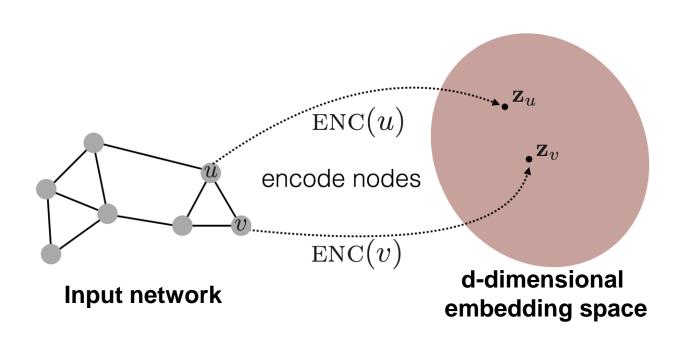
## Embedding is not the most important!

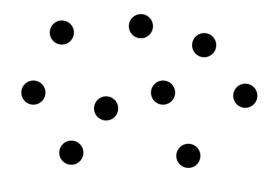


The embedding performs poorly when

- SNR is too low in dataset.
- the relationship is incorrect.
- the relationship is redundancy.

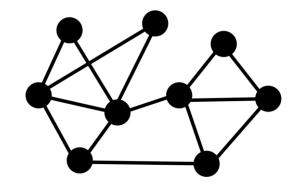
Dataset and relationship is much important!

### How to build a graph? GNN?



Similarity:

PCC 
$$r = rac{\sum \left(x_i - ar{x}
ight)\left(y_i - ar{y}
ight)}{\sqrt{\sum \left(x_i - ar{x}
ight)^2 \sum \left(y_i - ar{y}
ight)^2}}$$



An important topic!

#### Grale: Designing Networks for Graph Learning

Jonathan Halcrow<sup>†</sup>, Alexandru Moșoi<sup>‡</sup>, Sam Ruth<sup>†</sup>, Bryan Perozzi<sup>†</sup>
†: Google Research
‡: YouTube
{halcrow,mosoi,samruth}@google.com,bperozzi@acm.org

- In real world applications, the choice of which edges to use for computation is the first step in any graph learning process.
- The choice of edges can drastically affect the performance of downstream semisupervised learning systems.
- Grale: graph design for graphs with billions of nodes
- Grale operates by fusing together different measures of (potentially weak) similarity to create a graph which exhibits high task-specific homophily between its nodes.

#### Notation

#### consider a general multiclass learning setting

a partially labeled set of points  $X = \{x_1, x_2, ..., x_V\}$ the first L points have class labels  $Y = \{y_1, y_2, ..., y_L\}$  $y_k$  a one-hot vector of dimension C

$$x_i = \{x_{i,1}, x_{i,2}, \dots x_{i,d}\}$$

Each sub-representation  $x_{i,d}$  has its own natural distance measure  $\kappa_d$ 

#### Loss function

a classification problem:

$$y_k = \hat{y}(\mathbf{x_k})$$

$$\mathcal{L} = -\sum_{i \in \mathcal{Y}} \sum_{c \in C} y_{i,c} \log \hat{y}_{i,c}$$

assume a graph G = (V, E):

$$\hat{y}_{i,c}^{(n+1)} = \alpha y_{i,c} + \beta \frac{\sum_{j \in \mathcal{N}_i} w_{i,j} \hat{y}_{j,c}^{(n)}}{\sum_{j \in \mathcal{N}_i} w_{i,j}}$$

$$\mathcal{L} = \sum_{i,j \in E} w_{i,j} \sum_{c \in C} |\hat{y}_{i,c} - \hat{y}_{j,c}| + \sum_{i \in V, c \in C} |\hat{y}_{i,c} - y_{i,c}|$$

Potts model type loss function

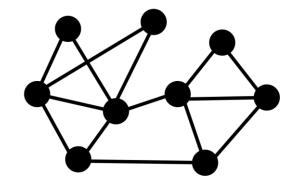
#### **GRALE**

Design **task specific graphs** by reducing the original task to training a classifier on pairs of points

$$w_{ij} := \log G(x_i, x_j) \quad G : \mathbf{R}^d x \mathbf{R}^d \to \mathbf{R} \quad 0 < G < 1 \quad w_{ij} < 0$$

$$G(x_i, x_j) = f(\kappa_1(x_i, x_j), \kappa_2(x_i, x_j), \dots, \kappa_d(x_i, x_j))$$

$$\mathcal{L} = -\sum_{c \in C} \sum_{i \in \mathcal{X}} \sum_{j \in \mathcal{X}} y_{i,c}, y_{j,c} \log G(x_i, x_j)$$



#### **GRALE**

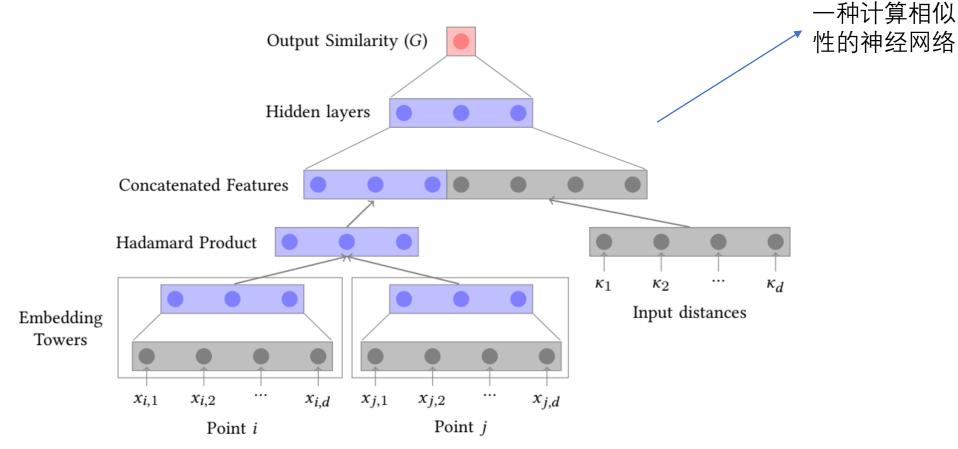
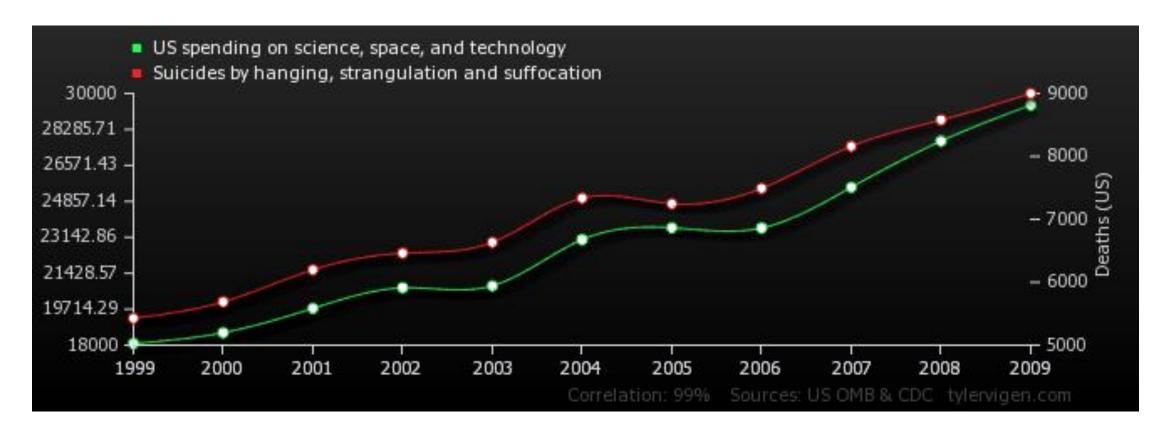


Figure 2: The Grale Neural Network model. The gray nodes are inputs, the blue are hidden layers, and red is the output. The network architecture combines a standard two-tower model with natural distances in the input feature spaces. Weights are shared between the two towers. The Hadamard product (pointwise multiplication) of the two towers is used to give us a pairwise embedding. We treat this as an additional set of distance features to augment the input distance features  $\kappa_1(x_i, x_j), \ldots, \kappa_d(x_i, x_j)$ . This combined set acts as an input to the second part of the model which computes a single similarity score.

## Spurious Correlations

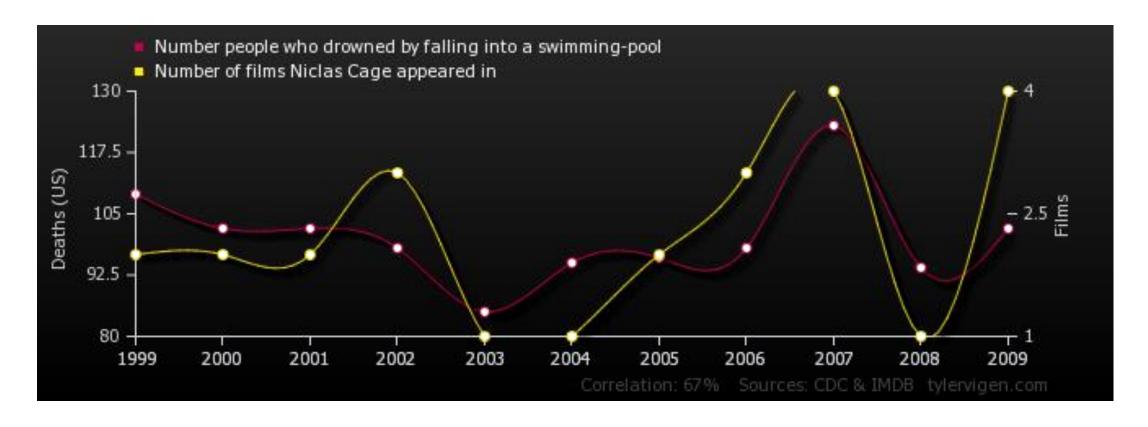
- Statistical significance: Standard threshold is 5%, meaning would be observed by chance 1 out of 20 times
- But if you look at enough relationships you'll find "significant" ones by chance
- Spurious means there's no real connection

## Spurious Correlations



US Spending on Science, Space and Technology Correlates with Suicides by Hanging, Strangulation and Suffocation

## Spurious Correlations



Number of People Who Drowned by Falling into a Swimming Pool Correlates with Number of Nicholas Cage Films

## Big Data Analysis Requires Causality

- Big data is not randomized
- We have to compare treatments when patients and providers choose what they think is best (AB test)
- We want to choose treatments and design interventions
- Causal inference is crucial

## If We Don't Think About Causality . . .

- Our predictions can be fragile
- Our interventions can be misguided

#### Causal Inference

#### **Relating Graph Neural Networks to Structural Causal Models**

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Computer Science Department, TU Darmstadt

**Devendra Singh Dhami**DEVENDRA.DHAMI@CS.TU-DARMSTADT.DE

Computer Science Department, TU Darmstadt

Petar Veličković Petarv@google.com

DeepMind, London

Kristian Kersting KERSTING@CS.TU-DARMSTADT.DE

Computer Science Department, Centre for Cognitive Science, TU Darmstadt, and Hessian Center for AI (hessian.AI)

https://www.youtube.com/watch?v=XC-Bfg3dO0I&ab\_channel=ValenceDiscovery

<u>Pearl Causal Hierarchy (PCH) - 馒头and花卷 - 博客园 (cnblogs.com)</u>

https://www.nature.com/articles/s41598-021-87411-8

https://proceedings.mlr.press/v139/lin21d.html

<u>CausalGNN: Causal-Based Graph Neural Networks for Spatio-Temporal Epidemic Forecasting</u>

| Proceedings of the AAAI Conference on Artificial Intelligence

# Relating Graph Neural Networks to Structural Causal Models

Graph GSCM & (unobserved Nature)  $f(\mathbf{V}, \mathbf{U}) \begin{pmatrix} X \leftarrow f_X(U_X) \\ Y \leftarrow f_Y(X, Z, U_Y) \\ Z \leftarrow f_Z(X, U_Z) \\ W \leftarrow f_W(Y, U_W) \end{pmatrix}$ Data **D** (c)  $f(\mathbf{D}, G \mid \mathbf{do(V_j)}) = \begin{bmatrix} - & g(\mathbf{d}_X, \mathbf{D}_{\mathcal{M}_X}) & - \\ - & g(\mathbf{d}_Y, \mathbf{D}_{\mathcal{M}_Y}) & - \\ - & g(\mathbf{d}_Z, \mathbf{D}_{\mathcal{M}_Z}) & - \\ - & g(\mathbf{d}_W, \mathbf{D}_{\mathcal{M}_W}) & - \end{bmatrix}$  $P(\mathbf{U})$  $(\mathcal{L}_1)P(\mathbf{V})$  $\mathcal{M}_i = \{ j \mid j \in \mathcal{N}_i,$  $(\mathcal{L}_2)P(\mathbf{V}_i \mid do(\mathbf{V}_i))$  $j \not\in pa_i \iff i \in \mathbf{V_i}$  $(\mathcal{L}_3)P(\mathbf{V}_i \mid do(\mathbf{V}_i), \mathbf{V}_k)$ 

AB实验的形式化

Judea Pearl提出的<mark>"因果阶梯"论</mark>(Pearl Causal Hierarchy,PCH)

CausalGNN: Causal-Based Graph Neural Networks for Spatio-Temporal Epidemic Forecasting

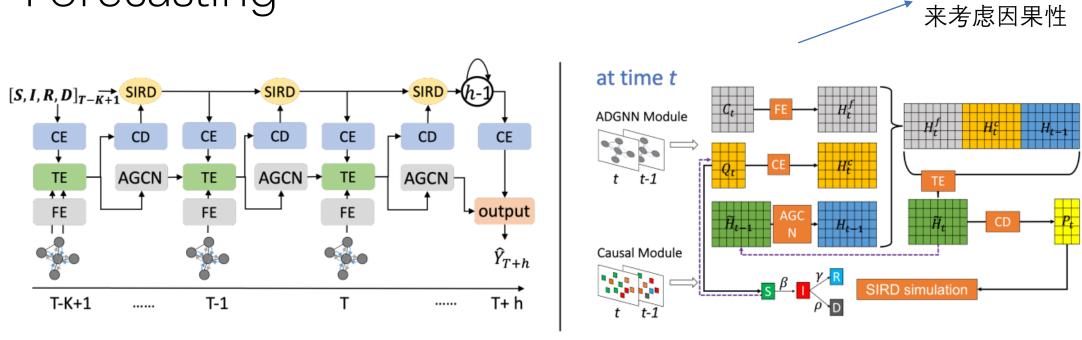


Figure 1: Framework of CausalGNN which consists of a causal module and an attention-based dynamic GNN module.

FE: feature encoding

CE: causal encoding

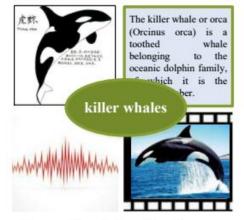
AGCN: dynamic graph encoding

TE: temporal encoding

CD: causal decoding

SIRD: susceptible(S)-infected(I)- recovered(R)-deceased(D)

#### Multi-view data



(a) A object is described by text, video, audio

Texture

Shape

Color

(d) An image is depicted by

heterogonous features

的比赛将于11月22日

James se llevará a cabo

el 22 de noviembre.

held On Nov. 22nd El 8 de agosto, hora de Beijing, se anunció la temporada 2018-19 en las primeras horas de la mañana. El juego de jinetes de los Lakers de

8 აგვისტოს, პეკინის 2018-19 სეზონი დილის საათებში გამოცხადდა, ლეიკერსის მხედარი 22 ნოემბერს გაიმართება.

