

## Day 04: Analyzing experimental data

Erin Rossiter

January 25, 2022

# Today's plan

## 1. Tidy up

- Abigail, will you:
  - » remind me to take a break at 4:30-4:45
  - » jot notes on typos & email after class
- Note that HW4 will ask for a one-pager on your research topic, question, and hypothesis(es)

## 2. Lecture part 1 and lab 1 (hypothesis testing)

## 3. Lecture part 2 and lab 2 (covariates in design)

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## Recap

# ATE

- The average treatment effect (ATE) is often an interesting, important, useful estimand.
- Difference-in-means is an **unbiased** estimator of the ATE assuming:
  1. Randomization of treatment
    - »  $E[Y_i(1)|D_i = 1] = E[Y_i(1)]$
    - »  $E[Y_i(0)|D_i = 0] = E[Y_i(0)]$
    - » We can estimate left-hand terms using our observed data!
  2. Excludability
  3. Noninterference
- What about **uncertainty**?



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# Standard error

To be clear:

- a **sampling distribution** is a distribution of a statistic (e.g.,  $\hat{ATE}$ )
- a **standard deviation** is a single value quantifying variability for any variable  $X$
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# Standard error

There's a true standard error:  $SE(\hat{ATE})$

- How much might our estimate vary across all hypothetical random assignments?
- Our design choices influence this!
  - »  $N$  size
  - » Potential outcome variability
  - » Randomization routine (blocking, clustering)
- Beneficial to reduce standard error in design phase.

Of course, we must estimate the standard error:  $\hat{SE}(\hat{ATE})$

- DeclareDesign helps understand both true standard error and how we plan to estimate it
  - » Is our estimation strategy getting a standard error that's too big? Meaning, we'd fail to reject a false null? No stars when there should be?!

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- ✓ Uncertainty associated with the  $\hat{ATE}$

Today → Hypothesis testing

1. (Typical) null hypotheses of no *average* effect and hypothesis testing with approximate p-values based on assumptions about sampling distributions
2. Sharp null hypotheses and randomization inference hypothesis testing with exact p-values

Today → More talk about covariates

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# Hypothesis testing

“Traditional” hypothesis testing

# Refresher on hypothesis testing

1. We state a null hypothesis
  - e.g.,  $H_0: ATE = 0$
  - No average treatment effect
  - The claim we'd like to reject
2. We choose a test statistic
  - e.g.,  $t$ -value
3. Determine the distribution of the test statistic under the null
  - A thought experiment. If the null is true, what data would we expect to see? (board)
  - e.g., Student's  $t$
4. Calculate the probability ( $p$ -value) of our test statistic under the null
  - Continuing our thought experiment. If the null is true, how surprising is our data? (board)



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## Example

- Data from page 65 of GG
- Treatment is encouragement to make a charitable donation
- Outcome is how much money donated

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df <- data.frame("Donation" = c(500, 100, 100, 50,  
                                25, 25, 0, 0, 0, 0,  
                                25, 20, 15, 15, 10,  
                                5, 5, 5, 0, 0),  
                 "Treatment" = c(rep(1,10),  
                                rep(0, 10)))  
  
head(df)
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##   Donation Treatment  
## 1      500         1  
## 2      100         1  
## 3      100         1  
## 4       50         1  
## 5       25         1  
## 6       25         1
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## t-test

1. State null hypothesis  $H_0 : ATE < 0$
2. Choose the  $t$  value as our test statistic
3. Assume sampling distribution of  $t$  follows Student's  $t$  under the null
  - *We're assuming sampling dist of DIM estimator has a certain shape*
4. Calculate probability of observing our test statistic (from #2) given assumed sampling distribution under the null (from #3)



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4. Calculate probability of observing our test statistic (from #2) given assumed sampling distribution under the null (from #3)

## t-test by hand

```
# 1. state null
h_not <- 0

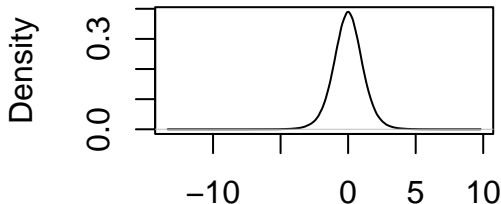
# 2. choose test statistic (t-test with unequal variances)
s1 <- sd(df$Donation[df$Treatment == 0])^2
s2 <- sd(df$Donation[df$Treatment == 1])^2
t <- (70-h_not)/sqrt(s1/10 + s2/10)
t

## [1] 1.44776
```

