ARONDICHT'S STANDARD CODE LIBRARY*

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 $^{{\}rm *https://github.com/footoredo/Arondight}$

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Chapter 1

计算几何

```
1 int sign(DB x) {
      return (x > eps) - (x < -eps);
2
3 }
4 DB msqrt(DB x) {
5
      return sign(x) > 0 ? sqrt(x) : 0;
  }
6
8
  struct Point {
9
      DB x, y;
      Point rotate(DB ang) const { // 逆时针旋转 ang 弧度
10
11
          return Point(cos(ang) * x - sin(ang) * y,
                   cos(ang) * y + sin(ang) * x);
12
13
      Point turn90() const { // 逆时针旋转 90 度
14
15
          return Point(-y, x);
16
      Point unit() const {
17
18
          return *this / len();
19
20 };
  DB dot(const Point& a, const Point& b) {
21
      return a.x * b.x + a.y * b.y;
22
  }
23
  DB det(const Point& a, const Point& b) {
24
      return a.x * b.y - a.y * b.x;
25
26 }
27 #define cross(p1,p2,p3) ((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
28 #define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
29|bool isLL(const Line& 11, const Line& 12, Point& p) { // 直线与直线交点
      DB s1 = det(12.b - 12.a, 11.a - 12.a),
30
         s2 = -det(12.b - 12.a, 11.b - 12.a);
31
32
      if (!sign(s1 + s2)) return false;
      p = (11.a * s2 + 11.b * s1) / (s1 + s2);
33
34
      return true;
35 }
```

CHAPTER 1. 计算几何

6

```
36 bool onSeg(const Line& 1, const Point& p) { // 点在线段上
      return sign(det(p - 1.a, 1.b - 1.a)) == 0 && sign(dot(p - 1.a, p - 1.b)) <= 0;
38 | }
  |Point projection(const Line & 1, const Point& p) {
39
      return 1.a + (1.b - 1.a) * (dot(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len2());
40
41
  DB disToLine(const Line& 1, const Point& p) { // 点到 * 直线 * 距离
42
      return fabs(det(p - 1.a, 1.b - 1.a) / (1.b - 1.a).len());
43
44 | }
45 DB disToSeg(const Line& 1, const Point& p) { // 点到线段距离
      return sign(dot(p - 1.a, 1.b - 1.a)) * sign(dot(p - 1.b, 1.a - 1.b)) == 1 ? disToLine(1, p)
46
    \rightarrow: std::min((p - l.a).len(), (p - l.b).len());
  }
47
  // 圆与直线交点
48
49 bool isCL(Circle a, Line 1, Point& p1, Point& p2) {
50
      DB x = dot(1.a - a.o, 1.b - 1.a),
         y = (1.b - 1.a).len2(),
51
         d = x * x - y * ((1.a - a.o).len2() - a.r * a.r);
52
      if (sign(d) < 0) return false;</pre>
53
      Point p = 1.a - ((1.b - 1.a) * (x / y)), delta = (1.b - 1.a) * (msqrt(d) / y);
54
55
      p1 = p + delta; p2 = p - delta;
      return true;
56
  }
57
58 //圆与圆的交面积
59 DB areaCC(const Circle& c1, const Circle& c2) {
      DB d = (c1.o - c2.o).len();
60
      if (sign(d - (c1.r + c2.r)) >= 0) return 0;
61
      if (sign(d - std::abs(c1.r - c2.r)) \le 0) {
62
          DB r = std::min(c1.r, c2.r);
63
          return r * r * PI;
64
65
      DB x = (d * d + c1.r * c1.r - c2.r * c2.r) / (2 * d),
66
          t1 = acos(x / c1.r), t2 = acos((d - x) / c2.r);
67
      return c1.r * c1.r * t1 + c2.r * c2.r * t2 - d * c1.r * sin(t1);
68
69 | }
  // 圆与圆交点
70
71
  bool isCC(Circle a, Circle b, P& p1, P& p2) {
      DB s1 = (a.o - b.o).len();
72
      if (sign(s1 - a.r - b.r) > 0 \mid \mid sign(s1 - std::abs(a.r - b.r)) < 0) return false;
73
      DB s2 = (a.r * a.r - b.r * b.r) / s1;
74
      DB aa = (s1 + s2) * 0.5, bb = (s1 - s2) * 0.5;
75
      P \circ = (b.o - a.o) * (aa / (aa + bb)) + a.o;
76
      P delta = (b.o - a.o).unit().turn90() * msqrt(a.r * a.r - aa * aa);
77
      p1 = o + delta, p2 = o - delta;
78
      return true;
79
80 | }
81 // 求点到圆的切点,按关于点的顺时针方向返回两个点
82 | bool tanCP(const Circle &c, const Point &p0, Point &p1, Point &p2) {
      double x = (p0 - c.o).len2(), d = x - c.r * c.r;
```

```
if (d < eps) return false; // 点在圆上认为没有切点
84
       Point p = (p0 - c.o) * (c.r * c.r / x);
       Point delta = ((p0 - c.o) * (-c.r * sqrt(d) / x)).turn90();
86
       p1 = c.o + p + delta;
87
       p2 = c.o + p - delta;
88
89
       return true;
90
   }
   // 求圆到圆的外共切线, 按关于 c1.o 的顺时针方向返回两条线
91
   vector<Line> extanCC(const Circle &c1, const Circle &c2) {
92
       vector<Line> ret;
93
       if (sign(c1.r - c2.r) == 0) {
94
           Point dir = c2.o - c1.o;
95
           dir = (dir * (c1.r / dir.len())).turn90();
96
           ret.push_back(Line(c1.o + dir, c2.o + dir));
97
           ret.push_back(Line(c1.o - dir, c2.o - dir));
98
99
       } else {
           Point p = (c1.0 * -c2.r + c2.o * c1.r) / (c1.r - c2.r);
100
           Point p1, p2, q1, q2;
101
           if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
102
               if (c1.r < c2.r) swap(p1, p2), swap(q1, q2);
103
               ret.push_back(Line(p1, q1));
               ret.push_back(Line(p2, q2));
105
           }
106
       }
107
       return ret;
108
109
   // 求圆到圆的内共切线,按关于 c1.o 的顺时针方向返回两条线
110
   std::vector<Line> intanCC(const Circle &c1, const Circle &c2) {
111
       std::vector<Line> ret;
112
       Point p = (c1.0 * c2.r + c2.o * c1.r) / (c1.r + c2.r);
113
       Point p1, p2, q1, q2;
114
       if (tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) { // 两圆相切认为没有切线
115
           ret.push_back(Line(p1, q1));
116
           ret.push_back(Line(p2, q2));
117
       }
118
119
       return ret;
120
121
   bool contain(vector<Point> polygon, Point p) { // 判断点 p 是否被多边形包含,包括落在边界上
       int ret = 0, n = polygon.size();
122
       for(int i = 0; i < n; ++ i) {
123
           Point u = polygon[i], v = polygon[(i + 1) % n];
124
           if (onSeg(Line(u, v), p)) return true; // Here I guess.
125
           if (sign(u.y - v.y) \le 0) swap(u, v);
126
           if (sign(p.y - u.y) > 0 \mid \mid sign(p.y - v.y) \le 0) continue;
127
           ret += sign(det(p, v, u)) > 0;
128
129
130
       return ret & 1;
131 | }
132 /// 用半平面(q1,q2)的逆时针方向去切凸多边形
```

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```
std::vector<Point> convexCut(const std::vector<Point>&ps, Point q1, Point q2) {
       std::vector<Point> qs; int n = ps.size();
       for (int i = 0; i < n; ++i) {
135
           Point p1 = ps[i], p2 = ps[(i + 1) % n];
136
137
            int d1 = crossOp(q1,q2,p1), d2 = crossOp(q1,q2,p2);
138
            if (d1 \ge 0) qs.push_back(p1);
            if (d1 * d2 < 0) qs.push_back(isSS(p1, p2, q1, q2));
139
       }
140
141
       return qs;
   }
142
   // 求凸包
143
   std::vector<Point> convexHull(std::vector<Point> ps) {
144
       int n = ps.size(); if (n <= 1) return ps;</pre>
145
       std::sort(ps.begin(), ps.end());
146
       std::vector<Point> qs;
147
       for (int i = 0; i < n; qs.push_back(ps[i ++]))
148
149
            while (qs.size() > 1 \&\& sign(det(qs[qs.size() - 2], qs.back(), ps[i])) \le 0)
150
                qs.pop_back();
       for (int i = n - 2, t = qs.size(); i \ge 0; qs.push_back(ps[i --]))
151
            while ((int)qs.size() > t && sign(det(qs[qs.size() - 2], qs.back(), ps[i])) \le 0)
152
153
                qs.pop_back();
       return qs;
154
```

1.1 凸包