On Aug. 8th, Beijing

time, the 2018-2019

season was announced

in the early hours of the

morning. James's Laker

vs Cavaliers will be

(b) A news is reported by different languages



(e) A social image along with user tags



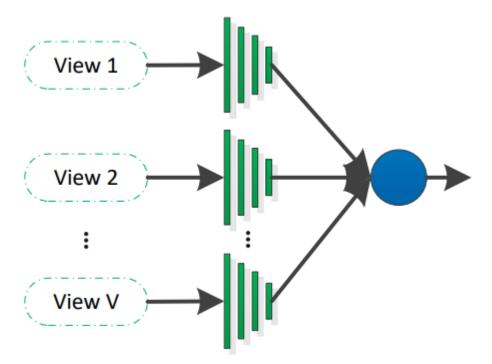
(c) A product can be represented by multi-view graphs



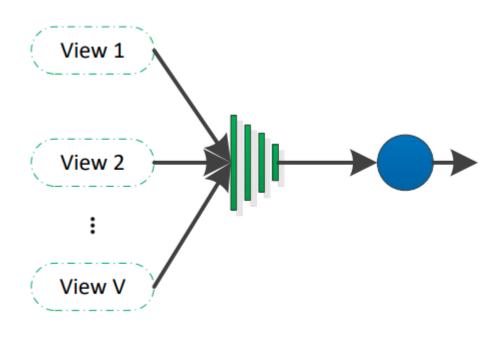
(f) One action can be captured from different camera viewpoints

# Multi-view learning

• Multi-modal?



