24

Estructuras p/=2;25 val=operacion(t[p*2], t[p*2+1]); 26 27 RMQ (static) } Dado un arreglo y una operacion asociativa idempotente, get(i, j) opera sobre el rango [i, j).²⁸ }rmq; Restriccion: LVL ≥ ceil(logn); Usar [] para llenar arreglo y luego build(). //Usage: 1 | struct RMQ{ 31 | cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall(); #define LVL 10 RMQ (lazy) tipo vec[LVL] [1<<(LVL+1)];</pre> tipo &operator[](int p){return vec[0][p];} //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre tipo get(int i, int j) {//intervalo [i,j) el rango [i, j). int p = 31-__builtin_clz(j-i); typedef int Elem;//Elem de los elementos del arreglo return min(vec[p][i],vec[p][j-(1<<p)]);</pre> typedef int Alt; //Elem de la alteracion #define operacion(x,y) x+y void build(int n) {//O(nlogn) 9 const Elem neutro=0; const Alt neutro2=0; int mp = 31-__builtin_clz(n); 10 #define MAXN 1024000 forn(p, mp) forn(x, n-(1 << p)) 11 struct RMQ{ vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);12 int sz; }}; 13 Elem t[4*MAXN]; Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem RMQ (dynamic) Elem &operator[](int p){return t[sz+p];} 1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre void init(int n){//O(nlgn) el rango [i, j). $sz = 1 \ll (32-_builtin_clz(n));$ 2 #define MAXN 100000 forn(i, 2*sz) t[i]=neutro; #define operacion(x, y) max(x, y) forn(i, 2*sz) dirty[i]=neutro2; 15 const int neutro=0; 16 struct RMO{ void updall() ${//0(n)}$ 17 dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);} int sz: 18 void opAltT(int n,int a,int b){//altera el valor del nodo n segun su dirty y tipo t[4*MAXN]; tipo &operator[](int p){return t[sz+p];} el intervalo que le corresponde. void init(int n){//O(nlgn) t[n] += dirty[n]*(b-a); 20 $sz = 1 \ll (32-_builtin_clz(n));$ } //en este caso la alteracion seria sumarle a todos los elementos del 10 forn(i, 2*sz) t[i]=neutro; intervalo [a,b) el valor dirty[n] 11 } void opAltD(int n ,Alt val){ 22 12 void updall() ${//0(n)}$ dirty[n] += val; 13 23 dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);} }//actualiza el valor de Dirty "sumandole" val. podria cambiar el valor de 14 tipo get(int i, int j){return get(i,j,1,0,sz);} // [i,j) ! dirty dependiendo de la operacion que se quiera al actualizar un rango. 15 tipo get(int i, int j, int n, int a, int b) ${\frac{1}{0}}$ Ej:11402.cpp 16 void push(int n, int a, int b){//propaga el dirty a sus hijos if(j<=a || i>=b) return neutro; 25 17 if(dirty[n]!=neutro2){ if(i<=a && b<=j) return t[n];</pre> 18 26 opAltT(n,a,b); //t[n]+=dirty[n]*(b-a);//altera el nodo int c=(a+b)/2: 27 19 return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b)); if(n<sz){ 28 20 } opAltD(2*n,dirty[n]);//dirty[2*n]+=dirty[n]; 21 29 opAltD(2*n+1,dirty[n]);//dirty[2*n+1]+=dirty[n]; void set(int p, tipo val){//O(lgn) 22 30 for(p+=sz; p>0 && t[p]!=val;){ 23 31 t[p]=val; dirty[n]=neutro2;

32

```
}
                                                                                     5 | struct node{
33
     }
                                                                                          tipo v; node *1,*r;
34
     Elem get(int i, int j, int n, int a, int b){\frac{1}{0}}
                                                                                          node(tipo v):v(v), 1(NULL), r(NULL) {}
       if(j<=a || i>=b) return neutro;
                                                                                            node(node *1, node *r) : 1(1), r(r){
       push(n, a, b);//corrige el valor antes de usarlo
                                                                                                if(!1) v=r->v;
       if(i<=a && b<=j) return t[n];
                                                                                                else if(!r) v=l->v;
       int c=(a+b)/2;
                                                                                                else v=oper(1->v, r->v);
39
                                                                                     11
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
                                                                                            }
                                                                                     12
                                                                                        };
41
                                                                                    13
     Elem get(int i, int j){return get(i,j,1,0,sz);}
                                                                                        node *build (tipo *a, int tl, int tr) {//modificar para que tome tipo a
42
                                                                                          if (tl+1==tr) return new node(a[tl]);
     //altera los valores en [i, j) con una alteracion de val
43
     void alterar(Alt val, int i, int j, int n, int a, int b)\frac{1}{0(\lg n)}
                                                                                          int tm=(tl + tr)>>1;
44
       push(n, a, b);
                                                                                          return new node(build(a, tl, tm), build(a, tm, tr));
45
                                                                                    17
       if(j<=a || i>=b) return;
                                                                                     18
46
       if(i<=a && b<=j){
                                                                                        node *update(int pos, int new_val, node *t, int tl, int tr){
47
                                                                                          if (tl+1==tr) return new node(new_val);
         opAltD(n,val);//actualiza el valor de Dirty por val.
48
                                                                                          int tm=(tl+tr)>>1;
         push(n,a,b);
49
         return; //este nodo esta totalmente contenido por el intervalo a alterar,
                                                                                          if(pos < tm) return new node(update(pos, new_val, t->1, tl, tm), t->r);
50
             no es necesario que se lo pases a los hijos.. por ahora..
                                                                                          else return new node(t->1, update(pos, new_val, t->r, tm, tr));
       }
                                                                                    24
51
       int c=(a+b)/2;
                                                                                        tipo get(int 1, int r, node *t, int tl, int tr){
52
                                                                                    25
                                                                                            if(l==tl && tr==r) return t->v;
       alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
53
       t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
                                                                                          int tm=(tl + tr)>>1:
54
                                                                                            if(r<=tm) return get(1, r, t->1, t1, tm);
55
                                                                                            else if(l>=tm) return get(l, r, t->r, tm, tr);
     void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
56
                                                                                          return oper(get(1, tm, t->1, tl, tm), get(tm, r, t->r, tm, tr));
57
     //setea de a un elemento. Esto lo "hace" dinmico.
                                                                                    31 }
58
     void set(int p, Elem val){//O(lgn)
59
                                                                                                                        Union Find
       if(p<0) return; //OJO chequear que p no sea muy grande
60
       this->get(p,p+1); //para que acomode los dirty del camino de la raz a p
61
                                                                                     1 struct UnionFind{
       int a=p, b=p+1, ancho=1, vecino;
                                                                                          vector<int> f;//the array contains the parent of each node
62
       for(p+=sz; p>0 && t[p]!=val; ancho*=2){
63
                                                                                          void init(int n){f.clear(); f.insert(f.begin(), n, -1);}
         t[p]=val;
                                                                                          int comp(int x){return (f[x]=-1?x:f[x]=comp(f[x]));}//0(1)
64
         if(p&1){ vecino=p-1; push(vecino,a,b); a-=ancho; }
                                                                                          bool join(int i, int j) {
65
         else{ vecino=p+1; push(vecino,a,b); b+=ancho; }
                                                                                           bool con=comp(i)==comp(j);
66
         p/=2;
67
                                                                                            if(!con) f[comp(i)] = comp(j);
         val=operacion(t[p*2], t[p*2+1]);
68
                                                                                            return con;
69
                                                                                          }};
     }
                                                                                                                    Disjoint Intervals
                                                                                     | bool operator< (const ii &a, const ii &b) {return a.fst<b.fst;}
                              RMQ (persistente)
                                                                                        //Stores intervals as [first, second]
1 typedef int tipo;
                                                                                        //in case of a collision it joins them in a single interval
2 tipo oper(const tipo &a, const tipo &b){
                                                                                        struct disjoint_intervals {
                                                                                          set<ii>> segs;
       return a+b:
4 }
                                                                                          void insert(ii v) {//O(lgn)
```

```
if(v.snd-v.fst==0.) return://0J0
       set<ii>>::iterator it,at;
       at = it = segs.lower_bound(v);
       if (at!=segs.begin() && (--at)->snd >= v.fst)
         v.fst = at->fst, --it;
11
       for(; it!=segs.end() && it->fst <= v.snd; segs.erase(it++))</pre>
         v.snd=max(v.snd, it->snd);
13
       segs.insert(v);
    }
15
<sub>16</sub> };
                                    RMQ (2D)
struct RMO2D{//n filas x m columnas
     int sz:
     RMQ t[4*MAXN];
     void init(int n, int m){\frac{}{/0(n*m)}}
       sz = 1 << (32-__builtin_clz(n));</pre>
       forn(i, 2*sz) t[i].init(m); }
     void set(int i, int j, tipo val){//0(lgm.lgn)
       for(i+=sz; i>0;){
         t[i].set(j, val);
         i/=2;
         val=operacion(t[i*2][j], t[i*2+1][j]);
11
       } }
12
     tipo get(int i1, int j1, int i2, int j2){return get(i1,j1,i2,j2,1,0,sz);}
     //O(lgm.lgn), rangos cerrado abierto
14
     int get(int i1, int j1, int i2, int j2, int n, int a, int b){
15
       if(i2<=a || i1>=b) return neutro;
16
       if(i1<=a && b<=i2) return t[n].get(j1, j2);
       int c=(a+b)/2;
       return operacion(get(i1, j1, i2, j2, 2*n, a, c),
            get(i1, j1, i2, j2, 2*n+1, c, b));
     }
   } rmq;
   //Example to initialize a grid of M rows and N columns:
  RMQ2D rmq; rmq.init(n,m);
  forn(i, n) forn(j, m){
     int v; cin >> v; rmq.set(i, j, v);}
                                      Big Int
1 #define BASEXP 6
2 #define BASE 1000000
3 #define LMAX 1000
4 | struct bint{int 1;ll n[LMAX];bint(ll x=0){l=1;forn(i,LMAX){if(x)l=i+1;n[i]=x%
       BASE; x/=BASE; }} bint(string x) {1=(x.size()-1)/BASEXP+1; fill(n,n+LMAX,0); 11
       r=1;forn(i,sz(x))\{n[i/BASEXP]+=r*(x[x.size()-1-i]-,0,0);r*=10;if(r==BASE)r\}
```

```
=1;}}void out(){cout<<n[l-1];dforn(i,l-1)printf("%6.6llu",n[i]);}void
invar(){fill(n+l,n+LMAX,0); while(l>1&&!n[l-1])l--;}}; bint operator+(const
bint&a,const bint&b){bint c;c.l=max(a.l,b.l);ll q=0;forn(i,c.l)q+=a.n[i]+b
.n[i],c.n[i]=q%ASE,q/=BASE;if(q)c.n[c.1++]=q;c.invar();return c;}pair<
bint,bool>lresta(const bint&a,const bint&b){bint c;c.l=max(a.1,b.1);ll q
=0;forn(i,c.l)q+=a.n[i]-b.n[i],c.n[i]=(q+BASE) %BASE,q=(q+BASE)/BASE-1;c.
invar();return make_pair(c,!q);}bint&operator==(bint&a,const bint&b){
return a=lresta(a,b).first;}bint operator-(const bint&a,const bint&b){
return lresta(a,b).first;}bool operator<(const bint&a,const bint&b){return
!lresta(a,b).second;}bool operator<=(const bint&a,const bint&b){return
lresta(b,a).second;}bool operator==(const bint&a,const bint&b){return a<=b</pre>
&&b<=a;}bint operator*(const bint&a,ll b){bint c;ll q=0;forn(i,a.l)q+=a.n[
i]*b,c.n[i]=q%BASE,q/=BASE;c.l=a.l;while(q)c.n[c.l++]=q%BASE,q/=BASE;c.
invar(); return c; bint operator*(const bint&a, const bint&b) {bint c; c.l=a.l
+b.1;fill(c.n,c.n+b.1,0);forn(i,a.1){ll q=0;forn(j,b.1)q+=a.n[i]*b.n[j]+c.
n[i+j],c.n[i+j]=q'BASE,q/=BASE;c.n[i+b.1]=q;}c.invar();return c;}pair<br/>cbint
,ll>ldiv(const bint&a,ll b){bint c;ll rm=0;dforn(i,a.l){rm=rm*BASE+a.n[i];
c.n[i]=rm/b;rm%=b;}c.l=a.l;c.invar();return make_pair(c,rm);}bint operator
/(const bint&a,ll b){return ldiv(a,b).first;}ll operator%(const bint&a,ll
b){return ldiv(a,b).second;}pair<bint,bint>ldiv(const bint&a,const bint&b)
{bint c;bint rm=0;dforn(i,a.1){if(rm.l==1&&!rm.n[0])rm.n[0]=a.n[i];else{
dforn(j,rm.l)rm.n[j+1]=rm.n[j];rm.n[0]=a.n[i];rm.l++;}ll q=rm.n[b.l]*BASE+
rm.n[b.l-1];ll u=q/(b.n[b.l-1]+1);ll v=q/b.n[b.l-1]+1;while(u<v-1){ll m=(u<v-1)}
+v)/2;if(b*m<=rm)u=m;else v=m;}c.n[i]=u;rm-=b*u;}c.l=a.1;c.invar();return
make_pair(c,rm);}bint operator/(const bint&a,const bint&b){return ldiv(a,b
).first;}bint operator%(const bint&a,const bint&b){return ldiv(a,b).second
;}
```

