

Programming Task

Differential Evolution

Continuous Optimization

Continuous Optimization Problems arise in

- Machine Learning (minimize loss function)
- Probability Theory (compute probability bounds)
- Natural Sciences (physical and chemical models)
- Engineering (optimal design and control problems)
- Economics (maximize utility)

Differential evolution is particularly interesting if objective function is non-smooth and non-convex

Power Plant Optimization

- suppose, you work for an electric utility service provider
- you can generate energy with different plane types with different costs
- you can sell energy at different markets at different prices (e.g. business, consumer)



- **Problem:** determine how much **energy to generate** with which plane type, how much **energy to sell** to which market and at what **price** in order to maximize profit

High-Level Profit Model

- Profit = Revenue - Cost

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- Revenue = SoldQuantity * Price

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- $\text{Profit} = \text{Revenue} - \text{Cost}$
- $\text{Revenue} = \text{SoldQuantity} * \text{Price}$
- $\text{Cost} = \text{ProductionCost} + \text{PurchasingCost}$

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- Purchasing Cost
 $= \max(\text{SoldQuantity} - \text{GeneratedQuantity}, 0) * \text{CostPrice}$

High-Level Profit Model

- Profit = Revenue - Cost
- Revenue = SoldQuantity * Price
- Cost = ProductionCost + PurchasingCost
- Production Cost = GeneratedQuantity * CostFactor
- Purchasing Cost
= max(SoldQuantity - GeneratedQuantity, 0) * CostPrice

(if you sell more energy than you can provide, you have to buy energy from another provider)

Plant Cost Model

We describe each plant type by three parameters

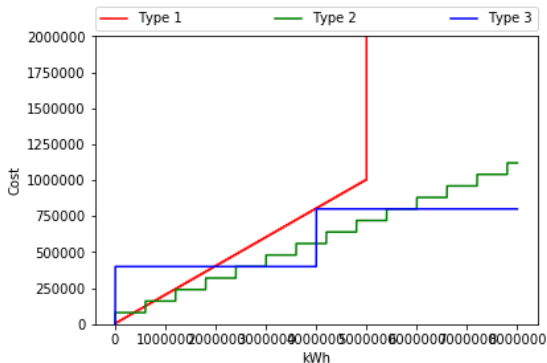
- k - kWh per plant
- c - cost per plant
- m - maximum number of plants that can be used

```
def cost(x, kwhPerPlant, costPerPlant, maxPlants):  
  
    #if x is non-positive, return 0  
    if(x <= 0):  
        return 0  
  
    #if x is greater than what can be generated return prohibitively large value  
    if(x > kwhPerPlant * maxPlants):  
        return LARGE  
  
    #otherwise determine number of plants needed to generate x  
    plantsNeeded = math.ceil(x / kwhPerPlant)  
  
    #cost is number of plants needed times cost per plant  
    return plantsNeeded * costPerPlant
```

Plant Types

We consider three plant types

- Type 1: $k = 50,000$, $c = 10,000$, $m = 100$
- Type 2: $k = 600,000$, $c = 80,000$, $m = 50$
- Type 3: $k = 4,000,000$, $c = 400,000$, $m = 3$



Market Model

We describe each market by two parameters

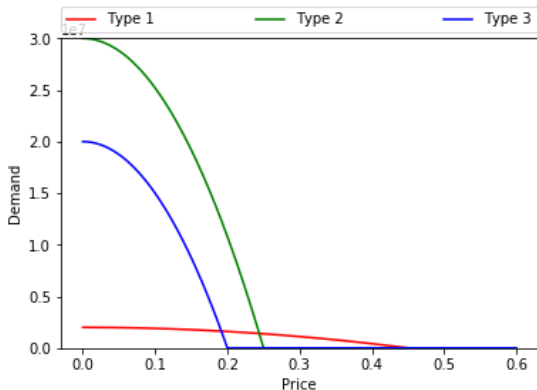
- p - maximum price at which customers buy
- d - maximum demand

```
def demand(price, maxPrice, maxDemand):  
  
    #if price is greater than max price, return 0  
    if(price > maxPrice):  
        return 0  
  
    #if product is free return maxDemand (ignore negative price)  
    if(price <= 0):  
        return maxDemand  
  
    #else determine demand based on price  
    demand = maxDemand - price**2 * maxDemand / maxPrice**2  
  
    return demand
```

Market Types

We consider three market types

- Type 1: $p = 0.45$, $d = 2,000,000$
- Type 2: $p = 0.25$, $d = 30,000,000$
- Type 3: $p = 0.2$, $d = 20,000,000$



Profit Model

9 Variables ($e_1, e_2, e_3, s_1, s_2, s_3, p_1, p_2, p_3$)

- 1 e_1, e_2, e_3 : energy produced with plants of type i
- 2 s_1, s_2, s_3 : planned amount of energy sold to market of type i
- 3 p_1, p_2, p_3 : price for market of type i

Profit model

- Profit = Revenue - Cost
- Revenue = $\sum_{i=1}^3 \min(\text{demand}_i(p_i), s_i) \cdot p_i$
- Cost = ProductionCost + PurchasingCost
- Production Cost = $\sum_{i=1}^3 \text{cost}_i(e_i)$
- Purchasing Cost = $\max((\sum_{i=1}^3 s_i) - (\sum_{i=1}^3 e_i), 0) \cdot 0.6$

(cost price is 0.6)

DE Programming Task

- solve Power Plant Problem using Basic DE
- as usual, **decompose your implementation**
 - Initialization
 - Donor Generation (parameter for scale factor)
 - Trial Generation (parameter for crossover rate)
 - Selection
- document what scheme you use for which component (try several if you have time)
- divide work among group members

DE Programming Task

- make some **experiments** with different parameter settings
- document your findings and prepare a **small presentation** (5-10 minutes)
- send me a compressed archive containing
 - 1 slides (structure findings in table or other visualization)
 - 2 source files/ notebook
 - 3 assignment of tasks to group members

- there are other (and perhaps better) ways to model this problem equivalently
- if you have a better idea, feel free to try an alternative model
- if you have time, also try different (and more) plant and market types
- note that you are completely flexible in the choice of your objective function (non-linear, non-differentiable, ...)

Some Results

Problem	Plants			Markets		Cost Price	Profit Achieved
	k	c	m	p	d		
P1	50k	10k	100	0.45	2M	0.6	1,514,312
	600k	80k	50	0.25	30M		
	4M	400k	3	0.2	20M		
P2	50k	10k	100	0.45	2M	0.1	1,818,406
	600k	80k	50	0.25	30M		
	4M	400k	3	0.2	20M		
P3	50k	10k	100	0.5	1M	0.6	404,041
	600k	80k	50	0.3	5M		
	4M	400k	3	0.1	5M		