## t-test by hand

```
# 3. think about data we'd observe if the null is true  
# (Notice the assumption about the sampling  
# distribution we're making here!)  
rand_data_under_null <- rt(n = 1000000, df = 9.0558)  
plot(density(rand_data_under_null),  
      xlab = "", cex = .25)
```

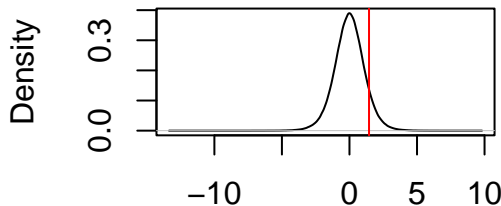
**nsity.default(x = rand\_data\_unde**



## t-test by hand

```
# (from step 3)
plot(density(rand_data_under_null), main = "", xlab = "", cex =

# 4. how odd is our data (or something bigger) given the null?
abline(v = t, col = "red")
```



```
pt(t, df = 9.0558, lower.tail = F) #or...
```

```
## [1] 0.09070126
```

```
sum(rand_data_under_null > t)/1000000
```

```
## [1] 0.090729
```

## t-test in R using t.test()

```
t.test(df$Donation[df$Treatment == 1],  
       df$Donation[df$Treatment == 0],  
       var.equal = F, alternative = "greater")
```

```
##
```

```
##  Welch Two Sample t-test
```

```
##
```

```
## data:  df$Donation[df$Treatment == 1] and df$Donation[df$Trea
```

```
## t = 1.4478, df = 9.0558, p-value = 0.0907
```

```
## alternative hypothesis: true difference in means is greater t
```

```
## 95 percent confidence interval:
```

```
##   -18.56994      Inf
```

```
## sample estimates:
```

```
## mean of x mean of y
```

```
##          80          10
```



## t-test in R using difference\_in\_means()

Identical, but

- no one-sided tests
- allows for easy design-based estimation when you use blocking and clustering (see homework)
- *I encourage this package since it's built with experiments in mind*

```
options(width = 60)
estimatr::difference_in_means(Donation ~ Treatment,
                              data = df)
```

```
## Design: Standard
##           Estimate Std. Error t value  Pr(>|t|)  CI Lower
## Treatment      70    48.35057  1.44776  0.1814026 -39.27398
##           CI Upper      DF
## Treatment  179.274  9.05578
```

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## t-test big picture

- We're making assumptions about sampling distribution
  - » sampling dist for DIM estimate follows  $t$  distribution
- Good assumption when...
  - » Outcomes distributed normally, or
  - » Outcome distributed non-normally, but big sample (invoke CLT for sampling distribution to be approximately normal)
- In general, we should be wary when we're using small and/or skewed samples
  - » "Rules of thumb" are hard...

Next, an alternative approach that starts from a different null hypothesis...

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## Randomization inference

## Sharp null hypothesis of no effect

$$H_0 : \tau_i = Y_i(1) - Y_i(0) = 0 \quad \forall i$$

- Think, “no effect means no effect”
- Different than no **average** treatment effect
  - » No average treatment effect does not imply sharp null.
- Example on board



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# Recall our hypothesis testing steps

## 1. We state a null hypothesis

- $H_0 : \tau_i = Y_i(1) - Y_i(0) = 0 \quad \forall i$
- Or simply,  $H_0 : Y_i(1) = Y_i(0)$

## 2. We choose a test statistic

- Keep in mind, many to choose from
- Let's stick with DIM

## 3. Determine the distribution of the test statistic under the null

- **This is where we shake things up!** Example next.
- Null hypothesis is about *individual* rather than *average* effect
- We have a link between observed data and the potential outcomes.
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## How do we determine the distribution of the test statistic under the null?

1. What do we know about potential outcomes from what we *observe*?

Unit	$d_i$	$Y_i$	$Y_i(0)$	$Y_i(1)$
1	0	1	?	?
2	0	4	?	?
3	0	2	?	?
4	0	1	?	?
5	1	5	?	?
6	1	7	?	?
7	1	3	?	?
8	1	3	?	?

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  - $Y_i(0)|d_i = 0$
  - $Y_i(1)|d_i = 1$

Unit	$d_i$	$Y_i$	$Y_i(0)$	$Y_i(1)$
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## How do we determine the distribution of the test statistic under the null?

