

Advanced Models and Methods in Operations Research

Project: Unrelated parallel machines scheduling

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For each problem considered, instances and a code skeleton containing an instance parser and a solution checker are provided in the `data/` and `python/` folders of the project.

The algorithms must be implemented in the provided files between the tags `TODO START` and `TODO END`.

The algorithms must be tested on all the given instances with the command:
`./problem.py -i instance.txt -c certificate.txt`

Each solution must be verified with the provided checker: `./problem.py -a checker -i instance.txt -c certificate.txt`

The deliverable must contain:

- A *short* report describing and justifying the proposed algorithms
- The code implementing the algorithms
- The solution files obtained on the provided instances

1 Dynamic Programming

We consider the Single machine order acceptance and scheduling problem with objective Total tardiness:

- Input:
 - n jobs with $(j = 1, \dots, n)$
 - * processing time $p_j \in \mathbf{N}^+$
 - * due date $d_j \in \mathbf{N}^+$
 - * profit $v_j \in \mathbf{N}^+$
- Problem: find a sub-sequence of jobs
- Objective: maximize the total profit minus the total tardiness of the scheduled job

For a job j starting at s , its tardiness is equal to:

$$T_j = \max \{0, d_j - (s + p_j)\}$$

Propose and implement an algorithm based on Dynamic Programming for this problem.

2 Heuristic Tree Search

We consider the Single machine order acceptance and scheduling problem with objective Total weighted tardiness:

- Input:
 - n jobs with $(j = 1, \dots, n)$
 - * processing time $p_j \in \mathbf{N}^+$
 - * due date $d_j \in \mathbf{N}^+$
 - * profit $v_j \in \mathbf{N}^+$
 - * weight $w_j \in \mathbf{N}^+$
- Problem: find a sub-sequence of jobs
- Objective: maximize the total profit minus the total weighted tardiness of the scheduled job

For a job j starting at s , its weighted tardiness is equal to $w_j T_j$.

Propose and implement an algorithm based on Heuristic Tree Search with Dynamic Programming for this problem.

3 Column Generation Heuristic + Dynamic Programming

We consider the Unrelated parallel machine scheduling problem with objective Total tardiness:

- Input:
 - m machines
 - n jobs with $(j = 1, \dots, n)$
 - * processing time $p_j^i \in \mathbf{N}^+$ for each machine $i = 1, \dots, m$
 - * due date $d_j \in \mathbf{N}^+$
- Problem: find a schedule for each machine such that
 - each job is scheduled exactly once
- Objective: minimize the total tardiness of the schedule

Propose an exponential formulation and implement an algorithm based on a Column Generation heuristic for this problem.

4 Column Generation Heuristic + Heuristic Tree Search

We consider the Unrelated parallel machine scheduling problem with objective Total weighted tardiness:

- Input:

- m machines
- n jobs with $(j = 1, \dots, n)$
 - * processing time $p_j^i \in \mathbf{N}^+$ for each machine $i = 1, \dots, m$
 - * due date $d_j \in \mathbf{N}^+$
 - * weight $d_j \in \mathbf{N}^+$
- Problem: find a schedule for each machine such that
 - each job is scheduled exactly once
- Objective: minimize the total weighted tardiness of the schedule

Propose an exponential formulation and implement an algorithm based on a Column Generation heuristic for this problem.