tipo get(int i, int j){return get(i,j,1,0,sz);} // [i,j) !

return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));

tipo get(int i, int j, int n, int a, int b) ${\frac{1}{0}}$

if(j<=a || i>=b) return neutro;

if(i<=a && b<=j) return t[n];</pre>

void set(int p, tipo val){//0(lgn)

for(p+=sz; p>0 && t[p]!=val;){

int c=(a+b)/2:

t[p]=val;

9

10

11

12

13

10

11

12

13

14

15

16

 17

18

19

20

21

22

23

24

}

dependiendo de la operacion que se quiera al actualizar un rango. Ej:11402.

void push(int n, int a, int b){//propaga el dirty a sus hijos

opAltT(n,a,b); //t[n]+=dirty[n]*(b-a);//altera el nodo

opAltD(2*n,dirty[n]);//dirty[2*n]+=dirty[n];

opAltD(2*n+1,dirty[n]);//dirty[2*n+1]+=dirty[n];

if(dirty[n]!=neutro2){

dirty[n]=neutro2;

if(n<sz){

1 ESTRUCTURAS -Estructuras p/=2;25 val=operacion(t[p*2], t[p*2+1]); 26 27 RMQ (static) } Dado un arreglo y una operacion asociativa idempotente, get(i, j) opera sobre el rango [i, j).²⁸ }rmq; Restriccion: LVL ≥ ceil(logn); Usar [] para llenar arreglo y luego build(). //Usage: 31 | cin >> n; rmq.init(n); forn(i, n) cin >> rmq[i]; rmq.updall(); 1 | struct RMQ{ #define LVL 10 RMQ (lazy) tipo vec[LVL] [1<<(LVL+1)];</pre> tipo &operator[](int p){return vec[0][p];} //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre el tipo get(int i, int j) {//intervalo [i,j) rango [i, j). int p = 31-_builtin_clz(j-i); typedef int Elem;//Elem de los elementos del arreglo return min(vec[p][i],vec[p][j-(1<<p)]);</pre> typedef int Alt;//Elem de la alteracion #define operacion(x,y) x+y void build(int n) {//O(nlogn) const Elem neutro=0; const Alt neutro2=0; int mp = 31- builtin clz(n); #define MAXN 1024000 forn(p, mp) forn(x, n-(1 << p))struct RMQ{ vec[p+1][x] = min(vec[p][x], vec[p][x+(1<<p)]);int sz; }}; Elem t[4*MAXN]; Alt dirty[4*MAXN];//las alteraciones pueden ser de distinto Elem RMQ (dynamic) Elem &operator[](int p){return t[sz+p];} 1 //Dado un arreglo y una operacion asociativa con neutro, get(i, j) opera sobre el void init(int n){//O(nlgn) rango [i, j). $sz = 1 \ll (32- builtin clz(n));$ 2 #define MAXN 100000 forn(i, 2*sz) t[i]=neutro; 14 #define operacion(x, y) max(x, y) forn(i, 2*sz) dirty[i]=neutro2; 15 const int neutro=0; 16 struct RMO{ void updall() ${//0(n)}$ 17 dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);} int sz: 18 void opAltT(int n,int a,int b){//altera el valor del nodo n segun su dirty y el tipo t[4*MAXN]; 19 intervalo que le corresponde. tipo &operator[](int p){return t[sz+p];} void init(int n) ${\frac{1}{0}}$ t[n] += dirty[n]*(b-a);20 sz = 1 << (32-_builtin_clz(n));</pre> } //en este caso la alteracion seria sumarle a todos los elementos del intervalo 21 forn(i, 2*sz) t[i]=neutro; [a,b) el valor dirty[n] } void opAltD(int n ,Alt val){ 22 void updall() ${//0(n)}$ dirty[n] += val; 23 dforn(i, sz) t[i]=operacion(t[2*i], t[2*i+1]);} }//actualiza el valor de Dirty "sumandole" val. podria cambiar el valor de dirty

25

26

27

28

29

30

31

32

```
}
                                                                                         5 | struct node{
33
     }
                                                                                              tipo v; node *1,*r;
34
     Elem get(int i, int j, int n, int a, int b){\frac{1}{0}}
                                                                                              node(tipo v):v(v), 1(NULL), r(NULL) {}
       if(j<=a || i>=b) return neutro;
                                                                                                node(node *1, node *r) : 1(1), r(r){
       push(n, a, b);//corrige el valor antes de usarlo
                                                                                                    if(!1) v=r->v;
       if(i<=a && b<=j) return t[n];</pre>
                                                                                                    else if(!r) v=l->v;
       int c=(a+b)/2;
                                                                                                    else v=oper(1->v, r->v);
39
                                                                                         11
       return operacion(get(i, j, 2*n, a, c), get(i, j, 2*n+1, c, b));
                                                                                                }
                                                                                         12
                                                                                            };
41
                                                                                         13
     Elem get(int i, int j){return get(i,j,1,0,sz);}
                                                                                            node *build (tipo *a, int tl, int tr) {//modificar para que tome tipo a
42
     //altera los valores en [i, j) con una alteración de val
                                                                                              if (tl+1==tr) return new node(a[tl]);
43
     void alterar(Alt val, int i, int j, int n, int a, int b)\frac{1}{0(lgn)}
                                                                                              int tm=(tl + tr)>>1;
44
       push(n, a, b);
                                                                                              return new node(build(a, tl, tm), build(a, tm, tr));
45
                                                                                         17
       if(j<=a || i>=b) return;
                                                                                         18
46
       if(i<=a && b<=j){
                                                                                            node *update(int pos, int new val, node *t, int tl, int tr){
47
                                                                                              if (tl+1==tr) return new node(new val);
         opAltD(n,val);//actualiza el valor de Dirty por val.
48
                                                                                              int tm=(tl+tr)>>1;
         push(n,a,b);
49
         return; //este nodo esta totalmente contenido por el intervalo a alterar, no
                                                                                              if(pos < tm) return new node(update(pos, new val, t->1, tl, tm), t->r);
50
             es necesario que se lo pases a los hijos.. por ahora..
                                                                                              else return new node(t->1, update(pos, new val, t->r, tm, tr));
       }
                                                                                         24
51
       int c=(a+b)/2;
                                                                                            tipo get(int 1, int r, node *t, int tl, int tr){
52
       alterar(val, i, j, 2*n, a, c), alterar(val, i, j, 2*n+1, c, b);
                                                                                                if(l==tl && tr==r) return t->v;
53
       t[n]=operacion(t[2*n], t[2*n+1]);//por esto es el push de arriba
                                                                                              int tm=(t1 + tr)>>1:
                                                                                        27
54
                                                                                                if(r<=tm) return get(l, r, t->l, tl, tm);
55
                                                                                                else if(l>=tm) return get(l, r, t->r, tm, tr);
     void alterar(Alt val, int i, int j){alterar(val,i,j,1,0,sz);}
56
                                                                                              return oper(get(1, tm, t->1, tl, tm), get(tm, r, t->r, tm, tr));
57
                                                                                         30
     //setea de a un elemento. Esto lo "hace" dinámico.
                                                                                        31 }
58
     void set(int p, Elem val){//O(lgn)
59
                                                                                                                              Union Find
       if(p<0) return; //OJO chequear que p no sea muy grande
60
       this->get(p,p+1); //para que acomode los dirty del camino de la raíz a p
61
                                                                                         struct UnionFind{
       int a=p, b=p+1, ancho=1, vecino;
                                                                                              vector<int> f;//the array contains the parent of each node
62
       for(p+=sz; p>0 && t[p]!=val; ancho*=2){
                                                                                              void init(int n){f.clear(); f.insert(f.begin(), n, -1);}
63
         t[p]=val;
                                                                                              int comp(int x){return (f[x]=-1?x:f[x]=comp(f[x]));}//0(1)
64
         if(p&1){ vecino=p-1; push(vecino,a,b); a-=ancho; }
                                                                                              bool join(int i, int j) {
65
         else{ vecino=p+1; push(vecino,a,b); b+=ancho; }
                                                                                                bool con=comp(i)==comp(j);
66
         p/=2;
67
                                                                                                if(!con) f[comp(i)] = comp(j);
         val=operacion(t[p*2], t[p*2+1]);
68
                                                                                                return con;
                                                                                              }};
69
     }
70
                                                                                                                          Disjoint Intervals
71 | };
                                                                                          | bool operator< (const ii &a, const ii &b) {return a.fst<b.fst;}
                                RMQ (persistente)
                                                                                            //Stores intervals as [first, second]
1 typedef int tipo;
                                                                                            //in case of a collision it joins them in a single interval
tipo oper(const tipo &a, const tipo &b){
                                                                                            struct disjoint intervals {
                                                                                              set<ii>> segs;
       return a+b:
4 }
                                                                                              void insert(ii v) {//O(lgn)
```

```
if(v.snd-v.fst==0.) return;//0J0
       set<ii>>::iterator it,at;
       at = it = segs.lower bound(v);
       if (at!=segs.begin() && (--at)->snd >= v.fst)
         v.fst = at->fst, --it;
11
       for(; it!=segs.end() && it->fst <= v.snd; segs.erase(it++))</pre>
12
         v.snd=max(v.snd, it->snd);
13
       segs.insert(v);
14
     }
15
<sub>16</sub> };
                                     RMQ (2D)
struct RMO2D{//n filas x m columnas
     int sz:
     RMQ t[4*MAXN];
     void init(int n, int m){\frac{1}{0}(n*m)}
       sz = 1 \ll (32- builtin clz(n));
       forn(i, 2*sz) t[i].init(m); }
     void set(int i, int j, tipo val){//0(lgm.lgn)
       for(i+=sz; i>0;){
         t[i].set(j, val);
         i/=2:
         val=operacion(t[i*2][j], t[i*2+1][j]);
11
       } }
12
     tipo get(int i1, int j1, int i2, int j2){return get(i1,j1,i2,j2,1,0,sz);}
     //O(lgm.lgn), rangos cerrado abierto
14
     int get(int i1, int j1, int i2, int j2, int n, int a, int b){
15
       if(i2<=a || i1>=b) return neutro;
16
       if(i1<=a && b<=i2) return t[n].get(j1, j2);
17
       int c=(a+b)/2;
18
       return operacion(get(i1, j1, i2, j2, 2*n, a, c),
            get(i1, j1, i2, j2, 2*n+1, c, b));
     }
   } rma:
    //Example to initialize a grid of M rows and N columns:
   RMQ2D rmq; rmq.init(n,m);
   forn(i, n) forn(j, m){
     int v; cin >> v; rmq.set(i, j, v);}
                                        Big Int
1 #define BASEXP 6
2 #define BASE 1000000
3 #define LMAX 1000
4 | struct bint{int 1;11 n[LMAX];bint(11 x=0){l=1;forn(i,LMAX){if(x)l=i+1;n[i]=x %BASE; 17 |}
       x/=BASE;}}bint(string x){l=(x.size()-1)/BASEXP+1;fill(n,n+LMAX,0);ll r=1;forn( 18
       i,sz(x))\{n[i/BASEXP]+=r*(x[x.size()-1-i]-'0');r*=10;if(r==BASE)r=1;\}\}void out
```

(){cout<<n[1-1];dforn(i,1-1)printf("%6.61lu",n[i]);}void invar(){fill(n+1,n+ LMAX,0); while(1>1&&!n[1-1])1--;}; bint operator+(const bint&a,const bint&b){ bint c;c.l=max(a.1,b.1);11 q=0;forn(i,c.1)q+=a.n[i]+b.n[i],c.n[i]=q BASE,q/= BASE; if (q)c.n[c.l++]=q;c.invar();return c;}pair
bint,bool>lresta(const bint&a, const bint&b){bint c;c.l=max(a.l,b.l);ll q=0;forn(i,c.l)q+=a.n[i]-b.n[i],c.n[i]=(q+BASE) %BASE,q=(q+BASE)/BASE-1;c.invar();return make_pair(c,!q);}bint& operator-=(bint&a,const bint&b){return a=lresta(a,b).first;}bint operator-(const bint&a,const bint&b){return lresta(a,b).first;}bool operator<(const bint &a,const bint&b){return!lresta(a,b).second;}bool operator<=(const bint&a,const bint&b){return lresta(b,a).second;}bool operator==(const bint&a,const bint&b) {return a <= blub <= a; }bint operator*(const bint la, ll b) {bint c; ll q=0; forn(i, a.l q+a.n[i]*b.c.n[i]=q BASE, q/=BASE; c.l=a.l; while (q)c.n[c.l++]=q BASE, q/=BASE; c.l=a.l; while (q)c.n[c.l++]=q BASE, (q)c.n[c.l++]=q.invar();return c;}bint operator*(const bint&a,const bint&b){bint c;c.l=a.l+b. l;fill(c.n,c.n+b.1,0);forn(i,a.1){ll q=0;forn(j,b.1)q+=a.n[i]*b.n[j]+c.n[i+j], c.n[i+j]=q%ASE,q/=BASE;c.n[i+b.1]=q;}c.invar();return c;}pair
bint,11>ldiv(const bint&a,11 b){bint c;11 rm=0;dforn(i,a.1){rm=rm*BASE+a.n[i];c.n[i]=rm/b; rm %+0;}c.l=a.l;c.invar();return make pair(c,rm);}bint operator/(const bint&a, 11 b){return ldiv(a,b).first;}ll operator%(const bint&a,ll b){return ldiv(a,b) .second;}pair<bint,bint>ldiv(const bint&a,const bint&b){bint c;bint rm=0;dforn (i,a.l){if(rm.l==1&&!rm.n[0])rm.n[0]=a.n[i];else{dforn(j,rm.l)rm.n[j+1]=rm.n[j];rm.n[0]=a.n[i];rm.l++;}ll q=rm.n[b.l]*BASE+rm.n[b.l-1];ll u=q/(b.n[b.l-1]+1) ; | v = q/b.n[b.l-1] + 1; while (u < v-1) = (u+v)/2; if (b*m < m) = m; else v=m; c.n[i]=u;rm-=b*u;}c.l=a.l;c.invar();return make pair(c,rm);}bint operator/(const bint&a,const bint&b){return ldiv(a,b).first;}bint operator%(const bint&a,const bint&b){return ldiv(a,b).second;}