2. What do we know about potential outcomes from what we *assume*?

Unit	$d_i$	$Y_i$	$Y_i(0)$	$Y_i(1)$
1	0	1	1	?
2	0	4	4	?
3	0	2	2	?
4	0	1	1	?
5	1	5	?	5
6	1	7	?	7
7	1	3	?	3
8	1	3	?	3

## How do we determine the distribution of the test statistic under the null?

2. What do we know about potential outcomes from what we *assume*?
  - We can use the sharp null to fill in remaining potential outcomes
  - $Y_i(1) - Y_i(0) = 0$

Unit	$d_i$	$Y_i$	$Y_i(0)$	$Y_i(1)$
1	0	1	1	(1)
2	0	4	4	(4)
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  - What is this called?

## How do we determine the distribution of the test statistic under the null?

3. Since we have *all* potential outcomes, we can calculate test-statistic for all hypothetical randomizations!!!
  - What is this called? **Sampling distribution**
  - Also called “randomization distribution”
4. Compare our test statistic to all possible test statistics under the null to get p-value.

## Example

Unit	$d_i$	$Y_i$	$Y_i(0)$	$Y_i(1)$
1	0	1	1	(1)
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```
df <- data.frame(Z = c(0,0,0,0,1,1,1,1),  
                 Y = c(1,4,2,1,5,7,3,3))
```



## Example

- For randomization inference (often called RI), you need exact randomization procedure
- Why is this so important?

```
random_assignment <- randomizr::declare_ra(N = 8, m = 4)
random_assignment

## Random assignment procedure: Complete random assignment
## Number of units: 8
## Number of treatment arms: 2
## The possible treatment categories are 0 and 1.
## The number of possible random assignments is 70.
## The probabilities of assignment are constant across units:
## prob_0 prob_1
##      0.5      0.5
```

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## Example

```
out <- ri2::conduct_ri(formula = Y ~ Z,  
                        data = df,  
                        declaration = random_assignment)  
out
```

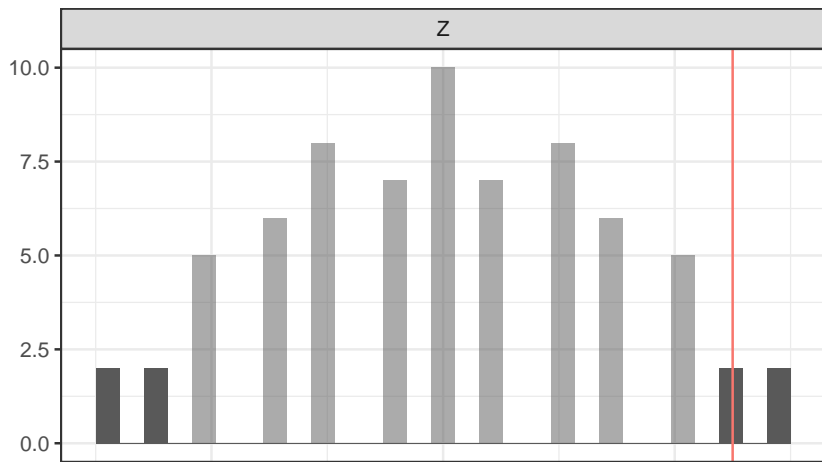
```
##   term estimate two_tailed_p_value  
## 1    Z       2.5         0.1142857
```

## Example

```
plot(out)
```

```
## Warning: It is deprecated to specify `guide = FALSE` to  
## remove a guide. Please use `guide = "none"` instead.
```

### Randomization Inference



## Example 2

Let's re-do the GG t-test example

```
df <- data.frame("Donation" = c(500, 100, 100, 50,  
                                25, 25, 0, 0, 0, 0,  
                                25, 20, 15, 15, 10,  
                                5, 5, 5, 0, 0),  
                 "Treatment" = c(rep(1,10),  
                                 rep(0, 10)))  
head(df)
```

##	Donation	Treatment
## 1	500	1
## 2	100	1
## 3	100	1
## 4	50	1
## 5	25	1
## 6	25	1

## Example 2

```
random_assignment <- randomizr::declare_ra(N = 20)
random_assignment
```

```
## Random assignment procedure: Complete random assignment
## Number of units: 20
## Number of treatment arms: 2
## The possible treatment categories are 0 and 1.
## The number of possible random assignments is 184756.
## The probabilities of assignment are constant across units:
## prob_0 prob_1
##      0.5      0.5
```

## Example 2