```
// 凸包中的点按逆时针方向
  struct Convex {
2
3
      int n;
4
      std::vector<Point> a, upper, lower;
      void make_shell(const std::vector<Point>& p,
5
6
               std::vector<Point>& shell) { // p needs to be sorted.
7
           clear(shell); int n = p.size();
           for (int i = 0, j = 0; i < n; i++, j++) {
8
               for (; j \ge 2 \&\& sign(det(shell[j-1] - shell[j-2],
9
                                p[i] - shell[j-2])) <= 0; --j) shell.pop_back();</pre>
10
               shell.push_back(p[i]);
11
           }
12
      }
13
      void make_convex() {
14
           std::sort(a.begin(), a.end());
15
           make_shell(a, lower);
16
           std::reverse(a.begin(), a.end());
17
           make_shell(a, upper);
18
           a = lower; a.pop_back();
19
           a.insert(a.end(), upper.begin(), upper.end());
20
           if ((int)a.size() >= 2) a.pop_back();
21
           n = a.size();
22
      }
23
```

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```
void init(const std::vector<Point>& _a) {
24
          clear(a); a = _a; n = a.size();
25
          make_convex();
26
      }
      void read(int _n) { // Won't make convex.
28
29
          clear(a); n = _n; a.resize(n);
          for (int i = 0; i < n; i++)
30
              a[i].read();
31
32
      std::pair<DB, int> get_tangent(
33
              const std::vector<Point>& convex, const Point& vec) {
34
          int 1 = 0, r = (int)convex.size() - 2;
35
          assert(r >= 0);
36
          for (; l + 1 < r; ) {
37
              int mid = (1 + r) / 2;
38
              if (sign(det(convex[mid + 1] - convex[mid], vec)) > 0)
39
40
                  r = mid;
              else 1 = mid;
41
          }
42
          return std::max(std::make_pair(det(vec, convex[r]), r),
43
44
                  std::make_pair(det(vec, convex[0]), 0));
45
      int binary_search(Point u, Point v, int 1, int r) {
46
          int s1 = sign(det(v - u, a[1 \% n] - u));
47
          for (; 1 + 1 < r; ) {
48
              int mid = (1 + r) / 2;
49
              int smid = sign(det(v - u, a[mid % n] - u));
50
              if (smid == s1) 1 = mid;
51
              else r = mid;
52
53
          return 1 % n;
54
55
      // 求凸包上和向量 vec 叉积最大的点,返回编号,共线的多个切点返回任意一个
56
      int get_tangent(Point vec) {
57
          std::pair<DB, int> ret = get_tangent(upper, vec);
58
          ret.second = (ret.second + (int)lower.size() - 1) % n;
59
60
          ret = std::max(ret, get_tangent(lower, vec));
61
          return ret.second;
      }
62
      // 求凸包和直线 u, v 的交点,如果不相交返回 false,如果有则是和 (i, next(i))的交点,交在点上不
63
    → 确定返回前后两条边其中之-
      bool get intersection(Point u, Point v, int &i0, int &i1) {
64
          int p0 = get_tangent(u - v), p1 = get_tangent(v - u);
65
          if (sign(det(v - u, a[p0] - u)) * sign(det(v - u, a[p1] - u)) <= 0) {
66
              if (p0 > p1) std::swap(p0, p1);
67
              i0 = binary_search(u, v, p0, p1);
68
              i1 = binary_search(u, v, p1, p0 + n);
69
70
              return true;
71
          }
```

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1.2 三角形的心

```
Point inCenter(const Point &A, const Point &B, const Point &C) { // 内心
      double a = (B - C).len(), b = (C - A).len(), c = (A - B).len(),
2
3
          s = fabs(det(B - A, C - A)),
4
          r = s / p;
      return (A * a + B * b + C * c) / (a + b + c);
5
6 }
7
  |Point circumCenter(const Point &a, const Point &b, const Point &c) { // 外心
      Point bb = b - a, cc = c - a;
8
      double db = bb.len2(), dc = cc.len2(), d = 2 * det(bb, cc);
9
      return a - Point(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
10
11
  |}
12 Point othroCenter(const Point &a, const Point &b, const Point &c) { // 垂心
      Point ba = b - a, ca = c - a, bc = b - c;
13
      double Y = ba.y * ca.y * bc.y,
14
             A = ca.x * ba.y - ba.x * ca.y,
15
             x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
16
             y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
17
18
      return Point(x0, y0);
19 }
```

1.3 半平面交

```
1 struct Point {
2
       int quad() const { return sign(y) == 1 \mid \mid (sign(y) == 0 \&\& sign(x) >= 0);}
3 };
4 struct Line {
       bool include(const Point &p) const { return sign(det(b - a, p - a)) > 0; }
5
       Line push() const{ // 将半平面向外推 eps
6
           const double eps = 1e-6;
7
           Point delta = (b - a).turn90().norm() * eps;
8
           return Line(a - delta, b - delta);
9
10
11 | };
12 bool sameDir(const Line &10, const Line &11) { return parallel(10, 11) && sign(dot(10.b - 10.a,
    \hookrightarrow 11.b - 11.a)) == 1; }
  bool operator < (const Point &a, const Point &b) {</pre>
13
       if (a.quad() != b.quad()) {
14
           return a.quad() < b.quad();</pre>
15
       } else {
16
           return sign(det(a, b)) > 0;
17
18
```

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```
19 }
  bool operator < (const Line &10, const Line &11) {
      if (sameDir(10, 11)) {
21
           return 11.include(10.a);
22
23
      } else {
24
           return (10.b - 10.a) < (11.b - 11.a);
25
26 }
  bool check(const Line &u, const Line &v, const Line &w) { return w.include(intersect(u, v)); }
27
  vector<Point> intersection(vector<Line> &1) {
28
      sort(l.begin(), l.end());
29
      deque<Line> q;
30
       for (int i = 0; i < (int)1.size(); ++i) {</pre>
31
           if (i && sameDir(l[i], l[i - 1])) {
32
               continue;
33
34
35
           while (q.size() > 1 \& ! check(q[q.size() - 2], q[q.size() - 1], l[i])) q.pop_back();
           while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
36
           q.push_back(l[i]);
37
38
      while (q.size() > 2 \&\& !check(q[q.size() - 2], q[q.size() - 1], q[0])) q.pop_back();
39
      while (q.size() > 2 \&\& !check(q[1], q[0], q[q.size() - 1])) q.pop_front();
40
      vector<Point> ret;
41
      for (int i = 0; i < (int)q.size(); ++i) ret.push_back(intersect(q[i], q[(i + 1) %
42
     \hookrightarrow q.size()]));
43
      return ret;
44 }
```

1.4 圆交面积及重心

```
1 struct Event {
2
      Point p;
3
      double ang;
      int delta;
      Event (Point p = Point(0, 0), double ang = 0, double delta = 0) : p(p), ang(ang),
5

    delta(delta) {}
  };
6
  bool operator < (const Event &a, const Event &b) {</pre>
7
8
      return a.ang < b.ang;</pre>
  }
9
  void addEvent(const Circle &a, const Circle &b, vector<Event> &evt, int &cnt) {
10
      double d2 = (a.o - b.o).len2(),
11
              dRatio = ((a.r - b.r) * (a.r + b.r) / d2 + 1) / 2,
12
              pRatio = sqrt(-(d2 - sqr(a.r - b.r)) * (d2 - sqr(a.r + b.r)) / (d2 * d2 * 4));
13
      Point d = b.o - a.o, p = d.rotate(PI / 2),
14
             q0 = a.o + d * dRatio + p * pRatio,
15
             q1 = a.o + d * dRatio - p * pRatio;
16
      double ang 0 = (q0 - a.o).ang(),
17
```

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```
ang1 = (q1 - a.o).ang();
18
       evt.push_back(Event(q1, ang1, 1));
      evt.push_back(Event(q0, ang0, -1));
20
      cnt += ang1 > ang0;
21
  }
22
23
  bool issame(const Circle &a, const Circle &b) { return sign((a.o - b.o).len()) == 0 && sign(a.r
     \rightarrow - b.r) == 0; }
24 | bool overlap(const Circle &a, const Circle &b) { return sign(a.r - b.r - (a.o - b.o).len()) >=
25 bool intersect(const Circle &a, const Circle &b) { return sign((a.o - b.o).len() - a.r - b.r) <
    \hookrightarrow 0; }
26 Circle c[N];
  double area[N]; // area[k] -> area of intersections >= k.
28 Point centroid[N];
29 bool keep[N];
30 void add(int cnt, DB a, Point c) {
31
       area[cnt] += a;
       centroid[cnt] = centroid[cnt] + c * a;
32
33 }
  void solve(int C) {
34
      for (int i = 1; i <= C; ++ i) {
35
           area[i] = 0;
36
           centroid[i] = Point(0, 0);
37
38
      for (int i = 0; i < C; ++i) {
39
           int cnt = 1;
40
           vector<Event> evt;
41
           for (int j = 0; j < i; ++j) if (issame(c[i], c[j])) ++cnt;
42
           for (int j = 0; j < C; ++j) {
43
               if (j != i && !issame(c[i], c[j]) && overlap(c[j], c[i])) {
44
45
                   ++cnt;
               }
46
           }
47
           for (int j = 0; j < C; ++j) {
48
               if (j != i && !overlap(c[j], c[i]) && !overlap(c[i], c[j]) && intersect(c[i], c[j]))
49
     → {
50
                   addEvent(c[i], c[j], evt, cnt);
               }
51
           }
52
           if (evt.size() == 0u) {
53
               add(cnt, PI * c[i].r * c[i].r, c[i].o);
54
55
               sort(evt.begin(), evt.end());
56
               evt.push_back(evt.front());
57
               for (int j = 0; j + 1 < (int)evt.size(); ++j) {
58
                   cnt += evt[j].delta;
                   add(cnt, det(evt[j].p, evt[j + 1].p) / 2, (evt[j].p + evt[j + 1].p) / 3);
60
61
                   double ang = evt[j + 1].ang - evt[j].ang;
                   if (ang < 0) {
62
```

1.5. 极角排序 13

```
ang += PI * 2;
63
                     }
                     if (sign(ang) == 0) continue;
65
                     add(cnt, ang * c[i].r * c[i].r / 2, c[i].o +
66
                         Point(sin(ang1) - sin(ang0), -cos(ang1) + cos(ang0)) * (2 / (3 * ang) *
67
     \hookrightarrow c[i].r));
68
                     add(cnt, -sin(ang) * c[i].r * c[i].r / 2, (c[i].o + evt[j].p + evt[j + 1].p) /
     \hookrightarrow 3);
                }
69
            }
70
71
       for (int i = 1; i <= C; ++ i)
72
            if (sign(area[i])) {
73
                centroid[i] = centroid[i] / area[i];
74
            }
75
76 | }
```

1.5 极角排序

1.6 最小圆覆盖

1.7 三维向量绕轴旋转

```
// 三维绕轴旋转, 大拇指指向 axis 向量方向, 四指弯曲方向转 w 弧度
Point rotate(const Point& s, const Point& axis, DB w) {
    DB x = axis.x, y = axis.y, z = axis.z;
    DB s1 = x * x + y * y + z * z, ss1 = msqrt(s1),
    cosw = cos(w), sinw = sin(w);
    DB a[4][4];
    memset(a, 0, sizeof a);
```