Modnum

```
static const tipo mod=MOD;
                                                                                                      c.pb(1);
                                                                                           21
     tipo v;
21
                                                                                           22
     mnum(tipo v=0): v((v \( \) nod+mod) \( \) nod) {}
                                                                                                inline bool fbin(tipo x, int m) {return inter(acc(m), acc(m+1))>x;}
22
     mnum operator+(mnum b){return v+b.v;}
                                                                                                 tipo eval(tipo x){
     mnum operator-(mnum b){return v-b.v;}
                                                                                                  int n = sz(c);
24
     mnum operator*(mnum b){return v*b.v;} //Si mod<=1e9+9
                                                                                                  //query con x no ordenados O(lgn)
     //~ mnum operator*(mnum b){return mul(v,b.v,mod);} //Si mod<=1e18+9</pre>
                                                                                                  int a=-1, b=n-1;
26
     mnum operator(ll n) \{ //0 (log n) \}
                                                                                                   while(b-a>1) { int m = (a+b)/2;
27
                                                                                                    if(fbin(x, m)) b=m;
       if(!n) return 1;
28
       mnum q = (*this)^(n/2);
                                                                                                    else a=m;
29
       return n %2 ? q*q*v : q*q;
                                                                                                  }
                                                                                           31
30
                                                                                                  return (acc(b).m*x+acc(b).h)*(mx?-1:1);
31
     mnum operator/(mnum n){return ~n*v;} //O(log n) //OJO! mod tiene que ser primo!
                                                                                                      //query 0(1)
32
         Sino no siempre existe inverso
                                                                                                  while(pos>0 && fbin(x, pos-1)) pos--;
                                                                                                  while(pos<n-1 && !fbin(x, pos)) pos++;</pre>
33
                                                                                           35
                                                                                                  return (acc(pos).m*x+acc(pos).h)*(mx?-1:1);
     mnum operator~(){ //inverso, O(log mod)
34
       assert(v!=0);
35
       //return (*this)^(eulerphi(mod)-1); //si mod no es primo (sacar a mano) PROBAR 38 } ch;
36
            ! Ver si rta*x == 1 modulo mod
                                                                                                                     Convex Hull Trick (Dynamic)
       return (*this)^(mod-2);//si mod es primo
37
38
                                                                                             const 11 is_query = -(1LL<<62);</pre>
39 | };
                                                                                              struct Line {
                                 Convex Hull Trick
                                                                                                  ll m, b;
                                                                                                  mutable multiset<Line>::iterator it;
struct Line{tipo m,h;};
                                                                                                  const Line *succ(multiset<Line>::iterator it) const;
  tipo inter(Line a, Line b){
                                                                                                  bool operator<(const Line& rhs) const {
       tipo x=b.h-a.h, y=a.m-b.m;
                                                                                                       if (rhs.b != is query) return m < rhs.m;</pre>
       return x/y+(x\%?!((x>0)^(y>0)):0);//==ceil(x/y)
                                                                                                      const Line *s=succ(it):
                                                                                                      if(!s) return 0;
   struct CHT {
                                                                                                      11 x = rhs.m;
                                                                                                      return b - s \rightarrow b < (s \rightarrow m - m) * x;
     vector<Line> c;
                                                                                           11
     bool mx;
                                                                                                  }
                                                                                           12
                                                                                              };
     int pos;
                                                                                           13
     CHT(bool mx=0):mx(mx),pos(0){}//mx=1 si las query devuelven el max
                                                                                              struct HullDynamic : public multiset Line { // will maintain upper hull for
10
     inline Line acc(int i){return c[c[0].m>c.back().m? i : sz(c)-1-i];}
                                                                                                   maximum
11
     inline bool irre(Line x, Line y, Line z){
                                                                                                  bool bad(iterator y) {
                                                                                           15
12
       return c[0].m>z.m? inter(y, z) <= inter(x, y)
                                                                                                      iterator z = next(y);
                                                                                           16
13
                             : inter(y, z) >= inter(x, y);
                                                                                                      if (y == begin()) {
14
                                                                                           17
                                                                                                           if (z == end()) return 0;
15
                                                                                           18
     void add(tipo m, tipo h) {//O(1), los m tienen que entrar ordenados
                                                                                                           return y->m == z->m && y->b <= z->b;
16
                                                                                           19
           if(mx) m*=-1, h*=-1;
                                                                                           20
17
       Line l=(Line)\{m, h\};
                                                                                                      iterator x = prev(y);
18
           if(sz(c) && m==c.back().m) { 1.h=min(h, c.back().h), c.pop back(); if(pos) 22
                                                                                                      if (z == end()) return y->m == x->m && y->b <= x->b;
19
                                                                                                      return (x->b - y->b)*(z->m - y->m) >= (y->b - z->b)*(y->m - x->m);
                                                                                           23
           while(sz(c) \ge 2 \&\& irre(c[sz(c)-2], c[sz(c)-1], 1)) { c.pop back(); if(pos) 24
                 pos--; }
                                                                                                  iterator next(iterator y){return ++y;}
```

```
iterator prev(iterator y){return --y;}
26
       void insert line(ll m, ll b) {
27
           iterator y = insert((Line) { m, b });
           y->it=y;
           if (bad(y)) { erase(y); return; }
           while (next(y) != end() && bad(next(y))) erase(next(y));
           while (y != begin() && bad(prev(y))) erase(prev(y));
32
33
       ll eval(ll x) {
34
           Line l = *lower_bound((Line) { x, is_query });
35
           return 1.m * x + 1.b;
36
       }
37
   }h;
38
   const Line *Line::succ(multiset<Line>::iterator it) const{
       return (++it==h.end()? NULL : &*it);}
                         Set con búsq. binaria (Treap)
1 #include bits stdc++.h>
  #include<ext/pb ds/assoc container.hpp>
  #include<ext/pb_ds/tree_policy.hpp>
   using namespace __gnu_pbds;
   using namespace std;
   template <typename T>
   using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
       tree_order_statistics_node_update>;
   //o bien usar así:
   typedef tree<int,null_type,less<int>,//key, mapped type, comparator. Se puede usar
        como map<a,b> poniendo tree<a,b,...
       rb_tree_tag,tree_order_statistics_node_update> set_t;
12
   int main(){
     ordered set<int> s;
     s.insert(1):
     s.insert(3):
17
     cout << s.order of key(3) << endl; // s.order of key(x): number of elements in s
18
          strictly less than x.
     cout << *s.find by order(0) << endl; // s.find by order(i): i-th smallest number
19
          in s. (empieza en 0)
     cout << *s.lower_bound(1) << endl;</pre>
20
21 }
```

Algos

Longest Increasing Subsecuence

```
1 //Para non-increasing, cambiar comparaciones y revisar busq binaria
   //Given an array, paint it in the least number of colors so that each color turns
        to a non-increasing subsequence.
   //Solution:Min number of colors=Length of the longest increasing subsequence
   int N, a[MAXN];//secuencia y su longitud
   ii d[MAXN+1];//d[i]=ultimo valor de la subsecuencia de tamanio i
   int p[MAXN];//padres
   vector<int> R;//respuesta
   void rec(int i){
     if(i==-1) return;
     R.push_back(a[i]);
     rec(p[i]);
11
12
   int lis(){//O(nlogn)
     d[0] = ii(-INF, -1); forn(i, N) d[i+1]=ii(INF, -1);
     forn(i, N){
15
       int j = upper bound(d, d+N+1, ii(a[i], INF))-d;
16
       if (d[j-1].first < a[i]&&a[i] < d[j].first){</pre>
17
         p[i]=d[j-1].second;
18
         d[j] = ii(a[i], i);
19
       }
20
21
     R.clear():
22
     dforn(i, N+1) if(d[i].first!=INF){
       rec(d[i].second);//reconstruir
24
       reverse(R.begin(), R.end());
25
       return i;//longitud
26
     return 0;
29 }
```

Optimizaciones para DP

```
| convex hull 1: dp[i] = min\{dp[j] + b[j] * a[i]\}, j < i. Si se cumple b[j] >= b[j]
       +1] y a[i] <= a[i+1] entonces pasa de O(n^2) a O(n) sino pasa a O(nlogn)
   convex hull 2: dp[i][j] = min\{dp[i-1][k] + b[k] * a[j]\}, k < j. Si se cumple b[k]
       >= b[k+1] y a[j] \le a[j+1] entonces pasa de O(kn^2) a O(kn) sino pasa O(knlogn)
   divide and conquer: dp[i][j] = min\{dp[i-1][k] + C[k+1][j]\}, k < j. Se debe cumplir
       : A[i][j] \leftarrow A[i][j+1]. Pasa de O(kn^2) a O(knlogn)
   Donde A[i][j] es el minimo k tal que dp[i][j] = dp[i-1][k] + C[k][j]
   Tambien es aplicable si:
_{10} | C[a][c] + C[b][d] <= C[a][d] + C[b][c] y C[b][c] <= C[a][d], a<=b<=c<=d
```

```
}
                                                                                           55
11
                                                                                                   }
   def ComputeDP(i, jleft, jright, kleft, kright):
                                                                                           56
     # Select the middle point
                                                                                                 }
                                                                                           57
     jmid = (jleft + jright) / 2
                                                                                                                                    Strings
     # Compute the value of dp[i][jmid] by definition of DP
     dp[i][jmid] = +INFINITY
     bestk = -1
                                                                                                                                      KMP
17
     for k in range[kleft, jmid):
18
                                                                                            string T;//cadena donde buscar(where)
     if dp[i-1][k] + C[k+1][jmid] < best:
19
                                                                                              string P;//cadena a buscar(what)
       dp[i][jmid] = dp[i - 1][k] + C[k + 1][jmid]
20
                                                                                               int b[MAXLEN];//back table b[i] maximo borde de [0..i)
       bestk = k
21
                                                                                               void kmppre(){//by gabina with love
     # Divide and conquer
22
                                                                                                   int i =0, j=-1; b[0]=-1;
     if jleft < jmid:</pre>
23
                                                                                                   while(i<sz(P)){</pre>
     ComputeDP(i, jleft, jmid, kleft, bestk)
                                                                                                       while(j>=0 && P[i] != P[j]) j=b[j];
     if jmid + 1 < jright:</pre>
25
                                                                                                       i++, j++, b[i] = j;
     ComputeDP(i, jmid + 1, jright, bestk, kright)
26
                                                                                                   }
27
   def ComputeFullDP:
                                                                                           10
28
                                                                                               void kmp(){
     Initialize dp for i = 0 somehow
                                                                                           11
29
                                                                                                   int i=0, j=0;
     for i in range(1, m):
30
     ComputeDP(i, 0, n, 0, n)
                                                                                                   while(i<sz(T)){</pre>
31
                                                                                                       while(j>=0 && T[i]!=P[j]) j=b[j];
                                                                                           14
32
                                                                                                       i++, j++;
33
                                                                                                       if(j==sz(P)) printf("P<sub>i</sub> is found at index % in T\n", i-j), j=b[j];
   knuth: dp[i][j] = min{dp[i][k] + dp[k][j]} + C[i][j], i < k < j. Se debe cumplir: A[i] = 16
                                                                                                   }
        , j -1]<=A[i,j]<=A[i+1,j]. Pasa de O(n^3) a O(n^2)
                                                                                           17
   Donde A[i][j] es el minimo k tal que dp[i][j] = dp[i][k]+dp[k][j] + C[i][j]
                                                                                           18 }
   Tambien es aplicable si:
                                                                                                                                       Trie
   C[a][c] + C[b][d] \leftarrow C[a][d] + C[b][c] y C[b][c] \leftarrow C[a][d], a \leftarrow b \leftarrow c \leftarrow d
37
                                                                                              struct trie{
38
   for (int s = 0; s <= k; s++)
                                                                                                 map<char, trie> m;
                                                   //l - left point
     for (int 1 = 0; 1+s<=k; 1++) {
                                                                                                 bool end=false;
40
                                                   //r - right point
       int r = 1 + s;
                                                                                                 void add(const string &s, int p=0){
41
       if (s < 2) {
                                                                                                   if(s[p]) m[s[p]].add(s, p+1);
42
       res[1][r] = 0;
                                                 //DP base - nothing to break
                                                                                                   else end=true;
43
       A[1][r] = 1;
                                               //A is equal to left border
                                                                                                 }
44
       continue;
45
                                                                                                 void dfs(){
       }
                                                                                                   //Do stuff
46
       int aleft = A[1][r-1];
                                                 //Knuth's trick: getting bounds on m
                                                                                                   forall(it, m)
47
       int aright = A[l+1][r];
                                                                                                     it->second.dfs();
48
                                                                                           11
       res[1][r] = INF;
49
                                                                                            12
       for (int a = max(l+1,aleft); a<=min(r-1,aright); a++) {
                                                                      //iterating for a
50
            in the bounds only
                                                                                                                        Suffix Array (largo, nlogn)
       int act = res[l][a] + res[a][r] + (C[l][r]);
       if (res[1][r] > act) {
                                                //relax current solution
52
                                                                                             #define MAX N 112345
         res[1][r] = act;
53
                                                                                              #define rBOUND(x) ((x) < n ? r[(x)] : 0)
         A[1][r] = a;
54
                                                                                            3 //sa will hold the suffixes in order.
```

```
int sa[MAX N], r[MAX N], n;// OJO n = s.size()!
                                                                                         13
  string s; //input string, n=s.size()
                                                                                              forn(i, n) LCP[i]=PLCP[sa[i]];
                                                                                         14
                                                                                         15 }
   int f[MAX N], tmpsa[MAX N];
                                                                                                                                 Corasick
   void countingSort(int k){
     zero(f);
                                                                                           struct trie{
     forn(i, n) f[rBOUND(i+k)]++;
                                                                                              map<char, trie> next;
     int sum=0:
                                                                                              trie* tran[256];//transiciones del automata
11
     forn(i, max(255, n)){
^{12}
                                                                                              int idhoja, szhoja;//id de la hoja o 0 si no lo es
       int t=f[i]; f[i]=sum; sum+=t;}
13
                                                                                              //link lleva al sufijo mas largo, nxthoja lleva al mas largo pero que es hoja
     forn(i,n)
14
                                                                                              trie *padre, *link, *nxthoja;
       tmpsa[f[rBOUND(sa[i]+k)]++]=sa[i];
15
                                                                                              char pch;//caracter que conecta con padre
     forn(i,n) sa[i] = tmpsa[i];
                                                                                              trie(): next(), tran(), idhoja(), szhoja(), padre(), link(),nxthoja(),pch() {}
16
                                                                                              void insert(const string &s, int id=1, int p=0){//id>0!!!
17
   void constructsa(){\frac{1}{0}} n log n
                                                                                                if(p<sz(s)){
     n = s.size();
19
                                                                                                  trie &ch=next[s[p]];
                                                                                         11
     forn(i,n) sa[i]=i, r[i]=s[i];
20
                                                                                                  tran[(int)s[p]]=&ch;
     for(int k=1; k<n; k<<=1){</pre>
                                                                                                  ch.padre=this, ch.pch=s[p];
21
                                                                                         13
       countingSort(k), countingSort(0);
                                                                                                  ch.insert(s, id, p+1);
22
                                                                                         14
       int rank, tmpr[MAX N];
23
                                                                                                }
                                                                                         15
       tmpr[sa[0]]=rank=0;
24
                                                                                                else idhoja=id, szhoja=sz(s);
                                                                                         16
       forr(i, 1, n)
25
                                                                                         17
         tmpr[sa[i]] = (r[sa[i]] = r[sa[i-1]] \&\& r[sa[i] + k] = r[sa[i-1] + k]) ? rank : ++
                                                                                              trie* get_link() {
26
             rank;
                                                                                                if(!link){
       forn(i,n) r[i]=tmpr[i];
27
                                                                                                   if(!padre) link=this;//es la raiz
                                                                                         20
       if(r[sa[n-1]]==n-1) break;
^{28}
                                                                                                   else if(!padre->padre) link=padre;//hijo de la raiz
                                                                                         21
29
                                                                                                   else link=padre->get_link()->get_tran(pch);
                                                                                         22
30
                                                                                                }
                                                                                         23
   void print(){//for debugging
                                                                                                return link; }
                                                                                         24
     forn(i, n)
                                                                                              trie* get tran(int c) {
^{32}
       cout << i << ''' <<
                                                                                                if(!tran[c]) tran[c] = !padre? this : this->get link()->get tran(c);
33
       s.substr(sa[i], s.find('$',sa[i])-sa[i]) << endl;}
34
                                                                                                return tran[c]; }
                                                                                         27
                                                                                              trie *get nxthoja(){
                        LCP (Longest Common Prefix)
                                                                                                if(!nxthoja) nxthoja = get link()->idhoja? link : link->nxthoja;
                                                                                         29
                                                                                                return nxthoja; }
1 //Calculates the LCP between consecutives suffixes in the Suffix Array.
                                                                                         30
                                                                                              void print(int p){
   //LCP[i] is the length of the LCP between sa[i] and sa[i-1]
                                                                                         31
                                                                                                if(idhoja) cout << "found_" << idhoja << "__at_position_" << p-szhoja << endl;
  int LCP[MAX_N], phi[MAX_N], PLCP[MAX_N];
                                                                                                if(get_nxthoja()) get_nxthoja()->print(p); }
   void computeLCP(){//O(n)
                                                                                              void matching(const string &s, int p=0){
     phi[sa[0]]=-1;
                                                                                                print(p); if(p<sz(s)) get_tran(s[p])->matching(s, p+1); }
     forr(i, 1, n) phi[sa[i]]=sa[i-1];
                                                                                         35
                                                                                         36 }tri;
     int L=0;
     forn(i, n){
                                                                                                                           Suffix Automaton
       if(phi[i]==-1) {PLCP[i]=0; continue;}
       while(s[i+L] == s[phi[i]+L]) L++;
                                                                                           struct state {
10
       PLCP[i]=L:
                                                                                              int len, link;
11
       L=max(L-1, 0);
                                                                                              map<char,int> next;
```

