Prerequisites

Note 1

621caffff9ce421bb4309fc0c1cf144c

A function is said to be $\{(c2)$ -multilinear $\}$ if and only if it is $\{(c1)$ -linear separately in each variable. $\}$

Note 2

a514ffb24744a278834d0048496a850

A function is said to be {c2=bilinear} if and only if {c1=it is a multilinear function of two argument.}

Note 3

6712178af383453faa8c5bad8aeabc89

{{c2:}An endomorphism}} of a vector space is {{c1:}a linear map from this space to itself.}}

Note 4

d6b4c6b47276475dbc8548d1c524080

The characteristic of a ring R is (c) the smallest positive number n such that

$$\underbrace{1+\cdots+1}_{n}=0,$$

or 0, if no such n exists.

Note 5

7ea5080a9df1419e88226f7df77af8db

(c1: The characteristic) of a ring R is denoted (c2: $\operatorname{char} R$.)

Note 6

e270ce3bf39a4ad4b08726ec08e3353a

Let V be a vector space over a field K. (c.: A linear map

$$V \to K$$

)) is called ([c2::a linear form on the vector space V.))

Note 7

19d3a5he7380467e9f537fc3ce7h1193

Let V be a vector space over a field K. (C.1: The set of all the linear forms $V \to K$)) is called (C2: the dual space of V.)

 $\{\{c_1:: The dual space\}\}\ of a vector space V is denoted <math>\{\{c_2:: V^*.\}\}$

Note 9

c3c550f6f7284b649efd64a23b3fba07

Let V be a vector space over a field K. (Case A bilinear map

$$V \times V \to K$$

)) is called ([c2::a bilinear form on the vector space V.))

Note 10

b578c7a8572d40ffbe4a3f132fda2107

A bilinear form $f:V\times V\to K$ is said to be {{c2}} nondegenerate{{}} if {{c1}} each of its corresponding linear maps $V\to V^*$ is nondegenerate.

Note 11

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Let $f: V \times V \to K$ be a bilinear form with a matrix A. Then, f is {conndegenerate} {condegenerate} {conde

Note 12

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Let V be a vector space over a field K and e_1, \ldots, e_n be a basis in V. Here The matrix

$$A = \left(f(e_i, e_j) \right) \sim n \times n$$

)) is called ((e2) the matrix of the bilinear form f on the basis e_1,\ldots,e_n .))

1.1. The notion of Lie algebra

Note 1

86bbc96abfb46a883a4acb108450cc1

At the first place a Lie algebra is (ici: a vector space L over a field \mathbf{F}).

Note 2

a252531934f4c00829418ab1f3a1d01

What is the signature of the new operation in the definition of a Lie algebra?

 $L \times L \to L$.

Note 3

a1cc6426fa49471dad192df5295fb310

The operation $L \times L \to L$ from the definition of a Lie algebra is denoted $(c.s.(x,y) \mapsto [xy])$.

Note 4

8bb3c76247ab416a97f8f6e247a6c2a2

The operation $(x,y) \mapsto [xy]$ from the definition of a Lie algebra is called (set: the bracket or commutator of x and y).

Note 5

6c529b4b819a45c3b91755b1280be2a2

How many axioms are there in the definition of a Lie algebra?

(L1), (L2), (L3).

Note 6

f8d0434e7d3c404b8319bf527f96627c

What is the axiom (L1) from the definition of a lie algebra?

The bracket operation is bilinear.

Note 7

807fbd0c878541998eb3be30e870652c

What is the axiom (L2) from the definition of a lie algebra?

 $[xx] = 0 \quad \text{ for all } x \in L.$

Note 8

d096a87546b14acfa601179c2ae323e8

What is the axiom (L3) from the definition of a Lie algebra?

[x[yz]] + [y[zx]] + [z[xy]] = 0 for all $x, y, z \in L$.

Note 9

db6289e2261549bcb58877ac4d6f36f7

Here the axiom (L3) from the definition of a Lie algebra, is called Here the Jacobi identity.

Note 10

fdd2c3d3027e4a34be5e9540f148a9c

Let L, L' be two Lie algebras over F. Read A vector space isomorphism $\phi: L \to L'$ satisfying

$$\phi([xy]) = [\phi(x)\phi(y)] \quad \forall x, y \in L$$

} is called {{c2:}an isomorphism of Lie algebras.}}

Note 11

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We say that two Lie algebras L,L' over F are (c2-isomorphic) if (c1-there exists a Lie algebra isomorphism $\phi:L\to L'$.)

Note 12

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Let L be a Lie algebra over F. ${\it Colored}$ A subspace K of L satisfying

$$[xy] \in K \quad \forall x, y \in K.$$

 $aise is called {{ iny called subalgebra of L}}$