# Arondight's Standard Code Library\*

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 $<sup>{\</sup>rm ^*https://github.com/footoredo/Arondight}$ 

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# Chapter 1 计算几何

#### 1.1 二维

```
1.1.1 基础
```

```
int sign(DB x) {
           return (x > eps) - (x < -eps);
     DB msqrt(DB x)
          return sign(x) > 0 ? sqrt(x) : 0;
     struct Point {
           DB x, y;
 10
           Point rotate(DB ang) const { // 逆时针旋转 ang 弧度
11
                 return Point(cos(ang) * x - sin(ang) * y,
12
13
                            cos(ang) * y' + sin(ang) * x';
14
           Point turn90() const { // 逆时针旋转 90 度
15
                 return Point(-y, x);
16
          Point unit() const {
    return *this / len();
17
18
19
20
21
22
23
     DB dot(const Point& a, const Point& b) {
           return a.x * b.x + a.y * b.y;
24
     DB det(const Point& a, const Point& b) {
    return a.x * b.y - a.y * b.x;
25
26
    #define cross(p1,p2,p3) ((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
#define cross0p(p1,p2,p3) sign(cross(p1,p2,p3))
bool isLL(const Line& l1, const Line& l2, Point& p) { // 直线与直线交点
27
28
29
30
          DB s1 = det(l2.b - l2.a, l1.a - l2.a),
s2 = -det(l2.b - l2.a, l1.b - l2.a);
31
32
          if (!sign(s1 + s2)) return false;
p = (l1.a * s2 + l1.b * s1) / (s1 + s2);
33
34
35
           return true;
36
     bool onSeg(const Line& l, const Point& p) { // 点在线段上 return sign(det(p - l.a, l.b - l.a)) == 0 && sign(dot(p - l.a, p - l.b)) <= 0;
37
38
     Point projection(const Line & l, const Point& p) {
   return l.a + (l.b - l.a) * (dot(p - l.a, l.b - l.a) / (l.b - l.a).len2());
39
40
41
42
     DB disToLine(const Line& l, const Point& p) { // 点到 * 直线 * 距离
43
           return fabs(det(p - l.á, l.b - l.a) / (l.b - l.a).len());
44
45
     |DB disToSeg(const Line& l, const Point& p) { // 点到线段距离
          return sign(dot(p - l.a, l.b - l.a)) * sign(dot(p - l.b, l.a - l.b)) == 1 ?
         \rightarrow disToLine(l, p) : std::min((p - l.a).len(), (p - l.b).len()):
47
    // 圆与直线交点
bool isCL(Circle a, Line l, Point& p1, Point& p2) {
DB x = dot(l.a - a.o, l.b - l.a),
48
49
50
          y = (l.b - l.a).len2(),
d = x * x - y * ((l.a - a.o).len2() - a.r * a.r);
if (sign(d) < 0) return false;
Point p = l.a - ((l.b - l.a) * (x / y)), delta = (l.b - l.a) * (msqrt(d) / y);</pre>
51
52
53
55
56
           p1 = p + delta; p2 = p - delta;
           return true:
57
58
     //圆与圆的交面积
59
     DB areaCC(const Circle& c1, const Circle& c2) {
          DB d = (c1.o - c2.o).len();
if (sign(d - (c1.r + c2.r)) >= 0) return 0;
if (sign(d - std::abs(c1.r - c2.r)) <= 0) {
61
62
63
                DB r = std::min(cl.r, c2.r);
                return r * r * PI;
65
          DB x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),

t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);

return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
66
69
70 | // 圆与圆交点
```

```
71 | bool isCC(Circle a, Circle b, P& p1, P& p2) {
          DB s1 = (a.o - b.o).len();
if (sign(s1 - a.r - b.r) > 0 || sign(s1 - std::abs(a.r - b.r)) < 0) return false;
          DB s2 = (a.r * a.r - b.r * b.r) / s1;
          DB aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
P o = (b.o - a.o) * (aa / (aa + bb)) + a.o;
P delta = (b.o - a.o).unit().turn90() * msqrt(a.r * a.r - aa * aa);
 75
 76
 78
          p1 = o + delta, p2 = o - delta;
 79
          return true;
 80
 81 / / 求点到圆的切点,按关于点的顺时针方向返回两个点
 82 bool tantP(const Circle &c, const Point &p0, Point &p1, Point &p2) {
83     double x = (p0 - c.o).len2(), d = x - c.r * c.r;
          if (d < eps) return false; // 点在圆上认为没有切点
          Point p = (p0 - c.o) * (c.r * c.r / x);
          Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
 87
          p1 = c.o + p + delta;
 88
          p2 = c.o + p - delta;
 89
          return true;
 90
 91 // 求圆到圆的外共切线,按关于 cl.o 的顺时针方向返回两条线
92 vector<Line> extanCC(const Circle &cl, const Circle &c2) {
          vector<Line> ret;
 94
          if (sign(c1.r - c2.r) == 0) {
               dir = (2.0 - c1.0;
dir = (dir * (c1.r / dir.len())).turn90();
 95
               ret.push_back(Line(c1.0 + dir, c2.0 + dir));
ret.push_back(Line(c1.0 - dir, c2.0 - dir));
 97
 98
 99
100
               Point p = (c1.0 * -c2.r + c2.o * c1.r) / (c1.r - c2.r):
               Point p1, p2, q1, q2;
if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
   if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
101
103
                     ret.push_back(Line(p1, q1))
104
                     ret.push_back(Line(p2, q2));
105
106
107
108
          return ret;
109
     // 求圆到圆的内共切线,按关于 c1.o 的顺时针方向返回两条线
     std::vector<Line> intanCC(const Circle &c1, const Circle &c2) {
111
          std::vector<Line> ret;
112
113
          Point p = (c1.0 * c2.r + c2.o * c1.r) / (c1.r + c2.r);
114
          Point p1, p2, q1, q2;
115
          if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) { // 两圆相切认为没有切线
                ret.push_back(Line(p1, q1));
116
117
               ret.push_back(Line(p2, q2));
118
119
          return ret;
120
121
     bool_contain(vector<Point> polygon, Point p) { // 判断点 p 是否被多边形包含,包括落在边界上
          int ret = 0, n = polygon.size();
for(int i = 0; i < n; ++ i) {</pre>
123
               The first continue;
Point u = polygon[i], v = polygon[(i + 1) % n];
if (onSeg(Line(u, v), p)) return true; // Here I guess.
if (sign(u.y - v.y) <= 0) swap(u, v);
if (sign(p.y - u.y) > 0 || sign(p.y - v.y) <= 0) continue;</pre>
124
125
126
127
128
               ret += sign(det(p, v, u)) > 0;
129
130
          return ret & 1;
131
     // 用半平面 (q1,q2) 的逆时针方向去切凸多边形
132
     std::vector<Point> convexCut(const std::vector<Point>&ps, Point q1, Point q2) {
          std::vector<Point> qs; int n = ps.size();
134
          for (int i = 0; i < n; ++i) {
135
               Point p1 = ps[i], p2 = ps[(i + 1) % n];
136
               int d1 = crossOp(q1,q2,p1), d2 = crossOp(q1,q2,p2);
if (d1 >= 0) qs.push_back(p1);
if (d1 * d2 < 0) qs.push_back(isSS(p1, p2, q1, q2));
137
138
139
140
          return qs;
141
142
143 // 求凸包
     std::vector<Point> convexHull(std::vector<Point> ps) {
          int n = ps.size(); if (n <= 1) return ps;
std::sort(ps.begin(), ps.end());
145
146
147
          std::vector<Point> qs;
```

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#### 1.1.2 凸包

```
// 凸包中的点按逆时针方向
    struct Convex {
       shell.push_back(p[i]);
12
13
14
15
        void make_convex() {
            std::sort(a.begin(), a.end());
make_shell(a, lower);
std::reverse(a.begin(), a.end());
16
17
             make_shell(a, upper);
18
            a = lower; a.pop_back();
a.insert(a.end(), upper.begin(), upper.end());
if ((int)a.size() >= 2) a.pop_back();
19
20
21
22
23
24
25
26
27
28
29
30
             n = a.size();
        void init(const std::vector<Point>& _a) {
             clear(a); a = _a; n = a.size();
make convex();
        void read(int _n) { // Won't make convex.
            clear(a); n = _n; a.resize(n);
for (int i = 0; i < n; i++)</pre>
31
32
33
34
35
36
37
                 a[i].read();
        int l = 0, r = (int)convex.size() - 2;
             assert(r \ge 0);
             for (; l + 1 < r; ) {
int mid = (l + r) / 2;
38
39
                  if (sign(det(convex[mid + 1] - convex[mid], vec)) > 0)
40
41
42
                      r = mid:
                 else l = mid;
43
             return std::max(std::make_pair(det(vec, convex[r]), r),
44
                      std::make_pair(det(vec, convex[0]), 0));
45
46
        int binary_search(Point u, Point v, int l, int r) {
             int s1 = sign(det(v - u, a[l % n] - u));
for (; l + l < r; ) {</pre>
47
48
49
50
51
52
53
54
55
                  int mid = (l + r) / 2;
                  int smid = sign(det(v'- u, a[mid % n] - u));
                 if (smid == s1) \[ l = \]mid;
                 else r = mid;
             return 1 % n;
56
57
58
        // 求凸包上和向量 vec 叉积最大的点,返回编号,共线的多个切点返回任意一个
        int get_tangent(Point vec) {
            std::pair<DB, int> ret = get_tangent(upper, vec);
ret.second = (ret.second + (int)lower.size() - 1) % n;
ret = std::max(ret, get_tangent(lower, vec));
59
60
61
             return ret.second:
62
63
        // 求凸包和直线 u, v 的交点,如果不相交返回 false,如果有则是和 (i, next(i))的交点,交在点上
       → 不确定返回前后两条边其中之
        bool get_intersection(Point u, Point v, int &i0, int &i1) {
             int p0 = get_tangent(u - v), p1 = get_tangent(v - u);
```