last = cur;

```
state() { }
<sub>5</sub> |};
   const int MAXLEN = 10010;
                                                                                          46 }
  state st[MAXLEN*2]:
  int sz, last;
   void sa_init() {
     forn(i,sz) st[i].next.clear();
     sz = last = 0;
     st[0].len = 0;
     st[0].link = -1;
13
     ++sz;
14
15
   // Es un DAG de una sola fuente y una sola hoja
   // cantidad de endpos = cantidad de apariciones = cantidad de caminos de la clase
       al nodo terminal
18 // cantidad de miembros de la clase = st[v].len-st[st[v].link].len (v>0) = caminos
        del inicio a la clase
19 // El arbol de los suffix links es el suffix tree de la cadena invertida. La
       string de la arista link(v)->v son los caracteres que difieren
   void sa_extend (char c) {
     int cur = sz++;
21
     st[cur].len = st[last].len + 1;
22
     // en cur agregamos la posicion que estamos extendiendo
23
     //podria agregar tambien un identificador de las cadenas a las cuales pertenece
24
         (si hay varias)
^{25}
     for (p=last; p!=-1 && !st[p].next.count(c); p=st[p].link) // modificar esta
26
         linea para hacer separadores unicos entre varias cadenas (c=='$')
       st[p].next[c] = cur;
27
     if (p == -1)
^{28}
       st[cur].link = 0;
29
     else {
30
       int q = st[p].next[c];
31
       if (st[p].len + 1 == st[q].len)
32
         st[cur].link = q;
33
       else {
34
         int clone = sz++:
35
         // no le ponemos la posicion actual a clone sino indirectamente por el link
36
         st[clone].len = st[p].len + 1;
         st[clone].next = st[q].next;
         st[clone].link = st[q].link;
39
         for (; p!=-1 && st[p].next.count(c) && st[p].next[c]==q; p=st[p].link)
40
           st[p].next[c] = clone;
41
         st[q].link = st[cur].link = clone;
42
43
```

```
Z Function
```

```
char s[MAXN];
int z[MAXN]; // z[i] = i==0 ? 0 : max k tq s[0,k) match with s[i,i+k)
void z_function(char s[],int z[]) {
   int n = strlen(s);
   forn(i, n) z[i]=0;
   for (int i = 1, l = 0, r = 0; i < n; ++i) {
      if (i <= r) z[i] = min (r - i + 1, z[i - 1]);
      while (i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z[i];
      if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
}
```

Geometria

Punto

```
const double EPS=1e-9;
2 struct pto{
     double x, y;
     pto(double x=0, double y=0):x(x),y(y){}
     pto operator+(pto a){return pto(x+a.x, y+a.y);}
     pto operator-(pto a){return pto(x-a.x, y-a.y);}
     pto operator+(double a){return pto(x+a, y+a);}
     pto operator*(double a){return pto(x*a, y*a);}
     pto operator/(double a){return pto(x/a, y/a);}
     //dot product, producto interno:
     //Significado: a*b = a.norm * b.norm * cos(ang).
     double operator*(pto a){return x*a.x+y*a.y;}
     //module of the cross product or vectorial product:
     //if a is less than 180 clockwise from b, a^b>0. Significado: abs(a^b) = area
14
         del paralelogramo.
     double operator^(pto a){return x*a.y-y*a.x;}
     //returns true if this is at the left side of line qr
     bool left(pto q, pto r){return ((q-*this)^(r-*this))>0;}
17
     bool operator<(const pto &a) const{return x<a.x-EPS || (abs(x-a.x)<EPS && y<a.y-
18
     bool operator==(pto a){return abs(x-a.x)<EPS && abs(y-a.y)<EPS;}
     double norm(){return sqrt(x*x+y*y);}
     double norm sq(){return x*x+y*y;}
21
22
double dist(pto a, pto b){return (b-a).norm();}
```

```
10 | bool parallels(line 11, line 12){return abs(l1.a*l2.b-l2.a*l1.b)<EPS;}
double dist sq(pto a, pto b){return (b-a).norm sq();}
   typedef pto vec;
                                                                                           pto inter(line 11, line 12){//intersection
                                                                                             double det=11.a*12.b-12.a*11.b;
    //positivo si aob están en sentido antihorario con un ángulo <180º
                                                                                             if(abs(det) < EPS) return pto(INF, INF); //parallels
   double angle(pto a, pto o, pto b){ //devuelve radianes! (-pi,pi)
                                                                                             return pto(12.b*11.c-11.b*12.c, 11.a*12.c-12.a*11.c)/det;
     pto oa=a-o, ob=b-o;
                                                                                        15 |}
     return atan2(oa^ob, oa*ob);}
                                                                                                                               Segment
31
    //rotate p by theta rads CCW w.r.t. origin (0,0)
                                                                                         1 struct segm{
   pto rotate(pto p, double theta){
                                                                                             pto s,f;
     return pto(p.x*cos(theta)-p.y*sin(theta),
                                                                                             segm(pto s, pto f):s(s), f(f) {}
34
        p.x*sin(theta)+p.y*cos(theta));
                                                                                             pto closest(pto p) {//use for dist to point
35
36 }
                                                                                                double 12 = dist sq(s, f);
                                                                                                if(12==0.) return s;
                             Orden radial de puntos
                                                                                                double t = ((p-s)*(f-s))/12;
                                                                                                if (t<0.) return s;//not write if is a line
struct Cmp{//orden total de puntos alrededor de un punto r
                                                                                                 else if(t>1.)return f;//not write if is a line
     pto r;
2
     Cmp(pto r):r(r) {}
                                                                                                return s+((f-s)*t);
                                                                                        10
     int cuad(const pto &a) const{
                                                                                        11
       if(a.x > 0 && a.y >= 0)return 0;
                                                                                             bool inside(pto p){return abs(dist(s, p)+dist(p, f)-dist(s, f))<EPS;}</pre>
                                                                                        12
       if(a.x \le 0 \&\& a.y > 0)return 1;
                                                                                        13
       if(a.x < 0 && a.y <= 0)return 2;
                                                                                        14
       if(a.x >= 0 \&\& a.y < 0)return 3;
                                                                                            //NOTA: Si los segmentos son colineales sólo devuelve un punto de intersección
       assert(a.x ==0 && a.y==0);
                                                                                           pto inter(segm s1, segm s2){
                                                                                                if(s1.inside(s2.s)) return s2.s; //Fix cuando son colineales
       return -1;
                                                                                        17
                                                                                               if(s1.inside(s2.f)) return s2.f; //Fix cuando son colineales
                                                                                        18
11
                                                                                               pto r=inter(line(s1.s, s1.f), line(s2.s, s2.f));
     bool cmp(const pto&p1, const pto&p2)const{
                                                                                        19
12
       int c1 = cuad(p1), c2 = cuad(p2);
                                                                                               if(s1.inside(r) && s2.inside(r)) return r;
                                                                                        20
13
                                                                                               return pto(INF, INF);
       if(c1==c2) return p1.y*p2.x<p1.x*p2.y;
                                                                                        21
                                                                                        22 }
           else return c1 < c2;
16
                                                                                                                              Rectangle
       bool operator()(const ptokp1, const ptokp2) const{
17
       return cmp(pto(p1.x-r.x,p1.y-r.y),pto(p2.x-r.x,p2.y-r.y));
                                                                                          struct rect{
18
                                                                                             //lower-left and upper-right corners
19
20 | };
                                                                                             pto lw, up;
                                         Line
                                                                                            //returns if there's an intersection and stores it in r
                                                                                           bool inter(rect a, rect b, rect &r){
   int sgn(ll x){return x<0? -1 : !!x;}
                                                                                             r.lw=pto(max(a.lw.x, b.lw.x), max(a.lw.y, b.lw.y));
  struct line{
                                                                                             r.up=pto(min(a.up.x, b.up.x), min(a.up.y, b.up.y));
     line() {}
                                                                                            //check case when only a edge is common
     double a,b,c;//Ax+By=C
                                                                                             return r.lw.x<r.up.x && r.lw.y<r.up.y;
    //pto MUST store float coordinates!
                                                                                        11 }
     line(double a, double b, double c):a(a),b(b),c(c){}
     line(pto p, pto q): a(q.y-p.y), b(p.x-q.x), c(a*p.x+b*p.y) {}
                                                                                                                           Polygon Area
     int side(pto p){return sgn(ll(a) * p.x + ll(b) * p.y - c);}
                                                                                         double area(vector<pto> &p){//0(sz(p))
9 };
```

```
double area=0:
                                                                                         36 }
     forn(i, sz(p)) area+=p[i]^p[(i+1) %z(p)];
                                                                                             pair<pto, pto> interCL(Circle c, line 1){
     //if points are in clockwise order then area is negative
                                                                                               bool sw=false;
     return abs(area)/2:
                                                                                               if((sw=feq(0,1.b))){}
                                                                                               swap(1.a, 1.b);
                                                                                               swap(c.o.x, c.o.y);
   //Area ellipse = M_PI*a*b where a and b are the semi axis lengths
   //Area triangle = sqrt(s*(s-a)(s-b)(s-c)) where s=(a+b+c)/2
  //o mejor area triángulo = abs(x0 * (y1 - y2) + x1 * (y2 - y0) + x2 * (y0 - y1)) /
                                                                                               pair<tipo, tipo> rc = ecCuad(
        2;
                                                                                               sqr(l.a)+sqr(l.b),
                                                                                               2.0*1.a*1.b*c.o.v-2.0*(sqr(1.b)*c.o.x+1.c*1.a),
                                         Circle
                                                                                               sqr(1.b)*(sqr(c.o.x)+sqr(c.o.y)-sqr(c.r))+sqr(1.c)-2.0*1.c*1.b*c.o.y
                                                                                               );
                                                                                         47
vec perp(vec v){return vec(-v.y, v.x);}
                                                                                               pair<pto, pto> p( pto(rc.first, (l.c - l.a * rc.first) / l.b),
                                                                                         48
line bisector(pto x, pto y){
                                                                                                         pto(rc.second, (l.c - l.a * rc.second) / l.b));
     line l=line(x, y); pto m=(x+y)/2;
                                                                                               if(sw){
     return line(-1.b, 1.a, -1.b*m.x+1.a*m.y);
                                                                                               swap(p.first.x, p.first.y);
                                                                                               swap(p.second.x, p.second.y);
   struct Circle{
                                                                                         53
     pto o;
                                                                                               return p;
                                                                                         54
     double r;
                                                                                         55
     Circle(pto x, pto y, pto z){
                                                                                             pair<pto, pto> interCC(Circle c1, Circle c2){
       o=inter(bisector(x, y), bisector(y, z));
10
                                                                                               line 1:
                                                                                         57
       r=dist(o, x);
11
                                                                                              1.a = c1.o.x-c2.o.x:
                                                                                         58
     }
12
                                                                                              1.b = c1.o.v-c2.o.v;
     pair<pto, pto> ptosTang(pto p){
13
                                                                                              1.c = (sqr(c2.r) - sqr(c1.r) + sqr(c1.o.x) - sqr(c2.o.x) + sqr(c1.o.y)
       pto m=(p+o)/2;
14
                                                                                               -sqr(c2.o.y))/2.0;
       tipo d=dist(o, m);
15
                                                                                               return interCL(c1, 1);
                                                                                         62
       tipo a=r*r/(2*d);
16
                                                                                         63 | }
       tipo h=sqrt(r*r-a*a);
17
       pto m2=o+(m-o)*a/d;
                                                                                                                             Point in Poly
18
       vec per=perp(m-o)/d;
19
       return make_pair(m2-per*h, m2+per*h);
                                                                                            //checks if v is inside of P, using ray casting
20
                                                                                             //works with convex and concave.
21
                                                                                             bool inPolygon(pto v, vector<pto>& P) {
22
    //finds the center of the circle containing p1 and p2 with radius r
                                                                                               bool c = false;
    //as there may be two solutions swap p1, p2 to get the other
                                                                                               forn(i, sz(P)){
24
   bool circle2PtsRad(pto p1, pto p2, double r, pto &c){
                                                                                                int j=(i+1) %z(P);
25
           double d2=(p1-p2).norm_sq(), det=r*r/d2-0.25;
26
           if(det<0) return false;
                                                                                                 segm lado(P[i],P[j]);
27
           c=(p1+p2)/2+perp(p2-p1)*sqrt(det);
                                                                                                 if(lado.inside(v)) return true; //OJO: return true: incluye lados. return
28
                                                                                                     false: excluye lados.
           return true;
29
                                                                                         10
30
   #define sqr(a) ((a)*(a))
                                                                                                 if((P[i].y > v.y) != (P[i].y > v.y) &&
                                                                                         11
                                                                                                 (v.x < (P[i].x-P[j].x) * (v.y-P[j].y) / (P[i].y-P[j].y) + P[j].x))
   #define feq(a,b) (fabs((a)-(b))<EPS)</pre>
   pair<tipo, tipo > ecCuad(tipo a, tipo b, tipo c){//a*x*x+b*x+c=0
                                                                                                   c = !c;
                                                                                         13
     tipo dx = sqrt(b*b-4.0*a*c);
                                                                                         14
    return make pair((-b + dx)/(2.0*a), (-b - dx)/(2.0*a));
                                                                                              return c;
```