Modnum

```
while(sz(c) \ge 2 \&\& irre(c[sz(c)-2], c[sz(c)-1], 1)) { c.pop_back(); if(
   struct mnum{
                                                                                                     pos) pos--; }
     static const tipo mod=MOD;
                                                                                                 c.pb(1);
                                                                                     21
     tipo v:
                                                                                     22
     mnum(tipo v=0): v((v mod+mod) mod) {}
                                                                                           inline bool fbin(tipo x, int m) {return inter(acc(m), acc(m+1))>x;}
     mnum operator+(mnum b){return v+b.v;}
                                                                                           tipo eval(tipo x){
                                                                                            int n = sz(c);
     mnum operator-(mnum b){return v-b.v;}
24
                                                                                             //query con x no ordenados O(lgn)
     mnum operator*(mnum b){return v*b.v;} //Si mod<=1e9+9</pre>
25
     //~ mnum operator*(mnum b){return mul(v,b.v,mod);} //Si mod<=1e18+9
                                                                                             int a=-1, b=n-1;
26
                                                                                             while(b-a>1) { int m = (a+b)/2;
     mnum operator(ll n) \{ //0 (log n) \}
27
       if(!n) return 1;
                                                                                               if(fbin(x, m)) b=m;
28
       mnum q = (*this)^n(n/2);
                                                                                               else a=m;
29
                                                                                     30
       return n %2 ? q*q*v : q*q;
30
                                                                                     31
                                                                                             return (acc(b).m*x+acc(b).h)*(mx?-1:1);
31
     mnum operator/(mnum n){return ~n*v;} //O(log n) //OJO! mod tiene que ser
                                                                                                 //query 0(1)
32
         primo! Sino no siempre existe inverso
                                                                                             while(pos>0 && fbin(x, pos-1)) pos--;
                                                                                             while(pos<n-1 && !fbin(x, pos)) pos++;
33
                                                                                     35
     mnum operator~(){ //inverso, O(log mod)
                                                                                             return (acc(pos).m*x+acc(pos).h)*(mx?-1:1);
                                                                                     36
34
       assert(v!=0):
                                                                                     37
35
       //return (*this)^(eulerphi(mod)-1); //si mod no es primo (sacar a mano)
                                                                                     38 } ch;
36
           PROBAR! Ver si rta*x == 1 modulo mod
                                                                                                              Convex Hull Trick (Dynamic)
       return (*this)^(mod-2);//si mod es primo
37
38
                                                                                      const ll is_query = -(1LL<<62);
39 };
                                                                                         struct Line {
                                                                                             ll m, b;
                               Convex Hull Trick
                                                                                             mutable multiset<Line>::iterator it:
struct Line{tipo m,h;};
                                                                                             const Line *succ(multiset<Line>::iterator it) const;
                                                                                             bool operator<(const Line& rhs) const {</pre>
  tipo inter(Line a, Line b){
       tipo x=b.h-a.h, y=a.m-b.m;
                                                                                                 if (rhs.b != is_query) return m < rhs.m;</pre>
       return x/y+(x\%?!((x>0)^(y>0)):0);//==ceil(x/y)
                                                                                                 const Line *s=succ(it);
                                                                                                 if(!s) return 0;
   struct CHT {
                                                                                                 11 x = rhs.m;
     vector<Line> c;
                                                                                                 return b - s -> b < (s -> m - m) * x;
                                                                                     11
     bool mx;
                                                                                             }
                                                                                     12
     int pos;
                                                                                     13
     CHT(bool mx=0):mx(mx),pos(0){}//mx=1 si las query devuelven el max
                                                                                         struct HullDynamic : public multiset<Line>{ // will maintain upper hull for
     inline Line acc(int i){return c[c[0].m>c.back().m? i : sz(c)-1-i];}
11
     inline bool irre(Line x, Line y, Line z){
                                                                                             bool bad(iterator y) {
12
                                                                                     15
       return c[0].m>z.m? inter(y, z) <= inter(x, y)
                                                                                                 iterator z = next(y);
13
                                                                                     16
                            : inter(y, z) >= inter(x, y);
                                                                                                 if (y == begin()) {
14
                                                                                     17
                                                                                                     if (z == end()) return 0;
                                                                                     18
15
     void add(tipo m, tipo h) {//0(1), los m tienen que entrar ordenados
                                                                                                     return y->m == z->m && y->b <= z->b;
                                                                                     19
16
           if (mx) m*=-1, h*=-1;
                                                                                     20
17
       Line l=(Line)\{m, h\};
                                                                                                 iterator x = prev(y);
18
           if(sz(c) && m==c.back().m) { 1.h=min(h, c.back().h), c.pop_back(); if( 22
                                                                                                 if (z == end()) return y->m == x->m && y->b <= x->b;
               pos) pos--; }
                                                                                                 return (x-b - y-b)*(z-m - y-m) >= (y-b - z-b)*(y-m - x-m);
```

```
24
       iterator next(iterator y){return ++y;}
25
       iterator prev(iterator y){return --y;}
       void insert line(ll m. ll b) {
           iterator y = insert((Line) { m, b });
           v->it=v;
           if (bad(y)) { erase(y); return; }
           while (next(y) != end() && bad(next(y))) erase(next(y));
31
           while (y != begin() && bad(prev(y))) erase(prev(y));
32
33
       ll eval(ll x) {
34
           Line 1 = *lower_bound((Line) { x, is_query });
35
           return 1.m * x + 1.b;
36
       }
37
   }h;
38
   const Line *Line::succ(multiset<Line>::iterator it) const{
       return (++it==h.end()? NULL : &*it);}
```

Set con bsq. binaria (Treap)

```
1 #include < bits / stdc++.h>
#include<ext/pb_ds/assoc_container.hpp>
#include<ext/pb_ds/tree_policy.hpp>
  using namespace __gnu_pbds;
   using namespace std;
   template <typename T>
   using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
       tree_order_statistics_node_update>;
   //o bien usar as:
  typedef tree<int,null_type,less<int>,//key, mapped type, comparator. Se puede
       usar como map<a,b> poniendo tree<a,b,...
       rb_tree_tag,tree_order_statistics_node_update> set_t;
12
13
   int main(){
14
     ordered_set<int> s;
     s.insert(1);
16
     s.insert(3);
17
     cout << s.order_of_key(3) << endl; // s.order_of_key(x): number of elements</pre>
18
         in s strictly less than x.
     cout << *s.find_by_order(0) << endl; // s.find_by_order(i): i-th smallest</pre>
19
         number in s. (empieza en 0)
     cout << *s.lower_bound(1) << endl;</pre>
21 }
```

Algos

Longest Increasing Subsecuence

```
//Para non-increasing, cambiar comparaciones y revisar busq binaria
   //Given an array, paint it in the least number of colors so that each color
       turns to a non-increasing subsequence.
   //Solution:Min number of colors=Length of the longest increasing subsequence
   int N, a[MAXN];//secuencia y su longitud
   ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
   int p[MAXN];//padres
   vector<int> R;//respuesta
   void rec(int i){
     if(i==-1) return;
     R.push_back(a[i]);
     rec(p[i]);
11
12
   int lis(){//O(nlogn)
     d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
     forn(i, N){
15
       int j = upper_bound(d, d+N+1, ii(a[i], INF))-d;
16
       if (d[j-1].first < a[i]&&a[i] < d[j].first){</pre>
17
         p[i]=d[j-1].second;
         d[i] = ii(a[i], i);
19
       }
20
21
     R.clear():
22
     dforn(i, N+1) if(d[i].first!=INF){
       rec(d[i].second);//reconstruir
       reverse(R.begin(), R.end());
       return i;//longitud
26
27
     return 0;
28
29 }
```

Optimizaciones para DP

```
convex hull 1: dp[i] = min{dp[j] + b[j] * a[i]}, j < i. Si se cumple b[j] >= b[
    j+1] y a[i] <= a[i+1] entonces pasa de O(n^2) a O(n) sino pasa a O(nlogn)

convex hull 2: dp[i][j] = min{dp[i-1][k] + b[k] * a[j]}, k < j. Si se cumple b[
    k] >= b[k+1] y a[j] <= a[j+1] entonces pasa de O(kn^2) a O(kn) sino pasa O
    (knlogn)

divide and conquer: dp[i][j] = min{dp[i-1][k] + C[k+1][j]}, k < j. Se debe</pre>
```

```
cumplir: A[i][j] <= A[i][j+1]. Pasa de O(kn^2) a O(knlogn)</pre>
                                                                                                     a in the bounds only
8 | Donde A[i][j] es el minimo k tal que dp[i][j] = dp[i-1][k] + C[k][j]
                                                                                                int act = res[1][a] + res[a][r] + (C[1][r]);
                                                                                        51
   Tambien es aplicable si:
                                                                                                if (res[l][r] > act) {
                                                                                                                                          //relax current solution
                                                                                        52
  C[a][c] + C[b][d] <= C[a][d] + C[b][c] y C[b][c] <= C[a][d], a <= b <= c <= d
                                                                                                  res[1][r] = act;
                                                                                                  A[1][r] = a;
   def ComputeDP(i, jleft, jright, kleft, kright):
                                                                                        55
     # Select the middle point
                                                                                                }
                                                                                        56
     jmid = (jleft + jright) / 2
                                                                                             }
                                                                                        57
14
     # Compute the value of dp[i][jmid] by definition of DP
15
                                                                                                                                Strings
     dp[i][imid] = +INFINITY
16
     bestk = -1
17
     for k in range[kleft, jmid):
                                                                                                                                 KMP
18
     if dp[i-1][k] + C[k+1][jmid] < best:
19
       dp[i][jmid] = dp[i - 1][k] + C[k + 1][jmid]
                                                                                            string T;//cadena donde buscar(where)
20
       bestk = k
                                                                                            string P://cadena a buscar(what)
21
     # Divide and conquer
                                                                                            int b[MAXLEN];//back table b[i] maximo borde de [0..i)
22
                                                                                            void kmppre(){//by gabina with love
     if jleft < jmid:</pre>
23
     ComputeDP(i, jleft, jmid, kleft, bestk)
                                                                                                int i =0, j=-1; b[0]=-1;
24
     if jmid + 1 < jright:</pre>
                                                                                                while(i<sz(P)){</pre>
25
                                                                                                    while(j>=0 && P[i] != P[j]) j=b[j];
     ComputeDP(i, jmid + 1, jright, bestk, kright)
26
                                                                                                    i++, j++, b[i] = j;
27
   def ComputeFullDP:
                                                                                                }
28
     Initialize dp for i = 0 somehow
                                                                                        10
29
     for i in range(1, m):
                                                                                            void kmp(){
                                                                                        11
30
     ComputeDP(i, 0, n, 0, n)
                                                                                                int i=0, j=0;
                                                                                        12
31
                                                                                                while(i<sz(T)){</pre>
32
                                                                                        13
                                                                                                    while(j>=0 && T[i]!=P[j]) j=b[j];
33
  knuth: dp[i][j]=min{dp[i][k]+dp[k][j]}+C[i][j], i < k < j. Se debe cumplir: A[i_{15}]
                                                                                                    i++, j++;
       ,j-1] \le A[i,j] \le A[i+1,j]. Pasa de O(n^3) a O(n^2)
                                                                                                    if(j==sz(P)) printf("P_is_found_at_index_%d_in_T\n", i-j), j=b[j];
                                                                                        16
  Donde A[i][j] es el minimo k tal que dp[i][j] = dp[i][k]+dp[k][j] + C[i][j]
                                                                                                }
                                                                                        17
                                                                                        18 }
   Tambien es aplicable si:
  C[a][c] + C[b][d] \leftarrow C[a][d] + C[b][c] y C[b][c] \leftarrow C[a][d], a \leftarrow b \leftarrow c \leftarrow d
37
                                                                                                                                  Trie
38
   for (int s = 0; s <= k; s ++)
                                                                                            struct trie{
     for (int l = 0; l+s <= k; l++) {
                                                    //l - left point
40
                                                                                              map<char, trie> m;
                                                    //r - right point
       int r = 1 + s;
41
                                                                                              bool end=false;
       if (s < 2) {
42
                                                                                              void add(const string &s, int p=0){
       res[1][r] = 0;
                                                  //DP base - nothing to break
43
                                                                                                if(s[p]) m[s[p]].add(s, p+1);
                                               //A is equal to left border
       A[1][r] = 1;
44
                                                                                                else end=true;
       continue;
45
                                                                                              }
                                                                                              void dfs(){
       int aleft = A[1][r-1];
                                                 //Knuth's trick: getting bounds on
47
                                                                                                //Do stuff
                                                                                                forall(it, m)
       int aright = A[l+1][r];
48
                                                                                                  it->second.dfs();
                                                                                        11
       res[1][r] = INF;
49
       for (int a = max(l+1,aleft); a<=min(r-1,aright); a++) {
                                                                       //iterating for
50
```

```
Suffix Array (largo, nlogn)
                                                                                               if(phi[i]==-1) {PLCP[i]=0; continue;}
                                                                                               while(s[i+L]==s[phi[i]+L]) L++;
                                                                                       10
1 #define MAX_N 112345
                                                                                              PLCP[i]=L;
                                                                                       11
  |\#define \ rBOUND(x) \ ((x) < n ? \ r[(x)] : 0)
                                                                                              L=max(L-1, 0);
                                                                                       12
   //sa will hold the suffixes in order.
                                                                                       13
  int sa[MAX_N], r[MAX_N], n;//OJO n = s.size()!
                                                                                            forn(i, n) LCP[i]=PLCP[sa[i]];
                                                                                       14
  string s; //input string, n=s.size()
                                                                                       15 }
   int f[MAX_N], tmpsa[MAX_N];
                                                                                                                              Corasick
   void countingSort(int k){
     zero(f):
                                                                                         struct trie{
     forn(i, n) f[rBOUND(i+k)]++;
                                                                                            map<char, trie> next;
                                                                                            trie* tran[256]://transiciones del automata
     int sum=0:
     forn(i, max(255, n)){
                                                                                            int idhoja, szhoja;//id de la hoja o 0 si no lo es
       int t=f[i]; f[i]=sum; sum+=t;}
                                                                                            //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que es hoja
                                                                                            trie *padre, *link, *nxthoja;
     forn(i,n)
14
                                                                                             char pch;//caracter que conecta con padre
       tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];
15
    forn(i,n) sa[i] = tmpsa[i];
                                                                                            trie(): next(), tran(), idhoja(), szhoja(), padre(), link(),nxthoja(),pch()
16
                                                                                                 {}
17
   void constructsa(){\frac{1}{0} \text{ n}}
                                                                                             void insert(const string &s, int id=1, int p=0){//id>0!!!
18
     n = s.size();
                                                                                               if(p \le z(s)){
                                                                                       10
19
     forn(i,n) sa[i]=i, r[i]=s[i];
                                                                                                 trie &ch=next[s[p]];
20
                                                                                       11
     for(int k=1; k<n; k<<=1){</pre>
                                                                                                 tran[(int)s[p]]=&ch;
21
                                                                                                 ch.padre=this, ch.pch=s[p];
       countingSort(k), countingSort(0);
22
       int rank, tmpr[MAX_N];
                                                                                                 ch.insert(s, id, p+1);
                                                                                       14
23
       tmpr[sa[0]]=rank=0;
                                                                                               }
                                                                                       15
24
       forr(i, 1, n)
                                                                                               else idhoja=id, szhoja=sz(s);
25
         tmpr[sa[i]] = (r[sa[i]] == r[sa[i-1]]) & r[sa[i] + k] == r[sa[i-1] + k]) ? rank : 17
26
                                                                                            trie* get_link() {
              ++rank:
       forn(i,n) r[i]=tmpr[i];
                                                                                               if(!link){
27
                                                                                       19
       if(r[sa[n-1]]==n-1) break;
                                                                                                 if(!padre) link=this;//es la raiz
28
                                                                                       20
     }
                                                                                                 else if(!padre->padre) link=padre;//hijo de la raiz
29
                                                                                       21
                                                                                                 else link=padre->get_link()->get_tran(pch);
                                                                                       22
30
   void print(){//for debugging
                                                                                               }
31
                                                                                       23
     forn(i, n)
                                                                                               return link; }
                                                                                       24
32
       cout << i << ''' <<
                                                                                            trie* get_tran(int c) {
33
       s.substr(sa[i], s.find('$',sa[i])-sa[i]) << endl;}</pre>
                                                                                              if(!tran[c]) tran[c] = !padre? this : this->get_link()->get_tran(c);
34
                                                                                       26
                                                                                               return tran[c]; }
                                                                                       27
                       LCP (Longest Common Prefix)
                                                                                            trie *get_nxthoja(){
                                                                                       28
    /Calculates the LCP between consecutives suffixes in the Suffix Array.
                                                                                               if(!nxthoja) nxthoja = get_link()->idhoja? link : link->nxthoja;
   //LCP[i] is the length of the LCP between sa[i] and sa[i-1]
                                                                                               return nxthoja; }
int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
                                                                                             void print(int p){
                                                                                       31
  void computeLCP(){//O(n)
                                                                                              if(idhoja) cout << "found<sub>i</sub>" << idhoja << "<sub>||||</sub>at<sub>||||</sub>position<sub>i||</sub>" << p-szhoja <<
                                                                                       32
     phi[sa[0]]=-1;
                                                                                                   endl:
    forr(i, 1, n) phi[sa[i]]=sa[i-1];
                                                                                               if(get_nxthoja()) get_nxthoja()->print(p); }
                                                                                       33
                                                                                            void matching(const string &s, int p=0){
     int L=0:
                                                                                       34
                                                                                              print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
    forn(i, n){
```

```
36 |}tri;
                               Suffix Automaton
1 struct state {
     int len, link;
     map<char,int> next;
     state() { }
   const int MAXLEN = 10010;
7 | state st[MAXLEN*2];
  int sz, last;
   void sa_init() {
     forn(i,sz) st[i].next.clear();
     sz = last = 0;
     st[0].len = 0;
     st[0].link = -1;
     ++sz;
14
15
   // Es un DAG de una sola fuente y una sola hoja
   // cantidad de endpos = cantidad de apariciones = cantidad de caminos de la
       clase al nodo terminal
                                                                                    11 }
18 // cantidad de miembros de la clase = st[v].len-st[st[v].link].len (v>0) =
       caminos del inicio a la clase
19 // El arbol de los suffix links es el suffix tree de la cadena invertida. La
       string de la arista link(v)->v son los caracteres que difieren
   void sa extend (char c) {
     int cur = sz++;
21
     st[cur].len = st[last].len + 1;
     // en cur agregamos la posicion que estamos extendiendo
23
     //podria agregar tambien un identificador de las cadenas a las cuales
24
         pertenece (si hay varias)
25
     for (p=last; p!=-1 && !st[p].next.count(c); p=st[p].link) // modificar esta
26
         linea para hacer separadores unicos entre varias cadenas (c=='$')
       st[p].next[c] = cur;
27
     if (p == -1)
28
       st[cur].link = 0;
29
     else {
30
       int q = st[p].next[c];
31
       if (st[p].len + 1 == st[q].len)
32
         st[cur].link = q;
33
       else {
34
         int clone = sz++;
35
         // no le ponemos la posicion actual a clone sino indirectamente por el
36
             link de cur
         st[clone].len = st[p].len + 1;
```

```
st[clone].next = st[q].next;
38
         st[clone].link = st[q].link;
         for (; p!=-1 && st[p].next.count(c) && st[p].next[c]==q; p=st[p].link)
           st[p].next[c] = clone;
         st[q].link = st[cur].link = clone;
42
43
44
    last = cur;
                                   Z Function
   char s[MAXN];
   int z[MAXN]; // z[i] = i==0 ? 0 : max k tq s[0,k) match with s[i,i+k)
   void z_function(char s[],int z[]) {
       int n = strlen(s);
       forn(i, n) z[i]=0;
       for (int i = 1, l = 0, r = 0; i < n; ++i) {
           if (i \le r) z[i] = min (r - i + 1, z[i - 1]);
           while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) ++z[i];
           if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
       }
10
```

Geometria

Punto

```
const double EPS=1e-9;
   struct pto{
     double x, y;
     pto(double x=0, double y=0):x(x),y(y){}
     pto operator+(pto a){return pto(x+a.x, y+a.y);}
     pto operator-(pto a){return pto(x-a.x, y-a.y);}
     pto operator+(double a){return pto(x+a, y+a);}
     pto operator*(double a){return pto(x*a, y*a);}
     pto operator/(double a){return pto(x/a, y/a);}
     //dot product, producto interno:
     //Significado: a*b = a.norm * b.norm * cos(ang).
11
     double operator*(pto a){return x*a.x+y*a.y;}
     //module of the cross product or vectorial product:
     //if a is less than 180 clockwise from b, a^b>0. Significado: abs(a^b) = area
          del paralelogramo.
     double operator^(pto a){return x*a.y-y*a.x;}
     //returns true if this is at the left side of line gr
     bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
     bool operator<(const pto &a) const{return x<a.x-EPS || (abs(x-a.x)<EPS && y<a
         .y-EPS);}
```

```
bool operator==(pto a){return abs(x-a.x) < EPS && abs(y-a.y) < EPS;}
                                                                                      5 //pto MUST store float coordinates!
     double norm(){return sqrt(x*x+y*y);}
                                                                                          line(double a, double b, double c):a(a),b(b),c(c){}
20
     double norm_sq(){return x*x+y*y;}
                                                                                          line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
22 | };
   double dist(pto a, pto b){return (b-a).norm();}
  double dist_sq(pto a, pto b){return (b-a).norm_sq();}
   typedef pto vec;
26
   //positivo si aob estn en sentido antihorario con un ngulo <180
   double angle(pto a, pto o, pto b){ //devuelve radianes! (-pi,pi)
     pto oa=a-o, ob=b-o;
                                                                                     15 }
     return atan2(oa^ob, oa*ob);}
   //rotate p by theta rads CCW w.r.t. origin (0,0)
                                                                                      1 struct segm{
   pto rotate(pto p, double theta){
                                                                                          pto s,f;
     return pto(p.x*cos(theta)-p.y*sin(theta),
34
        p.x*sin(theta)+p.y*cos(theta));
35
36 }
                                                                                             if(12==0.) return s;
                            Orden radial de puntos
  struct Cmp{//orden total de puntos alrededor de un punto r
     pto r;
                                                                                             return s+((f-s)*t);
     Cmp(pto r):r(r) {}
                                                                                     10
     int cuad(const pto &a) const{
                                                                                     11
       if(a.x > 0 && a.y >= 0)return 0;
       if(a.x \le 0 \&\& a.y > 0)return 1;
                                                                                        };
                                                                                     13
       if(a.x < 0 && a.y <= 0)return 2;
       if(a.x >= 0 \&\& a.y < 0)return 3;
       assert(a.x ==0 && a.y==0);
       return -1;
                                                                                     17
     bool cmp(const pto&p1, const pto&p2)const{
       int c1 = cuad(p1), c2 = cuad(p2);
       if(c1==c2) return p1.y*p2.x<p1.x*p2.y;</pre>
                                                                                            return pto(INF, INF);
                                                                                     21
           else return c1 < c2;
                                                                                     22 }
15
     }
16
       bool operator()(const pto&p1, const pto&p2) const{
17
       return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
18
                                                                                        struct rect{
19
20 };
                                                                                          pto lw, up;
                                        Line
int sgn(ll x){return x<0? -1 : !!x;}</pre>
2 struct line
    line() {}
    double a,b,c;//Ax+By=C
                                                                                        //check case when only a edge is common
```

```
int side(pto p){return sgn(ll(a) * p.x + ll(b) * p.y - c);}
bool parallels(line 11, line 12){return abs(11.a*12.b-12.a*11.b)<EPS;}
pto inter(line 11, line 12){//intersection
  double det=11.a*12.b-12.a*11.b;
  if(abs(det) < EPS) return pto(INF, INF); //parallels</pre>
 return pto(12.b*11.c-11.b*12.c, 11.a*12.c-12.a*11.c)/det;
                                  Segment
  segm(pto s, pto f):s(s), f(f) {}
  pto closest(pto p) {//use for dist to point
     double 12 = dist_sq(s, f);
     double t = ((p-s)*(f-s))/12;
     if (t<0.) return s;//not write if is a line
     else if(t>1.)return f;//not write if is a line
  bool inside(pto p){return abs(dist(s, p)+dist(p, f)-dist(s, f))<EPS;}</pre>
//NOTA: Si los segmentos son colineales slo devuelve un punto de interseccin
pto inter(segm s1, segm s2){
    if(s1.inside(s2.s)) return s2.s; //Fix cuando son colineales
   if(s1.inside(s2.f)) return s2.f; //Fix cuando son colineales
    pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
    if(s1.inside(r) && s2.inside(r)) return r;
                                Rectangle
 //lower-left and upper-right corners
//returns if there's an intersection and stores it in r
bool inter(rect a, rect b, rect &r){
 r.lw=pto(max(a.lw.x, b.lw.x), max(a.lw.y, b.lw.y));
 r.up=pto(min(a.up.x, b.up.x), min(a.up.y, b.up.y));
```

```
return r.lw.x<r.up.x && r.lw.y<r.up.y;
                                                                                     31 #define sqr(a) ((a)*(a))
                                                                                        #define feq(a,b) (fabs((a)-(b))<EPS)</pre>
11 | }
                                                                                        pair<tipo, tipo > ecCuad(tipo a, tipo b, tipo c){//a*x*x+b*x+c=0
                                  Polygon Area
                                                                                           tipo dx = sqrt(b*b-4.0*a*c);
                                                                                          return make_pair((-b + dx)/(2.0*a), (-b - dx)/(2.0*a));
double area(vector<pto> &p){//O(sz(p))
                                                                                     36
     double area=0;
                                                                                         pair<pto, pto> interCL(Circle c, line 1){
     forn(i, sz(p)) area+=p[i]^p[(i+1)%z(p)];
                                                                                          bool sw=false;
     //if points are in clockwise order then area is negative
                                                                                          if((sw=feq(0,1.b))){
     return abs(area)/2:
                                                                                           swap(1.a, 1.b);
                                                                                           swap(c.o.x, c.o.y);
   //Area ellipse = M_PI*a*b where a and b are the semi axis lengths
                                                                                     41
   //Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
                                                                                           pair<tipo, tipo> rc = ecCuad(
_{9} //o mejor area tringulo = abs(x0 * (y1 - y2) + x1 * (y2 - y0) + x2 * (y0 - y1)
                                                                                           sqr(l.a)+sqr(l.b),
       ) / 2;
                                                                                          2.0*1.a*1.b*c.o.y-2.0*(sqr(1.b)*c.o.x+1.c*1.a),
                                       Circle
                                                                                           sqr(1.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(1.c)-2.0*1.c*1.b*c.o.y
                                                                                     47
  vec perp(vec v){return vec(-v.y, v.x);}
                                                                                           pair<pto, pto> p( pto(rc.first, (l.c - l.a * rc.first) / l.b),
                                                                                     48
line bisector(pto x, pto y){
                                                                                                     pto(rc.second, (1.c - 1.a * rc.second) / 1.b) );
                                                                                     49
    line l=line(x, y); pto m=(x+y)/2;
                                                                                           if(sw){
                                                                                     50
     return line(-1.b, 1.a, -1.b*m.x+1.a*m.y);
                                                                                           swap(p.first.x, p.first.y);
                                                                                     51
                                                                                           swap(p.second.x, p.second.y);
                                                                                     52
  struct Circle{
                                                                                     53
     pto o;
                                                                                          return p;
                                                                                     54
     double r;
                                                                                     55
     Circle(pto x, pto y, pto z){
                                                                                         pair<pto, pto> interCC(Circle c1, Circle c2){
       o=inter(bisector(x, y), bisector(y, z));
                                                                                          line 1:
                                                                                     57
       r=dist(o, x);
11
                                                                                          1.a = c1.o.x-c2.o.x;
     }
12
                                                                                          1.b = c1.o.v-c2.o.v;
     pair<pto, pto> ptosTang(pto p){
13
                                                                                          1.c = (sqr(c2.r) - sqr(c1.r) + sqr(c1.o.x) - sqr(c2.o.x) + sqr(c1.o.y)
       pto m=(p+o)/2;
14
                                                                                          -sqr(c2.o.y))/2.0;
       tipo d=dist(o, m);
15
                                                                                          return interCL(c1, 1);
       tipo a=r*r/(2*d);
16
                                                                                     63 | }
       tipo h=sqrt(r*r-a*a);
17
       pto m2=o+(m-o)*a/d;
                                                                                                                        Point in Poly
18
       vec per=perp(m-o)/d;
19
       return make_pair(m2-per*h, m2+per*h);
                                                                                       //checks if v is inside of P, using ray casting
20
     }
                                                                                         //works with convex and concave.
^{21}
                                                                                        bool inPolygon(pto v, vector<pto>& P) {
22
                                                                                          bool c = false;
   //finds the center of the circle containing p1 and p2 with radius r
                                                                                          forn(i, sz(P)){
   //as there may be two solutions swap p1, p2 to get the other
   bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
                                                                                            int j=(i+1) %z(P);
25
           double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
26
           if(det<0) return false;</pre>
                                                                                             segm lado(P[i],P[j]);
27
           c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
                                                                                             if(lado.inside(v)) return true; //0JO: return true: incluye lados. return
28
           return true:
                                                                                                 false: excluye lados.
29
                                                                                     10
```