#### 1.1.3 三角形的心

```
Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心 double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(), s = fabs(det(B - A, C - A)),
             r = s / p;
4
        return (A * a' + B * b + C * c) / (a + b + c);
    Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
        Point bb = b - a, cc = c - a;
        double db = bb.lén2(), dc = cc.len2(), d = 2 * det(bb, cc);
        return a - Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
11
12
13
   Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
        Point ba = b - a, ca = c - a, bc = b - c;
14
        double Y = ba.y * ca.y * bc.y,
15
                 A = ca.x * ba.y - ba.x * ca.y,
                 x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,

y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
16
17
18
        return Point(x0, y0);
19
```

#### 1.1.4 半平面交

```
struct Point
        int quad() const { return sign(y) == 1 \mid | (sign(y) == 0 \&\& sign(x) >= 0); }
   struct Line {
5
        bool include(const Point &p) const { return sign(det(b - a, p - a)) > 0; }
         Line push() const{ // 将半平面向外推 eps
             const double eps = 1e-6;
             Point delta = (b - a).turn90().norm() * eps;
             return Line(a - deltá, b - delta);
10
11
   bool sameDir(const Line &l0, const Line &l1) { return parallel(l0, l1) &&
12
       \rightarrow sign(dot(l0.b - l0.a, l1.b - l1.a)) == 1; }
   bool operator < (const Point &a, const Point &b) {
   if (a.quad() != b.quad()) {</pre>
14
15
             return a.quad() < b.quad();</pre>
16
17
             return sign(det(a, b)) > 0;
18
19
20
   bool operator < (const Line &l0, const Line &l1) {
   if (sameDir(l0, l1)) {</pre>
22
23
24
25
26
             return l1.include(l0.a);
             return (l0.b - l0.a) < (l1.b - l1.a);
   bool check(const Line &u, const Line &v, const Line &w) { return

    w.include(intersect(u, v)); }
vector<Point> intersection(vector<Line> &l) {
    sort(l.begin(), l.end());
}

28
29
30
        for (int i = 0; i < (int)l.size(); ++i) {
   if (i && sameDir(l[i], l[i - 1])) {
31
32
33
                  continue:
34
35
             while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], l[i]))

    q.pop_back();
             while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
36
37
             q.push_back(l[i]);
38
```

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#### 1.1.5 圆交面积及重心

```
struct Event {
        Point p;
        double ang;
         int delta:
        Event (Point p = Point(0, 0), double ang = 0, double delta = 0) : p(p), ang(ang),

    delta(delta) {}
    bool operator < (const Event &a, const Event &b) {
        return a.ang < b.ang;</pre>
10
   void addEvent(const Circle &a, const Circle &b, vector<Event> &evt, int &cnt) {
        double d2 = (a.o - b.o).len2(),
dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2,
11
12
13
                 pRatio = \dot{sqr}(-(d2 - \dot{sqr}(a.r - b.r)) * (d2 - \dot{sqr}(a.r + b.r)) / (d2 * d2 *
14
        Point d = b.o - a.o, p = d.rotate(PI / 2),
q0 = a.o + d * dRatio + p * pRatio,
15
16
                q1 = a.o + d * dRatio - p * pRatio;
17
        double ang 0 = (q0 - a.o).ang(),
                 ang1 = (q1 - a.o).ang()
18
        evt.push_back(Event(q1, ang1, 1));
evt.push_back(Event(q0, ang0, -1));
19
20
21
22
        cnt += ang1 > ang0;
23 | bool issame(const Circle &a, const Circle &b) { return sign((a.o - b.o).len()) == 0 &&
       \hookrightarrow sign(a.r - b.r) == 0; }
   bool overlap(const Circle &a, const Circle &b) { return sign(a.r - b.r - (a.o -
       \rightarrow b.o).len()) >= 0;
   bool intersect(const Circle &a, const Circle &b) { return sign((a.o - b.o).len() - a.r
       \hookrightarrow - b.r) < 0; }
   Circle c[N]
   double area[N];
                        // area[k] -> area of intersections >= k.
28 | Point centroid[N];
   bool keep[N];
   void add(int cnt, DB a, Point c) {
30
31
        area[cnt] += a;
32
        centroid[cnt] = centroid[cnt] + c * a;
33
34
    void solve(int C) {
35
36
        for (int i = 1; i <= C; ++ i) {
             area[i] = 0;
centroid[i] = Point(0, 0);
37
38
39
        for (int i = 0; i < C; ++i) {
40
              int cnt = 1:
41
             vector<Event> evt;
42
43
             for (int j = 0; j < i; ++j) if (issame(c[i], c[j])) ++cnt;
for (int j = 0; j < C; ++j) {</pre>
44
45
                  if (j != i && !issame(c[i], c[j]) && overlap(c[j], c[i])) {
    ++cnt;
46
47
48
              for (int j = 0; j < C; ++j) {
    if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) &&
       \hookrightarrow intersect(c[i], c[i]))
                       addÉvent(c[i], c[j], evt, cnt);
50
51
52
53
54
55
             if (evt.size() == 0u) {
                  `add(cnt,`PI * c[i].r * c[i].r, c[i].o);
56
57
                  sort(evt.begin(), evt.end());
                  evt.push_back(evt.front());
for (int j = 0; j + 1 < (int)evt.size(); ++j) {
    cnt += evt[j].delta;</pre>
58
```

```
add(cnt, det(evt[j].p, evt[j + 1].p) / 2, (evt[j].p + evt[j + 1].p) /
                             \hookrightarrow 3);
61
                                                                                                  double ang = evt[j + 1].ang - evt[j].ang;
                                                                                                 if (ang < 0) {
62
                                                                                                                    `ang += PI * 2;
63
64
65
                                                                                                   if (sign(ang) == 0) continue;
66
                                                                                                  add(cnt, ang * c[i].r * c[i].r / 2, c[i].o +
67
                                                                                                                     Point(\sin(ang1) - \sin(ang0), -\cos(ang1) + \cos(ang0)) * (2 / (3 *
                             \rightarrow ang) * c[i].r))
                                                                                                  add(cnt, -sin(ang) * c[i].r * c[i].r / 2, (c[i].o + evt[j].p + evt[j + c[i].n + c[
68
                              \hookrightarrow 1].p) / 3);
70
71
72
73
                                     for (int i = 1; i <= C; ++ i)
                                                         if (sign(area[i])) {
74
75
76
                                                                             centroid[i] = centroid[i] / area[i];
```

#### 1.2 三维

#### 1.2.1 基础

```
// 三维绕轴旋转, 大拇指指向 axis 向量方向, 四指弯曲方向转 w 弧度
    Point rotate(const Point& s, const Point& axis, DB w) {
          DB x = axis.x, y = axis.y, z = axis.z;
          DB s1 = x * x + y * y + z * z, ss1 = msqrt(s1),
              cosw = cos(w), sinw = sin(w);
          DB a[4][4];
          memset(\bar{a}, \bar{0}, sizeof a); a[3][3] = 1;
                    = ((y * y + z * z) * cosw + x * x) / s1;
= x * y * (1 - cosw) / s1 + z * sinw / ss1;
10
                     = x * z * (1 - \cos w)
                                                   / s1 - y * sinw / ss1;
                     = x * y * (1 - \cos w) / s1 - z * \sin w / ss1;
12
13
                     = ((x * x + z * z) * cosw + y * y) / s1;
                     = y * z * (1 - cosw) / s1 + x * sinw / ss1;
= x * z * (1 - cosw) / s1 + y * sinw / ss1;
14
15
         [2][1] = y * z * (1 - cosw) / s1 - x * sinw / ss1;
a[2][2] = ((x * x + y * y) * cos(w) + z * z) / s1;
DB ans[4] = {0, 0, 0, 0}, c[4] = {s.x, s.y, s.z, 1};
for (int i = 0; i < 4; ++ i)
18
19
                for (int j = 0; j < 4; ++ j)
ans[i] += a[j][i] * c[j]
20
21
22
          return Point(ans[0], ans[1], ans[2]);
23
```

#### 1.2.2 凸包

```
__inline P cross(const P& a, const P& b) {
       return P(
                a.y * b.z - a.z * b.y,
                a.\dot{z} * b.x - a.x * b.\dot{z}
5
                a.x * b.y - a.y * b.x
           );
    __inline DB mix(const P& a, const P& b, const P& c) {
10
       return dot(cross(a, b), c);
11
13
   __inline DB volume(const P& a, const P& b, const P& c, const P& d) {
       return mix(b - a, c - a, d - a);
15
16
17
   struct Face {
18
       int a, b, c;
19
       __inline Face() {}
20
       __inline Face(int _a, int _b, int _c):
21
           a(_a), b(_b), c(_c) {}
22
       __inline DB area() const
23
           return 0.5 \times cross(p[b] - p[a], p[c] - p[a]).len();
24
25
       __inline P normal() const {
```

```
return cross(p[b] - p[a], p[c] - p[a]).unit();
27
28
29
            __inline DB dis(const P& p0) const {
                   return dot(normal(), p0 - p[a]);
30
31 };
32
33 st
     std::vector<Face> face, tmp; // Should be O(n).
34
35
      int mark[N][N], Time, n;
36
       __inline void add(int v) {
37
            ++ Time:
38
            clear(tmp);
39
            for (int i = 0; i < (int)face.size(); ++ i) {</pre>
                   int a = face[i].a, b = face[i].b, c = face[i].c;
if (sign(volume(p[v], p[a], p[b], p[c])) > 0) {
    mark[a][b] = mark[b][a] = mark[a][c] =
    mark[c][a] = mark[b][c] = mark[c][b] = Time;
40
41
42
43
44
45
                   else {
46
                          tmp.push_back(face[i]);
47
48
           flear(face); face = tmp;
for (int i = 0; i < (int) tmp.size(); ++ i) {
   int a = face[i].a, b = face[i].b, c = face[i].c;
   if (mark[a][b] == Time) face.emplace_back(v, b, a);
   if (mark[b][c] == Time) face.emplace_back(v, c, b);
   if (mark[b][c] == Time) face.emplace_back(v, c, c);</pre>
49
50
51
52
53
                   if (mark[c][a] == Time) face.emplace_back(v, a, c);
54
55
56
                   assert(face.size() < 500u);
57
58
59
      void reorder() {
           for (int i = 2; i < n; ++ i) {
    P tmp = cross(p[i] - p[0], p[i] - p[1]);
    if (sign(tmp.len())) {
60
61
62
63
                          std::swap(p[i], p[2]);
for (int j = 3; j < n; ++ j)
64
65
                                if (sign(volume(p[0], p[1], p[2], p[j]))) {
    std::swap(p[j], p[3]);
66
67
                                        return;
68
69
70
            }
71
72
73
      void build_convex() {
74
            reorder();
75
76
            clear(face);
            face.emplace_back(0, 1, 2);
            face.emplace_back(0, 2, 1);
for (int i = 3; i < n; ++ i)</pre>
77
78
79
                   add(i);
```

## Chapter 2 数论

11

Given  $a_0, a_1, \dots, a_{m-1}$  $a_n = c_0 \times a_{n-m} + \dots + c_{m-1} \times a_{n-1}$ 

}else {

# 2.1 $O(m^2 \log n)$ 求线性递推数列第 n 项

Solve for  $a_n = v_0 \times a_0 + v_1 \times a_1 + \cdots + v_{m-1} \times a_{m-1}$ 

u[x] = 1 % p;

```
for(int i(0); i < m; i++) {
    for(int j(0), t(i + b); j < m; j++, t++) {
        u[t] = (u[t] + v[i] * v[j]) % p;</pre>
13
14
15
16
                      for(int i((m << 1) - 1); i >= m; i--) {
    for(int j(0), t(i - m); j < m; j++, t++) {
        u[t] = (u[t] + c[j] * u[i]) % p;</pre>
18
19
20
21
22
23
24
25
26
                copy(u, u + m, v);
           //a[n] = v[0] * a[0] + v[1] * a[1] + ... + v[m - 1] * a[m - 1].
27
28
           for(int i(m); i < 2 * m; i++) {
                `a[i] = 0
                a[i] = (a[i] + (long long)c[j] * a[i + j - m]) % p;
30
31
32
33
          for(int j(0); j < m; j++) {</pre>
34
35
                b[j] = 0;
                for(int i(0); i < m; i++) {
                      b[j] = (b[j] + v[i] * a[i + j]) % p;
36
37
38
39
          for(int j(0); j < m; j++) {
   a[j] = b[j];</pre>
40
41
42
```

#### 2.2 求逆元

```
void ex_gcd(long long a, long long b, long long &x, long long &y) {
         if (b == 0)^{-}
             \dot{x} = 1;
              y = 0;
              return;
         long long xx, yy;
         ex_gcd(b, a % b, xx, yy);
         y = xx - a / b * yy;
10
         \dot{x} = yy;
11
12
13
   long long inv(long long x, long long MODN) {
   long long inv_x, y;
   ex_gcd(x, MODN, inv_x, y);
15
16
         return (inv_x % MODN + MODN) % MODN;
17
```

## 2.3 中国剩余定理

## 2.4 魔法 CRT

```
for (int j = 0; j < i; j ++) {
    int t = (x[i] - x[j] + mod[i]) % mod[i];
    if (t < 0) t += mod[i];
    x[i] = 1LL * t * Inv[j][i] % mod[i];
}

int sum = 1, ret = x[0] % MOD;
for (int i = 1; i < N; i ++) {
    sum = 1LL * sum * mod[i - 1] % MOD;
    ret += 1LL * x[i] * sum % MOD;
    if (ret >= MOD) ret -= MOD;
}

for (int i = 0; i < N; i ++) {
    Inv[i][j] = fpw(mod[i], mod[j] - 2, mod[j]);
}</pre>
```

### 2.5 素性测试

```
int strong_pseudo_primetest(long long n,int base) {
         long long n2=n-1,res;
         while(n2\%2==0) n2>>=1,s++;
         res=powmod(base,n2,n);
         if((res==1)||(res==n-1)) return 1;
         while(s > = 0)
              res=muĺmod(res,res,n);
              if(res==n-1) return 1;
11
13
         return 0; // n is not a strong pseudo prime
14
   int isprime(long long n) {
    static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
    static LL lim[]={4,0,1373653LL,25326001LL,252000000000LL,2152302898747LL,
15
16
17

→ 3474749660383LL,341550071728321LL,0,0,0,0,0);

18
         if(n<2||n==3215031751LL) return 0;
        for(int i=0;i<12;++i){
    if(n<lim[i]) return 1;</pre>
19
20
21
22
23
              if(strong_pseudo_primétest(n,testNum[i])==0) return 0;
24
```

## 2.6 质因数分解

```
int ansn; LL ans[1000];
   LL func(LL x, LL n) { return(mod_mul(x,x,n)+1)%n; }
   LL Pollard(LĹ n){
        LL i,x,y,p;
if(Rabin_Miller(n)) return n;
        if(!(n&1)) return 2;
        for(i=1;i<20;i++){
             x=i; y=fúnc(x,n); p=gcd(y-x,n);
while(p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)%n,n)%n;}
             if(p==0||p==n) continue;
             return b
13 }
14 void factor(LL n){
15 LL x:
16
        x=Pollard(n);
        if(x==n){ ans[ansn++]=x; return; }
17
18
        factor(x), factor(n/x);
```

# 2.7 线下整点

```
 \begin{array}{c} 1 \\ \text{//} \sum_{i=0}^{n-1} \left\lfloor \frac{a+bi}{m} \right\rfloor, \; n,m,a,b>0 \\ \text{LL solve(LL n,LL a,LL b,LL m)} \\ \text{if}(b==0) \; \text{return n*(a/m);} \end{array}
```

```
4     if(a>=m) return n*(a/m)+solve(n,a%m,b,m);
5     if(b>=m) return (n-1)*n/2*(b/m)+solve(n,a,b%m,m);
6     return solve((a+b*n)/m,(a+b*n)%m,m,b);
7 }
```

# Chapter 3 代数

### 3.1 快速傅里叶变换

### 3.2 自适应辛普森积分

```
namespace adaptive_simpson
         template<typename function>
         inline double area(function f, const double &left, const double &right) {
   double mid = (left + right) / 2;
   return (right - left) * (f(left) + 4 * f(mid) + f(right)) / 6;
         template<typename function>
         inline double simpson(function f, const double &left, const double &right, const
       → double &eps, const double &area_sum) {
   double mid = (left + right) / 2;
   double area_left = area(f, left, mid);
   double area_right = area(f, mid, right);
11
12
              double area_total = area_left + area_right;
13
14
              if (fabs(area_total - area_sum) <= 15 * eps)
15
                   return area_total + (area_total - area_sum) / 15;
16
17
              return simpson(f, left, right, eps / 2, area_left) + simpson(f, mid, right,
       18
19
20
         template<typename function>
21
         inline double simpson(function f, const double &left, const double &right, const

    double &eps) {
22
              return simpson(f, left, right, eps, area(f, left, right));
23
24
```

## 3.3 单纯形

```
1 const double eps = 1e-8:
   // max{c * x | Ax <= b, x >= 0} 的解,无解返回空的 vector,否则就是解.
   vector<double> simplex(vector<vector<double> > &A, vector<double> b, vector<double> c)
        int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
5
        vector<vector<double> > D(n + 2, vector<double>(m + 1));
        vector<int> ix(n + m);
        for(int i = 0; i < n' + m; i++) {
            ix[i] = i;
        for(int i = 0; i < n; i++) {
    for(int j = 0; j < m - 1; j++) {
        D[i][j] = -A[i][j];</pre>
10
11
12
13
            \tilde{D}[i][m-1]=1;
14
            D[i][m] = b[i];
15
```

```
if (D[r][m] > D[i][m]) {
17
                    r = i;
18
19
20
21
22
23
24
25
26
27
28
29
30
          for(int_j = 0; j < m - 1; j++) {
               `D[n][j] = c[j];
         \hat{D}[n + 1][m - 1] = -1;
          for(double d; ;) {
               if (r < ń)
                    31
32
33
34
35
36
37
38
39
                               `Ď[r][jĺ *= -D[r][s];
                    for(int i = 0; i <= n + 1; i++) {
    if (i != r) {
                                for(int j = 0; j <= m; j++) {
                                     if (j != s) {
    D[i][j] += D[r][j] * D[i][s];
40
41
                               D[i][s] *= D[r][s];
42
43
44
45
              f = -1, s = -1;
for(int j = 0; j < m; j++) {
    if (s < 0 || ix[s] > ix[j]) {
46
47
48
                          if (D[n + 1][j] > eps || D[n + 1][j] > -eps && D[n][j] > eps) {
49
50
51
52
53
               if (s < 0) {
54
55
                    break;
               for(int i = 0; i < n; i++) {
    if (D[i][s] < -eps) {
56
57
58
                          if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -eps
59
                                || d < eps && ix[r + m] > ix[i + m]) {
60
61
62
                               r = i;
63
64
65
66
67
               if (r < 0) {
                     return vector<double> ();
68
69
70
          if (D[n + 1][m] < -eps) {
71
72
73
               return vector<double> ();
74
75
76
77
         vector<double> x(m - 1);
         for(int i = m; i < n + m; i++) {
    if (ix[i] < m - 1) {
        x[ix[i]] = D[i - m][m];
    }
78
79
80
         return x;
```