sort(P.begin(), P.end());//first x, then y

```
16 }
                                                                                              forn(i, sz(P)){//lower hull
                                                                                                while(sz(S) \ge 2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop back();
                          Point in Convex Poly log(n)
                                                                                                S.pb(P[i]);
  |void normalize(vector<pto> &pt){//delete collinear points first!
                                                                                              S.pop_back();
     //this makes it clockwise:
                                                                                         10
                                                                                              int k=sz(S);
       if(pt[2].left(pt[0], pt[1])) reverse(pt.begin(), pt.end());
                                                                                              dforn(i, sz(P)){//upper hull
     int n=sz(pt), pi=0;
                                                                                                while(sz(S) \ge k+2 \&\& S[sz(S)-1].left(S[sz(S)-2], P[i])) S.pop_back();
     form(i, n)
                                                                                                S.pb(P[i]);
       if(pt[i].x<pt[pi].x || (pt[i].x==pt[pi].x && pt[i].y<pt[pi].y))
                                                                                         14
         pi=i;
                                                                                         15
                                                                                              S.pop_back();
     vector<pto> shift(n);//puts pi as first point
                                                                                         16
       forn(i, n) shift[i]=pt[(pi+i) %n];
                                                                                         17 }
       pt.swap(shift);
10
                                                                                                                             Cut Polygon
11
                                                                                           //cuts polygon Q along the line ab
12
                                                                                            //stores the left side (swap a, b for the right one) in P
    /* left debe decir >0 para que considere los bordes. Ojo que Convex Hull
13
       necesita que left diga >= 0 para limpiar los colineales, hacer otro left
                                                                                             void cutPolygon(pto a, pto b, vector<pto> Q, vector<pto> &P){
14
       si hace falta */
                                                                                              P.clear();
15
   bool inPolygon(pto p, const vector<pto> &pt){
                                                                                              forn(i, sz(Q)){
     //call normalize first!
                                                                                                double left1=(b-a)^(Q[i]-a), left2=(b-a)^(Q[(i+1) / z(Q)]-a);
17
     if(p.left(pt[0], pt[1]) || p.left(pt[sz(pt)-1], pt[0])) return false;
                                                                                                if(left1>=0) P.pb(Q[i]);
18
     int a=1, b=sz(pt)-1;
                                                                                                if(left1*left2<0)
19
                                                                                                  P.pb(inter(line(Q[i], Q[(i+1) \sl z(Q)]), line(a, b)));
     while(b-a>1){
20
       int c=(a+b)/2:
21
                                                                                         10
       if(!p.left(pt[0], pt[c])) a=c;
                                                                                         11 }
22
       else b=c;
23
                                                                                                                              Bresenham
     }
24
     return !p.left(pt[a], pt[a+1]);
25
                                                                                            //plot a line approximation in a 2d map
<sub>26</sub> |}
                                                                                            void bresenham(pto a, pto b){
                                                                                              pto d=b-a; d.x=abs(d.x), d.y=abs(d.y);
                             Convex Check CHECK
                                                                                              pto s(a.x<b.x? 1: -1, a.y<b.y? 1: -1);
| bool isConvex(vector<int> &p){//O(N), delete collinear points!
                                                                                              int err=d.x-d.y;
                                                                                              while(1){
     int N=sz(p);
     if(N<3) return false;
                                                                                                m[a.x][a.y]=1;//plot
     bool isLeft=p[0].left(p[1], p[2]);
                                                                                                if(a==b) break:
     forr(i, 1, N)
                                                                                                int e2=err:
       if(p[i].left(p[(i+1) \mathbb{M}], p[(i+2) \mathbb{M}])!=isLeft)
                                                                                                if(e2 >= 0) err=2*d.y, a.x+=s.x;
         return false;
                                                                                                if(e2 <= 0) err+= 2*d.x, a.y+= s.y;
                                                                                         11
     return true; }
                                                                                         12
                                                                                         13 }
                                    Convex Hull
                                                                                                                            Rotate Matrix
1 //stores convex hull of P in S, CCW order
2 //left must return >=0 to delete collinear points!
                                                                                          1 //rotates matrix t 90 degrees clockwise
3 | void CH(vector<pto>& P, vector<pto> &S){
                                                                                            //using auxiliary matrix t2(faster)
     S.clear():
                                                                                            void rotate(){
```

forn(x, n) forn(y, n)

```
t2[n-y-1][x]=t[x][y];
memcpy(t, t2, sizeof(t));
}
```

Math

Identidades

```
\begin{split} \sum_{i=0}^{n} \binom{n}{i} &= 2^n \\ \sum_{i=0}^{n} i \binom{n}{i} &= n*2^{n-1} \\ \sum_{i=m}^{n} i &= \frac{n(n+1)}{2} - \frac{m(m-1)}{2} = \frac{(n+1-m)(n+m)}{2} \\ \sum_{i=0}^{n} i &= \sum_{i=1}^{n} i = \frac{n(n+1)}{2} \\ \sum_{i=0}^{n} i^2 &= \frac{n(n+1)(2n+1)}{6} = \frac{n^3}{3} + \frac{n^2}{2} + \frac{n}{6} \\ \sum_{i=0}^{n} i(i-1) &= \frac{8}{6} (\frac{n}{2})(\frac{n}{2}+1)(n+1) \text{ (doubles)} \rightarrow \text{Sino ver caso impar y par} \\ \sum_{i=0}^{n} i^3 &= \left(\frac{n(n+1)}{2}\right)^2 &= \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4} = \left[\sum_{i=1}^{n} i\right]^2 \\ \sum_{i=0}^{n} i^4 &= \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} &= \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} - \frac{n}{30} \\ \sum_{i=0}^{n} i^p &= \frac{(n+1)^{p+1}}{p+1} + \sum_{k=1}^{p} \frac{B_k}{p-k+1} \binom{p}{k}(n+1)^{p-k+1} \\ \sum_{i=0}^{n} a^i &= \frac{a(n+1)-1}{a-1} slosia! = 1 \\ r &= e - v + k + 1 \end{split} Teorema de Pick: (Area, puntos interiores y puntos en el borde) A = I + \frac{B}{2} - 1
```

Ec. Caracteristica

```
\begin{array}{l} a_0T(n) + a_1T(n-1) + ... + a_kT(n-k) = 0 \\ p(x) = a_0x^k + a_1x^{k-1} + ... + a_k \\ \text{Sean } r_1, r_2, ..., r_q \text{ las raı́ces distintas, de mult. } m_1, m_2, ..., m_q \\ T(n) = \sum_{i=1}^q \sum_{j=0}^{m_i-1} c_{ij}n^jr_i^n \\ \text{Las constantes } c_{ij} \text{ se determinan por los casos base.} \end{array}
```

Combinatorio

```
forn(i, MAXN+1){//comb[i][k]=i tomados de a k
    comb[i][0]=comb[i][i]=1;
    forr(k, 1, i) comb[i][k]=(comb[i-1][k]+comb[i-1][k-1]) MOD;
}

ll lucas (ll n, ll k, int p){ //Calcula (n,k) % teniendo comb[p][p] precalculado.
    ll aux = 1;
    while (n + k) aux = (aux * comb[n % ][k % ]) % , n/=p, k/=p;
    return aux;
}
```

Log. Discreto

```
// IDEA: a^x=b mod MOD <=> x = i*sqrt(MOD)+j con i,j <= sqrt(MOD)=m
// entonces guardo todos los a^j: T[a^j mod MOD]=j
// y después busco si vi T[b/(a^(i*m) mod MOD] = T[b*a^-(i*m) mod MOD], return j+i
*m</pre>
```

Exp. de Matrices y Fibonacci en log(n)

```
#define SIZE 350
int NN;

double tmp[SIZE] [SIZE];

void mul(double a[SIZE] [SIZE], double b[SIZE] [SIZE]){ zero(tmp);
    forn(i, NN) forn(j, NN) forn(k, NN) tmp[i] [j]+=a[i] [k]*b[k] [j];
    forn(i, NN) forn(j, NN) a[i] [j]=tmp[i] [j];

void powmat(double a[SIZE] [SIZE], int n, double res[SIZE] [SIZE]){
    forn(i, NN) forn(j, NN) res[i] [j]=(i==j);
    while(n){
        if(n&1) mul(res, a), n--;
        else mul(a, a), n/=2;
    }
}
```

```
Matrices y determinante O(n^3)
  struct Mat {
       vector<vector<double> > vec;
       Mat(int n): vec(n, vector<double>(n) ) {}
       Mat(int n, int m): vec(n, vector<double>(m) ) {}
       vector<double> &operator[](int f){return vec[f];}
       const vector<double> &operator[](int f) const {return vec[f];}
       int size() const {return sz(vec);}
       Mat operator+(Mat &b) { ///this de n x m entonces b de n x m
           Mat m(sz(b), sz(b[0]));
           forn(i,sz(vec)) forn(j,sz(vec[0])) m[i][j] = vec[i][j] + b[i][j];
10
           return m;
11
       Mat operator*(const Mat &b) { ///this de n x m entonces b de m x t
12
           int n = sz(vec), m = sz(vec[0]), t = sz(b[0]);
13
           Mat mat(n,t);
14
           forn(i,n) forn(j,t) forn(k,m) mat[i][j] += vec[i][k] * b[k][j];
15
           return mat;
16
       double determinant(){//sacado de e maxx ru
17
           double det = 1;
18
           int n = sz(vec);
19
           Mat m(*this);
           forn(i, n){//para cada columna
21
               int k = i;
22
               forr(j, i+1, n)//busco la fila con mayor val abs
23
                   if(abs(m[j][i])>abs(m[k][i])) k = j;
24
               if(abs(m[k][i])<1e-9) return 0;
25
               m[i].swap(m[k]);//la swapeo
26
               if(i!=k) det = -det;
27
               det *= m[i][i];
               forr(j, i+1, n) m[i][j] /= m[i][i];
               //hago 0 todas las otras filas
```

if(n>1) ret[n]++;
return ret;