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```
a[3][3] = 1;
8
9
      a[0][0] = ((y * y + z * z) * cosw + x * x) / s1;
      a[0][1] = x * y * (1 - cosw) / s1 + z * sinw / ss1;
10
      a[0][2] = x * z * (1 - cosw) / s1 - y * sinw / ss1;
11
      a[1][0] = x * y * (1 - cosw) / s1 - z * sinw / ss1;
12
13
      a[1][1] = ((x * x + z * z) * cosw + y * y) / s1;
      a[1][2] = y * z * (1 - cosw) / s1 + x * sinw / ss1;
14
      a[2][0] = x * z * (1 - cosw) / s1 + y * sinw / ss1;
15
      a[2][1] = y * z * (1 - cosw) / s1 - x * sinw / ss1;
16
      a[2][2] = ((x * x + y * y) * cos(w) + z * z) / s1;
17
      DB ans [4] = \{0, 0, 0, 0\}, c[4] = \{s.x, s.y, s.z, 1\};
18
      for (int i = 0; i < 4; ++ i)
19
           for (int j = 0; j < 4; ++ j)
20
               ans[i] += a[j][i] * c[j];
21
      return Point(ans[0], ans[1], ans[2]);
22
23 | }
```

1.8 三维凸包

```
__inline P cross(const P& a, const P& b) {
2
      return P(
3
               a.y * b.z - a.z * b.y,
               a.z * b.x - a.x * b.z,
4
5
               a.x * b.y - a.y * b.x
           );
6
7
  | }
8
  __inline DB mix(const P& a, const P& b, const P& c) {
      return dot(cross(a, b), c);
10
11 | }
12
13 __inline DB volume(const P& a, const P& b, const P& c, const P& d) {
      return mix(b - a, c - a, d - a);
14
15 | }
16
  struct Face {
17
      int a, b, c;
18
      __inline Face() {}
19
20
       __inline Face(int _a, int _b, int _c):
           a(_a), b(_b), c(_c) {}
21
       __inline DB area() const {
22
          return 0.5 * cross(p[b] - p[a], p[c] - p[a]).len();
23
24
       __inline P normal() const {
25
          return cross(p[b] - p[a], p[c] - p[a]).unit();
26
27
       __inline DB dis(const P& p0) const {
28
           return dot(normal(), p0 - p[a]);
29
```

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```
30
       }
  |};
32
  std::vector<Face> face, tmp; // Should be O(n).
33
  int mark[N][N], Time, n;
34
35
   __inline void add(int v) {
36
       ++ Time;
37
       clear(tmp);
38
       for (int i = 0; i < (int)face.size(); ++ i) {</pre>
39
           int a = face[i].a, b = face[i].b, c = face[i].c;
40
           if (sign(volume(p[v], p[a], p[b], p[c])) > 0) {
41
                mark[a][b] = mark[b][a] = mark[a][c] =
42
                    mark[c][a] = mark[b][c] = mark[c][b] = Time;
43
           }
44
45
           else {
46
                tmp.push_back(face[i]);
47
       }
48
       clear(face); face = tmp;
49
       for (int i = 0; i < (int)tmp.size(); ++ i) {</pre>
50
           int a = face[i].a, b = face[i].b, c = face[i].c;
51
           if (mark[a][b] == Time) face.emplace_back(v, b, a);
52
           if (mark[b][c] == Time) face.emplace_back(v, c, b);
53
           if (mark[c][a] == Time) face.emplace_back(v, a, c);
           assert(face.size() < 500u);
55
56
       }
  }
57
58
   void reorder() {
59
       for (int i = 2; i < n; ++ i) {
60
           P \text{ tmp} = cross(p[i] - p[0], p[i] - p[1]);
61
           if (sign(tmp.len())) {
62
                std::swap(p[i], p[2]);
63
                for (int j = 3; j < n; ++ j)
64
                    if (sign(volume(p[0], p[1], p[2], p[j]))) {
65
66
                        std::swap(p[j], p[3]);
67
                        return;
                    }
68
           }
69
       }
70
  | }
71
72
  void build_convex() {
73
       reorder();
74
       clear(face);
75
       face.emplace_back(0, 1, 2);
76
77
       face.emplace_back(0, 2, 1);
78
       for (int i = 3; i < n; ++ i)
```

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79 add(i); 80 }

Chapter 2

数论

$2.1 \quad O(m^2 \log n)$ 求线性递推数列第 n 项

```
Given a_0, a_1, \dots, a_{m-1}

a_n = c_0 \times a_{n-m} + \dots + c_{m-1} \times a_{n-1}

Solve for a_n = v_0 \times a_0 + v_1 \times a_1 + \dots + v_{m-1} \times a_{m-1}
```

```
void linear_recurrence(long long n, int m, int a[], int c[], int p) {
2
       long long v[M] = \{1 \% p\}, u[M << 1], msk = !!n;
       for(long long i(n); i > 1; i >>= 1) {
3
           msk <<= 1;
4
5
       for(long long x(0); msk; msk >>= 1, x <<= 1) {
6
7
           fill_n(u, m << 1, 0);
           int b(!!(n & msk));
8
9
           x \mid = b;
           if(x < m) {
10
               u[x] = 1 \% p;
11
12
           }else {
13
               for(int i(0); i < m; i++) {
                    for(int j(0), t(i + b); j < m; j++, t++) {
14
                        u[t] = (u[t] + v[i] * v[j]) % p;
15
16
17
               for(int i((m << 1) - 1); i >= m; i--) {
18
                    for(int j(0), t(i - m); j < m; j++, t++) {
19
20
                        u[t] = (u[t] + c[j] * u[i]) % p;
21
               }
22
           }
23
24
           copy(u, u + m, v);
       }
25
       //a[n] = v[0] * a[0] + v[1] * a[1] + ... + v[m - 1] * a[m - 1].
26
       for(int i(m); i < 2 * m; i++) {</pre>
27
28
           a[i] = 0;
           for(int j(0); j < m; j++) {</pre>
29
```

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```
a[i] = (a[i] + (long long)c[j] * a[i + j - m]) % p;
30
            }
31
       }
32
       for(int j(0); j < m; j++) {</pre>
33
           b[j] = 0;
34
35
           for(int i(0); i < m; i++) {
                b[j] = (b[j] + v[i] * a[i + j]) % p;
36
37
       }
38
       for(int j(0); j < m; j++) {</pre>
39
            a[j] = b[j];
40
       }
41
  }
42
```

2.2 求逆元

```
1
  void ex_gcd(long long a, long long b, long long &x, long long &y) {
2
      if (b == 0) {
           x = 1;
3
           y = 0;
4
5
           return;
6
7
      long long xx, yy;
8
      ex_gcd(b, a % b, xx, yy);
      y = xx - a / b * yy;
9
      x = yy;
10
11
  |}
12
  long long inv(long long x, long long MODN) {
13
      long long inv_x, y;
14
      ex_gcd(x, MODN, inv_x, y);
15
      return (inv_x % MODN + MODN) % MODN;
16
17 }
```

2.3 中国剩余定理

```
1 // 返回 (ans, M), 其中 ans 是模 M 意义下的解
2
  std::pair<long long, long long> CRT(const std::vector<long long>& m, const std::vector<long
    \rightarrow long>& a) {
      long long M = 1, ans = 0;
3
      int n = m.size();
4
      for (int i = 0; i < n; i++) M *= m[i];
5
      for (int i = 0; i < n; i++) {
6
          ans = (ans + (M / m[i]) * a[i] % M * inv(M / m[i], m[i])) % M; // 可能需要大整数相乘取模
7
8
9
      return std::make_pair(ans, M);
10 }
```

2.4. 魔法 CRT 19

```
11 // 模数不互质的情况
  |bool solve(int n, std::pair<long long, long long> input[],
                     std::pair<long long, long long> &output) {
13
      output = std::make_pair(1, 1);
14
      for (int i = 0; i < n; ++i) {
15
16
          long long number, useless;
          // euclid(a, b, x, y)
17
          euclid(output.second, input[i].second, number, useless);
18
          long long divisor = std::__gcd(output.second, input[i].second);
19
          if ((input[i].first - output.first) % divisor) return false;
20
          number *= (input[i].first - output.first) / divisor;
21
          fix(number, input[i].second);
                                            // fix 成正的
22
23
          output.first += output.second * number;
          output.second *= input[i].second / divisor;
24
          fix(output.first, output.second);
25
26
      }
27
      return true;
28 }
```

2.4 魔法 CRT

```
1 \mid // MOD is the given module
  // Do not depend on LL * LL % LL
3 inline int CRT(int *a) {
      static int x[N];
      for (int i = 0; i < N; i ++) {
5
           x[i] = a[i];
6
           for (int j = 0; j < i; j ++) {
7
               int t = (x[i] - x[j] + mod[i]) \% mod[i];
8
9
               if (t < 0) t += mod[i];</pre>
               x[i] = 1LL * t * Inv[j][i] % mod[i];
10
           }
11
      }
12
      int sum = 1, ret = x[0] % MOD;
13
14
      for (int i = 1; i < N; i ++) {
           sum = 1LL * sum * mod[i - 1] % MOD;
15
           ret += 1LL * x[i] * sum % MOD;
16
           if (ret >= MOD) ret -= MOD;
17
      }
18
      return ret;
19
  }
20
  for (int i = 0; i < N; i ++)
21
      for (int j = i + 1; j < N; j ++) {
22
           Inv[i][j] = fpw(mod[i], mod[j] - 2, mod[j]);
23
24
      }
```

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2.5 素性测试

```
int strong_pseudo_primetest(long long n,int base) {
       long long n2=n-1,res;
2
3
       int s=0;
       while (n2\%2==0) n2>>=1,s++;
4
       res=powmod(base,n2,n);
5
       if((res==1)||(res==n-1)) return 1;
6
7
       s--;
       while(s \ge 0) {
8
           res=mulmod(res,res,n);
9
10
           if(res==n-1) return 1;
11
           s--;
12
       return 0; // n is not a strong pseudo prime
13
  }
14
15
  int isprime(long long n) {
       static LL testNum[]={2,3,5,7,11,13,17,19,23,29,31,37};
16
       static LL lim[]={4,0,1373653LL,25326001LL,25000000000LL,2152302898747LL,
17
    → 3474749660383LL,341550071728321LL,0,0,0,0);
       if(n<2||n==3215031751LL) return 0;
18
       for(int i=0;i<12;++i){</pre>
19
20
           if(n<lim[i]) return 1;</pre>
           if(strong_pseudo_primetest(n,testNum[i])==0) return 0;
21
22
       return 1;
23
24 | }
```

2.6 EX-BSGS

