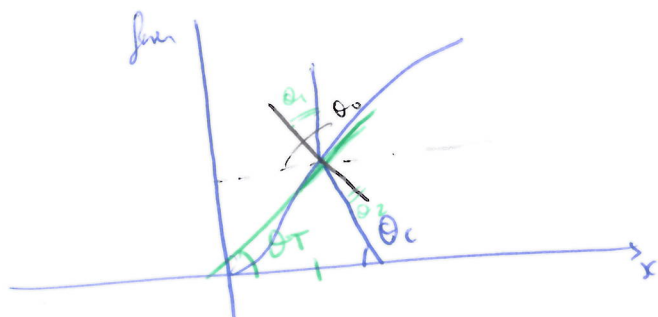


It is also possible to consider pre-fixed arbitrary curves  $f(x)$  for the pump and see what range of angles can be coupled using these.

Let's consider an arbitrary shape for  $f(x)$ .



• Coupling will occur if angle at the flat side of the pump is  $\theta_c$ .

The following still hold:

$$\begin{cases} \theta_0 = -\theta_T + \theta_1 + \frac{\pi}{2} \\ \theta_2 = \theta_T + \theta_c - \frac{\pi}{2} \\ n_a \sin \theta_1 = n_p \sin \theta_2 \Rightarrow \theta_1 = \sin^{-1} \left( \frac{n_p}{n_a} \sin(\theta_T + \theta_c - 90^\circ) \right) \end{cases}$$

$$\Rightarrow \theta_0 = -\theta_T + \frac{\pi}{2} + \sin^{-1} \left( \frac{n_p}{n_a} \sin(\theta_T + \theta_c - 90^\circ) \right)$$

Now  $\theta_T = \tan^{-1} \left( \frac{\partial f}{\partial x} \right)$  from before.

and if we fix  $\theta_c$  to the right value for the given frequency we will get coupling.

Hence, the values of  $\theta_0$  that can be coupled for a given curve  $f(x)$  will be:

$$\theta_0 = -\tan^{-1} \left( \frac{\partial f}{\partial x}(x) \right) + \frac{\pi}{2} + \sin^{-1} \left( \frac{n_p}{n_a} \sin \left( \tan^{-1} \left( \frac{\partial f}{\partial x}(x) \right) + \theta_c - \frac{\pi}{2} \right) \right)$$

Can use the above equation in Maple with different curves for  $f(x)$  to see which would allow a broader range of angles to be coupled.