## 05-Animations of phase space

January 4, 2021

## 1 Setting up the notebook

We begin by setting up the Jupyter notebook and importing the Python modules needed for plotting figures, create animations, etc. We include commands to view plots in the Jupyter notebook, and to create figures with good resolution and large labels. These commands can be customized to produce figures with other specifications.

```
[1]: # Imports python libraries
     import numpy as np
     import random as rd
     import wave
     import sys
     import matplotlib.pyplot as plt
     from matplotlib.pyplot import figure
     sys.path.insert(1, r'./../functions') # add to pythonpath
     #For creating animations and plotting in 3D
     from matplotlib import rc
     import matplotlib.animation as animation
     from JSAnimation import IPython_display
     from mpl_toolkits.mplot3d import Axes3D
     # commands to create high-resolution figures with large labels
     %config InlineBackend.figure_formats = {'png', 'retina'}
     plt.rcParams['axes.labelsize'] = 18 # fontsize for figure labels
     plt.rcParams['axes.titlesize'] = 20 # fontsize for figure titles
     plt.rcParams['font.size'] = 16 # fontsize for figure numbers
     plt.rcParams['lines.linewidth'] = 1.6 # line width for plotting
```

```
[2]: #Function that extracts the number of recording channels, sampling rate, time

→ and signal

#variable is the path and filename of the .wav file

def ecg(variable):

record = wave.open(variable, 'r') # load the data

# Get the number of channels, sample rate, etc.

numChannels = record.getnchannels() #number of channels
```

```
numFrames = record.getframes() #number of frames
sampleRate = record.getframerate() #sampling rate
sampleWidth = record.getsampwidth()

# Get wave data
dstr = record.readframes(numFrames * numChannels)
waveData = np.frombuffer(dstr, np.int16)

# Get time window
timeEMG = np.linspace(0, len(waveData)/sampleRate, num=len(waveData))
return timeEMG, waveData
```

## 2 Animations

In medicine, the duration of the QRS complex in a healthy heart is considered to be less than 12 ms [Szulewski, 2018]. Notice that when considering a time delay around this value, the attractor's dynamic unfolds i.e., the cycle is clearly visible.

```
[4]: x, y = ecg("ECG_samples\S1_rest.wav") #x is time and y is the voltage signal
```

```
[5]: # Ecq animation!
     # Based on: https://towardsdatascience.com/
     \rightarrow animations-with-matplotlib-d96375c5442c
     steps = 300 #Number of points between one frame and the next
     number_of_frames = 220
     fig,ax = plt.subplots() #Using objects
     ax.set_xlim((0,x[steps*number_of_frames])),ax.set_ylim((min(y),max(y)))
     ax.set_title("ECG")
     #trajectory and particle are pointers
     trayectory,=ax.plot([],[],'k.', markersize = 2)
     particle,=ax.plot([],[],'ro', markersize=10)
     def initialize():
         trayectory.set_data([],[])
         particle.set data([],[])
         return(trayectory,particle,)
     def animate(i):
         trayectory.set_data(x[:i*steps], y[:i*steps])
         particle.set_data(x[i*steps],y[i*steps])
         return(trayectory,particle,)
     animation.FuncAnimation(fig, animate, init_func=initialize,
```

```
frames=number_of_frames, interval=40, blit=True)
```

[5]: <matplotlib.animation.FuncAnimation at 0x7f6fcf0919e8>

```
[6]: # Reconstructed attractor animation!
     period = 125
     time = period*0.1
     steps = 300 #Number of points between one frame and the next
     number_of_frames = 220
     fig,ax = plt.subplots() #Manejo de objetos
     ax.set_xlim((min(y),max(y))),ax.set_ylim((min(y),max(y))) #A una variable le_1
     →pegas una funcion
     ax.set title("Reconstructed phase space, time lag of "+str(time))
     #trayectoria y bolita son apuntadores
     trayectory, = ax.plot([],[],'k.', markersize = 0.5)
     particle, = ax.plot([],[],'ro', markersize=2)
     def initialize():
         trayectory.set_data([],[])
         particle.set_data([],[])
         return(trayectory,particle,)
     def animate(i):
         trayectory.set_data(y[:i*steps], y[period:i*steps+period])
         particle.set_data(y[i*steps],y[i*steps+period])
         return(trayectory,particle,)
     animation.FuncAnimation(fig, animate, init_func=initialize,
                                    frames=number of frames, interval=40, blit=True)
```

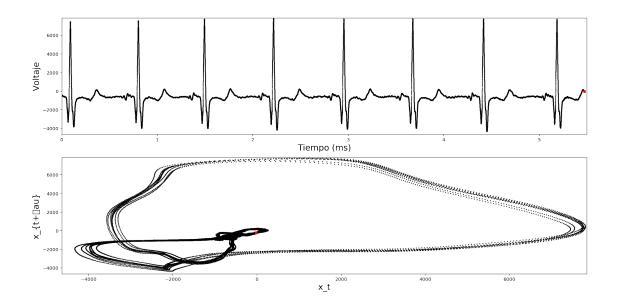
[6]: <matplotlib.animation.FuncAnimation at 0x7f6fcc8aad30>

```
[9]: # The following part is based on:
    # https://pythonmatplotlibtips.blogspot.com/2018/01/
    →combine-two-2d-animations-in-one-figure-matplotlib-artistanimation.html

period = 125 #Time delay for reconstructing attractor
    num_frames = 220 #Number of iterations for animation
    steps = 250 #Number of steps the animation will skip for red marker

#Initializing the graphic space
fig = plt.figure(figsize=(20,10))
ax1 = fig.add_subplot(2, 1, 1)
ax2 = fig.add_subplot(2, 1, 2)
```