```
1 /*
   * a^x = b \pmod{p}
3
   * p may not be a prime
   */
  unordered_map<int,int> mp;
6
  ll exbsgs(ll a,ll b,ll p)
7
8 {
9
       if (b == 1) return 0;
      11 t, d = 1, k = 0;
10
      while ((t = \_gcd(a, p)) != 1) {
11
           if (b \% t) return -1;
12
           ++k, b /= t, p /= t, d = d * (a / t) % p;
13
           if (b == d) return k;
14
      }
15
      mp.clear();
16
      11 m = std::ceil(std::sqrt(p));
17
      11 a_m = powmod(a, m, p);
18
```

2.7. 质因数分解 21

```
19
       11 mul = b;
20
       for (ll j = 1; j \le m; ++j) {
           mul = mul * a % p;
21
           mp[mul] = j;
22
       }
23
24
       for (ll i = 1; i <= m; ++i) {
25
           d = d * a_m \% p;
           if (mp.count(d)) return i * m - mp[d] + k;
26
       }
27
       return -1;
28
29 }
```

2.7 质因数分解

```
int ansn; LL ans[1000];
  LL func(LL x,LL n) { return(mod_mul(x,x,n)+1)%n; }
3 LL Pollard(LL n){
      LL i,x,y,p;
4
      if(Rabin_Miller(n)) return n;
5
6
      if(!(n&1)) return 2;
7
      for(i=1;i<20;i++){
           x=i; y=func(x,n); p=gcd(y-x,n);
8
           while (p==1) {x=func(x,n); y=func(func(y,n),n); p=gcd((y-x+n)\%n,n)\%n;}
9
10
           if(p==0||p==n) continue;
11
           return p;
      }
12
  }
13
  void factor(LL n){
14
      LL x:
15
      x=Pollard(n);
16
      if(x==n){ ans[ansn++]=x; return; }
17
      factor(x), factor(n/x);
18
19 }
```

2.8 线下整点

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2.9 线性同余不等式

2.10 原根相关

- 1. 模 m 有原根的充要条件: $m=2,4,p^a,2p^a$, 其中 p 是奇素数;
- 2. 求任意数 p 原根的方法: 对 $\phi(p)$ 因式分解, 即 $\phi(p) = p_1^{r_1} p_2^{r_2} \cdots p_k^{r_k}$, 若恒成立:

$$g^{\frac{p-1}{g}} \neq 1 \pmod{p}$$

那么g就是p的原根。

3. 若模 m 有原根,那么它一共有 $\Phi(\Phi(m))$ 个原根。

Chapter 3

代数

3.1 快速傅里叶变换

```
int prepare(int n) {
1
2
      int len = 1;
      for (; len <= 2 * n; len <<= 1);
3
      for (int i = 0; i < len; i++) {
4
           e[0][i] = Complex(cos(2 * pi * i / len), sin(2 * pi * i / len));
5
           e[1][i] = Complex(cos(2 * pi * i / len), -sin(2 * pi * i / len));
6
7
8
      return len;
9
  }
  void DFT(Complex *a, int n, int f) {
10
      for (int i = 0, j = 0; i < n; i++) {
11
12
           if (i > j) std::swap(a[i], a[j]);
           for (int t = n >> 1; (j ^= t) < t; t >>= 1);
13
14
      for (int i = 2; i \le n; i \le 1)
15
           for (int j = 0; j < n; j += i)
16
17
               for (int k = 0; k < (i >> 1); k++) {
                   Complex A = a[j + k];
18
                   Complex B = e[f][n / i * k] * a[j + k + (i >> 1)];
19
                   a[j + k] = A + B;
20
                   a[j + k + (i >> 1)] = A - B;
21
22
      if (f == 1) {
23
           for (int i = 0; i < n; i++)
24
               a[i].a /= n;
25
      }
26
27 | }
```

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3.2 任意数快速傅里叶变换

```
1 int prepare(int n) {
2
      int len = 1;
      for (; len <= 2 * n; len <<= 1);
3
      for (int i = 0; i < len; i++) {
4
           e[0][i] = Complex(cos(2 * pi * i / len), sin(2 * pi * i / len));
5
           e[1][i] = Complex(cos(2 * pi * i / len), -sin(2 * pi * i / len));
6
7
8
      return len;
  |}
9
10
  void DFT(Complex *a, int n, int f) {
      for (int i = 0, j = 0; i < n; i++) {
11
           if (i > j) std::swap(a[i], a[j]);
12
           for (int t = n >> 1; (j ^= t) < t; t >>= 1);
13
      }
14
      for (int i = 2; i <= n; i <<= 1)
15
           for (int j = 0; j < n; j += i)
16
               for (int k = 0; k < (i >> 1); k++) {
17
                   Complex A = a[j + k];
18
                   Complex B = e[f][n / i * k] * a[j + k + (i >> 1)];
19
                   a[j + k] = A + B;
20
                   a[j + k + (i >> 1)] = A - B;
21
22
       if (f == 1) {
23
           for (int i = 0; i < n; i++)
24
25
               a[i].a /= n;
      }
26
27 }
```

3.3 fwt

```
1 /*
  xor(A) = (xor(A0+A1), xor(A0-A1))
  xor(A) = (xor((A0+A1)/2), xor((A0-A1)/2))
3
4
   and(A) = (and(A0+A1), and(A1))
5
  and(A) = (and(A0-A1), and(A1))
6
7
   or(A) = (or(A0), or(A0+A1))
8
  _{or(A)} = (_{or(A0)}, _{or(A1-A0)})
  */
10
11
12
  void FWT(int *a,int n)
13 {
      for (int h=2;h<=n;h<<=1)
14
           for (int j=0; j<n; j+=h)
15
               for (int k=j;k<j+h/2;k++)
16
```

3.4. 快速数论变换 25

```
{
17
                    int u=a[k], v=a[k+h/2];
18
                    //xor : a[k] = (u+v) mo; a[k+h/2] = (u-v+mo) mo;
19
                    //and : a[k]=(u+v)%mo; a[k+h/2]=v;
20
                    //or : a[k]=u; a[k+h/2]=(u+v)%mo;
21
22
23
  void IFWT(int *a,int n)
24
  {
25
       for (int h=2;h<=n;h<<=1)
26
27
           for (int j=0; j<n; j+=h)
                for (int k=j;k<j+h/2;k++)
28
29
                    int u=a[k], v=a[k+h/2];
30
                    //xor : a[k]=((u+v)*1LL*inv_2)%mo; a[k+h/2]=((u-v)*1LL*inv_2 %mo + mo)%mo;
31
32
                    //and : a[k]=(u-v+mo)\%mo; a[k+h/2]=v;
33
                    //or : a[k]=u; a[k+h/2]=(u-v+mo)%mo;
                }
34
  }
35
  void cheng(int *a,int *b,int *c,int len)
36
37
38
       int l=1;
       while (1<len)</pre>
                          <=1;
39
       len=1;
40
       FWT(a,len);
41
       FWT(b,len);
42
       for (int i=0;i<len;i++)</pre>
43
           c[i]=(a[i]*1LL*b[i])%mo;
44
45
       IFWT(c,len);
46 }
```

3.4 快速数论变换

```
1 // meminit(A, 1, r) 是将数组 A 的 [1, r) 清 0。
  // memcopy(target, source, l, r) 是将 source 的 [l, r) 复制到 target 的 [l, r)
  #define meminit(A, 1, r) memset(A + (1), 0, sizeof(*A) * ((r) - (1)))
  #define memcopy(B, A, 1, r) memcpy(B, A + (1), sizeof(*A) * ((r) - (1)))
4
  void DFT(int *a, int n, int f) { // 封闭形式,常数小(10<sup>7</sup> 跑 2.23 秒)
5
6
      for (register int i = 0, j = 0; i < n; i++) {
          if (i > j) std::swap(a[i], a[j]);
7
          for (register int t = n >> 1; (j ^= t) < t; t >>= 1);
8
      }
9
      for (register int i = 2; i <= n; i <<= 1) {
10
          static int exp[MAXN];
11
          exp[0] = 1; exp[1] = fpm(PRT, (MOD - 1) / i);
12
          if (f == 1) \exp[1] = fpm(\exp[1], MOD - 2);
13
          for (register int k = 2; k < (i >> 1); k++) {
              \exp[k] = 111 * \exp[k - 1] * \exp[1] % MOD;
15
```

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```
16
          for (register int j = 0; j < n; j += i) {
17
              for (register int k = 0; k < (i >> 1); k++) {
18
                  register int &pA = a[j + k], &pB = a[j + k + (i >> 1)];
19
20
                  register int A = pA, B = 111 * pB * exp[k] % MOD;
21
                  pA = (A + B) \% MOD;
22
                  pB = (A - B + MOD) \% MOD;
              }
23
          }
24
      }
25
      if (f == 1) {
26
          register int rev = fpm(n, MOD - 2, MOD);
          for (register int i = 0; i < n; i++) {
28
              a[i] = 111 * a[i] * rev % MOD;
29
30
      }
31
32 }
  // 在不写高精度的情况下合并 FFT 所得结果对 MOD 取模后的答案
  // 值得注意的是,这个东西不能最后再合并,而是应该每做一次多项式乘法就 CRT 一次
  int CRT(int *a) {
35
      static int x[3];
36
      for (int i = 0; i < 3; i++) {
37
          x[i] = a[i];
38
          for (int j = 0; j < i; j++) {
39
              int t = (x[i] - x[j] + FFT[i] \rightarrow MOD) \% FFT[i] \rightarrow MOD;
40
              if (t < 0) t += FFT[i] -> MOD;
41
              x[i] = 1LL * t * inv[j][i] % FFT[i] -> MOD;
42
          }
43
      }
      int sum = 1, ret = x[0] % MOD;
45
      for (int i = 1; i < 3; i ++) {
46
          sum = 1LL * sum * FFT[i - 1] \rightarrow MOD % MOD;
47
          ret += 1LL * x[i] * sum % MOD;
48
          if(ret >= MOD) ret -= MOD;
49
      }
50
51
      return ret;
52
53
  for (int i = 0; i < 3; i++) // inv 数组的预处理过程, inverse(x, p) 表示求 x 在 p 下逆元
      for (int j = 0; j < 3; j++)
54
          inv[i][j] = inverse(FFT[i] -> MOD, FFT[j] -> MOD);
```

3.5 自适应辛普森积分

```
namespace adaptive_simpson {
   template<typename function>
   inline double area(function f, const double &left, const double &right) {
      double mid = (left + right) / 2;
      return (right - left) * (f(left) + 4 * f(mid) + f(right)) / 6;
}
```

3.6. 单纯形 27

```
}
6
7
8
      template<typename function>
      inline double simpson(function f, const double &left, const double &right, const double
9
    10
          double mid = (left + right) / 2;
          double area_left = area(f, left, mid);
11
          double area_right = area(f, mid, right);
12
          double area_total = area_left + area_right;
13
          if (fabs(area_total - area_sum) <= 15 * eps) {</pre>
14
              return area_total + (area_total - area_sum) / 15;
15
          }
16
          return simpson(f, left, right, eps / 2, area_left) + simpson(f, mid, right, eps / 2,
17

→ area_right);
      }
18
19
20
      template<typename function>
      inline double simpson(function f, const double &left, const double &right, const double
21
    → &eps) {
          return simpson(f, left, right, eps, area(f, left, right));
22
23
      }
24 }
```

3.6 单纯形

```
const double eps = 1e-8;
  // \max\{c * x \mid Ax \le b, x >= 0\} 的解, 无解返回空的 vector, 否则就是解.
  vector<double> simplex(vector<vector<double> > &A, vector<double> b, vector<double> c) {
3
      int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
4
      vector < double > D(n + 2, vector < double > (m + 1));
5
6
      vector<int> ix(n + m);
7
      for(int i = 0; i < n + m; i++) {
           ix[i] = i;
8
9
      for(int i = 0; i < n; i++) {
10
           for(int j = 0; j < m - 1; j++) {
11
               D[i][j] = -A[i][j];
12
           }
13
          D[i][m - 1] = 1;
14
          D[i][m] = b[i];
15
           if (D[r][m] > D[i][m]) {
16
               r = i;
17
           }
18
      }
19
20
      for(int j = 0; j < m - 1; j++) {
21
          D[n][j] = c[j];
22
23
```

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```
D[n + 1][m - 1] = -1;
24
       for(double d; ;) {
           if (r < n) {
26
                swap(ix[s], ix[r + m]);
                D[r][s] = 1. / D[r][s];
28
29
                for(int j = 0; j \le m; j++) {
                    if (j != s) {
30
                        D[r][j] *= -D[r][s];
31
                    }
32
                }
33
                for(int i = 0; i <= n + 1; i++) {
34
                    if (i != r) {
35
                         for(int j = 0; j <= m; j++) {
36
                             if (j != s) {
37
                                 D[i][j] += D[r][j] * D[i][s];
38
39
40
                        }
                        D[i][s] *= D[r][s];
41
                    }
42
               }
43
           }
           r = -1, s = -1;
45
           for(int j = 0; j < m; j++) {
46
                if (s < 0 || ix[s] > ix[j]) {
47
                    if (D[n + 1][j] > eps || D[n + 1][j] > -eps && D[n][j] > eps) {
48
49
                        s = j;
                    }
50
               }
51
52
           if (s < 0) {
53
               break;
54
           }
55
           for(int i = 0; i < n; i++) {
56
                if (D[i][s] < -eps) {</pre>
57
                    if (r < 0 \mid \mid (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -eps
58
                         || d < eps && ix[r + m] > ix[i + m]) {
59
60
61
                        r = i;
                    }
62
               }
63
           }
64
65
           if (r < 0) {
66
                return vector<double> ();
67
           }
68
69
       if (D[n + 1][m] < -eps) {
70
71
           return vector<double> ();
72
       }
```

3.6. 单纯形 29

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Chapter 4

字符串

4.1 后缀数组

```
1 const int MAXN = MAXL * 2 + 1;
| int a[MAXN], x[MAXN], y[MAXN], c[MAXN], sa[MAXN], rank[MAXN], height[MAXN];
3
  void calc_sa(int n) {
       int m = alphabet, k = 1;
4
5
      memset(c, 0, sizeof(*c) * (m + 1));
6
      for (int i = 1; i \le n; ++i) c[x[i] = a[i]]++;
      for (int i = 1; i \le m; ++i) c[i] += c[i - 1];
7
      for (int i = n; i; --i) sa[c[x[i]]--] = i;
8
9
      for (; k <= n; k <<= 1) {
           int tot = k;
10
           for (int i = n - k + 1; i \le n; ++i) y[i - n + k] = i;
11
           for (int i = 1; i <= n; ++i)
12
13
               if (sa[i] > k) y[++tot] = sa[i] - k;
          memset(c, 0, sizeof(*c) * (m + 1));
14
           for (int i = 1; i \le n; ++i) c[x[i]]++;
15
16
           for (int i = 1; i \le m; ++i) c[i] += c[i - 1];
           for (int i = n; i; --i) sa[c[x[y[i]]]--] = y[i];
17
           for (int i = 1; i \le n; ++i) y[i] = x[i];
18
           tot = 1; x[sa[1]] = 1;
19
           for (int i = 2; i <= n; ++i) {
20
               if (max(sa[i], sa[i-1]) + k > n || y[sa[i]] != y[sa[i-1]] || y[sa[i] + k] !=
21
     \rightarrow y[sa[i - 1] + k]) ++tot;
               x[sa[i]] = tot;
23
           if (tot == n) break; else m = tot;
24
25
  }
26
  void calc_height(int n) {
27
      for (int i = 1; i <= n; ++i) rank[sa[i]] = i;</pre>
28
      for (int i = 1; i <= n; ++i) {
29
          height[rank[i]] = max(0, height[rank[i - 1]] - 1);
30
           if (rank[i] == 1) continue;
31
           int j = sa[rank[i] - 1];
32
```

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4.2 后缀自动机

```
1 static const int MAXL = MAXN * 2; // MAXN is original length
2 static const int alphabet = 26; // sometimes need changing
| int 1, last, cnt, trans[MAXL][alphabet], par[MAXL], sum[MAXL], seq[MAXL], mxl[MAXL], size[MAXL];
     _{\hookrightarrow} // mxl is maxlength, size is the size of right
  char str[MAXL];
  inline void init() {
5
6
      l = strlen(str + 1); cnt = last = 1;
      for (int i = 0; i \le 1 * 2; ++i) memset(trans[i], 0, sizeof(trans[i]));
7
      memset(par, 0, sizeof(*par) * (1 * 2 + 1));
8
      memset(mxl, 0, sizeof(*mxl) * (1 * 2 + 1));
9
      memset(size, 0, sizeof(*size) * (1 * 2 + 1));
10
11
  }
12
  inline void extend(int pos, int c) {
       int p = last, np = last = ++cnt;
13
      mxl[np] = mxl[p] + 1; size[np] = 1;
14
      for (; p && !trans[p][c]; p = par[p]) trans[p][c] = np;
15
16
      if (!p) par[np] = 1;
       else {
17
           int q = trans[p][c];
18
           if (mxl[p] + 1 == mxl[q]) par[np] = q;
19
           else {
20
               int nq = ++cnt;
21
22
               mxl[nq] = mxl[p] + 1;
               memcpy(trans[nq], trans[q], sizeof(trans[nq]));
23
               par[nq] = par[q];
24
               par[np] = par[q] = nq;
25
               for (; trans[p][c] == q; p = par[p]) trans[p][c] = nq;
26
27
           }
      }
28
29 }
  inline void buildsam() {
30
      for (int i = 1; i <= 1; ++i) extend(i, str[i] - 'a');</pre>
31
      memset(sum, 0, sizeof(*sum) * (1 * 2 + 1));
32
      for (int i = 1; i <= cnt; ++i) sum[mxl[i]]++;</pre>
33
      for (int i = 1; i <= 1; ++i) sum[i] += sum[i - 1];</pre>
      for (int i = cnt; i; --i) seq[sum[mxl[i]]--] = i;
35
      for (int i = cnt; i; --i) size[par[seq[i]]] += size[seq[i]];
36
37 | }
```

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4.3 EX 后缀自动机

```
inline void add_node(int x, int &last) {
1
2
       int lastnode = last;
       if (c[lastnode][x]) {
3
           int nownode = c[lastnode][x];
4
           if (1[nownode] == 1[lastnode] + 1) last = nownode;
5
6
               int auxnode = ++cnt; l[auxnode] = l[lastnode] + 1;
7
               for (int i = 0; i < alphabet; ++i) c[auxnode][i] = c[nownode][i];</pre>
8
               par[auxnode] = par[nownode]; par[nownode] = auxnode;
9
10
               for (; lastnode && c[lastnode][x] == nownode; lastnode = par[lastnode]) {
                   c[lastnode][x] = auxnode;
11
12
13
               last = auxnode;
           }
14
      } else {
15
           int newnode = ++cnt; l[newnode] = l[lastnode] + 1;
16
           for (; lastnode && !c[lastnode][x]; lastnode = par[lastnode]) c[lastnode][x] = newnode;
17
           if (!lastnode) par[newnode] = 1;
18
           else {
19
               int nownode = c[lastnode][x];
20
               if (l[lastnode] + 1 == l[nownode]) par[newnode] = nownode;
21
               else {
22
                   int auxnode = ++cnt; l[auxnode] = l[lastnode] + 1;
23
                   for (int i = 0; i < alphabet; ++i) c[auxnode][i] = c[nownode][i];</pre>
24
                   par[auxnode] = par[nownode]; par[nownode] = par[newnode] = auxnode;
25
                   for (; lastnode && c[lastnode][x] == nownode; lastnode = par[lastnode]) {
26
                        c[lastnode][x] = auxnode;
                   }
28
               }
30
           last = newnode;
31
      }
32
33 }
```

4.4 后缀树

- 1. 边上的字符区间是左闭右开区间;
- 2. 如果要建立关于多个串的后缀树,请用不同的分隔符,并且对于每个叶子结点,去掉和它父亲的连边上出现的第一个分隔符之后的所有字符;

4.5 回文自动机

```
int nT, nStr, last, c[MAXT][26], fail[MAXT], r[MAXN], l[MAXN], s[MAXN];
int allocate(int len) {
    l[nT] = len;
```

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```
r[nT] = 0;
4
      fail[nT] = 0;
      memset(c[nT], 0, sizeof(c[nT]));
6
      return nT++;
7
8 }
9
  void init() {
10
      nT = nStr = 0;
      int newE = allocate(0);
11
      int new0 = allocate(-1);
12
13
      last = newE;
      fail[newE] = newO;
14
      fail[new0] = newE;
15
      s[0] = -1;
16
17
18 void add(int x) {
      s[++nStr] = x;
19
20
      int now = last;
      while (s[nStr - l[now] - 1] != s[nStr]) now = fail[now];
21
      if (!c[now][x]) {
22
           int newnode = allocate(l[now] + 2), &newfail = fail[newnode];
23
           newfail = fail[now];
           while (s[nStr - l[newfail] - 1] != s[nStr]) newfail = fail[newfail];
25
          newfail = c[newfail][x];
26
          c[now][x] = newnode;
27
      }
28
      last = c[now][x];
29
30
      r[last]++;
31 }
  void count() {
32
      for (int i = nT - 1; i \ge 0; i--) {
33
           r[fail[i]] += r[i];
34
35
36 }
```

Chapter 5

数据结构

5.1 KD-Tree

```
1 long long norm(const long long &x) {
            For manhattan distance
      return std::abs(x);
3
            For euclid distance
4
5
      return x * x;
  }
6
7
  struct Point {
8
9
      int x, y, id;
10
      const int& operator [] (int index) const {
11
           if (index == 0) {
12
13
               return x;
           } else {
14
               return y;
15
           }
16
      }
17
18
      friend long long dist(const Point &a, const Point &b) {
19
           long long result = 0;
20
           for (int i = 0; i < 2; ++i) {
21
               result += norm(a[i] - b[i]);
22
           }
23
24
           return result;
      }
25
  } point[N];
26
27
  struct Rectangle {
28
      int min[2], max[2];
29
30
      Rectangle() {
31
           min[0] = min[1] = INT_MAX; // sometimes int is not enough
32
           max[0] = max[1] = INT_MIN;
33
```

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```
}
34
35
       void add(const Point &p) {
36
           for (int i = 0; i < 2; ++i) {
37
                min[i] = std::min(min[i], p[i]);
38
39
                max[i] = std::max(max[i], p[i]);
40
           }
       }
41
42
       long long dist(const Point &p) {
43
           long long result = 0;
44
           for (int i = 0; i < 2; ++i) {
45
                      For minimum distance
46
                result += norm(std::min(std::max(p[i], min[i]), max[i]) - p[i]);
47
                     For maximum distance
48
                result += std::max(norm(max[i] - p[i]), norm(min[i] - p[i]));
49
           }
50
           return result;
51
       }
52
  };
53
54
55
  struct Node {
       Point seperator;
56
       Rectangle rectangle;
57
       int child[2];
58
59
       void reset(const Point &p) {
60
           seperator = p;
61
62
           rectangle = Rectangle();
           rectangle.add(p);
63
           child[0] = child[1] = 0;
64
65
  } tree[N << 1];</pre>
66
67
  int size, pivot;
68
69
  bool compare(const Point &a, const Point &b) {
70
71
       if (a[pivot] != b[pivot]) {
           return a[pivot] < b[pivot];</pre>
72
73
       return a.id < b.id;</pre>
74
75 | }
76
  // 左閉右開: build(1, n + 1)
77
  int build(int 1, int r, int type = 1) {
78
       pivot = type;
79
       if (1 >= r) {
80
81
           return 0;
82
       }
```

5.1. KD-TREE 37

```
int x = ++size;
83
       int mid = 1 + r >> 1;
       std::nth_element(point + 1, point + mid, point + r, compare);
85
       tree[x].reset(point[mid]);
86
       for (int i = 1; i < r; ++i) {
87
88
            tree[x].rectangle.add(point[i]);
89
       tree[x].child[0] = build(1, mid, type ^ 1);
90
       tree[x].child[1] = build(mid + 1, r, type ^ 1);
91
       return x;
92
93 }
94
   int insert(int x, const Point &p, int type = 1) {
95
96
       pivot = type;
       if (x == 0) {
97
98
            tree[++size].reset(p);
99
            return size;
       }
100
       tree[x].rectangle.add(p);
101
       if (compare(p, tree[x].seperator)) {
102
            tree[x].child[0] = insert(tree[x].child[0], p, type ^ 1);
103
104
           tree[x].child[1] = insert(tree[x].child[1], p, type ^ 1);
105
106
       return x;
107
108 }
109
110 // For minimum distance
   // For maximum: 下面递归 query 时 0, 1 换顺序;< and >;min and max
111
   void query(int x, const Point &p, std::pair<long long, int> &answer, int type = 1) {
112
       pivot = type;
113
       if (x == 0 || tree[x].rectangle.dist(p) > answer.first) {
114
            return;
115
       }
116
       answer = std::min(answer,
117
                 std::make_pair(dist(tree[x].seperator, p), tree[x].seperator.id));
118
119
       if (compare(p, tree[x].seperator)) {
           query(tree[x].child[0], p, answer, type ^ 1);
120
            query(tree[x].child[1], p, answer, type ^ 1);
121
122
            query(tree[x].child[1], p, answer, type ^ 1);
123
            query(tree[x].child[0], p, answer, type ^ 1);
124
       }
125
126
127
   std::priority_queue<std::pair<long long, int> > answer;
128
129
   void query(int x, const Point &p, int k, int type = 1) {
131
       pivot = type;
```

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```
if (x == 0 || (int)answer.size() == k && tree[x].rectangle.dist(p) > answer.top().first) {
132
133
           return;
134
       answer.push(std::make_pair(dist(tree[x].seperator, p), tree[x].seperator.id));
135
       if ((int)answer.size() > k) {
136
137
            answer.pop();
138
       if (compare(p, tree[x].seperator)) {
139
            query(tree[x].child[0], p, k, type ^ 1);
140
            query(tree[x].child[1], p, k, type ^ 1);
141
       } else {
142
            query(tree[x].child[1], p, k, type ^ 1);
143
            query(tree[x].child[0], p, k, type ^ 1);
144
       }
145
146 }
```

5.2 Treap

```
struct Node{
2
       int mn, key, size, tag;
3
       bool rev;
       Node* ch[2];
4
       Node(int mn, int key, int size): mn(mn), key(key), size(size), rev(0), tag(0){}
5
      void downtag();
6
       Node* update(){
7
           mn = min(ch[0] \rightarrow mn, min(key, ch[1] \rightarrow mn));
8
           size = ch[0] -> size + 1 + ch[1] -> size;
9
10
           return this;
11
       }
12 };
13 typedef pair<Node*, Node*> Pair;
14 Node *null, *root;
  void Node::downtag(){
15
       if(rev){
16
           for(int i = 0; i < 2; i++)
17
                if(ch[i] != null){
18
                    ch[i] -> rev ^= 1;
19
                    swap(ch[i] -> ch[0], ch[i] -> ch[1]);
20
21
           rev = 0;
22
       }
23
       if(tag){
24
           for(int i = 0; i < 2; i++)
25
                if(ch[i] != null){
26
                    ch[i] -> key += tag;
27
                    ch[i] -> mn += tag;
28
                    ch[i] -> tag += tag;
29
30
```

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```
tag = 0;
31
       }
33 }
34 int r(){
35
       static int s = 3023192386;
36
       return (s += (s << 3) + 1) & (\sim 0u >> 1);
37
38 bool random(int x, int y){
       return r() \% (x + y) < x;
39
40 }
41 Node* merge(Node *p, Node *q){
       if(p == null) return q;
42
       if(q == null) return p;
43
       p -> downtag();
44
       q -> downtag();
45
46
       if(random(p -> size, q -> size)){
47
            p \rightarrow ch[1] = merge(p \rightarrow ch[1], q);
            return p -> update();
48
       }else{
49
            q \rightarrow ch[0] = merge(p, q \rightarrow ch[0]);
50
51
            return q -> update();
52
53 }
54 Pair split(Node *x, int n){
       if(x == null) return make_pair(null, null);
55
       x -> downtag();
56
57
       if(n \le x \rightarrow ch[0] \rightarrow size){
            Pair ret = split(x \rightarrow ch[0], n);
58
            x \rightarrow ch[0] = ret.second;
59
            return make_pair(ret.first, x -> update());
60
61
       Pair ret = split(x \rightarrow ch[1], n - x \rightarrow ch[0] \rightarrow size - 1);
62
       x \rightarrow ch[1] = ret.first;
63
       return make_pair(x -> update(), ret.second);
64
65 }
66 pair < Node*, Pair > get_segment(int 1, int r){
67
       Pair ret = split(root, l - 1);
68
       return make_pair(ret.first, split(ret.second, r - 1 + 1));
69 }
70 | int main(){
       null = new Node(INF, INF, 0);
71
       null \rightarrow ch[0] = null \rightarrow ch[1] = null;
72
       root = null;
73
74 | }
```

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5.3 Link/cut Tree

```
inline void reverse(int x) {
      tr[x].rev ^= 1; swap(tr[x].c[0], tr[x].c[1]);
2
3 }
  inline void rotate(int x, int k) {
5
      int y = tr[x].fa, z = tr[y].fa;
6
      tr[x].fa = z; tr[z].c[tr[z].c[1] == y] = x;
7
      tr[tr[x].c[k ^ 1]].fa = y; tr[y].c[k] = tr[x].c[k ^ 1];
      tr[x].c[k ^ 1] = y; tr[y].fa = x;
9
10 }
11
  inline void splay(int x, int w) {
12
13
      int z = x; pushdown(x);
      while (tr[x].fa != w) {
14
           int y = tr[x].fa; z = tr[y].fa;
15
           if (z == w) {
16
               pushdown(z = y); pushdown(x);
17
               rotate(x, tr[y].c[1] == x);
18
               update(y); update(x);
19
20
           } else {
               pushdown(z); pushdown(y); pushdown(x);
21
               int t1 = tr[y].c[1] == x, t2 = tr[z].c[1] == y;
22
23
               if (t1 == t2) rotate(y, t2), rotate(x, t1);
               else rotate(x, t1), rotate(x, t2);
24
               update(z); update(y); update(x);
25
           }
26
27
      }
      update(x);
28
      if (x != z) par[x] = par[z], par[z] = 0;
29
30 | }
31
  inline void access(int x) {
32
      for (int y = 0; x; y = x, x = par[x]) {
33
           splay(x, 0);
34
           if (tr[x].c[1]) par[tr[x].c[1]] = x, tr[tr[x].c[1]].fa = 0;
35
           tr[x].c[1] = y; par[y] = 0; tr[y].fa = x; update(x);
36
      }
37
38
  |}
39
  inline void makeroot(int x) {
40
      access(x); splay(x, 0); reverse(x);
41
  }
42
43
44 inline void link(int x, int y) {
      makeroot(x); par[x] = y;
45
46 }
47
```

