Functional Programming in Typed Racket

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Just call me Florian!

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GitHub Course Page

All slides and course materials are available on:

https://github.com/fbie/parallel-functional-lectures

Functional programming is old but recently it has become very popular!

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- Used in financial industry, modern compilers and more.
- Jobs in functional programming pay better!



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- Racket is dynamically typed, Typed Racket has a static, strong type system.
- ► Functional language, no side-effects (mostly).
- Good for meta-programming (we won't look at that).

Hello World in Typed Racket

```
;; This is a comment!
;; Tell the run-time, which language to use.
#lang typed/racket

;; Now, print something.
(print "Nihao!")
```

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We can check its value in the interactive mode:
> x
59
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Some functions are variadic:

$$(+ x y z) \Rightarrow x + y + z$$

Local Bindings

Just like local variables in Java, but you can never change them!

What does this program do?

Note: You cannot reference x and y after the last closing parenthesis of the let expression!

The Same Program in Java

```
public static void main(String[] args) {
  int x = 2 * 16;
  int y = 3 * 17;
  System.out.println(x + y);
}
```

```
#lang typed/racket
(: times-two (-> Number Number))
(define (times-two x)
  (* 2 x))
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- ► Functions need no return statement. Their return value is the last executed statement!
- Type annotations start with : and describe the type of a symbol.
- ► The type of times-two is Number → Number.

Types in Typed Racket

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Which types are parameter types, which ones are return types?

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Conditionals have the form (if B E1 E2).

Polymorphic Types

Polymorphic types in Typed Racket are very explicit:

```
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(define (twice a)
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It's just like generic types in Java!

The Same Program in Java

```
public static Pairof <A, A> twice(A a) {
  return new Pairof <A, A>(a);
}
```

Note: There is no build-in pair type in Java :(

State is Immutable!

You cannot change a variable's value. Instead, use **recursion**:

```
(: is-even? (-> Integer Boolean))
(define (is-even? n)
  (if (< 0 n)
        (is-even? (- n 2))
        (= n 0)))</pre>
```

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Now, we can call the function:

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> (is-even? 1)
#f
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Now, we can call the function:

```
> (is-even? 1)
#f
> (is-even? 2048)
#t
```

The Same Program in Java

```
public static bool isEven(int n) {
  while (0 < n)
    n = n - 2;
  return n == 0;
}</pre>
```

Anonymous Functions

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We will often come across lambda expressions in functional programming!

Structs in Typed Racket

Structs are containers for values.

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Next, we will do a live coding session!

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- You can download Racket from
 - ► racket-lang.org

Java Equivalent to Maybe

```
public abstract class Maybe<A> {}
public class None < A > extends Maybe < A > {
  public None() {}
}
public class Some < A > extends Maybe < A > {
  public final A a;
  public Some(A a) {
    this.a = a;
```

Singly-Linked Cons List 1/2

```
(define xs (cons 'a (cons 'b (cons 'c (cons 'd (cons 'e '()))))))
```

Singly-Linked Cons List 1/2

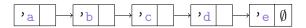
```
(define xs (cons 'a (cons 'b
          (cons 'c (cons 'd (cons 'e '()))))))
Get the first element of xs, the "head":
> (first xs)
'a
> (cdr xs)
'a
```

Singly-Linked Cons List 1/2

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Get the first element of xs, the "head":
> (first xs)
, a
> (cdr xs)
, a
Get the remaining part of xs, the "tail":
> (rest xs)
'('b 'c 'd 'e)
> (cdr xs)
'('b'c'd'e)
```

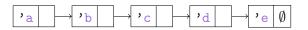
Singly-Linked Cons List 2/2

References to tail **cannot be changed**, because all **references are immutable**:



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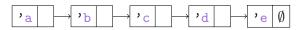
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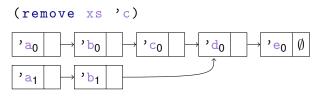
If we want to remove an element, we must build a new list, but we can re-use the tail of the element that we have deleted:

Singly-Linked Cons List 2/2

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Java Equivalent to Cons List

```
public abstract class LinkedList <A> {}
public class Nil<A> extends LinkedList<A> {
  public Nil() {}
}
public class Cons<A> extends LinkedList<A> {
  public final A a;
  public final LinkedList <A> tail;
  public Cons(A a, LinkedList <A> tail) {
    this.a = a;
    this.tail = tail;
```

Java Equivalent to Binary Tree

```
public abstract class BinaryTree <A> {}
public class Leaf <A> extends BinaryTree <A> {
  public final A a;
  public Leaf(A a) {
    this.a = a;
public class Node<A> extends BinaryTree<A> {
  public final BinaryTree <A> left, right;
  public Node(BinaryTree < A > left,
              BinaryTree < A > right) {
    this.left = left; this.right = right;
```