13 //factoriza bien numeros hasta MAXP

11 12

```
forn(j, n) if (j!= i && abs(m[j][i])>1e-9)
                                                                                               | map<11,11> fact2(11 n){ //0 (lg n)}
31
                    forr(k, i+1, n) m[j][k]-=m[i][k]*m[j][i];
                                                                                                     map<11,11> ret;
32
                                                                                                     while (criba[n]){
            return det;
                                                                                                       ret[criba[n]]++:
                                                                                                       n/=criba[n];
36 };
                                                                                                     if(n>1) ret[n]++;
                              Teorema Chino del Resto
                                                                                                     return ret;
                           y = \sum_{j=1}^{n} (x_j * (\prod_{i=1, i \neq j}^{n} m_i)_{m_j}^{-1} * \prod_{i=1, i \neq j}^{n} m_i)
                                                                                               22
                                                                                                   //Usar asi: divisores(fac, divs, fac.begin()); NO ESTA ORDENADO
                                                                                                   void divisores(const map<11,11> &f, vector<11> &divs, map<11,11>::iterator it, 11
                                                                                                       n=1){
                                                                                                       if(it==f.begin()) divs.clear();
                                                                                               25
                                                                                                       if(it==f.end()) { divs.pb(n); return; }
#define MAXP 100000 //no necesariamente primo
                                                                                                      ll p=it->fst, k=it->snd; ++it;
1 int criba[MAXP+1]:
                                                                                                       forn( , k+1) divisores(f, divs, it, n), n*=p;
3 | void crearcriba(){
     int w[] = \{4,2,4,2,4,6,2,6\};
                                                                                               29
                                                                                                   ll sumDiv (ll n){
     for(int p=25;p<=MAXP;p+=10) criba[p]=5;</pre>
                                                                                                     ll rta = 1;
     for(int p=9;p<=MAXP;p+=6) criba[p]=3;</pre>
                                                                                                     map<ll,11> f=fact(n);
     for(int p=4;p<=MAXP;p+=2) criba[p]=2;</pre>
                                                                                                     forall(it, f) {
     for(int p=7,cur=0;p*p<=MAXP;p+=w[cur++&7]) if (!criba[p])
       for(int j=p*p;j<=MAXP;j+=(p<<1)) if(!criba[j]) criba[j]=p;</pre>
                                                                                                     11 \text{ pot} = 1, \text{ aux} = 0;
                                                                                                     forn(i, it->snd+1) aux += pot, pot *= it->fst;
10
                                                                                                     rta*=aux;
   vector<int> primos;
   void buscarprimos(){
                                                                                               37
     crearcriba();
                                                                                                     return rta;
                                                                                               38
     forr (i,2,MAXP+1) if (!criba[i]) primos.push_back(i);
14
                                                                                                   ll eulerPhi (ll n){ // con criba: O(lg n)
15
   //~ Useful for bit trick: \#define SET(i) ( criba[(i)>>5] |=1<<((i)&31) ), <math>\#define SET(i) = 1
                                                                                                     11 \text{ rta} = n;
                                                                                                     map<ll,ll> f=fact(n);
       INDEX(i) ( (criba[i>>5]>>((i)\&31))\&1), unsigned int criba[MAXP/32+1];
                                                                                                     forall(it, f) rta -= rta / it->first;
                                 Funciones de primos
                                                                                                     return rta;
Sea n = \prod p_i^{k_i}, fact(n) genera un map donde a cada p_i le asocia su k_i
                                                                                               45
                                                                                                   11 eulerPhi2 (11 n){ // 0 (sqrt n)
                                                                                               46
1 //factoriza bien numeros hasta MAXP^2
                                                                                                     11 r = n;
                                                                                               47
2 | map<11,11> fact(11 n){ //0 (cant primos)
                                                                                                     forr (i,2,n+1){
     map<11,11> ret;
                                                                                                      if ((ll)i*i > n) break;
     forall(p, primos){
                                                                                                      if (n \% i == 0){
       while(!(n \(\mathbb{*}p\)){
                                                                                                         while (n\%i == 0) n/=i;
         ret[*p]++;//divisor found
                                                                                                         r = r/i: 
         n/=*p;
       }
                                                                                                    if (n != 1) r-= r/n;
                                                                                                     return r;
```

Test de primalidad naive $O(\operatorname{sqrt}(n)/6)$

form (i, s-1){

Extended Euclid

```
int attribute ((const)) is prime(long long n)
                                                                                                x = mulmod(x, x, n);
                                                                                         29
                                                                                                if (x == 1) return false;
     if (n \le 1)
                                                                                                if (x+1 == n) return true;
       return 0:
                                                                                         32
     else if (n \le 3)
                                                                                              return false;
       return 1;
                                                                                         34
     else if (!(n %2) || !(n %3))
       return 0;
                                                                                            bool rabin (ll n){ //devuelve true si n es primo
                                                                                              if (n == 1) return false;
                                                                                              const int ar[] = \{2,3,5,7,11,13,17,19,23\};
     long long cap = sqrt(n) + 1;
10
     for (long long int i = 5; i \le cap; i += 6)
                                                                                              forn (j,9)
11
                                                                                                if (!es_primo_prob(n,ar[j]))
       if (!(n%i) || !(n%(i+2)))
12
         return 0;
                                                                                                  return false;
13
                                                                                         41
                                                                                              return true:
     return 1;
15
                                                                                         43
16 }
                                                                                         44
                                                                                            ll rho(ll n){
                            Phollard's Rho (rolando)
                                                                                                if((n \& 1) == 0) return 2:
                                                                                                11 x = 2, y = 2, d = 1;
1 | ll gcd(ll a, ll b){return a?gcd(b %a, a):b;}
                                                                                                ll c = rand() % n + 1;
                                                                                         48
                                                                                                while(d == 1){
                                                                                         49
   11 mulmod (11 a, 11 b, 11 c) { //returns (a*b) %, and minimize overfloor
                                                                                                    x = (mulmod(x, x, n) + c) n;
                                                                                         50
     11 x = 0, y = a\%;
                                                                                                    y = (mulmod(y, y, n) + c) n;
                                                                                         51
     while (b > 0){
                                                                                                    y = (mulmod(y, y, n) + c) n;
                                                                                         52
       if (b \%2 == 1) x = (x+y) \%c;
                                                                                                    if(x - y \ge 0) d = gcd(x - y, n);
                                                                                         53
       y = (y*2) %c;
                                                                                                    else d = gcd(y - x, n);
                                                                                         54
       b /= 2;
                                                                                                }
                                                                                         55
                                                                                                return d==n? rho(n):d;
                                                                                         56
     return x %c;
10
                                                                                         57
11
12
                                                                                            map<ll,ll> prim;
   ll expmod (ll b, ll e, ll m){\frac{1}{0}}
13
                                                                                            void factRho (ll n){ //O (lg n)^3. un solo numero
     if(!e) return 1;
14
                                                                                              if (n == 1) return;
     11 q= expmod(b,e/2,m); q=mulmod(q,q,m);
15
                                                                                              if (rabin(n)){
     return e %2? mulmod(b,q,m) : q;
16
                                                                                                prim[n]++;
                                                                                         63
17
                                                                                                return;
                                                                                         64
18
                                                                                         65
   bool es_primo_prob (ll n, int a)
19
                                                                                              11 factor = rho(n):
20
                                                                                              factRho(factor):
     if (n == a) return true;
^{21}
                                                                                              factRho(n/factor);
     11 s = 0, d = n-1;
                                                                                         69 }
     while (d \% 2 == 0) s++, d/=2;
23
                                                                                                                                  GCD
24
     11 x = expmod(a,d,n);
25
     if ((x == 1) \mid | (x+1 == n)) return true;
                                                                                          1 | tipo gcd(tipo a, tipo b){return a?gcd(b %a, a):b;}
```

```
void extendedEuclid (ll a, ll b) \{ //a * x + b * y = d \}
                                                                                                tipo a = mcd(q, o.q);
                                                                                        26
     if (!b) { x = 1; y = 0; d = a; return;}
                                                                                               return frac(p*(o.q/a)+o.p*(q/a), q*(o.q/a));}
                                                                                        27
     extendedEuclid (b, a%);
                                                                                             frac operator-(const frac& o){
                                                                                        28
                                                                                                tipo a = mcd(q, o.q);
     11 x1 = y;
    11 y1 = x - (a/b) * y;
                                                                                               return frac(p*(o.q/a)-o.p*(q/a), q*(o.q/a));}
    x = x1; y = y1;
                                                                                              frac operator*(frac o){
                                                                                                tipo a = mcd(q,o.p), b = mcd(o.q,p);
                                                                                               return frac((p/b)*(o.p/a), (q/a)*(o.q/b));}
                                        LCM
                                                                                              frac operator/(frac o){
                                                                                        34
                                                                                                tipo a = mcd(q,o.q), b = mcd(o.p,p);
tipo lcm(tipo a, tipo b){return a / gcd(a,b) * b;}
                                                                                        35
                                                                                               return frac((p/b)*(o.q/a),(q/a)*(o.p/b));}
                                                                                        36
                                      Simpson
                                                                                             bool operator<(const frac &o) const{return p*o.q < o.p*q;}//usar comp cuando el
                                                                                                  producto puede dar overflow
  double integral(double a, double b, int n=10000) {//O(n), n=cantdiv
                                                                                             bool operator==(frac o){return p==o.p&&q==o.q;}
                                                                                        38
     double area=0, h=(b-a)/n, fa=f(a), fb;
                                                                                        39 };
     forn(i, n){
       fb=f(a+h*(i+1));
                                                                                                                              Polinomio
       area+=fa+ 4*f(a+h*(i+0.5)) +fb, fa=fb;
    }
                                                                                           struct poly {
     return area*h/6.;}
                                                                                                vector<tipo> c://guarda los coeficientes del polinomio
                                                                                               poly(const vector<tipo> &c): c(c) {}
                                       Fraction
                                                                                               poly() {}
bool comp(tipo a, tipo b, tipo c, tipo d){//a*d < b*c}
                                                                                               void simplify(){
       int s1 = signo(a)*signo(d), s2 = signo(b)*signo(c);
                                                                                               int i = 0;
       if(s1 == 0) return s2 > 0;
                                                                                               /*tipo a0=0;
                                                                                               while(a0 == 0 && i < sz(c)) a0 = c[i], i++;*/
       if(s2 == 0) return s1 < 0;
                                                                                               int j = sz(c)-1;
       if(s1 > 0 and s2 < 0) return false:
       if(s1 < 0 and s2 > 0) return true:
                                                                                                tipo an=0:
       if(a / b != c / d) return a/b < c/d; //asume que b y d son positivos
                                                                                                while(an == 0 \&\& j >= i) an = c[j], j--;
       a \not= b, c \not= d;
                                                                                                vector<tipo> d;
                                                                                        12
       /*O(1) pero con double:
                                                                                               forr(k,i,j) d.pb(c[k]);
                                                                                        13
       long double d1 = ((long double)(a))/(b), d2 = ((long double)(c))/(d);
                                                                                                c=d;
10
                                                                                        14
       return d1 + EPS < d2;
                                                                                        15
11
                                                                                              bool isnull() { simplify(); return c.empty();}
12
                                                                                        16
       return comp(d, c, b, a);
                                                                                               poly operator+(const poly &o) const {
13
                                                                                        17
                                                                                                    int m = sz(c), n = sz(o.c);
14
                                                                                        18
                                                                                                    vector<tipo> res(max(m,n));
                                                                                        19
15
   tipo mcd(tipo a, tipo b){ return a ? mcd(b%,a) : b; }
                                                                                                    forn(i, m) res[i] += c[i];
                                                                                        20
   struct frac{
                                                                                                   forn(i, n) res[i] += o.c[i];
                                                                                        21
                                                                                                    return poly(res);
     tipo p,q;
                                                                                        22
     frac(tipo p=0, tipo q=1):p(p),q(q) {norm();}
                                                                                               poly operator*(const tipo cons) const {
19
                                                                                        23
     void norm(){
                                                                                               vector<tipo> res(sz(c));
20
                                                                                        24
       tipo a = mcd(p,q);
                                                                                                    forn(i, sz(c)) res[i]=c[i]*cons;
                                                                                        25
21
       if(a) p/=a, q/=a;
                                                                                                    return poly(res); }
22
                                                                                        26
                                                                                               poly operator*(const poly &o) const {
       else q=1;
23
                                                                                        27
       if (q<0) q=-q, p=-p;}
                                                                                                    int m = sz(c), n = sz(o.c);
                                                                                        28
     frac operator+(const frac& o){
                                                                                                    vector<tipo> res(m+n-1);
```

```
Li = Li * (1.0 / Li.eval(x[i])); // here put a multiple of the coefficients
           forn(i, m) forn(j, n) res[i+j]+=c[i]*o.c[j];
30
                                                                                                    instead of 1.0 to avoid using double -- si se usa mod usar el inverso!
           return poly(res); }
31
     tipo eval(tipo v) {
                                                                                                S = S + Li * y[i]; }
32
       tipo sum = 0:
                                                                                             return S:
       dforn(i, sz(c)) sum=sum*v + c[i];
                                                                                        76 }
       return sum; }
                                                                                                                              Ec. Lineales
       //poly contains only a vector<int> c (the coeficients)
     //the following function generates the roots of the polynomial
                                                                                            bool resolver_ev(Mat a, Vec y, Vec &x, Mat &ev){
    /it can be easily modified to return float roots
                                                                                              int n = a.size(), m = n?a[0].size():0, rw = min(n, m);
     set<tipo> roots(){
39
                                                                                              vector<int> p; forn(i,m) p.push back(i);
       set<tipo> roots;
40
                                                                                              forn(i, rw) {
       simplify();
41
                                                                                                int uc=i. uf=i:
       if(c[0]) roots.insert(0);
42
                                                                                                forr(f, i, n) forr(c, i, m) if(fabs(a[f][c])>fabs(a[uf][uc])) {uf=f;uc=c;}
       int i = 0;
                                                                                                if (feq(a[uf][uc], 0)) { rw = i; break; }
       tipo a0=0;
44
                                                                                                forn(j, n) swap(a[j][i], a[j][uc]);
       while(a0 == 0 && i < sz(c)) a0 = abs(c[i]), i++;
45
                                                                                                swap(a[i], a[uf]); swap(y[i], y[uf]); swap(p[i], p[uc]);
       tipo an = abs(c[sz(c)-1]);
46
                                                                                                tipo inv = 1 / a[i][i]; //aca divide
       vector<tipo> ps,qs;
                                                                                                forr(j, i+1, n) {
47
       forr(p,1,sqrt(a0)+1) if (a0 \%==0) ps.pb(p),ps.pb(a0/p);
                                                                                                  tipo v = a[i][i] * inv;
48
       forr(q,1,sqrt(an)+1) if (an \% ==0) qs.pb(q),qs.pb(an/q);
                                                                                                  forr(k, i, m) a[j][k]-=v * a[i][k];
49
       forall(pt,ps)
50
                                                                                                  y[j] = v*y[i];
                                                                                        14
         forall(qt,qs) if ((*pt) %(*qt)==0) { //sacar esto para obtener todas las
51
             raices racionales
                                                                                              } // rw = rango(a), aca la matriz esta triangulada
           tipo root = abs((*pt) / (*qt));
                                                                                              forr(i, rw, n) if (!feq(y[i],0)) return false; // checkeo de compatibilidad
52
           if (eval(root)==0) roots.insert(root);
53
                                                                                              x = \text{vector} < \text{tipo} > (m, 0);
           if (eval((-1)*root)==0) roots.insert((-1)*root);// las raices tambien
                                                                                              dforn(i, rw){
54
               pueden ser negativas!
                                                                                                tipo s = v[i];
                                                                                               forr(j, i+1, rw) s -= a[i][j]*x[p[j]];
55
                                                                                        21
       return roots; }
                                                                                                x[p[i]] = s / a[i][i]; //aca divide
56
                                                                                        22
57
   pair<poly,tipo> ruffini(const poly p, tipo r) { //divive el polinomio p por (x-r)
                                                                                              ev = Mat(m-rw, Vec(m, 0)); // Esta parte va SOLO si se necesita el ev
     int n = sz(p.c) - 1;
                                                                                              forn(k, m-rw) {
     vector<tipo> b(n);
60
                                                                                                ev[k][p[k+rw]] = 1;
     b[n-1] = p.c[n];
61
                                                                                                dforn(i, rw){
     dforn(k,n-1) b[k] = p.c[k+1] + r*b[k+1];
62
                                                                                                  tipo s = -a[i][k+rw];
     tipo resto = p.c[0] + r*b[0];
63
                                                                                                  forr(j, i+1, rw) s -= a[i][j]*ev[k][p[i]];
     poly result(b);
                                                                                                  ev[k][p[i]] = s / a[i][i]; //aca divide
64
     return make pair(result, resto);
65
                                                                                                }
                                                                                        31
66
  poly interpolate(const vector<tipo>& x,const vector<tipo>& y) { //O(n^2)
67
                                                                                              return true;
       poly A; A.c.pb(1);
68
       forn(i,sz(x)) { poly aux; aux.c.pb(-x[i]), aux.c.pb(1), A = A * aux; } // A =
69
                                                                                                                                  FFT
            (x-x0) * ... * (x-xn)
     poly S; S.c.pb(0);
                                                                                         1 //~ typedef complex<double> base; //menos codigo, pero mas lento
     forn(i,sz(x)) { poly Li;
                                                                                         2 //elegir si usar complejos de c (lento) o estos
       Li = ruffini(A,x[i]).fst;
                                                                                         3 struct base{
```

```
void toPoly(const string &s, vector<int> &P){//convierte un numero a polinomio
       double r,i;
       base(double r=0, double i=0):r(r), i(i){}
                                                                                                 P.clear():
       double real()const{return r;}
                                                                                                 dforn(i, sz(s)) P.pb(s[i]-'0');}
                                                                                         51
       void operator/=(const int c){r/=c, i/=c;}
                                                                                                                                  Grafos
  };
   base operator*(const base &a, const base &b){
       return base(a.r*b.r-a.i*b.i, a.r*b.i+a.i*b.r);}
                                                                                                                                 Dijkstra
   base operator+(const base &a, const base &b){
11
       return base(a.r+b.r, a.i+b.i);}
                                                                                             #define INF 1e9
12
   base operator-(const base &a, const base &b){
                                                                                             int N;
13
                                                                                             #define MAX_V 250001
       return base(a.r-b.r, a.i-b.i);}
14
   vector<int> rev; vector<base> wlen pw;
                                                                                             vector<ii> G[MAX V];
   inline static void fft(base a[], int n, bool invert) {
                                                                                             //To add an edge use
16
       forn(i, n) if(i<rev[i]) swap(a[i], a[rev[i]]);</pre>
                                                                                             #define add(a, b, w) G[a].pb(make_pair(w, b))
17
     for (int len=2; len<=n; len<<=1) {
                                                                                             ll dijkstra(int s, int t){\frac{1}{0}(|E| \log |V|)}
18
       double ang = 2*M PI/len * (invert?-1:+1);
                                                                                               priority queue<ii, vector<ii>, greater<ii> > Q;
19
       int len2 = len >> 1;
                                                                                               vector<ll> dist(N, INF); vector<int> dad(N, -1);
20
       base wlen (cos(ang), sin(ang));
                                                                                               Q.push(make pair(0, s)); dist[s] = 0;
21
       wlen pw[0] = base(1, 0);
                                                                                               while(sz(Q)){
                                                                                         11
22
           forr(i, 1, len2) wlen pw[i] = wlen pw[i-1] * wlen;
                                                                                                 ii p = Q.top(); Q.pop();
23
       for (int i=0; i<n; i+=len) {
                                                                                                 if(p.snd == t) break;
24
         base t, *pu = a+i, *pv = a+i+len2, *pu end = a+i+len2, *pw = &wlen pw[0];
                                                                                                 forall(it, G[p.snd])
25
                                                                                                   if(dist[p.snd]+it->first < dist[it->snd]){
         for (; pu!=pu end; ++pu, ++pv, ++pw)
26
           t = *pv * *pw, *pv = *pu - t, *pu = *pu + t;
                                                                                                     dist[it->snd] = dist[p.snd] + it->fst;
                                                                                          16
27
                                                                                                     dad[it->snd] = p.snd;
                                                                                         17
28
                                                                                                     Q.push(make_pair(dist[it->snd], it->snd)); }
     }
                                                                                          18
29
     if (invert) forn(i, n) a[i]/= n;}
                                                                                         19
30
   inline static void calc_rev(int n){//precalculo: llamar antes de fft!!
                                                                                               return dist[t];
                                                                                         20
31
       wlen_pw.resize(n), rev.resize(n);
                                                                                               if(dist[t]<INF)//path generator</pre>
                                                                                         21
^{32}
                                                                                                 for(int i=t; i!=-1; i=dad[i])
       int lg=31-_builtin_clz(n);
                                                                                         22
33
                                                                                                   printf("%1%c", i, (i==s?'\n':'\_'));}
       forn(i, n){
                                                                                         23
^{34}
       rev[i] = 0;
35
                                                                                                                              Bellman-Ford
           forn(k, lg) if(i&(1<<k)) rev[i]|=1<<(lg-1-k);</pre>
36
       }}
37
                                                                                             #define INF 1e9
   //multiplica vectores en nlgn
                                                                                             #define MAX_N 1001
   inline static void multiply(const vector<int> &a, const vector<int> &b, vector<int
                                                                                             vector<ii> G[MAX_N];//ady. list with pairs (weight, dst)
       > &res) {
                                                                                             //To add an edge use
     vector<base> fa (a.begin(), a.end()), fb (b.begin(), b.end());
40
                                                                                             #define add(a, b, w) G[a].pb(make_pair(w, b))
       int n=1; while(n < max(sz(a), sz(b))) n <<= 1; n <<= 1;
41
                                                                                             int dist[MAX N];
       calc rev(n);
42
                                                                                             int N; //cantidad de vertices -- setear!!
     fa.resize (n), fb.resize (n);
                                                                                             void bford(int src){//O(VE)
     fft (&fa[0], n, false), fft (&fb[0], n, false);
44
                                                                                               memset(dist,INF,sizeof dist);
     forn(i, n) fa[i] = fa[i] * fb[i];
                                                                                               dist[src]=0;
     fft (&fa[0], n, true);
46
                                                                                               forn(i, N-1) forn(j, N) if(dist[j]!=INF) forall(it, G[j])
     res.resize(n);
47
                                                                                                 dist[it->snd]=min(dist[it->snd], dist[i]+it->fst):
                                                                                          12
       forn(i, n) res[i] = int (fa[i].real() + 0.5); }
                                                                                          13 }
```

