

Diffusion processes in the brain

Fredrik E. Pettersen

April 25, 2014

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Brief introduction to the brain

Cells in the brain

Neurons:

- Signal processing

Neuroglia:

- Janitorial tasks

Basic diffusion

The basic diffusion equation reads

$$\frac{\partial C}{\partial t} = D \nabla^2 C \quad (1)$$

Einstein relations

$$D = \frac{k_B T}{6\pi\eta r} \quad (2)$$

$$\langle r^2 \rangle = 2dDt \quad (3)$$

Molecular dynamics

- Study of systems of atoms and their time-development
- Most research towards fracture mechanics and flow in tight rocks
- Much of the geometry is similar, but the length scale is a bit to small
- Dissipative fluid dynamics

My experiment - motivation

- Results from 2003 article
by Hrabětová and
Nicholson
- Max value of tortuosity
 $\lambda \leq 1.225$
- Diffusion modeling on
regular geometries

My experiment - results

- Making spheres of stationary atoms
- Measuring self diffusion constant of liquid using Einstein relation
- Comparing to self diffusion constant of bulk fluid
- Found $\lambda \approx 1.41$
- Limitations

Random walks

- Percolation theory
- Random walks and diffusion
- Spanning cluster
- Results from by Hrabětová and Nicholson
- Limitations

Firing in auditory nervous system

- Unanswered questions
 - limitation of tortuosity
 - tortuosity constant for increasing α
- Other modeling methods
- Multi scale models; the best from both worlds?

Thank you!

Output from DTI

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