```
inline void cut(int x, int y) {
    access(x); splay(y, 0);
    if (par[y] != x) swap(x, y), access(x), splay(y, 0);
    par[y] = 0;
}
inline void split(int x, int y) { // x will be the root of the tree
    makeroot(y); access(x); splay(x, 0);
}
```

5.4 树状数组查询第 k 小元素

```
inline void reverse(int x) {
2
      tr[x].rev ^= 1; swap(tr[x].c[0], tr[x].c[1]);
3 }
4
5 inline void rotate(int x, int k) {
      int y = tr[x].fa, z = tr[y].fa;
6
      tr[x].fa = z; tr[z].c[tr[z].c[1] == y] = x;
7
      tr[tr[x].c[k ^ 1]].fa = y; tr[y].c[k] = tr[x].c[k ^ 1];
8
9
      tr[x].c[k ^ 1] = y; tr[y].fa = x;
  }
10
11
12
  inline void splay(int x, int w) {
      int z = x; pushdown(x);
13
      while (tr[x].fa != w) {
14
           int y = tr[x].fa; z = tr[y].fa;
15
16
           if (z == w) {
               pushdown(z = y); pushdown(x);
17
               rotate(x, tr[y].c[1] == x);
18
19
               update(y); update(x);
           } else {
20
               pushdown(z); pushdown(y); pushdown(x);
21
               int t1 = tr[y].c[1] == x, t2 = tr[z].c[1] == y;
22
               if (t1 == t2) rotate(y, t2), rotate(x, t1);
23
               else rotate(x, t1), rotate(x, t2);
24
               update(z); update(y); update(x);
25
           }
26
27
      }
      update(x);
28
      if (x != z) par[x] = par[z], par[z] = 0;
29
  }
30
31
  inline void access(int x) {
32
33
      for (int y = 0; x; y = x, x = par[x]) {
          splay(x, 0);
34
           if (tr[x].c[1]) par[tr[x].c[1]] = x, tr[tr[x].c[1]].fa = 0;
35
          tr[x].c[1] = y; par[y] = 0; tr[y].fa = x; update(x);
36
```

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```
}
37
  }
39
40 inline void makeroot(int x) {
      access(x); splay(x, 0); reverse(x);
41
42
43
44 inline void link(int x, int y) {
      makeroot(x); par[x] = y;
45
46 }
47
  inline void cut(int x, int y) {
48
      access(x); splay(y, 0);
49
      if (par[y] != x) swap(x, y), access(x), splay(y, 0);
50
      par[y] = 0;
51
52 }
53
54 inline void split(int x, int y) { // x will be the root of the tree
      makeroot(y); access(x); splay(x, 0);
55
56 }
```

Chapter 6

图论

6.1 基础

```
struct Graph { // Remember to call .init()!
2
      int e, nxt[M], v[M], adj[N], n;
3
      bool base;
4
       __inline void init(bool _base, int _n = 0) {
           assert(n < N);</pre>
5
           n = _n; base = _base;
6
           e = 0; memset(adj + base, -1, sizeof(*adj) * n);
7
8
       __inline int new_node() {
9
           adj[n + base] = -1;
10
           assert(n + base + 1 < N);
11
           return n++ + base;
12
13
       __inline void ins(int u0, int v0) { // directional
14
           assert(u0 < n + base && v0 < n + base);
15
           v[e] = v0; nxt[e] = adj[u0]; adj[u0] = e++;
16
           assert(e < M);</pre>
17
18
       __inline void bi_ins(int u0, int v0) { // bi-directional
19
           ins(u0, v0); ins(v0, u0);
20
21
22 };
```

6.2 KM

```
bool used[N];
6
       void init() {
7
           for (int i = 1; i <= n; i++) {
8
                match[i] = 0;
9
10
                lx[i] = 0;
11
                ly[i] = 0;
12
                way[i] = 0;
           }
13
       }
14
       void hungary(int x) {
15
           match[0] = x;
16
           int j0 = 0;
17
           for (int j = 0; j \le n; j++) {
18
                slack[j] = INF;
19
                used[j] = false;
20
           }
21
22
23
           do {
                used[j0] = true;
24
                int i0 = match[j0], delta = INF, j1 = 0;
25
                for (int j = 1; j \le n; j++) {
26
27
                    if (used[j] == false) {
                         int cur = -w[i0][j] - lx[i0] - ly[j];
28
                         if (cur < slack[j]) {</pre>
29
30
                             slack[j] = cur;
                             way[j] = j0;
31
                         }
32
                         if (slack[j] < delta) {</pre>
33
                             delta = slack[j];
34
                             j1 = j;
35
                         }
36
                    }
37
                }
38
                for (int j = 0; j \le n; j++) {
39
                    if (used[j]) {
40
                         lx[match[j]] += delta;
41
42
                         ly[j] -= delta;
43
                    else slack[j] -= delta;
44
                }
45
                j0 = j1;
46
           } while (match[j0] != 0);
47
48
49
           do {
                int j1 = way[j0];
50
                match[j0] = match[j1];
51
                j0 = j1;
52
53
           } while (j0);
54
       }
```

6.3. HK 45

```
55
       int get_ans() {
           int sum = 0;
57
           for(int i = 1; i <= n; i++) {
58
               if (w[match[i]][i] == -INF); // 无解
59
60
               if (match[i] > 0) sum += w[match[i]][i];
61
           return sum;
62
      }
63
 } km;
```

6.3 HK

```
int matchx[N], matchy[N], level[N];
  vector<int> edge[N];
2
  bool dfs(int x) {
3
       for (int i = 0; i < (int)edge[x].size(); ++i) {</pre>
           int y = edge[x][i];
5
           int w = matchy[y];
6
           if (w == -1 \mid | level[x] + 1 == level[w] && dfs(w)) {
7
               matchx[x] = y;
8
9
               matchy[y] = x;
               return true;
10
           }
11
       }
12
       level[x] = -1;
13
       return false;
14
  }
15
16
  int solve() {
       memset(matchx, -1, sizeof(*matchx) * n);
17
       memset(matchy, -1, sizeof(*matchy) * m);
18
19
       for (int ans = 0; ; ) {
           std::vector<int> q;
20
           for (int i = 0; i < n; ++i) {
21
                if (matchx[i] == -1) {
22
                    level[i] = 0;
23
                    q.push_back(i);
24
               } else {
25
26
                    level[i] = -1;
27
28
           for (int head = 0; head < (int)q.size(); ++head) {</pre>
29
                int x = q[head];
30
               for (int i = 0; i < (int)edge[x].size(); ++i) {</pre>
31
                    int y = edge[x][i];
32
                    int w = matchy[y];
33
                    if (w != -1 \&\& level[w] < 0) {
34
                        level[w] = level[x] + 1;
35
```

```
q.push_back(w);
36
                     }
37
                }
38
            }
39
40
            int delta = 0;
41
            for (int i = 0; i < n; ++i) {
42
                if (matchx[i] == -1 && dfs(i)) {
                     delta++;
43
44
            }
45
            if (delta == 0) {
46
                return ans;
47
            } else {
48
                ans += delta;
49
50
51
       }
52 }
```

6.4 点双连通分量

bcc.forest is a set of connected tree whose vertices are chequered with cut-vertex and BCC.

```
const bool BCC_VERTEX = 0, BCC_EDGE = 1;
  struct BCC { // N = NO + MO. Remember to call init(&raw_graph).
2
3
      Graph *g, forest; // g is raw graph ptr.
      int dfn[N], DFN, low[N];
      int stack[N], top;
5
      int expand_to[N];
                               // Where edge i is expanded to in expaned graph.
6
7
      // Vertex i expaned to i.
      int compress\_to[N]; // Where vertex i is compressed to.
8
      bool vertex_type[N], cut[N], compress_cut[N], branch[M];
9
10
      //std::vector<int> BCC_component[N]; // Cut vertex belongs to none.
      __inline void init(Graph *raw_graph) {
11
           g = raw_graph;
12
13
      void DFS(int u, int pe) {
14
           dfn[u] = low[u] = ++DFN; cut[u] = false;
15
           if (!~g->adj[u]) {
16
               cut[u] = 1;
17
18
               compress_to[u] = forest.new_node();
               compress_cut[compress_to[u]] = 1;
19
20
           for (int e = g->adj[u]; ~e; e = g->nxt[e]) {
21
               int v = g \rightarrow v[e];
22
               if ((e ^ pe) > 1 && dfn[v] > 0 && dfn[v] < dfn[u]) {
23
                   stack[top++] = e;
24
                   low[u] = std::min(low[u], dfn[v]);
25
26
               else if (!dfn[v]) {
27
```

6.4. 点双连通分量 47

```
stack[top++] = e; branch[e] = 1;
28
29
                    DFS(v, e);
                    low[u] = std::min(low[v], low[u]);
30
                    if (low[v] >= dfn[u]) {
31
32
                        if (!cut[u]) {
33
                            cut[u] = 1;
                            compress_to[u] = forest.new_node();
34
                            compress_cut[compress_to[u]] = 1;
35
                        }
36
                        int cc = forest.new_node();
37
                        forest.bi_ins(compress_to[u], cc);
38
                        compress_cut[cc] = 0;
39
                        //BCC_component[cc].clear();
40
                        do {
41
                            int cur_e = stack[--top];
42
43
                            compress_to[expand_to[cur_e]] = cc;
44
                            compress_to[expand_to[cur_e^1]] = cc;
                            if (branch[cur_e]) {
45
                                 int v = g->v[cur_e];
46
                                 if (cut[v])
47
                                     forest.bi_ins(cc, compress_to[v]);
48
49
                                 else {
                                     //BCC_component[cc].push_back(v);
50
                                     compress_to[v] = cc;
51
                                 }
52
53
                        } while (stack[top] != e);
54
                    }
55
               }
56
           }
57
58
       void solve() {
59
           forest.init(g->base);
60
           int n = g->n;
61
           for (int i = 0; i < g->e; i++) {
62
               expand_to[i] = g->new_node();
63
64
           memset(branch, 0, sizeof(*branch) * g->e);
65
           memset(dfn + g->base, 0, sizeof(*dfn) * n); DFN = 0;
66
           for (int i = 0; i < n; i++)
67
               if (!dfn[i + g->base]) {
68
                    top = 0;
69
                    DFS(i + g->base, -1);
70
               }
71
72
  } bcc;
73
74
  bcc.init(&raw_graph);
76 bcc.solve();
```

77 // Do something with bcc.forest ...

