

Question 1:

A = [31, 41, 59, 26, 41, 58]

(Note: The sorted part will be colored red and arrays are counted from 1)

1st iteration: i = 2,

A = [31, 41, 59, 26, 41, 58]

Number of iterations executed: 0

More precisely: only one comparison operation ($1 > 0 \ \&\& \ 31 > 41$), which returns False and breaks the **while** loop.

2nd iteration: i = 3,

A = [31, 41, 59, 26, 41, 58]

Number of iterations executed: 0

More precisely: ($2 > 0 \ \&\& \ 41 > 59$) => False, breaks **while** loop

3rd iteration: i = 4,

A = [26, 31, 41, 59, 41, 58]

Number of iterations executed: 3

More precisely: ($3 > 0 \ \&\& \ 59 > 26$) => True

($2 > 0 \ \&\& \ 41 > 26$) => True

($1 > 0 \ \&\& \ 31 > 26$) => True

($0 > 0 \ \&\& \ A[0] > 26$) => False, breaks **while** loop

4th iteration: i = 5,

A = [26, 31, 41, 41, 59, 58]

Number of iterations executed: 1

More precisely: ($4 > 0 \ \&\& \ 59 > 41$) => True

($3 > 0 \ \&\& \ 41 > 41$) => False, breaks **while** loop

5th iteration: i = 6,

A = [26, 31, 41, 41, 58, 59]

Number of iterations executed: 1

More precisely: ($5 > 0 \ \&\& \ 59 > 58$) => True

($4 > 0 \ \&\& \ 41 > 58$) => False, breaks **while** loop

Question 2:

A = [4, 3, 2, 1]

1st iteration: A = [3, 4, 2, 1], number of basic operations: 2

2nd iteration: A = [2, 3, 4, 1], number of basic operations: 3

3rd iteration: A = [1, 2, 3, 4], number of basic operations: 4

=> Total: 2 + 3 + 4 = 9 basic operations.

B = [1, 2, 3, 4]

1st iteration: A = [1, 2, 3, 4], number of basic operations: 1

2nd iteration: A = [1, 2, 3, 4], number of basic operations: 1

3rd iteration: A = [1, 2, 3, 4], number of basic operations: 1

=> Total: 1 + 1 + 1 = 3 basic operations.

C = [3, 1, 4, 2]

1st iteration: A = [1, 3, 4, 2], number of basic operations: 2

2nd iteration: A = [1, 3, 4, 2], number of basic operations: 1

3rd iteration: A = [1, 2, 3, 4], number of basic operations: 3

=> Total: 2 + 1 + 3 = 6 basic operations.

The detailed solution for each operation should be similar to that of question 1. Note that the number of basic operations (the number of comparison operations in the **while** clause) is different from the number of iterations (the number of times the **while** loop iterates successfully).

Question 3:

InsertionSort(A[1..n])

for (*i* = 2; *i* <= *n*; *i*++)

 v = A[i];

 j = i - 1;

 while (*j* > 0 & A[j] > v)

 A[j + 1] = A[j];

 j--;

 A[j + 1] = v;

We simply alter the comparison criterion in the **while** loop so that the larger numbers are “pulled” towards the head of the array.

Question 4:

Elementary operation: ($i \leq n-1$ & ascending).

Size of the input: n (The length of the input array).

Worst-case input: L is already sorted in ascending order.

Number of elementary operations performed: n

In particular: ($i \leq n-1$ & ascending) returns True for $n-1$ times, and returns False when $i = n$, which will then break the **while** loop.

Best-case input: L is already sorted but in descending order.

Number of elementary operations performed: 2

In particular: The comparison operations ($1 \leq n-1$ & ascending) returns True. Then ascending will be set to False since the array is in descending order and i will be incremented to 2. After that ($2 \leq n-1$ & ascending) returns False and break the **while** loop.