1. Consider the relation R(a,b,c,d) with functional dependencies:

$$a \to bc, b \to a$$

Which of the following are BCNF decompositions of R?

- (a) R1(a,b,d), R2(a,c)
- (b) R1(a,b,d), R2(b,c)
- (c) R1(a,b,c), R2(b,d)
- (d) all decompositions are correct.

2. (2.5) Consider the relation R(a,b,c,d,E) with functional dependencies:

$$d \rightarrow c, aE \rightarrow d, d \rightarrow a, cE \rightarrow a.$$

What relations would be produced by the BCNF decomposition algorithm?

- (a) R1(a,b,c,d,E)
- (b) R1(a,b,c), R2(b,d,E)
- (c) R1(a,c,d), R2(b,d,E)
- (d) R1(a,d,E), R2(a,b,c,E)
- 3. (2.5) Consider the relation instance of R(a,b,c).

a	b	c
a1	b1	c1
a1	b2	c2
a1	b1	c2
a2	b1	c3
a2	b1	c1

Which of the following MVDs hold for this instance of R?

- (a) $A \rightarrow B$ YES NO
- (b) $B \rightarrow C$ YES NO
- (c) $A \rightarrow C$ YES NO
- (d) $C \rightarrow B$ YES NO
- 4. (2.5) Consider relation R(A, B, C, D, E). Suppose R contains the tuples (a, b, c, d, e) and (a, 2, c, 4,
 - 5). How many more tuples must be added so that R satisfies MVD A \rightarrow B and FD: B \rightarrow D.
 - (a) 2
 - (b) 4
 - (c) 6
 - (d) 8