1 //stores convex hull of P in S, CCW order

//left must return >=0 to delete collinear points!

```
if((P[i].y > v.y) != (P[i].y > v.y) &&
11
       (v.x < (P[i].x-P[j].x) * (v.y-P[j].y) / (P[i].y-P[j].y) + P[j].x))
12
     }
     return c;
15
16 }
                         Point in Convex Poly log(n)
   void normalize(vector<pto> &pt){//delete collinear points first!
     //this makes it clockwise:
       if(pt[2].left(pt[0], pt[1])) reverse(pt.begin(), pt.end());
     int n=sz(pt), pi=0;
     forn(i, n)
       if(pt[i].x<pt[pi].x || (pt[i].x==pt[pi].x && pt[i].y<pt[pi].y))</pre>
     vector<pto> shift(n);//puts pi as first point
       forn(i, n) shift[i]=pt[(pi+i) %n];
       pt.swap(shift);
10
11
^{12}
   /* left debe decir >0 para que considere los bordes. Ojo que Convex Hull
       necesita que left diga >= 0 para limpiar los colineales, hacer otro left
14
       si hace falta */
   bool inPolygon(pto p, const vector<pto> &pt){
     //call normalize first!
     if(p.left(pt[0], pt[1]) || p.left(pt[sz(pt)-1], pt[0])) return false;
     int a=1, b=sz(pt)-1;
19
     while(b-a>1){
20
       int c=(a+b)/2;
21
       if(!p.left(pt[0], pt[c])) a=c;
       else b=c:
     }
     return !p.left(pt[a], pt[a+1]);
26 | }
                            Convex Check CHECK
| bool isConvex(vector<int> &p){//O(N), delete collinear points!
     int N=sz(p);
     if(N<3) return false;
     bool isLeft=p[0].left(p[1], p[2]);
     forr(i, 1, N)
       if(p[i].left(p[(i+1) N], p[(i+2) N])!=isLeft)
         return false;
     return true; }
```

Convex Hull

```
void CH(vector<pto>& P, vector<pto> &S){
     S.clear():
     sort(P.begin(), P.end());//first x, then y
     forn(i, sz(P)){//lower hull
       while(sz(S) \ge 2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
       S.pb(P[i]);
     S.pop_back();
10
     int k=sz(S);
11
     dforn(i, sz(P)){//upper hull
       while(sz(S) \ge k+2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
13
       S.pb(P[i]);
15
     S.pop_back();
17 }
                                   Cut Polygon
  //cuts polygon Q along the line ab
   //stores the left side (swap a, b for the right one) in P
   void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
     P.clear();
     forn(i, sz(Q)){
       double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1) \%z(Q)]-a);
       if(left1>=0) P.pb(Q[i]);
       if(left1*left2<0)</pre>
         P.pb(inter(line(Q[i], Q[(i+1) \%z(Q)]), line(a, b)));
10
11 }
                                    Bresenham
   //plot a line approximation in a 2d map
   void bresenham(pto a, pto b){
     pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
     pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
     int err=d.x-d.y;
     while(1){
       m[a.x][a.y]=1;//plot
       if(a==b) break;
       int e2=err:
       if(e2 >= 0) err-=2*d.y, a.x+=s.x;
       if(e2 <= 0) err+= 2*d.x, a.y+= s.y;
11
12
13 }
```

23

Rotate Matrix

```
//rotates matrix t 90 degrees clockwise
//using auxiliary matrix t2(faster)
void rotate(){
forn(x, n) forn(y, n)
t2[n-y-1][x]=t[x][y];
memcpy(t, t2, sizeof(t));
}
```

Math

Identidades

```
\sum_{i=0}^{n} \binom{n}{i} = 2^{n}
\sum_{i=0}^{n} i \binom{n}{i} = n * 2^{n-1}
\sum_{i=m}^{n} i = \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2}
\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}
\sum_{i=0}^{n} i^{2} = \frac{n(n+1)(2n+1)}{2} = \frac{n^{3}}{3} + \frac{n^{2}}{2} + \frac{n}{6}
\sum_{i=0}^{n} i(i-1) = \frac{8}{6} (\frac{n}{2})(\frac{n}{2} + 1)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par}
\sum_{i=0}^{n} i^{3} = \left(\frac{n(n+1)}{2}\right)^{2} = \frac{n^{4}}{4} + \frac{n^{3}}{2} + \frac{n^{2}}{4} = \left[\sum_{i=1}^{n} i\right]^{2}
\sum_{i=0}^{n} i^{4} = \frac{n(n+1)(2n+1)(3n^{2}+3n-1)}{30} = \frac{n^{5}}{5} + \frac{n^{4}}{2} + \frac{n^{3}}{3} - \frac{n}{30}
\sum_{i=0}^{n} i^{9} = \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_{k}}{p-k+1} \binom{p}{k} (n+1)^{p-k+1}
\sum_{i=0}^{n} a^{i} = \frac{a^{(n+1)-1}}{a-1} slosia! = 1
r = e - v + k + 1
Teorema de Pick: (Area, puntos interiores y puntos en el borde)
A = I + \frac{B}{2} - 1
```

Ec. Caracteristica

```
\begin{array}{l} a_0T(n) + a_1T(n-1) + \ldots + a_kT(n-k) = 0 \\ p(x) = a_0x^k + a_1x^{k-1} + \ldots + a_k \\ \text{Sean } r_1, r_2, \ldots, r_q \text{ las races distintas, de mult. } m_1, m_2, \ldots, m_q \\ T(n) = \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij} n^j r_i^n \\ \text{Las constantes } c_{ij} \text{ se determinan por los casos base.} \end{array}
```

Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
   comb[i][0]=comb[i][i]=1;
   forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1]) MOD;
}
ll lucas (ll n, ll k, int p){ //Calcula (n,k) %p teniendo comb[p][p]
        precalculado.
ll aux = 1;
while (n + k) aux = (aux * comb[n%p][k%p]) %p, n/=p, k/=p;
   return aux;
}
```

```
Log. Discreto
  // IDEA: a^x=b mod MOD <=> x = i*sqrt(MOD)+j con i, j <= sqrt(MOD)=m</pre>
   // entonces guardo todos los a^j: T[a^j mod MOD]=j
_3 // y despus busco si vi T[b/(a^(i*m) mod MOD] = T[b*a^-(i*m) mod MOD], return
                  Exp. de Matrices y Fibonacci en log(n)
   #define SIZE 350
   int NN;
   double tmp[SIZE] [SIZE];
   void mul(double a[SIZE][SIZE], double b[SIZE][SIZE]){ zero(tmp);
       forn(i, NN) forn(j, NN) forn(k, NN) tmp[i][j]+=a[i][k]*b[k][j];
       forn(i, NN) forn(j, NN) a[i][j]=tmp[i][j];
   void powmat(double a[SIZE] [SIZE], int n, double res[SIZE] [SIZE]){
       forn(i, NN) forn(j, NN) res[i][j]=(i==j);
       while(n){
10
           if(n&1) mul(res, a), n--;
11
           else mul(a, a), n/=2;
12
       } }
13
                       Matrices y determinante O(n^3)
   struct Mat {
       vector<vector<double> > vec;
       Mat(int n): vec(n, vector<double>(n) ) {}
       Mat(int n, int m): vec(n, vector<double>(m) ) {}
       vector<double> &operator[](int f){return vec[f];}
       const vector<double> &operator[](int f) const {return vec[f];}
       int size() const {return sz(vec);}
       Mat operator+(Mat &b) { ///this de n x m entonces b de n x m
           Mat m(sz(b), sz(b[0]));
           forn(i,sz(vec)) forn(j,sz(vec[0])) m[i][j] = vec[i][j] + b[i][j];
10
           return m;
11
       Mat operator*(const Mat &b) { ///this de n x m entonces b de m x t
12
           int n = sz(vec), m = sz(vec[0]), t = sz(b[0]);
13
           Mat mat(n,t);
14
           forn(i,n) forn(j,t) forn(k,m) mat[i][j] += vec[i][k] * b[k][j];
15
           return mat;
16
       double determinant(){//sacado de e maxx ru
17
           double det = 1;
18
           int n = sz(vec);
19
           Mat m(*this);
20
           forn(i, n){//para cada columna
21
               int k = i:
22
```

forr(j, i+1, n)//busco la fila con mayor val abs

```
if(abs(m[j][i])>abs(m[k][i])) k = j;
if(abs(m[k][i])<1e-9) return 0;
m[i].swap(m[k]);//la swapeo
if(i!=k) det = -det;
det *= m[i][i];
forr(j, i+1, n) m[i][j] /= m[i][i];
//hago 0 todas las otras filas
forn(j, n) if (j!= i && abs(m[j][i])>1e-9)
forr(k, i+1, n) m[j][k]-=m[i][k]*m[j][i];
}
return det;
}
return det;
}
```

Teorema Chino del Resto

$$y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)$$

Criba

```
#define MAXP 100000 //no necesariamente primo
1 int criba[MAXP+1];
  void crearcriba(){
     int w[] = \{4,2,4,2,4,6,2,6\};
    for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
     for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
     for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
     for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])</pre>
       for(int j=p*p; j<=MAXP; j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
10
   vector<int> primos;
   void buscarprimos(){
     crearcriba();
     forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
15
  //^{\infty} Useful for bit trick: #define SET(i) ( criba[(i)>>5]|=1<<((i)&31) ), #
       define INDEX(i) ( (criba[i>>5]>>((i)&31))&1 ), unsigned int criba[MAXP
       /32+1];
```

Funciones de primos

Sea $n = \prod p_i^{k_i}$, fact(n) genera un map donde a cada p_i le asocia su k_i

```
//factoriza bien numeros hasta MAXP^2
map<ll,ll> fact(ll n){ //0 (cant primos)
map<ll,ll> ret;
forall(p, primos){
while(!(n%p)){
```

