view(batch, seq_len, num_directions, hidden_size).
- h_n.view(num_layers, num_directions, batch, hidden_size) with forward and backward being direction 0 and 1 respectively.

Stacked BiRNN Separated out

Let's reshape the Stacked BiRNN output to separate out forward and backward values using out.view(batch, seq len, num directions,

```
hidden size).
 out reshaped = out.view(BATCH SIZE, SEQ LENGTH, 2,
 HIDDEN SIZE)
 print("Shape of the output after directions are separated:
  ", out reshaped.shape)
 Shape of the output after directions are separated:
  torch.Size([4, 5, 2, 2])
The shape is now — (batch, seq_len, num_directions, hidden_size).
num directions is the 2nd dimension. To obtain forward and backward
outputs, we can do the following -
• out forward = (batch, seg len, 0, hidden size)
• out backward = (batch, seq_len, 1, hidden_size)
 out forward = out reshaped[:, :, 0, :]
 out_backward = out_reshaped[:, :, 1, :]
 print("Forward output: ", out_forward.shape, "n",
 out forward)
 print("nnBackward output: ", out backward.shape, "n",
 out backward)
 Forward output: torch.Size([4, 5, 2])
  tensor([[-0.4175, -0.6278],
          [0.1271, -0.5579],
```

```
[-0.2557, -0.6714],
         [0.0556, -0.6295],
         [-0.1510, -0.6863]
        [[-0.4311, -0.6939],
         [0.1423, -0.5335],
         [-0.2943, -0.6468],
         [0.0392, -0.5691],
         [-0.2070, -0.6238]],
        [[-0.4458, -0.6581],
         [0.0999, -0.4501],
         [-0.3441, -0.5669],
         [-0.0133, -0.4705],
         [-0.2617, -0.5444]],
        [[-0.4556, -0.6330],
         [0.0780, -0.4118],
         [-0.3608, -0.5393],
         [-0.0285, -0.4442],
         [-0.2739, -0.5259]]], grad_fn=<SliceBackward>)
Backward output: torch.Size([4, 5, 2])
 tensor([[[-0.0101, -0.4025],
         [0.2162, -0.4832],
         [0.3084, -0.4927],
         [0.3194, -0.4467],
         [0.3917, -0.6299]],
        [[-0.2381, -0.6894],
         [-0.0872, -0.6471],
         [0.0076, -0.6274],
         [0.0595, -0.5576],
         [0.2187, -0.6570],
        [[-0.6259, -0.8299],
         [-0.5715, -0.8090],
         [-0.4723, -0.7729],
         [-0.3131, -0.6745],
         [0.0042, -0.6820]],
        [[-0.7035, -0.8531],
```

```
[-0.6690, -0.8358],
[-0.5730, -0.7989],
[-0.3958, -0.6973],
[-0.0447, -0.6868]]], grad_fn=<SliceBackward>)
```

Stacked BiRNN Separated h_n

Let's reshape the Stacked BiRNN hidden to separate out forward and backward values using h_n.view(num_layers, num_directions, batch, hidden_size).

The shape is now — (num_layers, num_directions, batch, hidden_size).

num_directions is the 1st dimension. To obtain forward and backward hidden, we can do the following -

- hidden_forward = (num_layers, 0, batch, hidden_size)
- hidden backward = (num layers, 1, batch, hidden size)

```
h_n_{forward} = h_n_{reshaped}[:, 0, :, :]
h n backward = h n reshaped[:, 1, :, :]
print("Forward h_n: ", h_n_forward.shape, "n", h_n_forward)
print("nnBackward h_n: ", h_n_backward.shape, "n",
h n backward)
Forward h n: torch.Size([3, 4, 2])
tensor([[[ 0.9455, 0.5653],
         [ 0.9986, -0.1385], [ 1.0000, -0.7900],
         [1.0000, -0.9272]],
        [[-0.6463, 0.5301],
         [-0.5393, 0.6556],
         [-0.4089, 0.7277],
         [-0.3732, 0.7372]
        [[-0.1510, -0.6863],
         [-0.2070, -0.6238],
         [-0.2617, -0.5444],
         [-0.2739, -0.5259]]], grad_fn=<SliceBackward>)
Backward h_n: torch.Size([3, 4, 2])
 tensor([[[ 0.1570, 0.2765],
         [ 0.9959, 0.9972],
         [ 1.0000, 1.0000],
         [ 1.0000, 1.0000]],
        [[0.0474, -0.5973],
         [0.0082, -0.9715],
         [-0.1373, -0.9681],
         [-0.2362, -0.9658]
        [[-0.0101, -0.4025],
         [-0.2381, -0.6894],
         [-0.6259, -0.8299],
         [-0.7035, -0.8531]]], grad_fn=<SliceBackward>)
```