# Chapter 4 字符串

## 4.1 后缀数组

```
const int MAXN = MAXL * 2 + 1;
int a[MAXN], x[MAXN], y[MAXN], c[MAXN], sa[MAXN], rank[MAXN], height[MAXN];
void calc_sa(int n) {
   int m = alphabet, k = 1;
   memset(c, 0, sizeof(*c) * (m + 1));
   for (int i = 1; i <= n; ++i) c[x[i] = a[i]]++;
   for (int i = 1; i <= m; ++i) c[i] += c[i - 1];</pre>
```

```
for (int i = n; i; --i) sa[c[x[i]]--] = i;
for (; k <= n; k <<= 1) {</pre>
10
                         int tot = k;
                       for (int i = n - k + 1; i <= n; ++i) y[i - n + k] = i;
for (int i = 1; i <= n; ++i)
   if (sa[i] > k) y[++tot] = sa[i] - k;
memset(c, 0, sizeof(*c) * (m + 1));
for (int i = 1; i <= n; ++i) c[v[i]]++:
13
                       memset(c, w, sizeo(*c) * (m + 1));
for (int i = 1; i <= n; ++i) c[x[i]]++;
for (int i = 1; i <= m; ++i) c[i] += c[i - 1];
for (int i = n; i; --i) sa[c[x[y[i]]]--] = y[i];
for (int i = 1; i <= n; ++i) y[i] = x[i];
tot = 1; x[sa[1]] = 1;
for (int i = 2; i <= n; ++i) {</pre>
15
19
20
                                 if (max(sa[i], sa[i - 1]) + k > n || y[sa[i]] != y[sa[i - 1]] || y[sa[i] +
21
            \rightarrow k] != y[sa[i - 1] + k]) ++tot;
                                x[sa[i]] = tot;
23
24
25
26
27
28
                        if (tot == n) break; else m = tot;
      void calc_height(int n) {
   for (int i = 1; i <= n; ++i) rank[sa[i]] = i;
   for (int i = 1; i <= n; ++i) {</pre>
29
                       height[rank[i]] = max(0, height[rank[i - 1]] - 1);
if (rank[i] == 1) continue;
int j = sa[rank[i] - 1];
while (max(i, j) + height[rank[i]] <= n && a[i + height[rank[i]]] == a[j +
30
31
33
            → height[rank[i]]]) ++height[rank[i]];
34
35
```

#### 4.2 后缀自动机

```
static const int MAXL = MAXN * 2; // MAXN is original length static const int alphabet = 26; // sometimes need changing
    int l, last, cnt, trans[MAXL][álphabet], par[MAXL], sum[MAXL], seq[MAXL], mxl[MAXL],
       → size[MAXL]; // mxl is maxlength, size is the size of right
    char str[MAXL];
    inline void init()
        10
11
12
    inline void extend(int pos, int c)
13
         int p = last, np = last = ++cnt;
mxl[np] = mxl[p] + 1; size[np] = 1;
for (; p && !trans[p][c]; p = par[p]) trans[p][c] = np;
15
16
         if(!p) par[np] = 1;
17
         else {
18
              int q = trans[p][c];
if (mxl[p] + 1 == mxl[q]) par[np] = q;
19
20
               else {
21
22
23
                    int nq = ++cnt;
mxl[nq] = mxl[p] + 1;
                    memcpy(trans[nq], trans[q], sizeof(trans[nq]));
                    par[nq] = par[q];
par[np] = par[q] = nq;
25
26
27
                    for (; trans[p][c] == q; p = par[p]) trans[p][c] = nq;
28
         }
29
    30
31
        memset(sum, 0, sizeof(*sum) * (l * 2 + 1));
for (int i = 1; i <= cnt; ++i) sum[mxl[i]]++;
for (int i = 1; i <= l; ++i) sum[i] += sum[i - 1];
for (int i = cnt; i; --i) seq[sum[mxl[i]]--] = i;
for (int i = cnt; i; --i) size[par[seq[i]]] += size[seq[i]];</pre>
33
36
37
```

## 4.3 EX 后缀自动机

```
inline void add_node(int x, int &last) {
int lastnode = last;
```

```
if (c[lastnode][x]) {
   int nownode = c[lastnode][x];
                    if (l[nownode] == l[lastnode] + 1) last = nownode;
                          int auxnode = ++cnt; l[auxnode] = l[lastnode] + 1;
for (int i = 0; i < alphabet; ++i) c[auxnode][i] = c[nownode][i];</pre>
                          par[auxnode] = par[nownode]; par[nownode] = auxnode;
for (; lastnode && c[lastnode][x] == nownode; lastnode = par[lastnode]) {
    c[lastnode][x] = auxnode;
  11
 12
13
14
15
                           last = auxnode;
             } else {
 16
                    int newnode = ++cnt; l[newnode] = l[lastnode] + 1;
for (; lastnode && !c[lastnode][x]; lastnode = par[lastnode]) c[lastnode][x] =
 17
                    if (!lastnode) par[newnode] = 1;
  18
 19
                    else {
                          int nownode = c[lastnode][x];
if (l[lastnode] + 1 == l[nownode]) par[newnode] = nownode;
 20
21
22
23
24
                           else
                                 int auxnode = ++cnt; l[auxnode] = l[lastnode] + 1;
for (int i = 0; i < alphabet; ++i) c[auxnode][i] = c[nownode][i];
par[auxnode] = par[nownode]; par[nownode] = par[newnode] = auxnode;</pre>
 25
                                  for (; lastnode && c[lastnode][x] == nownode; lastnode =
            \hookrightarrow par[lastnode]) \cdot
27
28
29
30
31
32
33 }
                                        c[lastnode][x] = auxnode;
                     ĺast = newnode;
```

## 4.4 回文自动机

```
int nT, nStr, last, c[MAXT][26], fail[MAXT], r[MAXN], l[MAXN], s[MAXN];
int allocate(int len) {
    l[nT] = len;
    r[nT] = 0;
    fail[nT];
    o.
         fail[nT] = 0;
memset(c[nT], 0, sizeof(c[nT]));
          return nT++;
 8
    void init() {
    nT = nStr = 0;
          int newE = allocate(0)
11
12
          int new0 = allocate(-1);
13
          last = newE;
fail[newE] = newO;
14
15
16
          fail[new0] = newE;
s[0] = -1;
17 | }
18
    void add(int_x) {
19
          s[++nStr] = x
          int now = last;
20
21
          while (s[nStr - l[now] - 1] != s[nStr]) now = fail[now];
22
23
          if (!c[now][x]) {
  int newnode = allocate(l[now] + 2), &newfail = fail[newnode];
24
                newfail = fail[now];
25
26
27
28
29
30
                while (s[nStr - l[newfail] - 1] != s[nStr]) newfail = fail[newfail];
               newfail = c[newfail][x];
c[now][x] = newnode;
          last = c[now][x];
          r[last]+\bar{+};
31
32
   void count() {
   for (int i = nT - 1; i >= 0; i--) {
      r[fail[i]] += r[i];
}
33
34
35
```

# Chapter 5 数据结构

#### 5.1 KD-Tree

```
long long norm(const long long &x) {
    // For manhattan distance
         return std::abs(x);
// For euclid distance
4 5 6
         return x * x;
    struct Point {
         int x, y, id;
11
         const int& operator [] (int index) const {
12
              if (index == 0)
13
                    return x;
14
15
              } else {
                   return y;
16
17
18
         friend long long dist(const Point &a, const Point &b) {
   long long result = 0;
   for (int i = 0; i < 2; ++i) {</pre>
19
20
21
22 23
                   result += norm(a[i] - b[i]);
24
              return result:
25
26
27
    } point[N];
28
29
30
    struct Rectangle {
   int min[2], max[2];
         Rectangle() {
    min[0] = min[1] = INT_MAX; // sometimes int is not enough
    max[0] = max[1] = INT_MIN;
31
32
33
34
35
36
         void add(const Point &p) {
              for (int i = 0; i < 2; ++i) {
37
38
                   min[i] = std::min(min[i], p[i]);
max[i] = std::max(max[i], p[i]);
39
40
41
42
         }
43
         long long dist(const Point &p) {
44
               long long result = 0;
45
              for (int i = 0; i < 2; ++i) {
46
                           For minimum distance
47
48
                   result += norm(std::min(std::max(p[i], min[i]), max[i]) - p[i]);
                         For maximum distance
49
                   result += std::max(norm(max[i] - p[i]), norm(min[i] - p[i]));
50
51
              return result;
52
53
54
55
56
    struct Node {
         Point seperator;
57
         Rectangle rectangle;
58
59
         int child[2];
60
         void reset(const Point &p) {
61
              seperator = p;
rectangle = Rectangle();
62
              rectangle.add(p);
63
              child[0] = child[1] = 0;
65
66
    } tree[N << 1];</pre>
68
69
    int size, pivot;
70
    bool compare(const Point &a, const Point &b) {
         if (a[pivot] != b[pivot]) {
    return a[pivot] < b[pivot];</pre>
71
72
73
74
         return a.id < b.id;
```

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```
75 | }
76 |
77
    // 左閉右開: build(1, n + 1)
 78
    int build(int l, int r, int type = 1) {
         pivot = type;
79
80
         if (l >= r)
81
             return 0;
82
83
         int x = ++size;
 84
         int mid = l + r >> 1;
85
         std::nth_element(point + l, point + mid, point + r, compare);
86
         tree[x].reset(point[mid]);
87
         for (int i = l; i < r; ++i)
88
             tree[x].rectangle.add(point[i]);
 89
90
         tree[x].child[0] = build(l, mid, type ^ 1);
         tree[x].child[1] = build(mid + 1, r, type ^ 1);
91
92
93
94
95
     int insert(int x, const Point &p, int type = 1) {
96
         pivot = type;
         if (x == 0)
97
98
             tree[++size].reset(p);
99
             return size;
100
101
         tree[x].rectangle.add(p);
102
         if (compare(p, tree[x].seperator)) {
             tree[x].child[0] = insert(tree[x].child[0], p, type ^ 1);
103
104
         } else {
105
             tree[x].child[1] = insert(tree[x].child[1], p, type ^ 1);
106
107
         return x;
108
109
110
       For minimum distance
111
    // For maximum: 下面递归 query 时 0, 1 换顺序;< and >;min and max
112
     void query(int x, const Point &p, std::pair<long long, int> &answer, int type = 1) {
113
         pivot = type;
114
         if (x == 0 || tree[x].rectangle.dist(p) > answer.first) {
115
             return;
116
         answer = std::min(answer
117
118
                   std::make_pair(dist(tree[x].seperator, p), tree[x].seperator.id));
119
         if (compare(p, tree[x].seperator))
             query(tree[x].child[0], p, answer, type ^ 1);
query(tree[x].child[1], p, answer, type ^ 1);
120
122
         } else {
             query(tree[x].child[1], p, answer, type ^ 1);
query(tree[x].child[0], p, answer, type ^ 1);
123
124
125
126
128
    std::priority_queue<std::pair<long long, int> > answer;
129
130
    void query(int x, const Point &p, int k, int type = 1) {
131
         pivot = type;
132
         if (x == 0 | | (int)answer.size() == k && tree[x].rectangle.dist(p) >

    answer.top().first) {
133
134
135
         answer.push(std::make_pair(dist(tree[x].seperator, p), tree[x].seperator.id));
136
         if ((int)answer.size() > k) {
137
             answer.pop();
138
         if (compare(p, tree[x].seperator)) {
    query(tree[x].child[0], p, k, type ^ 1);
}
139
140
             query(tree[x].child[1], p, k, type ^ 1);
141
142
             query(tree[x].child[1], p, k, type ^ 1);
143
144
             query(tree[x].child[0], p, k, type ^ 1);
145
146
```

```
5.2 Treap
```

```
struct Node{
2 int mn, key, size, tag;
```

```
bool rev:
        Node* ch[2];
        Node(int mn, int key, int size): mn(mn), key(key), size(size), rev(0), tag(0){}
         void downtag()
         Node* update()
             mn = min(ch[0] -> mn, min(key, ch[1] -> mn));
size = ch[0] -> size + 1 + ch[1] -> size;
             return this;
11
12
13
   týpedef pair<Node*, Node*> Pair;
Node *null, *root;
15
   void Node::downtag(){
        if(rev){
             17
18
19
20
                        swap(ch[i] \rightarrow ch[0], ch[i] \rightarrow ch[1]);
21
22
23
24
25
             rev = 0;
        if(tag){
             cag){
  for(int i = 0; i < 2; i++)
      if(ch[i] != null){
      ch[i] -> key += tag;
      ch[i] -> mn += tag;
      ch[i] -> tag += tag;
26
27
28
30
31
              tag = 0;
32
33
34
35
    int r(){
        static int s = 3023192386;
36
        return (s += (s << 3) + 1) & (\sim0u >> 1);
37
    bool random(int x, int y){
39
        return r() % (x + y) < x;
40
41
   Node* merge(Node *p, Node *q){
    if(p == null) return q;
42
         if(q == null) return p;
44
        p -> downtag();
45
           -> downtag();
        46
48
49
        }else{
50
              q \rightarrow ch[0] = merge(p, q \rightarrow ch[0]);
51
             return q -> update();
52
53
54
55
   Pair split(Node *x, int n){
        if(x == null) return make_pair(null, null);
        x -> downtag();
        if(n <= x -> ch[0] -> size){
             Pair ret = split(x -> ch[0], n);
x -> ch[0] = ret.second;
59
60
             return make_pair(ret.first, x -> update());
        Pair ret = split(x -> ch[1], n - x -> ch[0] -> size - 1);
x -> ch[1] = ret.first;
63
        return make_pair(x -> update(), ret.second);
65
66
   pair<Node*, Pair> get_segment(int l, int r){
67
        Pair ret = split(root, l - 1);
68
        return make_pair(ret.first, split(ret.second, r - l + 1));
70
    int main(){
71
72
        null = new Node(INF, INF, 0);
null -> ch[0] = null -> ch[1] = null;
73
        root = null;
74
```

## 5.3 Link/cut Tree

```
inline void reverse(int x) {
    tr[x].rev ^= 1; swap(tr[x].c[0], tr[x].c[1]);
```

```
inline void rotate(int x, int k) {
         int y = tr[x].fa, z = tr[y].fa;
tr[x].fa = z; tr[z].c[tr[z].c[1] == y] = x;
tr[tr[x].c[k ^ 1]].fa = y; tr[y].c[k] = tr[x].c[k ^ 1];
tr[x].c[k ^ 1] = y; tr[y].fa = x;
10 }
11
12
    inline void splay(int x, int w) {
13
          int z = x; pushdown(x);
14
          while (tr[x].fa != w)
                int y = tr[x].fa; z = tr[y].fa;
15
16
                if (z == w)
                    pushdown(z = y); pushdown(x);
rotate(x, tr[y].c[1] == x);
update(y); update(x);
17
18
19
20
21
               } else
                    pushdown(z); pushdown(y); pushdown(x);
int t1 = tr[y].c[1] == x, t2 = tr[z].c[1] == y;
if (t1 == t2) rotate(y, t2), rotate(x, t1);
22
23
24
                     else rotate(x, t1), rotate(x, t2);
25
                     update(z); update(y); update(x);
26
27
28
29
30
31
          update(x);
          if (x \stackrel{!}{=} z) par[x] = par[z], par[z] = 0;
32
     inline void access(int x) {
33
          for (int y = 0; x; y = x, x = par[x]) {
34
               splay(x, 0);
35
               if (tr(x).c(1)) par[tr(x).c(1)] = x, tr[tr(x).c(1)].fa = 0;
tr(x).c(1) = y; par(y) = 0; tr(y).fa = x; update(x);
36
37
38
39
40
    inline void makeroot(int x) {
41
          access(x); splay(x, 0); reverse(x);
42
43
    inline void link(int x, int y) {
44
45
          makeroot(x); par[x] = y;
46
47
48
     inline void cut(int x, int y) {
         access(x); splay(\hat{y}, 0); if (par[y] != x) swap(x, y), access(x), splay(y, 0);
49
50
51
52
53
          par[y] = 0;
54
55
    inline void split(int x, int y) \{ // x will be the root of the tree
          makeroot(y); access(x); splay(x, 0);
```

## 5.4 树状数组查询第 k 小元素

```
inline void reverse(int x)
         tr[x].rev ^= 1; `swap(tr[x].c[0], tr[x].c[1]);
    inline void rotate(int x, int k) {
         int y = tr[x].\dot{f}a, z = tr[y].\dot{f}a;
         tr[x].fa = z; tr[z].c[tr[z].c[1] == y] = x;
tr[tr[x].c[k ^ 1]].fa = y; tr[y].c[k] = tr[x].c[k ^ 1];
tr[x].c[k ^ 1] = y; tr[y].fa = x;
10
11
12
    inline void splay(int x, int w) {
         int z = x; pushdown(x);
while (tr[x].fa != w) {
13
14
15
               int y = tr[x].fa; z = tr[y].fa;
16
               if (z == w)
                    `pushdown(z = y); pushdown(x);
17
18
                   rotate(x, tr[ý].c[1] == x);
update(y); update(x);
19
20
               l else
                    pushdown(z); pushdown(y); pushdown(x);
```

```
int t1 = tr[y].c[1] == x, t2 = tr[z].c[1] == y;
if (t1 == t2) rotate(y, t2), rotate(x, t1);
23
                 else rotate(x, t1), rotate(x, t2);
                 update(z); update(y); update(x);
26
27
28
        update(x);
29
30
        if (x != z) par[x] = par[z], par[z] = 0;
31
32
    inline void access(int x) {
33
        for (int y = 0; x; y = x, x = par[x]) {
            splay(x, 0);
             if (tr[x].c[1]) par[tr[x].c[1]] = x, tr[tr[x].c[1]].fa = 0;
36
37
            tr[x].c[1] = y; par[y] = 0; tr[y].fa = x; update(x);
38
39
40
    inline void makeroot(int x) {
41
42
        access(x); splay(x, 0); reverse(x);
43
   inline void link(int_x, int y) {
44
45
        makeroot(x); par[x] = y;
46
47
48
    inline void cut(int x, int y) {
        access(x); splay(y, 0); if (par[y] != x) swap(x, y), access(x), splay(y, 0);
49
        par[\dot{y}] = \dot{0};
51
52
53
54
    inline void split(int x, int y) \{ // x will be the root of the tree
        makeroot(y); access(x); splay(x, 0);
```

## Chapter 6 图论

## 6.1 基础

```
struct Graph { // Remember to call .init()!
        int_e, nxt[M], v[M], adj[N], n;
        bool base;
        __inline void init(bool _base, int _n = 0) {
            assert(n < N);</pre>
            n = n; base =
                             _base;
            e = \overline{0}; memset(adj + base, -1, sizeof(*adj) * n);
       __inline int new_node() {
   adj[n + base] = -1;
10
11
            assert(n + base + 1 < N);
12
13
            return n++ + base;
14
        __inline void ins(int u0, int v0) { // directional
15
            assert(u0 < n + base \&\& v0 < n + base);
16
            v[e] = v0; nxt[e] = adj[u0]; adj[u0] = e++;
17
            assert(e < M);
18
19
        __inline void bi_ins(int u0, int v0) { // bi-directional
20
21
22 };
            ins(u0, v0); ins(v0, u0);
```

#### 6.2 KM

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```
lx[i] = 0;
ly[i] = 0;
11
                          way[i] = 0;
12
13
14
15
16
            void hungary(int x) {
                   match[0] = x;
                   int j0 = 0;
for (int j = 0; j <= n; j++) {
    slack[j] = INF;
    used[j] = false;</pre>
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
                   do {
                          used[j0] = true;
                          int i0 = match[j0], delta = INF, j1 = 0;
                          for (int j = 1; j <= n; j++) {
   if (used[j] == false) {</pre>
                                       int cur = -w[i0][j] - lx[i0] - ly[j];
if (cur < slack[j]) {</pre>
                                             slack[j] = cur;
way[j] = j0;
                                       if (slack[j] < delta) {
   delta = slack[j];</pre>
34
35
36
                                             j1 = j;
37
38
                         for (int j = 0; j <= n; j++) {
    if (used[j]) {
        lx[match[j]] += delta;</pre>
39
40
41
42
43
                                       ly[j] -= delta;
44
45
46
47
48
                                else slack[j] -= delta;
                          i0 = i1;
                   } while (match[j0] != 0);
49
50
51
52
53
54
55
56
57
58
59
60
                          int j1 = way[j0];
                         match[j0] = match[j1];
j0 = j1;
                   } while (j0);
            int get_ans() {
                   int sum = 0;
                   for(int i = 1; i <= n; i++) {
    if (w[match[i]][i] == -INF) ; // 无解
                          if (match[i] > 0) sum += w[match[i]][i];
61
62
                   return sum;
63
     } km;
```