```
ret[*p]++;//divisor found
         n/=*p;
       }
     if(n>1) ret[n]++;
     return ret;
12
    //factoriza bien numeros hasta MAXP
   map<11,11> fact2(11 n){ //0 (1g n)}
     map<ll,ll> ret;
     while (criba[n]){
       ret[criba[n]]++;
17
       n/=criba[n];
18
     if(n>1) ret[n]++;
     return ret;
22
   //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
   void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::iterator it,
       11 n=1){
       if(it==f.begin()) divs.clear();
25
       if(it==f.end()) { divs.pb(n); return; }
       ll p=it->fst, k=it->snd; ++it;
27
       forn(_, k+1) divisores(f, divs, it, n), n*=p;
28
29
   ll sumDiv (ll n){
30
     ll rta = 1;
     map<ll,ll> f=fact(n);
     forall(it, f) {
     11 pot = 1, aux = 0;
     forn(i, it->snd+1) aux += pot, pot *= it->fst;
     rta*=aux;
37
     return rta;
38
39
   11 eulerPhi (11 n){ // con criba: O(lg n)
     11 \text{ rta} = n:
     map<ll,ll> f=fact(n);
     forall(it, f) rta -= rta / it->first;
     return rta;
45
   11 eulerPhi2 (11 n){ // 0 (sqrt n)
     11 r = n;
     forr (i,2,n+1){
       if ((11)i*i > n) break;
       if (n \% i == 0){
```

```
while (n\%i == 0) n/=i:
                                                                                           if (n == a) return true;
         r = r/i; }
                                                                                           11 s = 0, d = n-1;
     }
                                                                                           while (d \% 2 == 0) s++, d/=2;
     if (n != 1) r= r/n:
     return r;
                                                                                           11 x = expmod(a,d,n);
                                                                                           if ((x == 1) \mid | (x+1 == n)) return true;
56 | }
                   Test de primalidad naive O(\operatorname{sqrt}(n)/6)
                                                                                           forn (i, s-1){
                                                                                             x = mulmod(x, x, n);
int __attribute__((const)) is_prime(long long n)
                                                                                             if (x == 1) return false;
                                                                                             if (x+1 == n) return true;
     if (n <= 1)
                                                                                      31
                                                                                      32
       return 0:
                                                                                           return false;
     else if (n \le 3)
                                                                                      33
                                                                                      34
       return 1:
     else if (!(n %2) || !(n %3))
                                                                                         bool rabin (ll n){ //devuelve true si n es primo
       return 0:
                                                                                           if (n == 1) return false;
                                                                                      37
                                                                                            const int ar[] = \{2,3,5,7,11,13,17,19,23\};
                                                                                      38
     long long cap = sqrt(n) + 1;
10
                                                                                           forn (i.9)
     for (long long int i = 5; i \le cap; i += 6)
                                                                                      39
11
                                                                                             if (!es_primo_prob(n,ar[j]))
       if (!(n%i) || !(n%(i+2)))
^{12}
                                                                                               return false;
                                                                                      41
         return 0;
13
                                                                                           return true;
                                                                                      42
14
                                                                                      43
     return 1;
15
                                                                                      44
16 }
                                                                                         ll rho(ll n){
                           Phollard's Rho (rolando)
                                                                                             if( (n & 1) == 0 ) return 2;
                                                                                             11 x = 2, y = 2, d = 1;
1 | ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}
                                                                                             ll c = rand() % n + 1;
                                                                                      48
                                                                                             while(d == 1){
                                                                                      49
3 | 11 mulmod (11 a, 11 b, 11 c) { //returns (a*b) %, and minimize overfloor
                                                                                                 x = (mulmod(x, x, n) + c) n;
     11 x = 0, y = a\%;
                                                                                                 y = (mulmod(y, y, n) + c) n;
     while (b > 0){
                                                                                                 y = (mulmod(y, y, n) + c) n;
                                                                                      52
       if (b \% 2 == 1) x = (x+y) \% c;
                                                                                                 if(x - y >= 0) d = gcd(x - y, n);
                                                                                      53
       y = (y*2) \% c;
                                                                                                  else d = gcd(y - x, n);
                                                                                      54
       b /= 2;
                                                                                      55
                                                                                             return d==n? rho(n):d;
                                                                                      56
     return x % c;
10
                                                                                      57
11
^{12}
                                                                                         map<ll,ll> prim;
   ll expmod (ll b, ll e, ll m){\frac{1}{0}} \log b
                                                                                         void factRho (ll n){ //O (lg n)^3. un solo numero
     if(!e) return 1;
                                                                                           if (n == 1) return;
     11 q= expmod(b,e/2,m); q=mulmod(q,q,m);
                                                                                           if (rabin(n)){
     return e %2? mulmod(b,q,m) : q;
16
                                                                                             prim[n]++;
17
                                                                                             return;
19 bool es_primo_prob (ll n, int a)
                                                                                           11 factor = rho(n);
```

```
factRho(factor);
                                                                                    17 | struct frac{
     factRho(n/factor);
                                                                                          tipo p,q;
69 }
                                                                                         frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
                                                                                          void norm(){
                                       GCD
                                                                                            tipo a = mcd(p,q);
                                                                                           if(a) p/=a, q/=a;
tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
                                                                                           else q=1;
                                Extended Euclid
                                                                                           if (q<0) q=-q, p=-p;}
                                                                                         frac operator+(const frac% o){
void extendedEuclid (ll a, ll b) \{ //a * x + b * y = d \}
                                                                                            tipo a = mcd(q, o.q);
                                                                                    26
    if (!b) { x = 1; y = 0; d = a; return;}
                                                                                           return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
                                                                                    27
     extendedEuclid (b, a%);
                                                                                          frac operator-(const frac& o){
                                                                                    28
    11 x1 = v;
                                                                                            tipo a = mcd(q, o.q);
                                                                                    29
    11 y1 = x - (a/b) * y;
                                                                                           return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
    x = x1; y = y1;
                                                                                         frac operator*(frac o){
                                                                                            tipo a = mcd(q,o.p), b = mcd(o.q,p);
                                                                                    32
                                                                                           return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
                                      LCM
                                                                                    33
                                                                                         frac operator/(frac o){
                                                                                    34
1 | tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
                                                                                           tipo a = mcd(q,o.q), b = mcd(o.p,p);
                                                                                    35
                                                                                           return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
                                                                                    36
                                     Simpson
                                                                                         bool operator<(const frac &o) const{return p*o.q < o.p*q;}//usar comp cuando
                                                                                    37
                                                                                              el producto puede dar overflow
  double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
                                                                                         bool operator==(frac o){return p==o.p&&q==o.q;}
     double area=0, h=(b-a)/n, fa=f(a), fb;
                                                                                    38
                                                                                    39 };
    forn(i, n){
      fb=f(a+h*(i+1));
                                                                                                                        Polinomio
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
    }
                                                                                     struct poly {
    return area*h/6.;}
                                                                                            vector<tipo> c;//guarda los coeficientes del polinomio
                                                                                            poly(const vector<tipo> &c): c(c) {}
                                     Fraction
                                                                                           poly() {}
1 | bool comp(tipo a, tipo b, tipo c, tipo d){\frac{1}{a*d}} < b*c
                                                                                           void simplify(){
       int s1 = signo(a)*signo(d), s2 = signo(b)*signo(c);
                                                                                            int i = 0;
       if(s1 == 0) return s2 > 0;
                                                                                           /*tipo a0=0;
                                                                                           while(a0 == 0 && i < sz(c)) a0 = c[i], i++;*/
      if(s2 == 0) return s1 < 0;
       if(s1 > 0 and s2 < 0) return false;
                                                                                           int j = sz(c)-1;
       if(s1 < 0 and s2 > 0) return true;
                                                                                            tipo an=0;
      if(a / b != c / d) return a/b < c/d; //asume que b y d son positivos
                                                                                           while(an == 0 && j >=i) an = c[j], j--;
      a %= b, c %= d;
                                                                                           vector<tipo> d;
                                                                                    12
                                                                                           forr(k,i,j) d.pb(c[k]);
      /*O(1) pero con double:
                                                                                    13
      long double d1 = ((long double)(a))/(b), d2 = ((long double)(c))/(d);
                                                                                    14
                                                                                            c=d;
      return d1 + EPS < d2;
                                                                                    15
11
       */
                                                                                          bool isnull() { simplify(); return c.empty();}
                                                                                    16
12
      return comp(d, c, b, a);
                                                                                           poly operator+(const poly &o) const {
13
                                                                                    17
                                                                                               int m = sz(c), n = sz(o.c);
14 | }
                                                                                    18
                                                                                                vector<tipo> res(max(m,n));
                                                                                    19
16 | tipo mcd(tipo a, tipo b) { return a ? mcd(b\( a, a \) : b; }
                                                                                                forn(i, m) res[i] += c[i];
```

```
forn(i, n) res[i] += o.c[i];
                                                                                         poly result(b);
21
                                                                                         return make_pair(result,resto);
           return poly(res); }
22
      poly operator*(const tipo cons) const {
23
      vector<tipo> res(sz(c));
                                                                                       poly interpolate(const vector<tipo>& x,const vector<tipo>& y) { //O(n^2)
           forn(i, sz(c)) res[i]=c[i]*cons;
                                                                                           poly A; A.c.pb(1);
                                                                                           forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux; } // A
           return poly(res); }
26
       poly operator*(const poly &o) const {
                                                                                                = (x-x0) * ... * (x-xn)
27
           int m = sz(c), n = sz(o.c);
                                                                                         poly S; S.c.pb(0);
28
           vector<tipo> res(m+n-1);
                                                                                         forn(i,sz(x)) { poly Li;
29
           forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
                                                                                           Li = ruffini(A,x[i]).fst;
30
           return poly(res); }
                                                                                           Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the coefficients
31
     tipo eval(tipo v) {
                                                                                                 instead of 1.0 to avoid using double -- si se usa mod usar el inverso
32
       tipo sum = 0;
33
       dforn(i, sz(c)) sum=sum*v + c[i];
                                                                                           S = S + Li * y[i]; }
34
      return sum: }
                                                                                         return S;
35
      //poly contains only a vector<int> c (the coeficients)
                                                                                    76 }
     //the following function generates the roots of the polynomial
37
                                                                                                                       Ec. Lineales
    /it can be easily modified to return float roots
38
     set<tipo> roots(){
39
                                                                                      | bool resolver_ev(Mat a, Vec y, Vec &x, Mat &ev){
       set<tipo> roots;
40
                                                                                         int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
       simplify();
41
                                                                                         vector<int> p; forn(i,m) p.push_back(i);
       if(c[0]) roots.insert(0);
42
                                                                                         forn(i, rw) {
       int i = 0:
43
                                                                                           int uc=i, uf=i;
       tipo a0=0;
44
                                                                                           forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;uc=c;}
       while(a0 == 0 && i < sz(c)) a0 = abs(c[i]), i++;
45
                                                                                           if (feg(a[uf][uc], 0)) { rw = i; break; }
       tipo an = abs(c[sz(c)-1]);
46
                                                                                           forn(j, n) swap(a[j][i], a[j][uc]);
       vector<tipo> ps,qs;
47
                                                                                           swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
      forr(p,1,sqrt(a0)+1) if (a0%p==0) ps.pb(p),ps.pb(a0/p);
48
                                                                                           tipo inv = 1 / a[i][i]; //aca divide
      forr(q,1,sqrt(an)+1) if (an)(q==0) qs.pb(q),qs.pb(an/q);
49
                                                                                           forr(j, i+1, n) {
       forall(pt,ps)
50
                                                                                             tipo v = a[j][i] * inv;
         forall(qt,qs) if ( (*pt) % (*qt)==0 ) { //sacar esto para obtener todas
51
                                                                                             forr(k, i, m) a[j][k]-=v * a[i][k];
             las raices racionales
                                                                                             y[j] -= v*y[i];
                                                                                    14
           tipo root = abs((*pt) / (*qt));
52
                                                                                           }
                                                                                    15
           if (eval(root)==0) roots.insert(root);
53
                                                                                         } // rw = rango(a), aca la matriz esta triangulada
           if (eval((-1)*root)==0) roots.insert((-1)*root);// las raices tambien
54
                                                                                         forr(i, rw, n) if (!feq(y[i],0)) return false; // checkeo de compatibilidad
               pueden ser negativas!
                                                                                         x = vector < tipo > (m, 0);
55
                                                                                         dforn(i, rw){
                                                                                    19
      return roots: }
56
                                                                                           tipo s = v[i];
                                                                                           forr(j, i+1, rw) s -= a[i][j]*x[p[j]];
  pair<poly, tipo > ruffini(const poly p, tipo r) { //divive el polinomio p por (x
                                                                                           x[p[i]] = s / a[i][i]; //aca divide
       -r)
     int n = sz(p.c) - 1;
                                                                                         ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
     vector<tipo> b(n);
                                                                                         forn(k, m-rw) {
     b[n-1] = p.c[n];
                                                                                           ev[k][p[k+rw]] = 1;
    dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
                                                                                           dforn(i, rw){
                                                                                    27
     tipo resto = p.c[0] + r*b[0];
                                                                                              tipo s = -a[i][k+rw];
```

}}

37

```
forr(j, i+1, rw) s -= a[i][j]*ev[k][p[j]];
                                                                                     38 //multiplica vectores en nlgn
29
         ev[k][p[i]] = s / a[i][i]; //aca divide
                                                                                        inline static void multiply(const vector<int> &a, const vector<int> &b, vector<
30
       }
                                                                                             int> &res) {
     }
                                                                                          vector<base> fa (a.begin(), a.end()), fb (b.begin(), b.end());
32
                                                                                            int n=1; while(n < \max(sz(a), sz(b))) n <<= 1; n <<= 1;
     return true;
33
                                                                                             calc_rev(n);
                                                                                          fa.resize (n), fb.resize (n);
                                       \mathbf{FFT}
                                                                                          fft (&fa[0], n, false), fft (&fb[0], n, false);
                                                                                          forn(i, n) fa[i] = fa[i] * fb[i];
1 //~ typedef complex<double> base; //menos codigo, pero mas lento
                                                                                          fft (&fa[0], n, true);
2 //elegir si usar complejos de c (lento) o estos
                                                                                          res.resize(n);
                                                                                     47
3 | struct base{
                                                                                            forn(i, n) res[i] = int (fa[i].real() + 0.5); }
       double r.i:
                                                                                         void toPoly(const string &s, vector<int> &P){//convierte un numero a polinomio
       base(double r=0, double i=0):r(r), i(i){}
                                                                                             P.clear();
       double real()const{return r:}
                                                                                             dforn(i, sz(s)) P.pb(s[i]-'0');}
       void operator/=(const int c){r/=c, i/=c;}
  |};
                                                                                                                           Grafos
  base operator*(const base &a, const base &b){
       return base(a.r*b.r-a.i*b.i, a.r*b.i+a.i*b.r);}
                                                                                                                           Dijkstra
  base operator+(const base &a, const base &b){
11
       return base(a.r+b.r, a.i+b.i);}
12
                                                                                       #define INF 1e9
  base operator-(const base &a, const base &b){
13
                                                                                        int N;
       return base(a.r-b.r, a.i-b.i);}
                                                                                         #define MAX V 250001
   vector<int> rev; vector<base> wlen_pw;
                                                                                         vector<ii>> G[MAX V]:
   inline static void fft(base a[], int n, bool invert) {
                                                                                         //To add an edge use
       forn(i, n) if(i<rev[i]) swap(a[i], a[rev[i]]);</pre>
17
                                                                                         #define add(a, b, w) G[a].pb(make_pair(w, b))
     for (int len=2; len<=n; len<<=1) {
18
                                                                                         ll dijkstra(int s, int t){\frac{}{|0(|E| \log |V|)}}
       double ang = 2*M_PI/len * (invert?-1:+1);
19
                                                                                          priority_queue<ii, vector<ii>, greater<ii> > Q;
       int len2 = len >> 1;
20
                                                                                          vector<ll> dist(N, INF); vector<int> dad(N, -1);
       base wlen (cos(ang), sin(ang));
21
                                                                                           Q.push(make_pair(0, s)); dist[s] = 0;
       wlen_pw[0] = base(1, 0);
22
                                                                                           while(sz(Q)){
                                                                                     11
           forr(i, 1, len2) wlen_pw[i] = wlen_pw[i-1] * wlen;
23
                                                                                             ii p = Q.top(); Q.pop();
                                                                                     12
       for (int i=0; i<n; i+=len) {
24
                                                                                             if(p.snd == t) break;
         base t, *pu = a+i, *pv = a+i+len2, *pu_end = a+i+len2, *pw = &wlen_pw
25
                                                                                            forall(it, G[p.snd])
                                                                                     14
              [0];
                                                                                               if(dist[p.snd]+it->first < dist[it->snd]){
                                                                                     15
         for (; pu!=pu_end; ++pu, ++pv, ++pw)
26
                                                                                                 dist[it->snd] = dist[p.snd] + it->fst;
                                                                                     16
           t = *pv * *pw, *pv = *pu - t,*pu = *pu + t;
27
                                                                                                 dad[it->snd] = p.snd;
                                                                                     17
28
                                                                                                 Q.push(make_pair(dist[it->snd], it->snd)); }
                                                                                     18
     }
29
                                                                                     19
     if (invert) forn(i, n) a[i]/= n;}
30
                                                                                          return dist[t];
   inline static void calc_rev(int n){//precalculo: llamar antes de fft!!
                                                                                          if(dist[t]<INF)//path generator</pre>
       wlen_pw.resize(n), rev.resize(n);
32
                                                                                             for(int i=t; i!=-1; i=dad[i])
                                                                                     22
       int lg=31-__builtin_clz(n);
33
                                                                                               printf("%%", i, (i==s?'\n':'\_'));}
       forn(i, n){
34
       rev[i] = 0;
                                                                                                                        Bellman-Ford
35
           forn(k, lg) if(i&(1<< k)) rev[i]|=1<<(lg-1-k);
                                                                                      1 #define INF 1e9
```

struct Ar{int a,b,w;}; //w y cost deberian tener el mismo tipo
bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}

7 | vector<Ar> E:

```
s | 11 kruskal(){ //no hace falta agregar las aristas en las dos direcciones! (en
2 #define MAX_N 1001
3 vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
                                                                                            prim si)
4 //To add an edge use
                                                                                            11 cost=0;
5 | #define add(a, b, w) G[a].pb(make_pair(w, b))
                                                                                            sort(E.begin(), E.end());//ordenar aristas de menor a mayor -- OJO cuando
6 | int dist[MAX_N];
                                                                                                ordena algo no necesariamente las cosas del mismo valor quedan en el
  int N; //cantidad de vertices -- setear!!
                                                                                                mismo orden!!
   void bford(int src){//O(VE)
                                                                                            uf.init(n);
                                                                                    11
     memset(dist,INF,sizeof dist);
                                                                                            forall(it, E){
                                                                                    12
     dist[src]=0;
                                                                                                if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
10
                                                                                    13
     forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                                    uf.join(it->a, it->b);//conectar
11
                                                                                    14
       dist[it->snd]=min(dist[it->snd], dist[j]+it->fst);
                                                                                                    cost+=it->w;
12
                                                                                    15
                                                                                                }
13
                                                                                    16
                                                                                    17
14
   bool hasNegCycle(){
                                                                                            return cost;
                                                                                     18
    forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                    19 }
16
       if(dist[it->snd]>dist[j]+it->fst) return true;
17
                                                                                                                            Prim
     //inside if: all points reachable from it->snd will have -INF distance(do bfs
18
         ) ?
                                                                                      vector<ii> G[MAXN];
     return false;
19
                                                                                        bool taken[MAXN];
20 | }
                                                                                        priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
                                                                                        void process(int v){
                                 Floyd-Warshall
                                                                                            taken[v]=true;
                                                                                            forall(e, G[v])
1 //G[i][j] contains weight of edge (i, j) or INF
                                                                                                if(!taken[e->second]) pq.push(*e);
2 //G[i][i]=0
3 int G[MAX_N][MAX_N];
  void floyd(){//0(N^3)}
5 | forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
                                                                                        11 prim(){
     G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
                                                                                            zero(taken);
                                                                                    11
                                                                                            process(0);
  |bool inNegCycle(int v){
                                                                                            11 cost=0;
     return G[v][v]<0:}
                                                                                            while(sz(pq)){
   //checks if there's a neg. cycle in path from a to b
                                                                                                ii e=pq.top(); pq.pop();
   bool hasNegCycle(int a, int b){
                                                                                                if(!taken[e.second]) cost+=e.first, process(e.second);
                                                                                     16
    forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
                                                                                            }
                                                                                    17
       return true;
                                                                                            return cost;
                                                                                     18
                                                                                     19 }
     return false;
14
15 | }
                                                                                                                  2-SAT + Tarjan SCC
                                     Kruskal
                                                                                     1 //We have a vertex representing a var and other for his negation.
                                                                                      //Every edge stored in G represents an implication. To add an equation of the
1 const int MAXN=100000;
                                                                                            form a||b, use addor(a, b)
vector<ii> G[MAXN];
3 | int n;
                                                                                       //MAX=max cant var, n=cant var
```

#define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))

//lw[i]=lowest index(closer from the root) reachable from i

vector<int> G[MAX*2];

//idx[i]=index assigned in the dfs

void addEdge(int u, int v) {

```
G[u].pb(sz(e)), G[v].pb(sz(e));
8 int lw[MAX*2], idx[MAX*2], qidx;
   stack<int> q;
                                                                                              e.pb((edge)\{u,v,-1,false\});
  int qcmp, cmp[MAX*2];
                                                                                         13
   //verdad[cmp[i]]=valor de la variable i
                                                                                            //V[i]=id de la dfs
   bool verdad[MAX*2+1];
                                                                                            //L[i]=lowest id reachable from i
                                                                                            int V[MAXN], L[MAXN], qV;
   int neg(int x) { return x>=n? x-n : x+n;}
                                                                                            int nbc;//cant componentes
                                                                                            int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
   void tjn(int v){
     lw[v]=idx[v]=++qidx;
                                                                                            void initDfs(int n) {
     q.push(v), cmp[v]=-2;
                                                                                              zero(G), zero(comp);
17
     forall(it, G[v]){
                                                                                              e.clear();
18
                                                                                        21
       if(!idx[*it] || cmp[*it]==-2){
                                                                                              forn(i,n) V[i]=-1;
19
         if(!idx[*it]) tjn(*it);
                                                                                              nbc = qV = 0;
20
                                                                                        23
         lw[v]=min(lw[v], lw[*it]);
                                                                                         24
21
       }
                                                                                            stack<int> st;
     }
                                                                                            void dfs(int u, int pe) \{//0(n + m)\}
23
     if(lw[v]==idx[v]){
                                                                                                L[u] = V[u] = qV++;
                                                                                        27
24
       int x:
                                                                                              comp[u] = (pe != -1);
                                                                                        28
25
       do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
                                                                                                for(auto &ne: G[u]) if (ne != pe){
                                                                                         29
26
       verdad[qcmp] = (cmp[neg(v)] < 0);</pre>
                                                                                                int v = e[ne].u \cdot e[ne].v \cdot u; // x \cdot v \cdot x = y!
27
                                                                                                if (V[v] == -1) \{ // \text{ todavia no se lo visito} \}
       qcmp++;
                                                                                        31
28
                                                                                                  st.push(ne);
29
                                                                                         32
                                                                                                  dfs(v,ne);
                                                                                         33
30
                                                                                                  if (L[v] > V[u]){// bridge => no pertenece a ninguna comp biconexa
    //remember to CLEAR G!!!
                                                                                         34
31
   bool satisf(){//O(n)
                                                                                                     e[ne].bridge = true;
32
                                                                                         35
     memset(idx, 0, sizeof(idx)), qidx=0;
                                                                                         36
33
                                                                                                  if (L[v] \ge V[u]) \{ // art \}
     memset(cmp, -1, sizeof(cmp)), qcmp=0;
                                                                                         37
34
     forn(i, n){
                                                                                                     int last;
                                                                                         38
35
       if(!idx[i]) tjn(i);
                                                                                                     do { //todas las aristas que estan entre dos puntos de articulacion
36
                                                                                         39
       if(!idx[neg(i)]) tjn(neg(i));
                                                                                                         pertenecen a la misma componente biconexa
37
                                                                                                       last = st.top(); st.pop();
38
                                                                                         40
     forn(i, n) if(cmp[i] == cmp[neg(i)]) return false;
                                                                                                       e[last].comp = nbc;
39
                                                                                         41
     return true:
                                                                                                     } while (last != ne):
                                                                                         42
40
41 | }
                                                                                                     nbc++;
                                                                                         43
                                                                                                     comp[u]++;
                                                                                         44
                          Comp. Biconexas y Puentes
                                                                                         45
                                                                                                  L[u] = min(L[u], L[v]);
                                                                                         46
1 const int MAXN=1010;
                                                                                         47
   int n, m;
                                                                                                else if (V[v] < V[u]) { // back edge
                                                                                         48
   vector<int> G[MAXN];
                                                                                                  st.push(ne);
                                                                                         49
                                                                                                  L[u] = min(L[u], V[v]);
                                                                                         50
   struct edge {
                                                                                                }
                                                                                         51
     int u,v, comp;
                                                                                         52
     bool bridge;
                                                                                         53
8 | };
   vector<edge> e;
                                                                                            set<int> C[2*MAXN];
```

