

So:

From (7): $\frac{\partial f}{\partial x} = \tan \theta_T = \frac{\cos \theta_c - \frac{n_a}{n_p} \cos \theta_0}{\sin \theta_c - \frac{n_a}{n_p} \sin \theta_0}$

θ_0 is a variable independent of x but can take any value between 0 and $\frac{\pi}{2}$.

If we let $\theta_0 \equiv x$ we will have that for each x there will be the appropriate inverse to couple to some θ_0 .

So to trace the wave we can integrate

$$\frac{\partial f}{\partial x} = \frac{\overset{\text{constant}}{\cos \theta_c} - \frac{n_a}{n_p} \cos x}{\sin \theta_c - \frac{n_a}{n_p} \sin x} \quad (8) \quad \theta_c \text{ given by } \sin \theta_c = \sqrt{\frac{\epsilon_a \epsilon_m}{(\epsilon_a + \epsilon_m) \epsilon_p}}$$

Working at 635 nm (laser available in the lab):

$$\begin{cases} \epsilon_a = 1,00059 \\ \epsilon_p = 2,04 \\ \epsilon_m = -12 \end{cases}$$

$$\begin{cases} n_a = 1,000293 \\ n_p = 1,429 \end{cases}$$

$$\Rightarrow \theta_c = \sin^{-1} \left(\sqrt{\frac{1,00059 \cdot (-12)}{(1,00059 - 12) 2,04}} \right) \approx \underline{\underline{47,0^\circ}}$$

• Plug these into 8 and use maple to integrate: