

1. Consider the relation instance of R(a,b,c).

a	b	c
a_1	b_1	c_1
a_1	b_1	c_2
a_2	b_1	c_1
a_2	b_1	c_3

(a) (5) Which of the following FDs hold for this instance of R?

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|--------------------------|-----|----|---------------------------|-----|----|
| (i) $a \rightarrow b$ | YES | NO | (ii) $a \rightarrow c$ | YES | NO |
| (iii) $b \rightarrow a$ | YES | NO | (iv) $b \rightarrow c$ | YES | NO |
| (v) $c \rightarrow a$ | YES | NO | (vi) $c \rightarrow b$ | YES | NO |
| (vii) $ac \rightarrow b$ | YES | NO | (viii) $bc \rightarrow a$ | YES | NO |
| (ix) $ab \rightarrow c$ | YES | NO | (x) $abc \rightarrow a$ | YES | NO |

(b) (0.5) What is a key for R?

(a) (2) Consider a relation R1(a,b,c,d,E) with functional dependencies $a, b \rightarrow c$ and $c, d \rightarrow E$. Suppose there are at most 2 different values for each of a, b, and d. What's the maximum number of different values for E?

- 2
- 4
- 8
- insufficient information to determine answer

(b) (0.5) What is a key for R1?

2. (2) In the relation WORK(ssn,pno,date,hours), what real-world constraint is captured by $ssn, pno \rightarrow date$?

- An employee cannot work on multiple projects on the same date.
- An employee cannot work on the same project on different dates.
- An employee must work on all projects on the same date.
- none of the above information can be inferred from the fd.