```
out <- ri2::conduct_ri(formula = Donation ~ Treatment,  
                        outcome = "Donation",  
                        assignment = "Treatment",  
                        p = "upper",  
                        sims = 10000,  
                        data = df,  
                        declaration = random_assignment)  
out
```

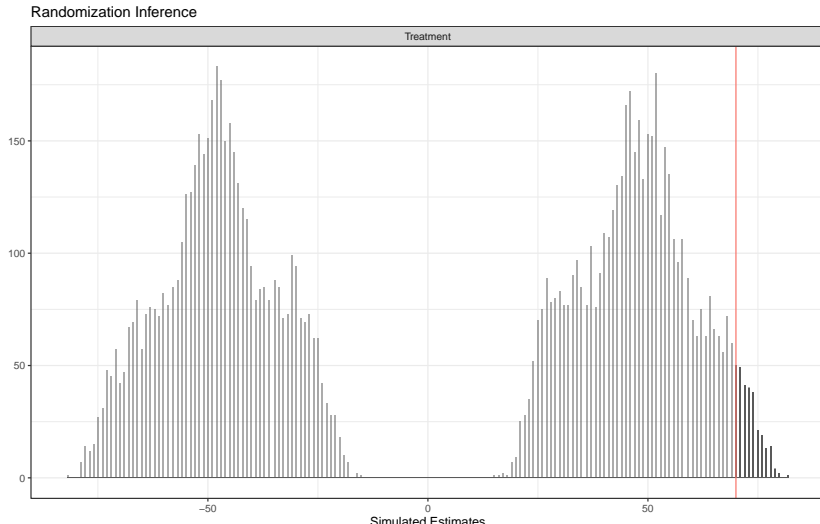
```
##           term estimate upper_p_value  
## 1 Treatment          70          0.0292
```



## Example 2

```
plot(out)
```

```
## Warning: It is deprecated to specify `guide = FALSE` to  
## remove a guide. Please use `guide = "none"` instead.
```



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## Sharp null hypothesis of no effect

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- good when assumptions about sampling distribution are worrisome
  - » small  $N$
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- good when we have complicated randomization procedures
  - » blocking, clustering, etc.
- it's simple and exact!
- but null hypothesis might be less interesting
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## Lab 1



## Covariates in experimental design

# Big picture

Recall,

- Randomization addresses the problem of omitted variables that plagues observational data
- Therefore, covariates are not a primary concern for causal inference
  - » However, covariates can have important roles in design and analysis (or can be mis-used!)
  - » Incorporation of covariates is best thought-out during the design of experiments
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  - » Rescaling the outcome
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- “Supplementary variables that predict outcomes” GG pg 95
- We assume that they are fixed pre-treatment
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Redefine the DV:

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Difference-in-differences estimator:

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- Give details of the random assignment procedure and any instances in which subjects are lost or excluded after allocation
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## Use #3. Regression adjustment

Switching equation  $Y_i = Y_i(0)(1 - d_i) + Y_i(1)d_i$

Rearrange  $Y_i = Y_i(0) + (Y_i(1) - Y_i(0))d_i$

Rename  $Y_i = \mu_{Y(0)} + [\mu_{Y(1)} - \mu_{Y(0)}]d_i + u_i$ ,

- see definition of  $u_i$  in text and see it matches how we think of disturbance in DeclareDesign

Rename  $Y_i = a + bd_i + u_i$

- $a$  is average value of untreated potential outcomes for all units
- $b$  is average shift in average potential outcomes for i.e., ATE
- OLS estimator produces equivalent  $\hat{ATE}$  as DIM

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# Readjustment

Including covariate(s) on RHS

$$Y_i = Y_i(0) + (Y_i(1) - Y_i(0))d_i = a + bd_i + cX_i + (u_i - cX_i)$$

- When  $X_i$  predicts the outcome, we reduce amount of unexplained variation in  $Y_i$ !
  - » Doing so reduces the standard error of  $\hat{b}$  like we talked about last time :)
- Restablishes balance if an unlucky randomization, administrative error, etc.

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## Summary on using covariates

- Use pre-treatment covariates identified by other researchers, pilot testing, or theory to influence outcome of interest (blocking, adjustment, re-scaling outcome)
- Helps to reduce variability in our estimate
- Including covariates that does not predict outcomes does nothing to the sampling variability of our estimates
- Avoid waiting to determine which covariates to include (tie your hands using a PAP)
- Report both unadjusted estimates of the causal estimates along with adjusted estimates

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