```
int compnodo [MAXN];
                                                                                           f[v][0]=fa, L[v]=lvl;
   int ptoart;
                                                                                           forall(it, G[v])if(*it!=fa)
   void blockcuttree(){
                                                                                             dfs(*it, v, lvl+1);
       ptoart = 0; zero(compnodo);
                                                                                      11
                                                                                         void build(int N){//f[i][0] must be filled previously, O(nlgn)
       forn(i,2*MAXN) C[i].clear();
                                                                                           forn(k, LOGN-1) forn(i, N) f[i][k+1]=f[f[i][k]][k];}
       for(auto &it: e){
61
           int u = it.u, v = it.v;
62
           if(comp[u] == 1) compnodo[u] = it.comp;
                                                                                         #define lg(x) (31-_builtin_clz(x))//=floor(log2(x))
63
           else{
64
               if(compnodo[u] == 0){ compnodo[u] = nbc+ptoart; ptoart++;}
                                                                                         int climb(int a, int d){\frac{1}{0}}
65
                   C[it.comp].insert(compnodo[u]);
                                                                                           if(!d) return a;
66
                   C[compnodo[u]].insert(it.comp);
                                                                                           dforn(i, lg(L[a])+1)
67
                                                                                     19
                                                                                             if(1<<i<=d)
68
                                                                                     20
           if(comp[v] == 1) compnodo[v] = it.comp;
                                                                                               a=f[a][i], d-=1<<i;
                                                                                     21
69
           else{
                                                                                             return a;
70
                                                                                     22
               if(compnodo[v] == 0){ compnodo[v] = nbc+ptoart; ptoart++;}
71
                                                                                      23
                   C[it.comp].insert(compnodo[v]);
                                                                                         int lca(int a, int b){\frac{1}{0}}
72
                   C[compnodo[v]].insert(it.comp);
                                                                                           if(L[a]<L[b]) swap(a, b);</pre>
73
           }
                                                                                           a=climb(a, L[a]-L[b]);
74
                                                                                     26
                                                                                           if(a==b) return a;
75
                                                                                     27
                                                                                           dforn(i, lg(L[a])+1)
76
                                                                                     28
                                                                                             if(f[a][i]!=f[b][i])
77
                                                                                     29
   int main() {
                                                                                               a=f[a][i], b=f[b][i];
78
                                                                                     30
     while(cin >> n >> m){
                                                                                           return f[a][0];
                                                                                     31
79
       initDfs(n);
                                                                                     32
80
       forn(i, m){
                                                                                         int dist(int a, int b) {//returns distance between nodes
81
                                                                                           return L[a]+L[b]-2*L[lca(a, b)];}
         int a,b; cin >> a >> b;
82
         addEdge(a,b);
83
                                                                                                               Heavy Light Decomposition
84
           dfs(0,-1);
85
                                                                                        int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
           forn(i, n) cout << "comp[" << i << "]_=_" << comp[i] << endl;
86
                                                                                         int dad[MAXN];//dad[v]=padre del nodo v
       for(auto &ne: e) cout << ne.u << "->" << ne.v << "|en_lla_comp.__" << ne.comp
87
                                                                                         void dfs1(int v, int p=-1){//pre-dfs
            << endl:
                                                                                           dad[v]=p;
       cout << "Cant., de, componentes, biconexas, =, " << nbc << endl;
88
                                                                                           treesz[v]=1;
     }
89
                                                                                           forall(it, G[v]) if(*it!=p){
       return 0;
90
                                                                                             dfs1(*it, v);
91 |}
                                                                                             treesz[v]+=treesz[*it];
                                  LCA + Climb
                                                                                      10
const int MAXN=100001;
                                                                                         //PONER Q EN O !!!!!
                                                                                         int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
2 const int LOGN=20:
3 //f[v][k] holds the 2^k father of v
                                                                                         //Las cadenas aparecen continuas en el recorrido!
4 //L[v] holds the level of v
                                                                                         int cantcad:
5 int f[MAXN] [LOGN], L[MAXN];
                                                                                         int homecad [MAXN];//dada una cadena devuelve su nodo inicial
6 //call before build:
                                                                                         int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
void dfs(int v, int fa=-1, int lvl=0){//generate required data
                                                                                      void heavylight(int v, int cur=-1){
```

forall(it, G[v]) if(!taken[*it])

```
if(cur==-1) homecad[cur=cantcad++]=v;
                                                                                             centroid(*it, v, lvl+1, -1);
                                                                                     26
                                                                                     27 }
     pos[v]=q++;
     cad[v]=cur;
                                                                                                                         Euler Cycle
     int mx=-1:
     forn(i, sz(G[v])) if(G[v][i]!=dad[v])
22
                                                                                         #define MAXN 1005
       if(mx==-1 || treesz[G[v][mx]]<treesz[G[v][i]]) mx=i;</pre>
                                                                                         #define MAXE 1005005
     if(mx!=-1) heavylight(G[v][mx], cur);
     forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
25
                                                                                         int n,ars[MAXE], eq;
       heavylight(G[v][i], -1);
26
                                                                                         vector<int> G[MAXN];//fill G,ars,eq
27
                                                                                         list<int> path;
   //ejemplo de obtener el maximo numero en el camino entre dos nodos
28
                                                                                         int used[MAXN]; //used[v] = i => para todo j<=i la arista v-G[v][j] fue usada y
   //RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
                                                                                              la arista v-G[v][i+1] no se uso
   //esta funcion va trepando por las cadenas
                                                                                         bool usede[MAXE];
   int query(int an, int v){//O(logn)
     //si estan en la misma cadena:
                                                                                         //encuentra el ciclo euleriano, el grafo debe ser conexo y todos los nodos
     if(cad[an] == cad[v]) return rmq.get(pos[an], pos[v]+1);
33
                                                                                             tener grado par para que exista
     return max(query(an, dad[homecad[cad[v]]]),
34
                                                                                         //para encontrar el camino euleriano conectar los dos vertices de grado impar y
            rmq.get(pos[homecad[cad[v]]], pos[v]+1));
35
                                                                                              empezar de uno de ellos.
36 }
                                                                                         queue<list<int>::iterator> q;
                            Centroid Decomposition
                                                                                         int get(int v){
                                                                                      14
                                                                                           while(used[v]\leq z(G[v]) && usede[G[v][used[v]]]) used[v]++;
1 | int n;
vector<int> G[MAXN];
                                                                                           return used[v];
                                                                                      16
3 bool taken[MAXN];//poner todos en FALSE al principio!!
                                                                                      17
  int padre[MAXN];//padre de cada nodo en el centroid tree
                                                                                         void explore(int v, int r, list<int>::iterator it){
                                                                                      18
                                                                                           int ar=G[v][get(v)]; int u=v^ars[ar];
                                                                                      19
   int szt[MAXN]:
                                                                                           usede[ar]=true:
                                                                                           list<int>::iterator it2=path.insert(it, u);
   void calcsz(int v, int p) {
     szt[v] = 1:
                                                                                           if(u!=r) explore(u, r, it2);
     forall(it,G[v]) if (*it!=p && !taken[*it])
                                                                                           if(get(v)<sz(G[v])) q.push(it);</pre>
                                                                                      23
       calcsz(*it,v), szt[v]+=szt[*it];
10
                                                                                     24
                                                                                         void euler(int a){
                                                                                      25
11
                                                                                           zero(used), zero(usede);
   void centroid(int v=0, int f=-1, int lvl=0, int tam=-1) {//0(nlogn)
12
                                                                                     26
     if(tam==-1) calcsz(v, -1), tam=szt[v];
                                                                                           path.clear();
13
                                                                                     27
     forall(it, G[v]) if(!taken[*it] && szt[*it]>=tam/2)
                                                                                           q=queue<list<int>::iterator>();
14
                                                                                     28
       {szt[v]=0; centroid(*it, f, lvl, tam); return;}
                                                                                           path.push_back(a); q.push(path.begin());
15
                                                                                     29
     taken[v]=true;
                                                                                           while(sz(q)){
16
                                                                                      30
                                                                                             list<int>::iterator it=q.front(); q.pop();
     padre[v]=f;
17
                                                                                     31
                                                                                             if(used[*it] < sz(G[*it])) explore(*it, *it, it);</pre>
     /*Analizar todos los caminos que pasan por este nodo:
18
                                                                                      32
      * Agregar la información de cada subarbol
19
                                                                                      33
                                                                                           reverse(path.begin(), path.end());
      * Para cada subarbol:
20
                                                                                     34
      * -sacar la informacion
                                                                                      35
21
                                                                                         void addEdge(int u, int v){
      * -analizar
                                                                                      36
22
                                                                                           G[u].pb(eq), G[v].pb(eq);
      * -agregar de nuevo la informacion
23
                                                                                     37
                                                                                           ars[eq++]=u^v;
24
                                                                                      38
```

39 | }

Diametro rbol

```
vector<int> G[MAXN]; int n,m,p[MAXN],d[MAXN],d2[MAXN];
  int bfs(int r, int *d) {
     queue<int> q;
     d[r]=0; q.push(r);
     int v;
     while(sz(q)) { v=q.front(); q.pop();
       forall(it,G[v]) if (d[*it]==-1)
         d[*it]=d[v]+1, p[*it]=v, q.push(*it);
     }
     return v;//ultimo nodo visitado
10
11
   vector<int> diams; vector<ii> centros;
   void diametros(){
     memset(d,-1,sizeof(d));
     memset(d2,-1,sizeof(d2));
     diams.clear(), centros.clear();
     forn(i, n) if(d[i]==-1){
       int v,c;
18
       c=v=bfs(bfs(i, d2), d);
19
       forn(_,d[v]/2) c=p[c];
20
       diams.pb(d[v]);
21
       if(d[v]&1) centros.pb(ii(c, p[c]));
22
       else centros.pb(ii(c, c));
23
    }
24
25 }
```

Chu-liu

```
void visit(graph&h,int v,int s,int r,vector<int>&no,vector<vector<int>>&comp,
      vector<int>&prev,vector<vector<int>>&next,vector<weight>&mcost,vector<int
      >&mark,weight&cost,bool&found){if(mark[v]){vector<int>temp=no;found=true;
      do\{cost+=mcost[v]; v=prev[v]; if(v!=s)\{while(comp[v].size()>0)\{no[comp[v].size()>0\}\}
      back()]=s;comp[s].push_back(comp[v].back());comp[v].pop_back();}}while(v
      !=s); forall(j,comp[s])if(*j!=r)forall(e,h[*j])if(no[e->src]!=s)e->w-=mcost
      [ temp[*j] ];}mark[v]=true;forall(i,next[v])if(no[*i]!=no[v]&&prev[no[*i
      ]]==v)if(!mark[no[*i]]||*i==s)visit(h,*i,s,r,no,comp,prev,next,mcost,mark,
      cost, found); \} weight minimumSpanningArborescence(const graph&g,int r) \{const 10
       int n=sz(g);graph h(n);forn(u,n)forall(e,g[u])h[e->dst].pb(*e);vector<int 11
      >no(n);vector<vector<int>>comp(n);forn(u,n)comp[u].pb(no[u]=u);for(weight
      cost=0;;){vector<int>prev(n,-1);vector<weight>mcost(n,INF);forn(j,n)if(j!= 13
      r)forall(e,h[j])if(no[e->src]!=no[j])if(e->w<mcost[ no[j] ])mcost[ no[j]
      ]=e->w,prev[ no[j] ]=no[e->src];vector<vector<int>>next(n);forn(u,n)if(
      prev[u]>=0)next[ prev[u] ].push_back(u);bool stop=true;vector<int>mark(n);
      forn(u,n)if(u!=r&&!mark[u]&&!comp[u].empty()){bool found=false;visit(h,u,u 17
      ,r,no,comp,prev,next,mcost,mark,cost,found);if(found)stop=false;}if(stop){ 18
      forn(u,n)if(prev[u]>=0)cost+=mcost[u];return cost;}}}
```

Hungarian

```
//Dado un grafo bipartito completo con costos no negativos, encuentra el
            matching perfecto de minimo costo.
   const tipo EPS=1e-9;const tipo INF=1e14;
   #define N 502
   tipo cost[N][N],lx[N],ly[N],slack[N];int n,max_match,xy[N],yx[N],slackx[N],
            prev2[N]; bool S[N], T[N]; void add_to_tree(int x, int prevx) {S[x] = true, prev2[
           x]=prevx; forn(y,n)if(lx[x]+ly[y]-cost[x][y]<slack[y]-EPS)slack[y]=lx[x]+ly[y]-cost[x][y]<slack[y]-EPS)slack[y]=lx[x]+ly[y]-cost[x][y]<slack[y]-EPS)slack[y]=lx[x]+ly[y]-cost[x][y]<slack[y]-EPS)slack[y]=lx[x]+ly[y]-cost[x][y]<slack[y]-EPS)slack[y]=lx[x]+ly[y]-cost[x][y]<slack[y]-EPS]slack[y]-EPS]slack[y]-lx[x]+ly[y]-cost[x][y]<slack[y]-EPS]slack[y]-lx[x]+ly[y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]-cost[x][y]
            [y]-cost[x][y],slackx[y]=x;}void update_labels(){tipo delta=INF;forn(y,n)
            if(!T[y])delta=min(delta,slack[y]);forn(x,n)if(S[x])lx[x]-=delta;forn(y,n)
           zero(ly);forn(x,n)forn(y,n)lx[x]=max(lx[x],cost[x][y]);}void augment(){if(
            max_match==n)return;int x,y,root,q[N],wr=0,rd=0;memset(S,false,sizeof(S)),
            memset(T,false,sizeof(T));memset(prev2,-1,sizeof(prev2));forn(x,n)if(xy[x
            ]=-1)\{q[wr++]=root=x,prev2[x]=-2;S[x]=true;break;\}forn(y,n)slack[y]=lx[
            root]+ly[y]-cost[root][y],slackx[y]=root;while(true){while(rd<wr){x=q[rd</pre>
           ++]; for (y=0; y<n; y++) if (cost[x][y]==lx[x]+ly[y] &&!T[y]) {if (yx[y]==-1) break;
           T[y]=true;q[wr++]=yx[y],add_to_tree(yx[y],x);}if(y<n)break;}if(y<n)break;</pre>
           update_labels(), wr=rd=0; for(y=0;y<n;y++)if(!T[y] \&\&slack[y]==0) \{if(yx[y=0;y<n;y++))\}
           ]==-1){x=slackx[y];break;}else{T[y]=true;if(!S[yx[y]])q[wr++]=yx[y],
           add_to_tree(yx[y],slackx[y]);}}if(y<n)break;}if(y<n){max_match++;for(int
           cx=x,cy=y,ty;cx!=-2;cx=prev2[cx],cy=ty)ty=xy[cx],yx[cy]=cx,xy[cx]=cy;
            augment();}}tipo hungarian(){tipo ret=0;max_match=0,memset(xy,-1,sizeof(xy))
           ));memset(yx,-1,sizeof(yx)),init_labels(),augment();forn(x,n)ret+=cost[x][
            xv[x]];return ret;}
```

Dynamic Connectivity