}

```
return cost;
                                                                                        18
14
   bool hasNegCycle(){
                                                                                        19 }
     forn(j, N) if(dist[j]!=INF) forall(it, G[j])
                                                                                                                                 Prim
       if(dist[it->snd]>dist[j]+it->fst) return true;
     //inside if: all points reachable from it->snd will have -INF distance(do bfs) ?
                                                                                          vector<ii> G[MAXN];
     return false;
19
                                                                                           bool taken[MAXN];
20 | }
                                                                                           priority_queue<ii, vector<ii>, greater<ii> > pq;//min heap
                                                                                            void process(int v){
                                  Floyd-Warshall
                                                                                               taken[v]=true;
1 //G[i][j] contains weight of edge (i, j) or INF
                                                                                               forall(e, G[v])
                                                                                                   if(!taken[e->second]) pq.push(*e);
   //G[i][i]=0
3 int G[MAX_N] [MAX_N];
4 void floyd(){//O(N^3)
forn(k, N) forn(i, N) if(G[i][k]!=INF) forn(j, N) if(G[k][j]!=INF)
                                                                                           11 prim(){
                                                                                        10
     G[i][j]=min(G[i][j], G[i][k]+G[k][j]);
                                                                                               zero(taken);
                                                                                        11
                                                                                               process(0);
   bool inNegCycle(int v){
                                                                                               11 cost=0;
     return G[v][v]<0;}
                                                                                               while(sz(pq)){
                                                                                        14
    //checks if there's a neg. cycle in path from a to b
                                                                                                   ii e=pq.top(); pq.pop();
                                                                                        15
                                                                                                   if(!taken[e.second]) cost+=e.first, process(e.second);
   bool hasNegCycle(int a, int b){
                                                                                        16
     forn(i, N) if(G[a][i]!=INF && G[i][i]<0 && G[i][b]!=INF)
12
                                                                                        17
       return true;
                                                                                               return cost;
13
                                                                                        18
     return false;
                                                                                        19 | }
14
15 }
                                                                                                                       2-SAT + Tarjan SCC
                                       Kruskal
                                                                                           //We have a vertex representing a var and other for his negation.
const int MAXN=100000:
                                                                                            //Every edge stored in G represents an implication. To add an equation of the form
vector<ii> G[MAXN];
                                                                                                 allb, use addor(a, b)
                                                                                            //MAX=max cant var, n=cant var
  int n;
                                                                                            #define addor(a, b) (G[neg(a)].pb(b), G[neg(b)].pb(a))
   struct Ar{int a,b,w;}; //w y cost deberian tener el mismo tipo
                                                                                            vector<int> G[MAX*2];
   |bool operator<(const Ar& a, const Ar &b){return a.w<b.w;}
                                                                                            //idx[i]=index assigned in the dfs
   vector<Ar> E;
                                                                                            //lw[i]=lowest index(closer from the root) reachable from i
                                                                                            int lw[MAX*2], idx[MAX*2], qidx;
  | 11 kruskal(){ //no hace falta agregar las aristas en las dos direcciones! (en prim
        si)
                                                                                            stack<int> q;
       11 cost=0;
                                                                                            int qcmp, cmp[MAX*2];
9
                                                                                           //verdad[cmp[i]]=valor de la variable i
       sort(E.begin(), E.end());//ordenar aristas de menor a mayor -- OJO cuando
10
                                                                                            bool verdad[MAX*2+1];
           ordena algo no necesariamente las cosas del mismo valor quedan en el mismo
            orden!!
       uf.init(n);
                                                                                           int neg(int x) { return x>=n? x-n : x+n;}
11
                                                                                           void tjn(int v){
       forall(it, E){
12
                                                                                             lw[v]=idx[v]=++qidx;
           if(uf.comp(it->a)!=uf.comp(it->b)){//si no estan conectados
13
               uf.join(it->a, it->b);//conectar
                                                                                             q.push(v), cmp[v]=-2;
                                                                                        17
14
                                                                                             forall(it, G[v]){
               cost+=it->w;
15
                                                                                        18
                                                                                               if(!idx[*it] || cmp[*it]==-2){
                                                                                        19
```

if(!idx[*it]) tjn(*it);