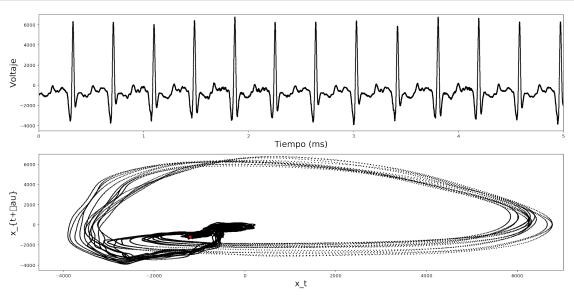
```
#ECG
ax1.set_ylabel('Voltaje')
ax1.set_xlabel('Tiempo (ms)')
ax1.set_xlim((0,x[steps*number_of_frames])),ax.set_ylim((min(y),max(y)))
ax1.set_ylim([min(y), max(y)])
trayectory_ecg, = ax1.plot([], [], 'k.', markersize=2)
particle_ecg, = ax1.plot([],[],'ro', markersize=5)
# Reconstructed phase space
ax2.set xlabel(u'x t')
ax2.set_ylabel(u'x_{t+\lambda u}')
ax2.set_xlim([min(y), max(y)])
ax2.set_ylim([min(y), max(y)])
trayectory, = ax2.plot([],[],'k.', label="ecg", markersize = 2)
particle, = ax2.plot([],[],'ro', markersize=5)
def initialize():
    trayectory_ecg.set_data([],[])
    particle_ecg.set_data([],[])
    trayectory.set_data([],[])
    particle.set_data([],[])
    return(trayectory_ecg,particle_ecg,trayectory, particle)
def animate(i):
    trayectory_ecg.set_data(x[:i*steps], y[:i*steps])
    particle_ecg.set_data(x[i*steps],y[i*steps])
    trayectory.set_data(y[:i*steps], y[period:i*steps+period])
    particle.set_data(y[i*steps],y[i*steps+period])
    return(trayectory_ecg,particle_ecg,trayectory, particle)
anim = animation.FuncAnimation(fig, animate, init_func=initialize,
                               frames=num_frames, interval=40, blit=True)
# For saving the animation in your computer
anim.save('ecg_and_attractor_rest.gif', writer='pillow')
```



What do you think will happen to the phase space after performing exercise?

```
[10]: x, y = ecg("S1_exercise.wav") #x is time and y is the voltage signal
[12]: #https://pythonmatplotlibtips.blogspot.com/2018/01/
                                  \hspace{0.2in} \color{red} \hspace{0.2in} \color{blue} \hspace{0.2in} \hspace{0.2in} \hspace{0.2in} \color{blue} \hspace{0.2in} \hspace{0.2in} \hspace{0.2in} \color{blue} \hspace{0.2in} \hspace{0.2in} \hspace{0.2in} \color{blue} \hspace{0.2in} \hspace{0.
                             period = 125 #Time delay for reconstructing attractor
                             num_frames = 220 #Number of iterations for animation
                             steps = 250 #Number of steps the animation will skip for red marker
                             #Initializing the graphic space
                             fig = plt.figure(figsize=(20,10))
                             ax1 = fig.add_subplot(2, 1, 1)
                             ax2 = fig.add_subplot(2, 1, 2)
                             #ECG
                             ax1.set_ylabel('Voltaje')
                             ax1.set_xlabel('Tiempo (ms)')
                             ax1.set_xlim([0, 5])
                             ax1.set_ylim([min(y), max(y)])
                             trayectory_ecg, = ax1.plot([], [], 'k.', markersize=2)
                             particle_ecg, = ax1.plot([],[],'ro', markersize=5)
                             # Reconstructed phase space
                             ax2.set_xlabel(u'x_t')
                             ax2.set_ylabel(u'x_{t+\lambda u}')
                             ax2.set_xlim([min(y), max(y)])
                             ax2.set_ylim([min(y), max(y)])
```

```
trayectory, = ax2.plot([],[],'k.', label="ecg", markersize = 2)
particle, = ax2.plot([],[],'ro', markersize=5)
def initialize():
   trayectory_ecg.set_data([],[])
   particle_ecg.set_data([],[])
   trayectory.set_data([],[])
   particle.set_data([],[])
   return(trayectory_ecg,particle_ecg,trayectory, particle)
def animate(i):
   trayectory_ecg.set_data(x[:i*steps], y[:i*steps])
   particle_ecg.set_data(x[i*steps],y[i*steps])
   trayectory.set_data(y[:i*steps], y[period:i*steps+period])
   particle.set_data(y[i*steps],y[i*steps+period])
   return(trayectory_ecg,particle_ecg,trayectory, particle)
anim = animation.FuncAnimation(fig, animate, init_func=initialize,
                               frames=num_frames, interval=40, blit=True)
#For saving animation in your computer
anim.save('ecg_and_attractor_exercise.gif', writer='pillow')
```



See the folder where this notebook is for playing the animations you just created.