```
struct UnionFind {
       int n, comp;
       vector<int> pre,si,c;
       UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
           forn(i,n) pre[i] = i; }
       int find(int u){return u==pre[u]?u:find(pre[u]);}
       bool merge(int u, int v) {
           if((u=find(u))==(v=find(v))) return false;
           if(si[u]<si[v]) swap(u, v);</pre>
           si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
           return true;
       }
12
       int snap(){return sz(c);}
       void rollback(int snap){
           while(sz(c)>snap){
               int v = c.back(); c.pop_back();
               si[pre[v]] -= si[v], pre[v] = v, comp++;
           }
       }
```

```
20 };
                                                                                          #define MAXN 212345
enum {ADD, DEL, QUERY};
22 | struct Query {int type,u,v;};
                                                                                          set<int> G[MAXN];
   struct DynCon {
       vector<Query> q;
                                                                                          set<int>::iterator it[MAXN];
       UnionFind dsu;
                                                                                          int S[2][MAXN];//pila
25
                                                                                          int szS[2];//tamano de la pila
       vector<int> match,res;
26
                                                                                          int szC[2];//tamano de la componente
       map<ii,int> last;//se puede no usar cuando hay identificador para cada
27
                                                                                          bool vis[MAXN];
           arista (mejora poco)
       DynCon(int n=0):dsu(n){}
                                                                                          void dfsparalelo(int a, int b){ //O(componente mas chica)
28
       void add(int u, int v) {
                                                                                            zero(vis);
                                                                                       11
29
           if(u>v) swap(u,v);
                                                                                             szS[0] = szS[1] = 0;
30
           q.pb((Query){ADD, u, v}), match.pb(-1);
                                                                                             szC[0] = szC[1] = 1;
31
           last[ii(u,v)] = sz(q)-1;
                                                                                            if(sz(G[a])){
32
       }
                                                                                              S[0][szS[0]++] = a;//.push(a);
33
                                                                                              it[a] = G[a].begin();
       void remove(int u, int v) {
                                                                                       16
34
           if(u>v) swap(u,v);
                                                                                       17
35
           q.pb((Query){DEL, u, v});
                                                                                       18
36
           int prev = last[ii(u,v)];
                                                                                            if(sz(G[b])){
                                                                                       19
37
           match[prev] = sz(q)-1;
                                                                                              S[1][szS[1]++] = b;//.push(b);
38
                                                                                       20
           match.pb(prev);
                                                                                              it[b] = G[b].begin();
                                                                                       21
39
       }
                                                                                       22
40
       void query() {//podria pasarle un puntero donde guardar la respuesta
                                                                                            int act = 0:
                                                                                       23
41
           q.pb((Query){QUERY, -1, -1}), match.pb(-1);}
                                                                                            vis[a] = vis[b] = true;
42
       void process() {
43
           forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] = sz(q); 26
                                                                                           //recorre las dos componentes en paralelo
44
                                                                                             while(szS[act]){
           go(0,sz(q));
45
       }
                                                                                              int v = S[act] [szS[act]-1];//.top();
                                                                                       28
46
       void go(int 1, int r) {
                                                                                              int u = *it[v];
                                                                                       29
47
                                                                                              it[v]++;
           if(l+1==r){
                                                                                       30
48
                                                                                              if(it[v] == G[v].end()) szS[act]--;//.pop();
                if (q[1].type == QUERY)//Aqui responder la query usando el dsu!
49
                   res.pb(dsu.comp);//aqui query=cantidad de componentes conexas
                                                                                              if(vis[u]){act = 1 - act; continue;}
                                                                                              szC[act]++;
               return;
                                                                                       33
51
                                                                                              if(sz(G[u])>1 \text{ or } *G[u].begin() != v){
           }
                                                                                       34
52
           int s=dsu.snap(), m = (l+r) / 2;
                                                                                                S[act][szS[act]++] = u;//.push(u);
53
           forr(i,m,r) if(match[i]!=-1 && match[i]<1) dsu.merge(q[i].u, q[i].v);</pre>
                                                                                                vis[u] = true;
54
                                                                                                it[u] = G[u].begin();
           go(1,m);
55
           dsu.rollback(s):
                                                                                              }
                                                                                       38
56
           s = dsu.snap();
                                                                                              act = 1 - act;
57
           forr(i,1,m) if(match[i]!=-1 && match[i]>=r) dsu.merge(q[i].u, q[i].v);
           go(m,r);
                                                                                            //ya recorrio la toda la componente de act
           dsu.rollback(s);
                                                                                            act = 1 - act;
60
                                                                                       42
62 | }dc;
                                                                                            //sigue recorriendo la otra componente hasta que ve un elemento mas o no
                                                                                                 tiene mas elementos.
                                   DFS Paralelo
                                                                                            while(szC[act] < szC[1-act]+1 and szS[act]){</pre>
```

17 struct Edge {

18

19

20

21 | };

int to, rev;

Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(cap) {}

11 f, cap;

```
int v = S[act][szS[act]-1];//.top();
                                                                                      vector<Edge> G[MAX];
46
       int u = *it[v];
                                                                                         void addEdge(int s, int t, ll cap){
47
       it[v]++;
                                                                                             G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0, 0));
       if(it[v] == G[v].end()) szS[act]--;//.pop();
                                                                                         bool dinic bfs(){
       if(vis[u]) continue;
                                                                                             fill(dist, dist+nodes, -1), dist[src]=0;
50
       szC[act]++;
                                                                                             int qt=0; q[qt++]=src;
51
       if(sz(G[u])>1 \text{ or } *G[u].begin() != v){
                                                                                             for(int qh=0; qh<qt; qh++){</pre>
52
         S[act][szS[act]++] = u;//.push(u);
                                                                                                  int u =q[qh];
53
         vis[u] = true;
                                                                                                  forall(e, G[u]){
54
         it[u] = G[u].begin();
                                                                                                      int v=e->to;
55
                                                                                      31
                                                                                                      if(dist[v]<0 \&\& e->f < e->cap)
56
                                                                                      32
     }
                                                                                                          dist[v]=dist[u]+1, q[qt++]=v;
57
                                                                                      33
                                                                                                 }
58
                                                                                      34
59 }
                                                                                      35
                                                                                             return dist[dst]>=0;
                                                                                      36
                                Network Flow
                                                                                      37
                                                                                         11 dinic_dfs(int u, ll f){
                                                                                      38
                                                                                             if(u==dst) return f:
                                                                                      39
                                       Dinic
                                                                                             for(int &i=work[u]; i<sz(G[u]); i++){</pre>
                                                                                      40
                                                                                                  Edge &e = G[u][i];
                                                                                      41
                                                                                                  if(e.cap<=e.f) continue;</pre>
                                                                                      42
2 const int MAX = 300;
                                                                                                  int v=e.to;
                                                                                      43
3 // Corte minimo: vertices con dist[v]>=0 (del lado de src) VS. dist[v]==-1 (
                                                                                                  if(dist[v] == dist[u] + 1){
       del lado del dst)
                                                                                                          11 df=dinic_dfs(v, min(f, e.cap-e.f));
4 // Para el caso de la red de Bipartite Matching (Sean V1 y V2 los conjuntos mas
                                                                                                          if(df>0){
        proximos a src y dst respectivamente):
                                                                                                                  e.f+=df, G[v][e.rev].f-= df;
                                                                                      47
5 // Reconstruir matching: para todo v1 en V1 ver las aristas a vertices de V2
                                                                                                                  return df; }
                                                                                      48
       con it->f>0, es arista del Matching
                                                                                     49
6 // Min Vertex Cover: vertices de V1 con dist[v] ==-1 + vertices de V2 con dist[v
                                                                                             }
                                                                                             return 0;
                                                                                      51
7 // Max Independent Set: tomar los vertices NO tomados por el Min Vertex Cover
                                                                                      52
8 // Max Clique: construir la red de G complemento (debe ser bipartito!) y
                                                                                            maxFlow(int _src, int _dst){
                                                                                      53
       encontrar un Max Independet Set
                                                                                             src=_src, dst=_dst;
                                                                                      54
9 // Min Edge Cover: tomar las aristas del matching + para todo vertices no
                                                                                             11 result=0;
                                                                                      55
       cubierto hasta el momento, tomar cualquier arista de el
                                                                                             while(dinic_bfs()){
                                                                                      56
10 //Complejidad:
                                                                                                 fill(work, work+nodes, 0);
                                                                                      57
   //Peor caso: O(V^2E)
                                                                                                  while(ll delta=dinic_dfs(src,INF))
                                                                                      58
   //Si todas las capacidades son 1: O(\min(E^1/2,V^2/3)E)
                                                                                                      result+=delta;
                                                                                      59
   //Para matching bipartito es: O(sqrt(V)E)
                                                                                      60
                                                                                             // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1 forman el
                                                                                      61
   int nodes, src, dst;
                                                                                                  min-cut
  int dist[MAX], q[MAX], work[MAX];
```

Min-cost Max-flow

```
const int MAXN=10000;
typedef ll tf;
```

return result; }

```
3 | typedef ll tc;
  const tf INFFLUJO = 1e14;
  const tc INFCOSTO = 1e14;
  struct edge {
     int u, v;
     tf cap, flow;
     tc cost;
     tf rem() { return cap - flow; }
11
   int nodes; //numero de nodos
   vector<int> G[MAXN]; // limpiar!
   vector<edge> e; // limpiar!
   void addEdge(int u, int v, tf cap, tc cost) {
     G[u].pb(sz(e)); e.pb((edge){u,v,cap,0,cost});
     G[v].pb(sz(e)); e.pb((edge)\{v,u,0,0,-cost\});
17
18
   tc dist[MAXN], mnCost;
   int pre[MAXN];
   tf cap[MAXN], mxFlow;
   bool in_queue[MAXN];
   void flow(int s, int t) {
     zero(in_queue);
24
     mxFlow=mnCost=0:
25
     while(1){
26
       fill(dist, dist+nodes, INFCOSTO); dist[s] = 0;
27
       memset(pre, -1, sizeof(pre)); pre[s]=0;
^{28}
       zero(cap); cap[s] = INFFLUJO;
29
       queue<int> q; q.push(s); in_queue[s]=1;
30
       while(sz(q)){
31
         int u=q.front(); q.pop(); in_queue[u]=0;
32
         for(auto it:G[u]) {
33
           edge &E = e[it];
34
           if(E.rem() \&\& dist[E.v] > dist[u] + E.cost + 1e-9){ // ojo EPS}
35
              dist[E.v] = dist[u] + E.cost;
36
             pre[E.v] = it;
37
              cap[E.v] = min(cap[u], E.rem());
38
             if(!in_queue[E.v]) q.push(E.v), in_queue[E.v]=1;
39
           }
40
         }
41
42
       if (pre[t] == -1) break;
43
       mxFlow +=cap[t];
44
       mnCost +=cap[t]*dist[t];
45
       for (int v = t; v != s; v = e[pre[v]].u) {
46
         e[pre[v]].flow += cap[t];
47
         e[pre[v]^1].flow -= cap[t];
48
```

```
49 }
50 }
51 }
```

Template

```
#include <bits/stdc++.h>
   using namespace std;
   #define forr(i,a,b) for(int i=(a); i<(b); i++)</pre>
   #define forn(i,n) forr(i,0,n)
   #define zero(v) memset(v, 0, sizeof(v))
   #define forall(it,v) for(auto it=v.begin();it!=v.end();++it)
   #define pb push_back
   #define fst first
   #define snd second
   typedef long long 11;
   typedef pair<ll, ll> pll;
   #define dforn(i,n) for(int i=n-1; i>=0; i--)
13
   int main() {
       ios::sync_with_stdio(0); cin.tie(0);
       return 0;
17 }
```

Ayudamemoria

Doubles Comp.

```
const double EPS = 1e-9;
define feq(a, b) (fabs((a)-(b))<EPS)
    x == y <=> fabs(x-y) < EPS
    x > y <=> x > y + EPS
    x >= y <=> x > y - EPS
```

Expandir pila

```
#include <sys/resource.h>
rlimit rl;
getrlimit(RLIMIT_STACK, &rl);
rl.rlim_cur=1024L*1024L*256L;//256mb
setrlimit(RLIMIT_STACK, &rl);
```

Iterar subconjunto

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
```