nbc = qV = 0;

```
lw[v]=min(lw[v], lw[*it]);
                                                                                            24 }
21
       }
                                                                                                stack<int> st;
22
     }
                                                                                                void dfs(int u, int pe) \{//0(n + m)\}
23
                                                                                                    L[u] = V[u] = qV++;
     if(lw[v]==idx[v]){
       int x;
                                                                                                   comp[u] = (pe != -1);
                                                                                                    for(auto &ne: G[u]) if (ne != pe){
       do{x=q.top(); q.pop(); cmp[x]=qcmp;}while(x!=v);
                                                                                                    int v = e[ne].u \cdot e[ne].v \cdot u; // x \cdot y \cdot x = y!
       verdad[qcmp] = (cmp[neg(v)] < 0);</pre>
27
                                                                                                    if (V[v] == -1) \{ // \text{ todavia no se lo visito} \}
       qcmp++;
28
                                                                                                      st.push(ne);
29
                                                                                             32
                                                                                                      dfs(v,ne);
30
                                                                                             33
    //remember to CLEAR G!!!
                                                                                                      if (L[v] > V[u]){// bridge \Rightarrow no pertenece a ninguna comp biconexa
                                                                                             34
31
   bool satisf(){\frac{}{0}}
                                                                                                         e[ne].bridge = true;
                                                                                             35
32
     memset(idx, 0, sizeof(idx)), qidx=0;
33
                                                                                             36
     memset(cmp, -1, sizeof(cmp)), qcmp=0;
                                                                                                      if (L[v] \ge V[u]) \{ // art \}
                                                                                             37
34
     forn(i, n){
                                                                                                         int last:
35
       if(!idx[i]) tjn(i);
                                                                                                         do { //todas las aristas que estan entre dos puntos de articulación
36
       if(!idx[neg(i)]) tjn(neg(i));
                                                                                                             pertenecen a la misma componente biconexa
37
                                                                                                           last = st.top(); st.pop();
                                                                                             40
38
     forn(i, n) if(cmp[i]==cmp[neg(i)]) return false;
                                                                                                           e[last].comp = nbc;
39
                                                                                             41
     return true:
                                                                                                         } while (last != ne);
40
                                                                                             42
41 | }
                                                                                                         nbc++;
                                                                                             43
                                                                                                         comp[u]++;
                                                                                             44
                            Comp. Biconexas y Puentes
                                                                                             45
                                                                                                      L[u] = min(L[u], L[v]);
                                                                                             46
const int MAXN=1010;
                                                                                             47
   int n, m;
                                                                                                    else if (V[v] < V[u]) { // back edge
                                                                                             48
   vector<int> G[MAXN];
                                                                                                       st.push(ne);
                                                                                             49
                                                                                                      L[u] = min(L[u], V[v]);
                                                                                             50
   struct edge {
                                                                                             51
     int u,v, comp;
                                                                                             52
     bool bridge;
                                                                                             53
   |};
   vector<edge> e;
                                                                                                set<int> C[2*MAXN];
   void addEdge(int u, int v) {
                                                                                                int compnodo[MAXN];
     G[u].pb(sz(e)), G[v].pb(sz(e));
11
                                                                                                int ptoart;
     e.pb((edge){u,v,-1,false});
12
                                                                                                 void blockcuttree(){
                                                                                             58
13
                                                                                                    ptoart = 0; zero(compnodo);
                                                                                             59
    //V[i]=id de la dfs
                                                                                                    forn(i,2*MAXN) C[i].clear();
    //L[i]=lowest id reachable from i
                                                                                                    for(auto &it: e){
                                                                                             61
   int V[MAXN], L[MAXN], qV;
                                                                                                         int u = it.u, v = it.v;
                                                                                             62
   int nbc;//cant componentes
                                                                                                         if(comp[u] == 1) compnodo[u] = it.comp;
   int comp[MAXN];//comp[i]=cant comp biconexas a la cual pertenece i
                                                                                                         else{
                                                                                             64
   void initDfs(int n) {
                                                                                                             if(compnodo[u] == 0){ compnodo[u] = nbc+ptoart; ptoart++;}
     zero(G), zero(comp);
                                                                                                                 C[it.comp].insert(compnodo[u]);
                                                                                             66
     e.clear();
21
                                                                                                                 C[compnodo[u]].insert(it.comp);
                                                                                             67
     forn(i,n) V[i]=-1;
                                                                                                         }
```

```
if(comp[v] == 1) compnodo[v] = it.comp;
                                                                                                    a=f[a][i], d-=1<<i;
                                                                                          21
69
           else
                                                                                                  return a;
70
                                                                                          22
               if(compnodo[v] == 0){ compnodo[v] = nbc+ptoart; ptoart++;}
                                                                                          23
                   C[it.comp].insert(compnodo[v]);
                                                                                              int lca(int a, int b){\frac{1}{0}}
                   C[compnodo[v]].insert(it.comp);
                                                                                               if(L[a]<L[b]) swap(a, b);</pre>
73
           }
                                                                                                a=climb(a, L[a]-L[b]);
74
                                                                                               if(a==b) return a;
75
                                                                                                dforn(i, lg(L[a])+1)
76
                                                                                                 if(f[a][i]!=f[b][i])
77
   int main() {
                                                                                                    a=f[a][i], b=f[b][i];
78
     while(cin >> n >> m){
                                                                                               return f[a][0];
79
                                                                                          31
       initDfs(n);
                                                                                          32
80
       forn(i, m){
                                                                                              int dist(int a, int b) {//returns distance between nodes
81
                                                                                               return L[a]+L[b]-2*L[lca(a, b)];}
         int a,b; cin >> a >> b;
82
         addEdge(a,b);
83
                                                                                                                     Heavy Light Decomposition
       }
84
           dfs(0,-1);
85
                                                                                            int treesz[MAXN];//cantidad de nodos en el subarbol del nodo v
           forn(i, n) cout << "comp[" << i << "] = " << comp[i] << endl;
86
                                                                                              int dad[MAXN];//dad[v]=padre del nodo v
       for(auto &ne: e) cout << ne.u << "->" << ne.v << "_en,la,comp.__" << ne.comp <<
87
                                                                                              void dfs1(int v, int p=-1){//pre-dfs
             endl:
                                                                                               dad[v]=p;
       cout << "Cant., de, componentes, biconexas, =, " << nbc << endl;
88
                                                                                               treesz[v]=1;
     }
89
                                                                                               forall(it, G[v]) if(*it!=p){
       return 0;
90
                                                                                                 dfs1(*it, v);
91 |}
                                                                                                 treesz[v]+=treesz[*it];
                                    LCA + Climb
                                                                                          10
const int MAXN=100001;
                                                                                              //PONER Q EN O !!!!!
                                                                                             int pos[MAXN], q;//pos[v]=posicion del nodo v en el recorrido de la dfs
2 const int LOGN=20;
  //f[v][k] holds the 2^k father of v
                                                                                              //Las cadenas aparecen continuas en el recorrido!
   //L[v] holds the level of v
                                                                                              int cantcad:
                                                                                              int homecad[MAXN];//dada una cadena devuelve su nodo inicial
   int f [MAXN] [LOGN] , L [MAXN] ;
                                                                                              int cad[MAXN];//cad[v]=cadena a la que pertenece el nodo
   //call before build:
                                                                                              void heavylight(int v, int cur=-1){
   void dfs(int v, int fa=-1, int lvl=0){//generate required data
                                                                                          17
                                                                                               if(cur==-1) homecad[cur=cantcad++]=v;
     f[v][0]=fa, L[v]=lvl;
                                                                                          18
     forall(it, G[v])if(*it!=fa)
                                                                                               pos[v]=q++;
                                                                                          19
                                                                                                cad[v]=cur;
       dfs(*it, v, lvl+1);
                                                                                          20
10
                                                                                                int mx=-1;
                                                                                          21
11
                                                                                               forn(i, sz(G[v])) if(G[v][i]!=dad[v])
   void build(int N){//f[i][0] must be filled previously, O(nlgn)
                                                                                                 if(mx==-1 || treesz[G[v][mx]]<treesz[G[v][i]]) mx=i;</pre>
     forn(k, LOGN-1) forn(i, N) f[i] [k+1]=f[f[i][k]][k];}
13
                                                                                          23
                                                                                                if(mx!=-1) heavylight(G[v][mx], cur);
                                                                                          24
                                                                                               forn(i, sz(G[v])) if(i!=mx && G[v][i]!=dad[v])
   #define lg(x) (31-_builtin_clz(x))//=floor(log2(x))
15
                                                                                          25
                                                                                                 heavylight(G[v][i], -1);
                                                                                          26
   int climb(int a, int d){\frac{}{(\log n)}}
                                                                                          27
17
                                                                                              //ejemplo de obtener el maximo numero en el camino entre dos nodos
     if(!d) return a;
     dforn(i, lg(L[a])+1)
                                                                                              //RTA: max(query(low, u), query(low, v)), con low=lca(u, v)
       if(1<<i<=d)
                                                                                             //esta funcion va trepando por las cadenas
```

```
int query(int an, int v){\frac{1}{10000}}
     //si estan en la misma cadena:
                                                                                              //encuentra el ciclo euleriano, el grafo debe ser conexo y todos los nodos tener
     if(cad[an] == cad[v]) return rmq.get(pos[an], pos[v]+1);
                                                                                                  grado par para que exista
     return max(query(an, dad[homecad[cad[v]]]),
                                                                                             //para encontrar el camino euleriano conectar los dos vertices de grado impar y
            rmq.get(pos[homecad[cad[v]]], pos[v]+1));
                                                                                                  empezar de uno de ellos.
35
36 | }
                                                                                          12
                                                                                             queue<list<int>::iterator> q;
                             Centroid Decomposition
                                                                                             int get(int v){
                                                                                               while(used[v]<sz(G[v]) && usede[ G[v][used[v]] ]) used[v]++;</pre>
1 | int n:
                                                                                               return used[v];
vector<int> G[MAXN];
                                                                                          16
3 bool taken[MAXN];//poner todos en FALSE al principio!!
                                                                                          17
                                                                                              void explore(int v, int r, list<int>::iterator it){
  int padre [MAXN];//padre de cada nodo en el centroid tree
                                                                                          18
                                                                                               int ar=G[v][get(v)]; int u=v^ars[ar];
                                                                                          19
                                                                                               usede[ar]=true:
   int szt[MAXN]:
                                                                                               list<int>::iterator it2=path.insert(it, u);
   void calcsz(int v, int p) {
                                                                                               if(u!=r) explore(u, r, it2);
     szt[v] = 1:
                                                                                               if(get(v)<sz(G[v])) q.push(it);</pre>
     forall(it,G[v]) if (*it!=p && !taken[*it])
                                                                                          23
                                                                                          24
       calcsz(*it,v), szt[v]+=szt[*it];
10
                                                                                              void euler(int a){
                                                                                          25
11
                                                                                               zero(used), zero(usede);
   void centroid(int v=0, int f=-1, int lvl=0, int tam=-1) {//O(nlogn)
                                                                                          26
^{12}
                                                                                               path.clear();
     if(tam==-1) calcsz(v, -1), tam=szt[v];
                                                                                          27
                                                                                               q=queue<list<int>::iterator>();
     forall(it, G[v]) if(!taken[*it] && szt[*it]>=tam/2)
                                                                                          28
14
                                                                                               path.push_back(a); q.push(path.begin());
       {szt[v]=0; centroid(*it, f, lvl, tam); return;}
                                                                                          29
15
                                                                                               while(sz(q)){
     taken[v]=true;
                                                                                          30
                                                                                                 list<int>::iterator it=q.front(); q.pop();
     padre[v]=f;
                                                                                          31
17
                                                                                                 if(used[*it] <sz(G[*it])) explore(*it, *it, it);</pre>
     /*Analizar todos los caminos que pasan por este nodo:
                                                                                          32
18
                                                                                          33
      * Agregar la informacion de cada subarbol
19
                                                                                               reverse(path.begin(), path.end());
      * Para cada subarbol:
                                                                                          34
20
                                                                                          35
      * -sacar la informacion
21
                                                                                              void addEdge(int u, int v){
      * -analizar
                                                                                          36
                                                                                               G[u].pb(eq), G[v].pb(eq);
                                                                                          37
      * -agregar de nuevo la informacion
                                                                                               ars[eq++]=u^v;
                                                                                          38
                                                                                          39 | }
     forall(it, G[v]) if(!taken[*it])
25
       centroid(*it, v, lvl+1, -1);
26
                                                                                                                             Diametro árbol
27 |}
                                                                                             vector<int> G[MAXN]; int n,m,p[MAXN],d[MAXN],d2[MAXN];
                                     Euler Cycle
                                                                                             int bfs(int r, int *d) {
   #define MAXN 1005
                                                                                               queue<int> q;
                                                                                               d[r]=0; q.push(r);
   #define MAXE 1005005
                                                                                               int v;
4 | int n,ars[MAXE], eq;
                                                                                               while(sz(q)) { v=q.front(); q.pop();
vector<int> G[MAXN];//fill G,ars,eq
                                                                                                 forall(it,G[v]) if (d[*it]==-1)
6 | list<int> path;
                                                                                                    d[*it]=d[v]+1, p[*it]=v, q.push(*it);
7 | int used[MAXN]; //used[v] = i => para todo j<=i la arista v-G[v][j] fue usada y la
         arista v-G[v][i+1] no se uso
                                                                                               return v;//ultimo nodo visitado
8 bool usede[MAXE];
                                                                                          11 |}
```

struct UnionFind {

```
vector<int> diams; vector<ii> centros;
   void diametros(){
     memset(d,-1,sizeof(d));
     memset(d2,-1,sizeof(d2));
     diams.clear(), centros.clear();
     forn(i, n) if(d[i]==-1){
17
       int v,c;
18
       c=v=bfs(bfs(i, d2), d);
       forn(_,d[v]/2) c=p[c];
20
       diams.pb(d[v]);
21
       if(d[v]&1) centros.pb(ii(c, p[c]));
22
       else centros.pb(ii(c, c));
23
^{24}
25 }
```

Chu-liu

```
void visit(graph&h,int v,int s,int r,vector<int>&no,vector<vector<int>&comp,
      vector<int>&prev,vector<vector<int>>&next,vector<weight>&mcost,vector<int>&
      mark,weight&cost,bool&found){if(mark[v]){vector<int>temp=no;found=true;do{cost
      +=mcost[v];v=prev[v];if(v!=s){while(comp[v].size()>0){no[comp[v].back()]=s;
      comp[s].push_back(comp[v].back());comp[v].pop_back();}}while(v!=s);forall(j,
      comp[s])if(*j!=r)forall(e,h[*j])if(no[e->src]!=s)e->w-=mcost[temp[*j]];}mark
       [v]=true;forall(i,next[v])if(no[*i]!=no[v]&&prev[no[*i]]==v)if(!mark[no[*i
      ]]||*i==s)visit(h,*i,s,r,no,comp,prev,next,mcost,mark,cost,found);}weight
      minimumSpanningArborescence(const graph&g,int r){const int n=sz(g);graph h(n);
      forn(u,n)forall(e,g[u])h[e->dst].pb(*e);vector<int>no(n);vector<vector<int>>>
      comp(n);forn(u,n)comp[u].pb(no[u]=u);for(weight cost=0;;){vector<int>prev(n
       ,-1); vector<weight>mcost(n,INF); forn(j,n)if(j!=r)forall(e,h[j])if(no[e->src]!=
      no[i])if(e->w<mcost[ no[i] ])mcost[ no[i] ]=e->w,prev[ no[i] ]=no[e->src];
      vector<vector<int>>next(n);forn(u,n)if(prev[u]>=0)next[ prev[u] ].push back(u)
       ; bool stop=true; vector < int > mark(n); forn(u,n) if (u!=r&&!mark[u]&&!comp[u].empty
       ()){bool found=false; visit(h,u,u,r,no,comp,prev,next,mcost,mark,cost,found); if
       (found)stop=false;}if(stop){forn(u,n)if(prev[u]>=0)cost+=mcost[u];return cost
       ;}}}
```