#### 6.3 点双连通分量

bcc.forest is a set of connected tree whose vertices are chequered with cut-vertex and BCC.

```
18
                   compress_to[u] = forest.new_node();
19
                   compress_cut[compress_to[u]] = 1;
20
21
              for (int e = g->adj[u]; ~e; e = g->nxt[e]) {
22
23
24
25
26
                   int v = g->v[e];
if ((e ^ pe) > 1 && dfn[v] > 0 && dfn[v] < dfn[u]) {
                         stack[top++] = e;
                         low[u] = std::min(low[u], dfn[v]);
27
                   else if (!dfn[v]) {
    stack[top++] = e; branch[e] = 1;
28
                        DFS(v, e);
low[u] = std::min(low[v], low[u]);
29
30
31
                         if (low[v] >= dfn[u]) {
32
33
                              if (!cut[u])
                                   cut[u] = 1;
34
                                   compress_to[u] = forest.new_node();
35
                                   compress_cut[compress_to[u]] = 1;
36
37
                              int cc = forest.new_node();
                              forest.bi_ins(compress_to[ú], cc);
38
39
                              compress_cut[cc] = 0;
40
                              //BCC_component[cc].clear();
41
42
                                  int cur_e = stack[--top];
compress_to[expand_to[cur_e]] = cc;
compress_to[expand_to[cur_e^1]] = cc;
43
44
45
                                   if (branch[cur e]) {
46
                                        int v = g->v[cur_e];
if (cut[v])
47
48
                                             forest.bi_ins(cc, compress_to[v]);
49
50
                                             //BCC_component[cc].push_back(v);
                                             compress_to[v] = cc;
51
52
53
54
55
                              } while (stack[top] != e);
56
                   }
57
              }
58
59
         void solve() {
60
              forest.init(g->base);
              int n = g->n;
for (int i = 0; i < g->e; i++) {
    expand_to[i] = g->new_node();
61
62
63
64
65
              memset(branch, 0, sizeof(*branch) * g->e);
              memset(dfn + g->base, 0, sizeof(*dfn) * n); DFN = 0;
for (int i = 0; i < n; i++)
    if (!dfn[i + g->base]) {
66
67
68
69
                        top = 0:
                        DFS(i + g \rightarrow base, -1);
70
71
72
73
74
    } bcc;
75
    bcc.init(&raw_graph);
   bcc.solve();
    // Do something with bcc.forest ...
```

## 6.4 边双连通分量

```
struct BCC {
    Graph *g, forest;
    int dfn[N], low[N], stack[N], tot[N], belong[N], vis[N], top, dfs_clock;
    // tot[] is the size of each BCC, belong[] is the BCC that each node belongs to
    pair<int, int > ori[M]; // bridge in raw_graph(raw node)
    bool is_bridge[M];
    __inline void init(Graph *raw_graph) {
        g = raw_graph;
        memset(is_bridge, false, sizeof(*is_bridge) * g -> e);
        memset(vis + g -> base, 0, sizeof(*vis) * g -> n);
    }
    void tarjan(int u, int from) {
        dfn[u] = low[u] = ++dfs_clock; vis[u] = 1; stack[++top] = u;
        for (int p = g -> adj[u]; ~p; p = g -> nxt[p]) {
```

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```
15
                    if ((p ^ 1) == from) continue;
                    int v = g -> v[p];
16
                    if (vis[v]) {
17
18
                         if (vis[v] == 1) low[u] = min(low[u], dfn[v]);
19
                    } else
20
                         tarjan(v, p)
21
                         low[u] `= min(low[u], low[v]);
if (low[v] > dfn[u]) is_bridge[p / 2] = true;
22
23
24
25
26
27
28
29
30
31
              if (dfn[u] != low[u]) return;
tot[forest.new_node()] = 0;
                    belong[stack[top]] = forest.n;
                    vis[stack[top]] = 2;
                    tot[forest.n]++;
                    --top;
32
33
              } while (stack[top + 1] != u);
34
35
         void solve() {
               forest.init(g -> base);
              int n = g -> n;
for (int i = 0; i < n; ++i)
if (!vis[i + g -> base]) {
36
37
38
39
                         top = dfs_clock = 0;
40
                         tarjan(i + g \rightarrow basé, -1);
41
42
               for (int i = 0; i < g -> e / 2; ++i)
43
                    if (is_bridge[i]) {
44
                          int e = forest.e;
45
                         forest.bi_ins(belong[g -> v[i * 2]], belong[g -> v[i * 2 + 1]], g ->
       \hookrightarrow w[i * 2]);
                         ori[e] = make_pair(g -> v[i * 2 + 1], g -> v[i * 2]);
ori[e + 1] = make_pair(g -> v[i * 2], g -> v[i * 2 + 1]);
46
47
48
49
    } bcc;
```

## 6.5 最小树形图

```
const int MAXN,INF;// INF >= sum( W_ij )
int from[MAXN + 10][MAXN * 2 + 10],n,m,edge[MAXN + 10][MAXN * 2 + 10];
     int sel[MAXN * 2 + 10], fa[MAXN * 2 + 10], vis[MAXN * 2 + 10];
     int getfa(int x){if(x == fa[x]) return x; return fa[x] = getfa(fa[x]);}
     void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
           fa[1] = 1;
          facili - 1;
for(int i = 2; i <= n; ++i){
    sel[i] = 1; fa[i] = i;
    for(int j = 1; j <= n; ++j) if(fa[j] != i)
        if(from[j][i] = i, edge[sel[i]][i] > edge[j][i]) sel[i] = j;
11
12
           int limit = n;
13
          while(1){
                 int prelimit = limit; memset(vis, 0, sizeof(vis)); vis[1] = 1;
for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){
    int j = i; while(!vis[j]) vis[j] = i, j = getfa(sel[j]);</pre>
14
15
16
17
                       if(j == 1 | | vis[j] != i) continue; vector<int> C; int k = j;
18
                       do C.push_back(k), k = getfa(sel[k]); while(k != j);
19
20
                       for(int i = 1; i <= n; ++i){
                             edge[i][limit] = INF, from[i][limit] = limit;
21
22
23
24
25
                       fa[limit] = vis[limit] = limit;
for(int i = 0; i < int(C.size()); ++i){</pre>
                             int x = C[i], fa[x] = limit;
for(int j = 1; j <= n; ++j)
    if(edge[j][x] != INF && edge[j][limit] > edge[j][x] -
26
27
         \hookrightarrow edge[sel[x]][x]){
28
                                         edge[j][limit] = edge[j][x] - edge[sel[x]][x];
from[j][limit] = x;
29
30
31
32
                       for(int j=1;j<=n;++j) if(getfa(j)==limit) edge[j][limit] = INF;</pre>
                      sel[limit] = 1;
for(int j = 1; j <= n; ++j)
    if(edge[sel[limit]][limit] > edge[j][limit]) sel[limit] = j;
33
34
35
```

#### 6.6 帯花树

```
vector<int> link[maxn];
    int n,match[maxn],Queue[maxn],head,tail;
    int pred[maxn],base[maxn],start,finish,newbase;
   bool InQueue[maxn], InBlossom[maxn];
   void push(int u){ Queue[tail++]=u; InQueue[u]=true; }
int pop(){ return Queue[head++]; }
    int FindCommonAncestor(int u,int v){
        bool InPath[maxn];
        for(int i=0;i<n;i+) InPath[i]=0;
while(true){ u=base[u];InPath[u]=true;if(u==start) break;u=pred[match[u]]; }</pre>
        while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
12
13
14
15
   void ResetTrace(int u){
        int v;
16
         while(base[u]!=newbase){
17
             v=match[u];
18
             InBlossom[base[u]]=InBlossom[base[v]]=true;
19
             u=pred[v]:
20
             if(base[u]!=newbase) pred[u]=v;
21
22
23
    void BlossomContract(int u,int v){
        newbase=FindCommonAncestor(u,v);
24
25
         for (int i=0;i<n;i++)</pre>
26
        InBlossom[i]=0;
27
        ResetTrace(u); ResetTrace(v);
28
         if(base[u]!=néwbase) pred[u]=v;
29
         if(base[v]!=newbase) pred[v]=u;
30
         for(int i=0;i<n;++i</pre>
31
         if(InBlossom[base[i]]){
32
             base[i]=newbase;
33
             if(!InQueue[i]) push(i);
34
35
36
   bool FindAugmentingPath(int u){
37
        bool found=false:
38
         for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;</pre>
39
        for (int i=0;i<n;i++) InQueue[i]=0;
start=u;finish=-1; head=tail=0; push(start);</pre>
40
41
        while(head<tail){</pre>
42
             int u=pop()
             for(int i=link[u].size()-1;i>=0;i--){
  int v=link[u][i];
  if(base[u]!=base[v]&&match[u]!=v)
    if(v==start|(match[v]>=0&&pred[match[v]]>=0))
43
44
45
46
                            BlossomContract(u,v);
47
48
                       else if(pred[v]==-1){
49
                            pred[v]=u;
                            if(match[v]>=0) push(match[v]);
50
                            else{ finish=v; return true; }
52
53
             }
54
55
        return found;
56
57
    void AugmentPath(){
58
        int u=finish,v,w;
59
        while(u>=0){ v=pred[u]; w=match[v]; match[v]=u; match[u]=v; u=w; }
60
   void FindMaxMatching(){
    for(int i=0;i<n;++i) match[i]=-1;</pre>
61
62
63
         for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();</pre>
64
```

#### 6.7 Dominator Tree