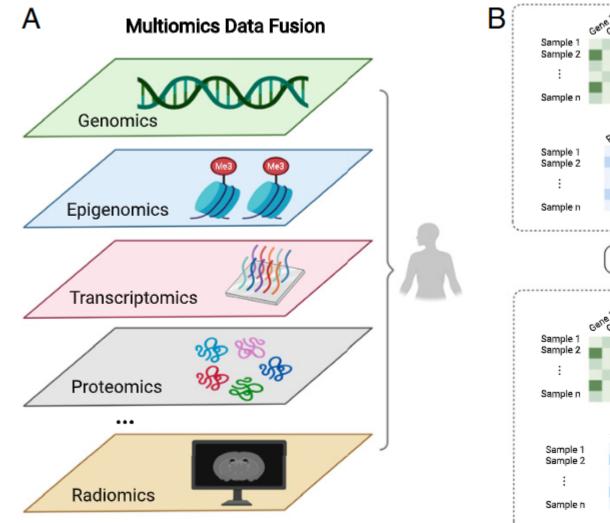
(a) One-view-one-network strategy

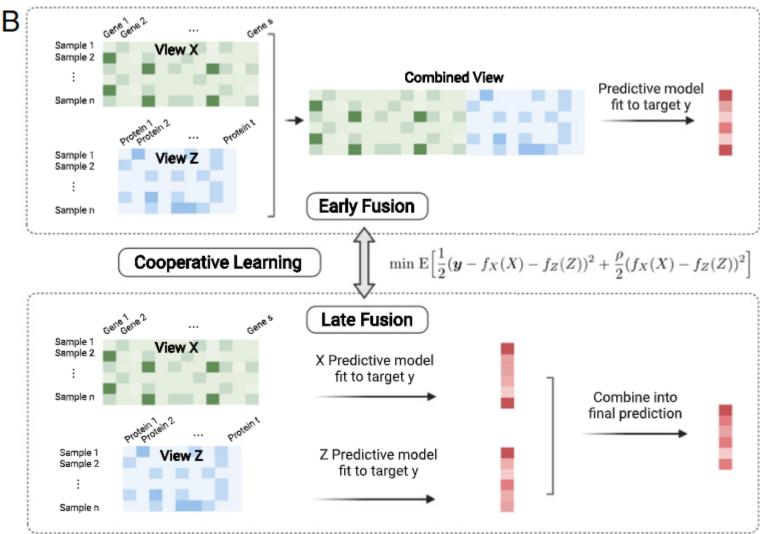


(b) Multi-view-one-network strategy

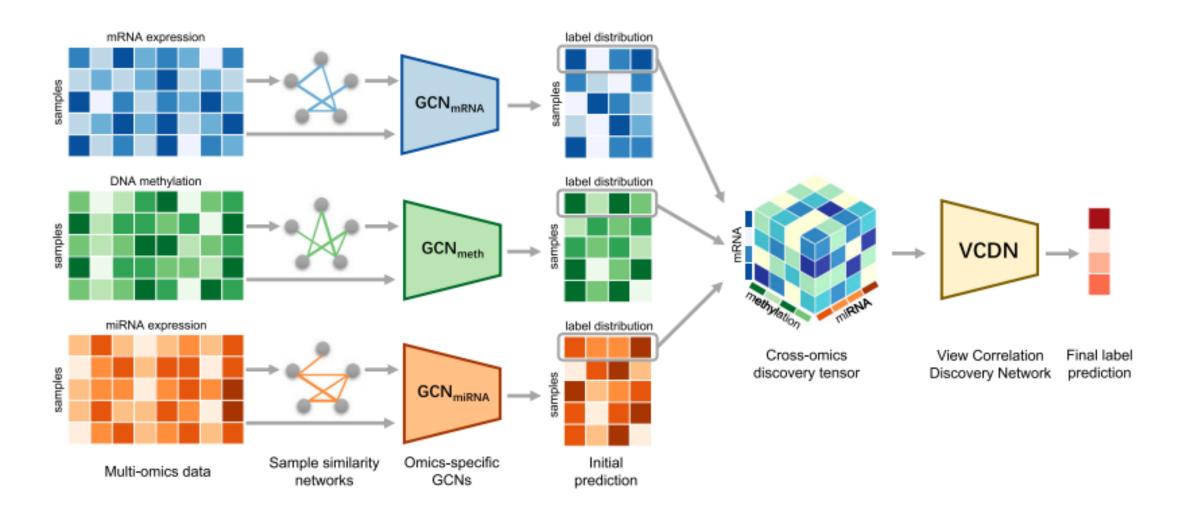
Deep multi-view learning methods: A review - ScienceDirect

# Multi-view learning

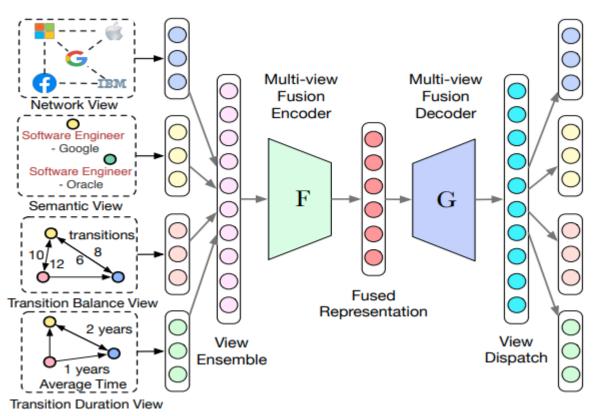




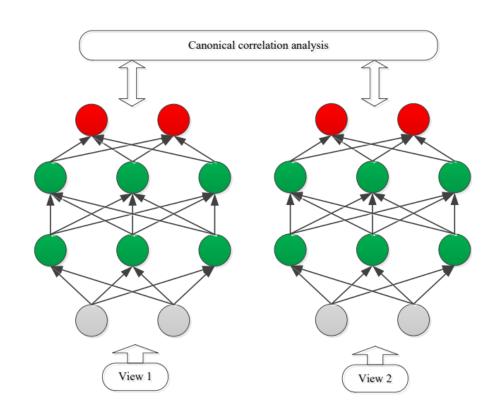
## Multi-view learning



#### How to fuse multi-view data



Auto-encoder



canonical correlation analysis

Deep multi-view learning methods: A review - ScienceDirect