Hungarian

```
//Dado un grafo bipartito completo con costos no negativos, encuentra el matching
perfecto de minimo costo.

const tipo EPS=1e-9; const tipo INF=1e14;

#define N 502

tipo cost[N][N],lx[N],ly[N],slack[N]; int n,max_match,xy[N],yx[N],slackx[N],prev2[N 26
]; bool S[N],T[N]; void add_to_tree(int x,int prevx){S[x]=true,prev2[x]=prevx;
forn(y,n)if(lx[x]+ly[y]-cost[x][y]<slack[y]-EPS)slack[y]=lx[x]+ly[y]-cost[x][y
],slackx[y]=x;}void update_labels(){tipo delta=INF;forn(y,n)if(!T[y])delta=min 28
(delta,slack[y]);forn(x,n)if(S[x])lx[x]-=delta;forn(y,n)if(T[y])ly[y]+=delta;
else slack[y]-=delta;}void init_labels(){zero(lx),zero(ly);forn(x,n)forn(y,n) 30}
```

```
 lx[x] = max(lx[x], cost[x][y]); \\ lx[x] = max(lx[x], cost[x]); \\ lx[x] = ma
```

Dynamic Connectivity

```
int n, comp;
       vector<int> pre,si,c;
       UnionFind(int n=0):n(n), comp(n), pre(n), si(n, 1) {
           forn(i,n) pre[i] = i; }
       int find(int u){return u==pre[u]?u:find(pre[u]);}
       bool merge(int u, int v) {
           if((u=find(u))==(v=find(v))) return false;
           if(si[u]<si[v]) swap(u, v);</pre>
           si[u]+=si[v], pre[v]=u, comp--, c.pb(v);
11
           return true:
       }
       int snap(){return sz(c);}
       void rollback(int snap){
           while(sz(c)>snap){
               int v = c.back(); c.pop back();
                si[pre[v]] -= si[v], pre[v] = v, comp++;
           }
       }
19
20
   enum {ADD,DEL,QUERY};
   struct Query {int type,u,v;};
   struct DynCon {
       vector<Query> q;
24
       UnionFind dsu;
       vector<int> match,res;
       map<ii,int> last;//se puede no usar cuando hay identificador para cada arista
            (mejora poco)
       DynCon(int n=0):dsu(n){}
       void add(int u, int v) {
           if(u>v) swap(u,v);
```

31

q.pb((Query){ADD, u, v}), match.pb(-1);

szC[0] = szC[1] = 1;

```
last[ii(u,v)] = sz(q)-1;
                                                                                                if(sz(G[a])){
32
                                                                                           14
       }
                                                                                                  S[0][szS[0]++] = a;//.push(a);
       void remove(int u, int v) {
                                                                                                   it[a] = G[a].begin();
34
           if(u>v) swap(u,v);
                                                                                           17
           q.pb((Query){DEL, u, v});
                                                                                           18
36
           int prev = last[ii(u,v)];
                                                                                                if(sz(G[b])){
37
                                                                                           19
           match[prev] = sz(q)-1;
                                                                                                   S[1][szS[1]++] = b;//.push(b);
38
           match.pb(prev);
                                                                                                   it[b] = G[b].begin();
39
                                                                                           21
40
                                                                                           22
       void query() {//podria pasarle un puntero donde guardar la respuesta
                                                                                                 int act = 0;
                                                                                           23
41
           q.pb((Query){QUERY, -1, -1}), match.pb(-1);}
                                                                                                 vis[a] = vis[b] = true;
42
       void process() {
43
           forn(i,sz(q)) if (q[i].type == ADD && match[i] == -1) match[i] = sz(q);
                                                                                               //recorre las dos componentes en paralelo
44
                                                                                                 while(szS[act]){
           go(0,sz(q));
45
                                                                                                   int v = S[act][szS[act]-1];//.top();
       }
46
       void go(int 1, int r) {
                                                                                                   int u = *it[v];
47
                                                                                           29
           if(l+1==r){
                                                                                                   it[v]++:
48
               if (q[1].type == QUERY)//Aqui responder la query usando el dsu!
                                                                                                   if(it[v] == G[v].end()) szS[act]--;//.pop();
49
                    res.pb(dsu.comp);//aqui query=cantidad de componentes conexas
                                                                                                   if(vis[u]){act = 1 - act; continue;}
50
                                                                                                   szC[act]++;
               return;
                                                                                           33
51
                                                                                                   if(sz(G[u])>1 \text{ or } *G[u].begin() != v){
                                                                                           34
52
                                                                                                     S[act][szS[act]++] = u;//.push(u);
           int s=dsu.snap(), m = (l+r) / 2;
                                                                                           35
53
           forr(i,m,r) if(match[i]!=-1 && match[i]<1) dsu.merge(q[i].u, q[i].v);</pre>
                                                                                                     vis[u] = true;
54
                                                                                                     it[u] = G[u].begin();
           go(1,m);
55
                                                                                           37
           dsu.rollback(s);
                                                                                           38
56
           s = dsu.snap();
                                                                                                   act = 1 - act;
57
                                                                                           39
           forr(i,1,m) if(match[i]!=-1 && match[i]>=r) dsu.merge(q[i].u, q[i].v);
                                                                                           40
58
           go(m,r);
                                                                                                 //ya recorrio la toda la componente de act
                                                                                           41
59
            dsu.rollback(s);
                                                                                                 act = 1 - act;
60
                                                                                           42
61
                                                                                           43
                                                                                                //sigue recorriendo la otra componente hasta que ve un elemento mas o no tiene
62 | }dc;
                                                                                           44
                                                                                                     mas elementos.
                                    DFS Paralelo
                                                                                                 while(szC[act] < szC[1-act]+1 and szS[act]){</pre>
                                                                                           45
                                                                                                  int v = S[act][szS[act]-1];//.top();
                                                                                           46
   #define MAXN 212345
                                                                                                   int u = *it[v];
                                                                                           47
                                                                                                   it[v]++:
                                                                                           48
   set<int> G[MAXN];
                                                                                                   if(it[v] == G[v].end()) szS[act]--;//.pop();
                                                                                           49
                                                                                                   if(vis[u]) continue;
                                                                                           50
   set<int>::iterator it[MAXN];
                                                                                                   szC[act]++;
                                                                                           51
  int S[2] [MAXN];//pila
                                                                                                   if(sz(G[u])>1 \text{ or } *G[u].begin() != v){
7 int szS[2];//tamano de la pila
                                                                                                     S[act][szS[act]++] = u;//.push(u);
8 int szC[2];//tamano de la componente
                                                                                                     vis[u] = true;
9 bool vis[MAXN];
                                                                                                     it[u] = G[u].begin();
                                                                                           55
void dfsparalelo(int a, int b){ //O(componente mas chica)
                                                                                           56
     zero(vis):
                                                                                           57
     szS[0] = szS[1] = 0:
```

58

59 }

```
Network Flow
                                         Dinic
                                                                                         41
2 const int MAX = 300;
                                                                                         44
3 // Corte minimo: vertices con dist[v]>=0 (del lado de src) VS. dist[v]==-1 (del
       lado del dst)
                                                                                         46
4 // Para el caso de la red de Bipartite Matching (Sean V1 y V2 los conjuntos mas
                                                                                         47
       proximos a src y dst respectivamente):
                                                                                         48
5 // Reconstruir matching: para todo v1 en V1 ver las aristas a vertices de V2 con
                                                                                                     }
                                                                                         49
       it->f>0, es arista del Matching
   // Min Vertex Cover: vertices de V1 con dist[v]==-1 + vertices de V2 con dist[v]>0
                                                                                                 return 0;
                                                                                         51
   // Max Independent Set: tomar los vertices NO tomados por el Min Vertex Cover
                                                                                         52
8 // Max Clique: construir la red de G complemento (debe ser bipartito!) y encontrar
                                                                                         53
        un Max Independet Set
   // Min Edge Cover: tomar las aristas del matching + para todo vertices no cubierto
                                                                                                 11 result=0;
                                                                                         55
        hasta el momento, tomar cualquier arista de el
                                                                                         56
   //Complejidad:
                                                                                         57
   //Peor caso: O(V^2E)
                                                                                         58
    //Si todas las capacidades son 1: O(min(E^1/2,V^2/3)E)
                                                                                         59
   //Para matching bipartito es: O(sqrt(V)E)
13
                                                                                         60
14
                                                                                         61
  int nodes, src, dst;
  int dist[MAX], q[MAX], work[MAX];
                                                                                         62
  struct Edge {
17
       int to, rev;
18
       ll f, cap;
19
       Edge(int to, int rev, ll f, ll cap) : to(to), rev(rev), f(f), cap(cap) {}
20
  |};
                                                                                             typedef 11 tf;
21
   vector<Edge> G[MAX];
                                                                                             typedef 11 tc;
   void addEdge(int s, int t, ll cap){
23
       G[s].pb(Edge(t, sz(G[t]), 0, cap)), G[t].pb(Edge(s, sz(G[s])-1, 0, 0));
24
   bool dinic bfs(){
                                                                                             struct edge {
25
       fill(dist, dist+nodes, -1), dist[src]=0;
                                                                                               int u, v;
26
       int qt=0; q[qt++]=src;
                                                                                               tf cap, flow;
27
       for(int qh=0; qh<qt; qh++){</pre>
                                                                                               tc cost;
28
           int u =q[qh];
29
           forall(e, G[u]){
30
               int v=e->to;
31
               if(dist[v]<0 \&\& e->f < e->cap)
32
                   dist[v]=dist[u]+1, q[qt++]=v;
           }
```

```
35
       return dist[dst]>=0;
36
37
   11 dinic dfs(int u, 11 f){
       if(u==dst) return f;
       for(int &i=work[u]; i<sz(G[u]); i++){</pre>
           Edge &e = G[u][i];
           if(e.cap<=e.f) continue;</pre>
           int v=e.to;
           if(dist[v]==dist[u]+1){
                   11 df=dinic_dfs(v, min(f, e.cap-e.f));
                    if(df>0){
                            e.f+=df, G[v][e.rev].f-= df;
                            return df; }
   ll maxFlow(int src, int dst){
       src=_src, dst=_dst;
       while(dinic bfs()){
           fill(work, work+nodes, 0);
           while(ll delta=dinic_dfs(src,INF))
                result+=delta;
       // todos los nodos con dist[v]!=-1 vs los que tienen dist[v]==-1 forman el min
       return result; }
```

Min-cost Max-flow

```
const int MAXN=10000;
typedef ll tf;
typedef ll tc;
const tf INFFLUJO = 1e14;
const tc INFCOSTO = 1e14;
struct edge {
  int u, v;
  tf cap, flow;
  tc cost;
  tf rem() { return cap - flow; }
};
int nodes; //numero de nodos
vector<int> G[MAXN]; // limpiar!
vector<edge> e; // limpiar!
void addEdge(int u, int v, tf cap, tc cost) {
```

```
G[u].pb(sz(e)); e.pb((edge)\{u,v,cap,0,cost\});
     G[v].pb(sz(e)); e.pb((edge){v,u,0,0,-cost});
17
18
   tc dist[MAXN], mnCost;
   int pre[MAXN];
   tf cap[MAXN], mxFlow;
   bool in_queue[MAXN];
   void flow(int s, int t) {
     zero(in_queue);
24
     mxFlow=mnCost=0;
25
     while(1){
26
       fill(dist, dist+nodes, INFCOSTO); dist[s] = 0;
27
       memset(pre, -1, sizeof(pre)); pre[s]=0;
28
       zero(cap); cap[s] = INFFLUJO;
29
       queue<int> q; q.push(s); in queue[s]=1;
30
       while(sz(q)){
31
         int u=q.front(); q.pop(); in_queue[u]=0;
32
         for(auto it:G[u]) {
33
            edge &E = e[it];
34
            if(E.rem() \&\& dist[E.v] > dist[u] + E.cost + 1e-9){ // ojo EPS}
35
              dist[E.v] = dist[u] + E.cost;
36
             pre[E.v] = it;
37
             cap[E.v] = min(cap[u], E.rem());
38
             if(!in_queue[E.v]) q.push(E.v), in_queue[E.v]=1;
39
40
         }
41
^{42}
       if (pre[t] == -1) break;
43
       mxFlow +=cap[t];
44
       mnCost +=cap[t]*dist[t];
^{45}
       for (int v = t; v != s; v = e[pre[v]].u) {
46
          e[pre[v]].flow += cap[t];
47
         e[pre[v]^1].flow -= cap[t];
48
       }
49
     }
50
51 }
```

Template

```
#include <bits/stdc++.h>
using namespace std;
#define forr(i,a,b) for(int i=(a); i<(b); i++)

#define forn(i,n) forr(i,0,n)

#define zero(v) memset(v, 0, sizeof(v))

#define forall(it,v) for(auto it=v.begin();it!=v.end();++it)

#define pb push_back</pre>
```

```
#define fst first
#define snd second
typedef long long ll;
typedef pair<11,11> pll;
#define dforn(i,n) for(int i=n-1; i>=0; i--)

int main() {
   ios::sync_with_stdio(0); cin.tie(0);
   return 0;
}
```

Ayudamemoria

Doubles Comp.

```
const double EPS = 1e-9;
define feq(a, b) (fabs((a)-(b))<EPS)
  x == y <=> fabs(x-y) < EPS
  x > y <=> x > y + EPS
  x >= y <=> x > y - EPS
```

Expandir pila

```
#include <sys/resource.h>
rlimit rl;
getrlimit(RLIMIT_STACK, &rl);
rl.rlim_cur=1024L*1024L*256L;//256mb
setrlimit(RLIMIT_STACK, &rl);
```

Iterar subconjunto

```
for(int sbm=bm; sbm; sbm=(sbm-1)&bm)
```