```
vector<int> prec[N], succ[N];
vector<int> ord;
```

CHAPTER 6. 图论 13

```
int stamp, vis[N];
int num[N];
    int fa[N];
    void dfs(int u) {
         vis[u] = stamp;
num[u] = ord.size();
         ord.push_back(u);
for (int i = 0; i < (int)succ[u].size(); ++i) {</pre>
10
11
              int v = succ[u][i];
              if (vis[v] != stamp) {
12
13
                   fa[v] = u;
14
                   dfs(v);
15
16
17
18
    int fs[N], mins[N], dom[N], sem[N];
int find(int u) {
19
20
         if (u != fs[u])
21
              int v = fs[u]
              fs[u] = find(fs[u]);
22
23
24
25
26
27
28
              if'(mins[v] \stackrel{\cdot}{!} = -1 \stackrel{\cdot}{.} \& num[sem[mins[v]]] < num[sem[mins[u]]]) 
                   mins[u] = mins[v];
         return fs[u];
29
29 void merge(int u, int v) { fs[u] = v; }
30 vector<int> buf[N];
31
    int buf2[N];
32
    void mark(int source) {
33
34
         ord.clear();
         ++stamp;
35
         dfs(source);
36
         for (int i = 0; i < (int)ord.size(); ++i) {
37
              int u = ord[i];
38
              fs[u] = u, mins[u] = -1, buf2[u] = -1;
40
         for (int i = (int)ord.size() - 1; i > 0; --i) {
41
              int u = ord[i], p = fa[u];
42
              sem[u] = p;
for (int j = 0; j < (int)prec[u].size(); ++j) {</pre>
43
44
                   int v = préc[u][j];
45
                   if (use[v] != stamp) continue;
if (num[v] > num[u]) {
46
47
                        find(v); v = sem[mins[v]];
48
                   if (num[v] < num[sem[u]]) {
    sem[u] = v;</pre>
49
50
51
52
53
              buf[sem[u]].push_back(u);
54
55
              mins[u] = u;
              merge(u, p);
56
57
58
              while (buf[p].size()) {
                   int v = buf[p].back();
                   buf[p].pop_back();
59
                   find(v);
                   if (sem[v] == sem[mins[v]]) {
    dom[v] = sem[v];
60
61
62
                   } else
63
                        buf2[v] = mins[v];
64
65
66
67
         dom[ord[0]] = ord[0];
68
         for (int i = 0; i < (int)ord.size(); ++i) {
              int u = ord[i];
69
70
71
72
73
              if (~buf2[u]) {
                   `dom[u] = dom[buf2[u]];
```

## 6.8 无向图最小割

```
int cost[maxn][maxn],seq[maxn],len[maxn],n,m,pop,ans;
bool used[maxn];
```

```
3 | void Init(){
        int i,j,a,b,c;
        for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;
        for(i=0;i<m;i++){
            pop=n; for(i=0;i<n;i++) seq[i]=i;</pre>
10
   void Work(){
    ans=inf; int i,j,k,l,mm,sum,pk;
11
12
13
        while(pop > 1){
            for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;
for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];
pk=0; mm=-inf; k=-1;</pre>
14
15
16
             17
            for(i=1;i<pop;i++){
    used[seq[l=k]]=1;</pre>
18
19
20
                 if(i==pop-2) pk=k;
if(i==pop-1) break;
21
22
                 mm=-inf;
                 for(j=1;j<pop;j++) if(!used[seq[j]])
    if((len[seq[j]]+=cost[seq[l]][seq[j]]) > mm)
23
24
25
                          mm=len[seq[j]], k=j;
26
27
            sum=0;
28
            for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];</pre>
29
            ans=min(ans,sum);
30
            for(i=0;i<pop;i++)</pre>
                 cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+=cost[seq[pk]][seq[i]];
31
32
            seq[pk]=seq[--pop];
33
        printf("%d\n",ans);
34
35
```

#### 6.9 重口味费用流

```
int S, T, totFlow, totCost;
    int dis[N], slack[N], visit[N];
    int modlable ()
5
          int delta `= ÌNF;
          for (int i = 1; i <= T; i++) {
    if (!visit[i] && slack[i] < delta) delta = slack[i];</pre>
               slack[i] = INF;
10
         if (delta == INF) return 1;
for (int i = 1; i <= T; i++)
    if (visit[i]) dis[i] += delta;</pre>
11
12
13
14
15
16
         return 0;
    int dfs (int x, int flow) {
   if (x == T) {
17
18
19
               `totFlow += flow;
20
               totCost += flow * (dis[S] - dis[T]);
21
               return flow;
22 23
24
25
         int left = flow:
         for (int i = e.last[x]; ~i; i = e.succ[i])
    if (e.cap[i] > 0 && !visit[e.other[i]]) {
26
27
                     int y = e.other[i];
                     if (dis[y] + e.cost[i] == dis[x]) {
  int delta = dfs (y, min (left, e.cap[i]));
28
29
30
                          e.cap[i] -= delta;
e.cap[i ^ 1] += delta;
31
                          left -= delta;
32
33
                          if (!left) { visit[x] = 0; return flow; }
34
                    } else
35
36
                          slack[y] = min (slack[y], dis[y] + e.cost[i] - dis[x]);
37
38
39
         return flow - left;
40
41 pair <int, int> minCost () {
```

# Chapter 7 其他

## 7.1 Dancing Links

```
Node *l, *r, *u, *d, *col; int size, line_no;
        Node() {
             size = 0; line_no = -1;
l = r = u = d = col = NULL;
    } *root;
    void cover(Node *c) {
11
        c \rightarrow l \rightarrow r = c \rightarrow r; c \rightarrow r \rightarrow l = c \rightarrow l;
12
         for (Node *u = c-d; u != c; u = u-d)
13
              for (Node *v = u->r; v != u; v = v->r) {
14
                  v->d->u = v->u;
15
                  v->u->d = v->d:
16
                  -- v->col->sizé;
17
18
19
20
    void uncover(Node *c) {
21
22
23
24
        for (Node *u = c - > u; u != c; u = u - > u) {
              for (Node *v = \hat{u} - > 1; v != u; v = \hat{v} - > 1) {
                  ++ v->col->size;
                  v->u->d = v;
25
26
27
28
29
30
                  v \rightarrow d \rightarrow u = v;
        c->l->r = c; c->r->l = c;
31
32
    std::vector<int> answer;
    bool search(int k) {
33
         if (root->r == root) return true;
34
        Node *r = NULL;
35
        for (Node *u = root->r; u != root; u = u->r)
36
37
             if (r == NULL || u->size < r->size)
                  `r = u;
38
        if (r == NULL | | r->size == 0) return false;
39
        else {
40
             cover(r);
41
             bool succ = false;
42
              for (Node *u = r->d; u != r && !succ; u = u->d) {
43
                  answer.push_back(u->line_no);
44
                  for (Node *\overline{v} = u - r; v = u - r) // Cover row
45
                       cover(v->col);
46
                  succ |= search(k' + 1);
                  for (Node *v = u->l; v != u; v = v->l)
47
48
                       uncover(v->col);
49
                  if (!succ) answer.pop_back();
50
51
52
53
54
55
             uncover(r);
             return succ:
56
57
    bool entry[CR][CC];
    Node *who[CR][CC];
    int cr, cc;
60
    void construct() {
61
        root = new Node();
        Node *last = root;
62
63
        for (int i = 0; i < cc; ++ i) {
             Node *u = new Node();
```

```
65
              last->r = u; u->l = last;
 66
              Node *v = u; u->line_no = i;
 67
               last = u;
              for (int´j = 0; j < cr; ++ j)
    if (entry[j][i]) {</pre>
 70
                        ++ u->size;
                        Node *cur = new Node();
 72
73
                        who[j][i] = cur;
                        cur->line_no = j;
 74
                        cur->col = u:
 75
76
77
78
                        cur->u = v; v->d = cur;
                        v = cur;
              v->d = u; u->u = v;
 79
 80
          last->r = root; root->l = last;
 81
         for (int j = 0; j < cr; ++ j) {
   Node *last = NULL;</pre>
 82
83
              for (int i = cc - 1; i >= 0; -- i)
    if (entry[j][i]) {
 84
 85
                        last = who[j][i];
                        break;
 87
 88
              for (int i = 0; i < cc; ++ i)
 89
                   if (entry[j][i])
                        last->r' = who[j][i];
who[j][i]->l = last;
 90
 91
 92
                        last = who[j][i];
 93
 94
         }
 95
 96
 97
98
    void destruct() {
         for (Node *u = root->r; u != root; ) {
 99
               for (Node *v = u - > d; v != u; ) {
100
                   Node *nxt = v->d;
101
                   delete(v);
102
                   v = nxt;
103
104
              Node *nxt = u->r;
              delete(u); u = nxt;
106
107
         delete root;
108
```

#### 7.2 蔡勒公式

```
int zeller(int y,int m,int d) {
   if (m<=2) y--,m+=12; int c=y/100; y%=100;
   int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
   if (w<0) w+=7; return(w);
}</pre>
```

# Chapter 8 技巧

## 8.1 真正的释放 STL 容器内存空间

```
template <typename T>
    __inline void clear(T& container) {
        container.clear(); // 或者删除了一堆元素
        T(container).swap(container);
}
```

## 8.2 无敌的大整数相乘取模

Time complexity O(1).

#### 8.3 无敌的读入优化

```
getchar() 读入优化 << 关同步 cin << 此优化
       用 isdigit() 会小幅变慢
   // 返回 false 表示读到文件尾
   namespace Reader {
        const int L = (1 << 15) + 5;
        char buffer[L], *S, *T;
        __inline bool getchar(char &ch) {
   if (S == T) {
                 T = (S'= buffer) + fread(buffer, 1, L, stdin);
                if (S == T) {
                     ch = EÓF;
                     return false:
13
14
15
            ch = *S++;
16
17
            return trúe;
        __inline bool getint(int &x) {
18
19
            char ch; bool neg = 0;
            for (; getchar(ch) && (ch < '0' || ch > '9'); ) neg ^= ch == '-'; if (ch == EOF) return false;
20
21
22
23
24
25
26
27
            x = ch - 0';
            for (; getchár(ch), ch >= '0' && ch <= '9'; )
                 x' = x * 10 + ch - '0';
            if (neg) x = -x;
            return true;
```

#### 8.4 梅森旋转算法

High quality pseudorandom number generator, twice as efficient as rand() with -02. C++11 required.

