

## FINAL EXAM CALCULUS 2

(90 minutes)

1. Find the area of the parallelogram with vertices  $A(0, 0, 0)$ ,  $B(1, 0, 1)$ ,  $C(2, 1, 3)$ , and  $D(0, -1, 1)$ .

2. Find the curvature of  $\vec{r}(t) = (e^t \cos t, e^t \sin t, t^2)$  at the point  $(1, 0, 0)$ .

3. Evaluate  $\iint_D (x + 2y) dx dy$ , where  $D$  is the domain bounded by  $y = \sqrt{x}$  and  $y = x^2$ .

4. Evaluate  $\iint_D x dx dy$ , where  $D$  is the domain outside the circle  $x^2 + y^2 = 1$  and inside the circle  $x^2 + y^2 = 2x$ .

5. Find the volume of the solid  $E$  enclosed by the planes  $z = 0$  and  $z = x + 2y + 3$  and by the cylinders  $x^2 + y^2 = 4$  and  $x^2 + y^2 = 9$ .

6. Evaluate  $\int_C xy^2 ds$ , where  $C$  is the curve given by  $x = 2 \sin t$ ,  $y = t$ ,  $z = -2 \cos t$ ,  $0 \leq t \leq \pi$ .

7. Using Green's Theorem to evaluate  $\int_C (e^x + x^2 y) dx + (e^y - xy^2) dy$ , where  $C$  is the boundary of the region between the circles  $x^2 + y^2 = 2y$ .

8. Determine whether or not  $\vec{F}$  is a conservative vector field? If it is, find a function  $f$  such that  $\vec{F} = \nabla f$ , where

$$\vec{F}(x, y, z) = e^y \vec{i} + x e^y \vec{j} + (z + 1) e^z \vec{k}.$$

9. Evaluate  $\iint_S z dS$ , where  $S$  is the surface with parametric equations  $x = u^2$ ,  $y = u \sin v$ ,  $z = u \cos v$ ,  $0 \leq u \leq 1$ ,  $0 \leq v \leq \pi/2$ .

10. Using Divergence Theorem to calculate the surface integral  $\iint_S \vec{F} \cdot d\vec{S}$ , where

$$\vec{F}(x, y, z) = (z + xy^2) \vec{i} + (y + x e^{-z}) \vec{j} + (\cos y + x^2 z) \vec{k},$$

and  $S$  is the surface of the solid bounded by paraboloid  $z = x^2 + y^2$  and plane  $z = 9$ .