

# Day 02: Basics of experimental design

Erin Rossiter

January 18, 2022

# Today's plan

## 1. Tidy up

- Peitong, will you:
  - » remind me to take a break at 4:30
  - » jot notes on typos & email after class
- Questions on syllabus, homework logistics, etc.
- More Github skills

## 2. Lecture

## 3. Lab

- Reinforce new concepts

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GitHub

# Grabbing my changes

- “Fetch origin” – Grab changes to the repo that I’ve made
- Check that they appear locally for you (Day02, HW1, etc.)

The screenshot shows the RStudio interface with the following elements:

- Top Bar:** Current Repository: ExperimentalDesignSpring2022, Current Branch: main, Fetch origin (Last fetched 22 minutes ago).
- Left Panel:** Changes tab selected, showing 0 changed files. Below this is a commit summary section with a profile icon, a text input for "Summary (required)", a text input for "Description", and a "Commit to main" button.
- Main Panel:** A message stating "No local changes" with a subtext: "There are no uncommitted changes in this repository. Here are some friendly suggestions for what to do next." Below this are three suggestions, each with a button:
  - "Open the repository in your external editor" with a button "Open in RStudio".
  - "View the files of your repository in Finder" with a button "Show in Finder".
  - "Open the repository page on GitHub in your browser" with a button "View on GitHub".
- Top Right:** A dark notification bubble showing the date and time: "Monday, January 17, 2022 9:29 AM".



# Workflow

1. Fetch any changes I might have made (If needed, like before class)
2. Each time you sit down to work:
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  - Commit changes
  - Repeat. . .
3. Push online (when you want me/classmates to be able to see)

We'll try later with the lab

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## Recap



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- We're interested in testing causal questions
- **Causal effect** difference in outcome(s) *caused by* an intervention.
  - » Compares units under two hypothetical situations: when they take an intervention and when they go without it (i.e., **counterfactuals**)
- Potential outcomes are a **formal way to discuss counterfactuals**
  - » Remember, you must use your imagination!

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## Notation recap

- Finite population of units:  $i \in 1, 2, \dots, N$
- Observed outcomes:  $Y_i$
- Binary treatment:
  - »  $D_i = 1$  if unit  $i$  is treated
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- Potential outcomes:
  - »  $Y_i(d_i)$  is the potential outcome for unit  $i$ , so:
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  - » Both versions of history
    - what would happen if a treatment were or were not administered
- For each unit, we want to know the causal effect of treatment
  - »  $\tau_i = Y_i(1) - Y_i(0)$
- **Fundamental problem of causal inference: we can only observe one potential outcome**

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## Treatment effects

- We can't observe *both* potential outcomes, we can only observe one.
- Formally, the relationship between **potential outcomes** and the **observed outcome** is:

$$Y_i = d_i Y_i(1) + (1 - d_i) Y_i(0)$$

- “switching equation”
- one term will always be 0
- we can only observe one potential outcome for each unit!!!!
- let's confirm on the board

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# Estimand vs. estimator vs. estimate

**Estimand** parameters that we aim to estimate, often written with greek letters ( $\mu$ ,  $\beta$ ,  $\tau$ )

**Estimator** rules for calculating an estimate; function of the observed sample data; used to learn about estimands ( $\hat{\beta}$ ,  $\hat{\tau}$ )

**Estimate** particular values of estimators that are realized in a given sample

Example:

- What's the average weight of newborns?
  - » Population mean (estimand)
  - » Sample mean (estimator)
  - » 7.5lb (estimate)
- Board?

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**Estimate** particular values of estimators that are realized in a given sample

Example:

- What's the average weight of newborns?
  - » Population mean (estimand)
  - » Sample mean (estimator)
  - » 7.5lb (estimate)
- Board?

Slide from Brandon Stewart here

## Our estimand today

An important parameter, or **estimand** is the **average treatment effect (ATE)**

- Why is it important, interesting, useful, etc?
- Can you think of other estimands we might want to use instead?
- In terms of potential outcomes:

$$\begin{aligned}ATE &= \frac{1}{N} \sum_{i=1}^N \tau_i \\&= \frac{1}{N} \sum_{i=1}^N [Y_i(1) - Y_i(0)] \\&= \frac{1}{N} \sum_{i=1}^N Y_i(1) - \frac{1}{N} \sum_{i=1}^N Y_i(0)\end{aligned}$$

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## An aside on expectations

# Why do we need this aside on expectations?

## Design process (so far)

- Establish estimand, or population parameter of interest
  - » ATE
- Draw a *random sample*
  - » selection procedure for inclusion in sample
  - » each unit in population equally likely to be included
  - » randomly assign units to treatment and control; observe one potential outcome
- Potential outcomes vary for each unit, so our estimate of ATE will vary across samples
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# Expectations

How should we think about expectations in terms of experiments?