```
#include <random>
int main() {
    std::mt19937 g(seed); // std::mt19937_64
    std::cout << g() << std::endl;
}</pre>
```

# Chapter 9 提示

## 9.1 控制 cout 输出实数精度

```
std::cout << std::fixed << std::setprecision(5);
```

#### **9.2** vimrc

```
1 set nu
2 set sw=4
3 set sts=4
4 set ts=4
5 syntax on set cindent
```

#### 9.3 让 make 支持 c ++ 11

In .bashrc or whatever:
export CXXFLAGS='-std=c++11 -Wall'

## 9.4 tuple 相关

```
mytuple = std::make_tuple (10, 2.6, 'a');
std::tie (myint, std::ignore, mychar) = mytuple;
std::get<I>(mytuple) = 20;
std::cout << std::get<I>(mytuple) << std::endl;
// get the Ith(const) element</pre>
```

## 9.5 线性规划转对偶

```
maximize \mathbf{c}^T \mathbf{x} \Longrightarrow minimize \mathbf{y}^T \mathbf{b} subject to \mathbf{A} \mathbf{x} \le \mathbf{b}, \mathbf{x} \ge 0 \Longrightarrow subject to \mathbf{v}^T \mathbf{A} > \mathbf{c}^T, \mathbf{v} > 0
```

#### 9.6 32-bit/64-bit 随机素数

32-bit	64-bit
73550053	1249292846855685773
148898719	1701750434419805569
189560747	3605499878424114901
459874703	5648316673387803781
1202316001	6125342570814357977
1431183547	6215155308775851301
1438011109	6294606778040623451
1538762023	6347330550446020547
1557944263	7429632924303725207
1981315913	8524720079480389849

#### 9.7 NTT 素数及其原根

Prime	Primitive root
1053818881	7
1051721729	6
1045430273	3
1012924417	5
1007681537	3

#### 9.8 Java Hints

```
import java.io.*;
    import java.lang.*;
    import java.math.*;
    import java.util.*;
6
         Regular usage:
           Slower IO:
8
               Scanner in = new Scanner (System.in);
9
               Scanner in = new Scanner (new BufferedInputStream (System.in));
10
11
                    in.nextInt () / in.nextBigInteger () / in.nextBigDecimal () / in.nextDouble ()
12
                    in.nextLine () / in.hasNext ()
13
               Output:
14
                    System.out.print (...);
15
                    System.out.println (...);
16
                    System.out.printf (...);
17
           Faster TO:
18
               Shown below.
19
           BigInteger :
20
               BigInteger.valueOf (int) : convert to BigInteger.
21
               abs / negate () / max / min / add / subtract / multiply /
22
                    divide / remainder (BigInteger) : BigInteger algebraic.
23
               gcd (BigInteger) / modInverse (BigInteger mod) /
24
                    modPow (BigInteger ex, BigInteger mod) / pow (int ex) : Number Theory.
               not () / and / or / xor (BigInteger) / shiftLeft / shiftRight (int) : Bit operation.
25
26
               compareTo (BigInteger) : comparation.
27
               intValue () / longValue () / toString (int radix) : converts to other types.
28
               isProbablePrime (int certainty) / nextProbablePrime () : checks primitive.
29
           BigDecimal:
30
               consists of a BigInteger value and a scale.
31
               The scale is the number of digits to the right of the decimal point.
32
               divide (BigDecimal) : exact divide.
33
               divide (BigDecimal, int scale, RoundingMode roundingMode) :
34
                    divide with roundingMode, which may be:
35
                       CEILING / DOWN / FLOOR / HALF_DOWN / HALF_EVEN / HALF_UP / UNNECESSARY / UP.
36
               BigDecimal setScale (int newScale, RoundingMode roundingMode):
37
                    returns a BigDecimal with newScale.
38
               doubleValue () / toPlainString () : converts to other types.
39
40
               Arrays.sort (T [] a);
41
               Arrays.sort (T [] a, int fromIndex, int toIndex);
42
               Arrays.sort (T [] a, int fromIndex, int toIndex, Comperator <? super T> comperator);
43
           LinkedList <E> :
```

CHAPTER 9. 提示 16

```
44
                addFirst / addLast (E) / getFirst / getLast / removeFirst / removeLast ():
 45
                     deque implementation.
 46
                clear () / add (int, E) / remove (int) : clear, add & remove.
 47
                size () / contains / removeFirstOccurrence / removeLastOccurrence (E) :
 48
                     deque methods.
 49
                ListIterator <E> listIterator (int index) : returns an iterator :
 50
                    E next / previous () : accesses and iterates.
 51
                     hasNext / hasPrevious () : checks availablity.
 52
                     nextIndex / previousIndex () : returns the index of a subsequent call.
 53
                     add / set (E) / remove () : changes element.
 54
            PriorityQueue <E> (int initcap, Comparator <? super E> comparator) :
 55
                add (E) / clear () / iterator () / peek () / poll () / size () :
 56
                    priority queue implementations.
 57
            TreeMap <K, V> (Comparator <? super K> comparator) :
 58
                Map.Entry <K, V> ceilingEntry / floorEntry / higherEntry / lowerEntry (K):
 59
                     getKey / getValue () / setValue (V) : entries.
 60
                clear () / put (K, V) / get (K) / remove (K) : basic operation.
 61
                size () : size.
 62
            StringBuilder:
 63
                Mutable string.
 64
                StringBuilder (string): generates a builder.
 65
                append (int, string, ...) / insert (int offset, ...) : adds objects.
 66
                charAt (int) / setCharAt (int, char) : accesses a char.
 67
                delete (int, int) : removes a substring.
 68
                reverse (): reverses itself.
 69
                length (): returns the length.
 70
                toString (): converts to string.
 71
 72
                Immutable string.
 73
                String.format (String, ...): formats a string. i.e. sprintf.
 74
                toLowerCase / toUpperCase () : changes the case of letters.
 75
 76
 77
     /* Examples on Comparator :
 78
     public class Main {
 79
         public static class Point {
 80
            public int x;
 81
            public int y;
 82
            public Point () {
 83
                x = 0;
 84
                y = 0;
 85
 86
            public Point (int xx, int yy) {
 87
                x = xx;
 88
                y = yy;
 89
 90
        };
 91
         public static class Cmp implements Comparator <Point> {
 92
            public int compare (Point a, Point b) {
 93
                if (a.x < b.x) return -1;
 94
                if (a.x == b.x) {
 95
                    if (a.y < b.y) return -1;
 96
                    if (a.y == b.y) return 0;
 97
 98
                return 1;
 99
100
         public static void main (String [] args) {
101
102
            Cmp c = new Cmp ();
103
            TreeMap <Point, Point> t = new TreeMap <Point, Point> (c);
104
            return:
105
106 };
107
108
109
          Another way to implement is to use Comparable.
        However, equalTo and hashCode must be rewritten.
```

```
111
         Otherwise, containers may fail.
112
113
         public static class Point implements Comparable <Point> {
114
             public int x;
115
             public int y;
116
             public Point () {
117
                 x = 0:
118
                 y = 0;
119
120
             public Point (int xx, int yy) {
121
                 x = xx;
122
                 y = yy;
123
124
             public int compareTo (Point p) {
125
                 if (x < p.x) return -1;
126
                 if (x == p.x) {
127
                     if (y < p.y) return -1;
128
                     if (y == p.y) return 0;
129
130
                 return 1;
131
132
             public boolean equalTo (Point p) {
133
                 return (x == p.x \&\& y == p.y);
134
135
             public int hashCode () {
136
                 return x + y;
137
138
        };
139
     */
140
141
     //Faster IO :
142
143
     public class Main {
144
145
         static class InputReader {
146
             public BufferedReader reader;
147
             public StringTokenizer tokenizer;
148
             public InputReader (InputStream stream) {
149
                 reader = new BufferedReader (new InputStreamReader (stream), 32768);
150
                 tokenizer = null;
151
152
             public String next() {
153
                 while (tokenizer == null || !tokenizer.hasMoreTokens()) {
154
                     try {
155
                         String line = reader.readLine();
156
                         tokenizer = new StringTokenizer (line);
157
                     } catch (IOException e) {
158
                         throw new RuntimeException (e);
159
160
                 }
161
                 return tokenizer.nextToken();
162
163
             public BigInteger nextBigInteger() {
164
                 return new BigInteger (next (), 10); // customize the radix here.
165
166
             public int nextInt() {
167
                 return Integer.parseInt (next());
168
169
             public double nextDouble() {
170
                 return Double.parseDouble (next());
171
172
173
174
         public static void main (String[] args) {
175
             InputReader in = new InputReader (System.in);
176
```

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 179 | } 180 | }