Advanced Models and Methods in Operations Research Project: Unrelated parallel machines scheduling

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For each problem considered, instances and a code skeleton containing an instance parser and a solution checker are provided in the data/ and python/ folders of the project.

The algorithms must be implemented in the provided files between the tags TODO START and TODO END.

They must be tested on all the provided instances with the command: python3 problem.py-i instance.json -c certificate.json

And each solution file must be validated by the provided checker: python3 problem.py -a checker -i instance.json -c certificate.json

The results must be reproducible.

The delivrable must contain:

- A *short* report describing and justifying the proposed algorithms
- The code implementing the algorithms
- The solution files obtained on the provided instances

1 Dynamic Programming

We consider the Single machine order acceptance and scheduling problem with objective Total tardiness:

- Input:
 - -n jobs with $(j=1,\ldots,n)$
 - * processing time $p_i \in \mathbf{N}^+$
 - * due date $d_j \in \mathbf{N}^+$
 - * profit $v_i \in \mathbf{N}^+$

- Problem: find a sub-sequence of jobs
- Objective: maximize the total profit minus the total tardiness of the scheduled job

For a job j starting at s, its tardiness is equal to:

$$T_j = \max\{0, (s+p_j) - d_j\}$$

Propose and implement an algorithm based on Dynamic Programming for this problem.

2 Heuristic Tree Search

We consider the Single machine order acceptance and scheduling problem with objective Total weighted tardiness:

- Input:
 - -n jobs with $(j=1,\ldots,n)$
 - * processing time $p_i \in \mathbf{N}^+$
 - * due date $d_j \in \mathbf{N}^+$
 - * profit $v_j \in \mathbf{N}^+$
 - * weight $w_i \in \mathbf{N}^+$
- Problem: find a sub-sequence of jobs
- Objective: maximize the total profit minus the total weighted tardiness of the scheduled job

For a job j starting at s, its weighted tardiness is equal to w_jT_j .

Propose and implement an algorithm based on Heuristic Tree Search with Dynamic Programming for this problem.

3 Column Generation

+ Dynamic Programming

We consider the Unrelated parallel machine scheduling problem with objective Total tardiness:

- Input:
 - -m machines
 - -n jobs with $(j=1,\ldots,n)$
 - * processing time $p_j^i \in \mathbf{N}^+$ for each machine $i = 1, \dots, m$
 - * due date $d_i \in \mathbf{N}^+$
- Problem: find a schedule for each machine such that
 - each job is scheduled exactly once
- Objective: minimize the total tardiness of the schedule

Propose an exponential formulation and implement an algorithm based on a Column Generation heuristic for this problem.

4 Column Generation

+ Heuristic Tree Search

We consider the Unrelated parallel machine scheduling problem with objective Total weighted tardiness:

- Input:
 - -m machines
 - -n jobs with $(j = 1, \ldots, n)$
 - * processing time $p_j^i \in \mathbf{N}^+$ for each machine $i = 1, \dots, m$
 - * due date $d_j \in \mathbf{N}^+$
 - * weight $w_j \in \mathbf{N}^+$
- Problem: find a schedule for each machine such that
 - each job is scheduled exactly once
- Objective: minimize the total weighted tardiness of the schedule

Propose an exponential formulation and implement an algorithm based on a Column Generation heuristic for this problem.