Recall the definition of expectation  $E[X] = \sum xPr[X = x]$

What is the expected value of random variable  $\tau_i$  in Table 2.1?  
Board?

Village	$\tau_i$
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$$E[Y_i(0)]$$

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$$E[Y|X = x] = \sum y \Pr[Y = y|X = x] = \sum y \frac{\Pr[Y = y|X = x]}{\Pr[X = x]}$$

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# Conditional expectations, potential outcomes, and random assignment

*(This is an important slide! pg. 33 of GG)*

Under what conditions is this true?

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When one subject sampled at random, what is the expected value of their treatment effect?

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## Estimating the ATE

# 1. Design

- Randomize  $D_i$  with probability  $p$ 
  - » first  $m$  units assigned to treatment
  - » remaining  $N - m$  units assigned to control
- Assume two potential outcomes  $Y_i(1), Y_i(0)$ 
  - » (more on this later)
- Observed outcome is  $Y_i$

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How do we write the DIM estimator? Struggle with it for a minute.

$$\hat{ATE} = ???$$

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## Technical details on random assignment

## In practice

- Beware “random” being used to mean arbitrary or haphazard—not here!
- Random assignment procedures:
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    - Ex: Flip a coin for each unit
  - » Complete random assignment
    - Ex: Randomly permute  $N$  units, assign first  $m$  units to treatment and  $N - m$  to control
- Usually, we'll use computational tools to accomplish random assignment, unless you're limited in the field
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Assumptions we're making about potential  
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# Key assumptions

Experiments provide unbiased estimates of the average treatment effect (ATE) under the following assumptions:

1. **Random assignment**
2. **Excludability** treatment is *solely* responsible for the outcome
3. **Non-interference (aka SUTVA)** potential outcomes are defined over the set of treatments that subject *itself* receives

Assumptions #2 and #3 are assumptions about how units respond to treatment allocation.

- Important to be clear about the causal effect of interest and assess assumptions in light of how the causal effect is defined.
- Example: effect of new vaccine on contagious disease
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# Excludability in practice

- Research activity should not be correlated with treatment assignment!
- Be careful to avoid measurement asymmetries
  - » Ex: different research teams measuring outcomes in control and treatment groups
  - » DIM estimator is biased if measurement errors have different expected values (see pg. 41 in GG)
- Safeguards:
  - » double-blind
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## Non-interference assumption

- We're assuming potential outcomes depend only on if unit  $i$  is treated

$$Y_i(\mathbf{d}) = Y_i(d_1, d_2, \dots, d_i, \dots, d_n) = Y_i(d)$$

- Where? Again, by only defining  $Y_i(0)$  and  $Y_i(1)$
- Problems arise if one unit's treatment status affects another unit!
- Ex: We could write four potential outcomes per unit:
  - »  $Y(d_i, d_5)$ 
    - $d_i$  is a unit's own treatment assignment
    - $d_j$  is treatment assignment of unit 5

Unit	$Y_i(0, 0)$	$Y_i(0, 1)$	$Y_i(1, 0)$	$Y_i(1, 1)$
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# Non-interference in practice

- Also called “spillovers”
- Violations:
  - » subjects are aware of treatments of other subjects
  - » treatments may be transmitted from treated to untreated subjects
  - » resources used to treat one set of subjects diminish resources that would otherwise be available to other subjects
- Examples from Alex Coppock’s EGAP 10 Things to Know:
  - » providing an vaccine to some individuals may decrease the probability that nearby individuals become ill.
  - » increased enforcement may displace crime to nearby areas
  - » students may share acquired knowledge or skills with friends
  - » election monitoring at some polling stations may displace fraud to neighboring polling stations
- Be on the look out for networks in your context:
  - » face-to-face social interaction
  - » social networks
  - » geographic proximity
- We’ll talk more about interference later in the semester
- Interference concerns in your experiments?

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- We proved that difference-in-means is an unbiased estimator of it.
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