6.5 边双连通分量

```
struct BCC {
       Graph *g, forest;
2
       int dfn[N], low[N], stack[N], tot[N], belong[N], vis[N], top, dfs_clock;
3
       // tot[] is the size of each BCC, belong[] is the BCC that each node belongs to
4
       pair<int, int > ori[M]; // bridge in raw_graph(raw node)
5
6
       bool is_bridge[M];
       __inline void init(Graph *raw_graph) {
7
8
           g = raw_graph;
9
           memset(is_bridge, false, sizeof(*is_bridge) * g -> e);
10
           memset(vis + g -> base, 0, sizeof(*vis) * g -> n);
       }
11
       void tarjan(int u, int from) {
12
           dfn[u] = low[u] = ++dfs\_clock; vis[u] = 1; stack[++top] = u;
13
           for (int p = g -> adj[u]; ~p; p = g -> nxt[p]) {
14
               if ((p ^ 1) == from) continue;
15
               int v = g \rightarrow v[p];
16
17
               if (vis[v]) {
                    if (vis[v] == 1) low[u] = min(low[u], dfn[v]);
18
               } else {
19
20
                    tarjan(v, p);
                    low[u] = min(low[u], low[v]);
21
                    if (low[v] > dfn[u]) is_bridge[p / 2] = true;
22
               }
23
           }
           if (dfn[u] != low[u]) return;
25
           tot[forest.new_node()] = 0;
26
27
           do {
               belong[stack[top]] = forest.n;
28
               vis[stack[top]] = 2;
29
               tot[forest.n]++;
30
               --top;
31
           } while (stack[top + 1] != u);
32
33
       void solve() {
34
35
           forest.init(g -> base);
           int n = g \rightarrow n;
36
           for (int i = 0; i < n; ++i)
37
               if (!vis[i + g -> base]) {
38
                    top = dfs_clock = 0;
39
                    tarjan(i + g \rightarrow base, -1);
40
41
           for (int i = 0; i < g -> e / 2; ++i)
42
               if (is_bridge[i]) {
43
                    int e = forest.e;
44
```

6.6. 最小树形图 49

```
forest.bi_ins(belong[g -> v[i * 2]], belong[g -> v[i * 2 + 1]], g -> w[i * 2]);
ori[e] = make_pair(g -> v[i * 2 + 1], g -> v[i * 2]);
ori[e + 1] = make_pair(g -> v[i * 2], g -> v[i * 2 + 1]);
}
bcc;
```

6.6 最小树形图

```
1 const int MAXN, INF; // INF >= sum( W_ij )
2 int from [MAXN + 10] [MAXN * 2 + 10], n, m, edge [MAXN + 10] [MAXN * 2 + 10];
int sel[MAXN * 2 + 10], fa[MAXN * 2 + 10], vis[MAXN * 2 + 10];
  int getfa(int x){if(x == fa[x]) return x; return fa[x] = getfa(fa[x]);}
  void liuzhu(){ // 1-base: root is 1, answer = (sel[i], i) for i in [2..n]
5
      fa[1] = 1;
6
      for(int i = 2; i \le n; ++i){
7
           sel[i] = 1; fa[i] = i;
8
           for(int j = 1; j <= n; ++j) if(fa[j] != i)
9
               if(from[j][i] = i, edge[sel[i]][i] > edge[j][i]) sel[i] = j;
10
11
12
       int limit = n;
       while(1){
13
           int prelimit = limit; memset(vis, 0, sizeof(vis)); vis[1] = 1;
14
           for(int i = 2; i <= prelimit; ++i) if(fa[i] == i && !vis[i]){</pre>
15
               int j = i; while(!vis[j]) vis[j] = i, j = getfa(sel[j]);
16
               if(j == 1 || vis[j] != i) continue; vector<int> C; int k = j;
17
               do C.push_back(k), k = getfa(sel[k]); while(k != j);
18
19
               ++limit;
               for(int i = 1; i <= n; ++i){
20
                   edge[i][limit] = INF, from[i][limit] = limit;
21
22
               fa[limit] = vis[limit] = limit;
23
               for(int i = 0; i < int(C.size()); ++i){</pre>
24
                   int x = C[i], fa[x] = limit;
25
                   for(int j = 1; j \le n; ++j)
26
                        if(edge[j][x] != INF && edge[j][limit] > edge[j][x] - edge[sel[x]][x]){
27
                            edge[j][limit] = edge[j][x] - edge[sel[x]][x];
28
                            from[j][limit] = x;
29
                        }
30
31
               for(int j=1;j<=n;++j) if(getfa(j)==limit) edge[j][limit] = INF;</pre>
32
               sel[limit] = 1;
33
               for(int j = 1; j \le n; ++j)
34
                   if(edge[sel[limit]][limit] > edge[j][limit]) sel[limit] = j;
35
36
           if(prelimit == limit) break;
37
38
      for(int i = limit; i > 1; --i) sel[from[sel[i]][i]] = sel[i];
39
```

40 | }

6.7 带花树

```
vector<int> link[maxn];
  int n,match[maxn],Queue[maxn],head,tail;
int pred[maxn],base[maxn],start,finish,newbase;
4 | bool InQueue [maxn], InBlossom [maxn];
5 void push(int u){ Queue[tail++]=u; InQueue[u]=true; }
  int pop(){ return Queue[head++]; }
  int FindCommonAncestor(int u,int v){
       bool InPath[maxn];
8
       for(int i=0;i<n;i++) InPath[i]=0;</pre>
9
       while(true){ u=base[u];InPath[u]=true;if(u==start) break;u=pred[match[u]]; }
10
       while(true){ v=base[v];if(InPath[v]) break;v=pred[match[v]]; }
11
       return v;
12
  }
13
  void ResetTrace(int u){
14
       int v;
15
       while(base[u]!=newbase){
16
17
           v=match[u];
           InBlossom[base[u]]=InBlossom[base[v]]=true;
18
           u=pred[v];
19
20
           if(base[u]!=newbase) pred[u]=v;
       }
21
  }
22
  void BlossomContract(int u,int v){
23
       newbase=FindCommonAncestor(u,v);
       for (int i=0;i<n;i++)</pre>
25
       InBlossom[i]=0;
26
       ResetTrace(u);ResetTrace(v);
27
       if(base[u]!=newbase) pred[u]=v;
28
       if(base[v]!=newbase) pred[v]=u;
29
       for(int i=0;i<n;++i)</pre>
30
       if(InBlossom[base[i]]){
31
           base[i]=newbase;
32
           if(!InQueue[i]) push(i);
33
       }
34
35
  }
  bool FindAugmentingPath(int u){
36
       bool found=false;
37
       for(int i=0;i<n;++i) pred[i]=-1,base[i]=i;</pre>
38
       for (int i=0;i<n;i++) InQueue[i]=0;</pre>
39
       start=u;finish=-1; head=tail=0; push(start);
40
       while(head<tail){</pre>
41
           int u=pop();
42
           for(int i=link[u].size()-1;i>=0;i--){
43
               int v=link[u][i];
44
```

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```
if (base[u]!=base[v]&&match[u]!=v)
45
                    if(v==start||(match[v]>=0&&pred[match[v]]>=0))
46
                        BlossomContract(u,v);
47
                    else if(pred[v]==-1){
48
49
                         pred[v]=u;
50
                         if(match[v]>=0) push(match[v]);
                         else{ finish=v; return true; }
51
                    }
52
           }
53
       }
55
       return found;
  |}
56
  void AugmentPath(){
57
       int u=finish,v,w;
58
       while(u>=0){ v=pred[u]; w=match[v]; match[v]=u; match[u]=v; u=w; }
59
60 | }
61
  void FindMaxMatching(){
       for(int i=0;i<n;++i) match[i]=-1;</pre>
62
       for(int i=0;i<n;++i) if(match[i]==-1) if(FindAugmentingPath(i)) AugmentPath();</pre>
63
64 }
```

6.8 带权带花树

```
//maximum weight blossom, change g[u][v].w to INF - g[u][v].w when minimum weight blossom is
     \rightarrow needed
  //type of ans is long long
  //replace all int to long long if weight of edge is long long
5
  struct WeightGraph {
      static const int INF = INT_MAX;
6
7
      static const int MAXN = 400;
      struct edge{
8
9
           int u, v, w;
           edge() {}
10
           edge(int u, int v, int w): u(u), v(v), w(w) {}
11
      };
12
13
      int n, n_x;
      edge g[MAXN * 2 + 1][MAXN * 2 + 1];
14
15
      int lab[MAXN * 2 + 1];
      int match[MAXN * 2 + 1], slack[MAXN * 2 + 1], st[MAXN * 2 + 1], pa[MAXN * 2 + 1];
16
      int flower_from[MAXN * 2 + 1] [MAXN+1], S[MAXN * 2 + 1], vis[MAXN * 2 + 1];
17
      vector<int> flower[MAXN * 2 + 1];
18
      queue<int> q;
19
      inline int e_delta(const edge &e){ // does not work inside blossoms
20
           return lab[e.u] + lab[e.v] - g[e.u][e.v].w * 2;
21
22
      inline void update_slack(int u, int x){
23
           if(!slack[x] || e_delta(g[u][x]) < e_delta(g[slack[x]][x]))</pre>
24
```

```
slack[x] = u;
25
26
       }
       inline void set_slack(int x){
27
           slack[x] = 0;
28
           for(int u = 1; u \le n; ++u)
29
30
                if(g[u][x].w > 0 \&\& st[u] != x \&\& S[st[u]] == 0)
                    update_slack(u, x);
31
       }
32
       void q_push(int x){
33
           if(x \le n)q.push(x);
34
           else for(size_t i = 0;i < flower[x].size(); i++)</pre>
35
               q_push(flower[x][i]);
36
37
       inline void set_st(int x, int b){
38
           st[x]=b;
39
40
           if(x > n) for(size_t i = 0;i < flower[x].size(); ++i)</pre>
41
                        set_st(flower[x][i], b);
42
       inline int get_pr(int b, int xr){
43
           int pr = find(flower[b].begin(), flower[b].end(), xr) - flower[b].begin();
44
           if(pr % 2 == 1){
45
               reverse(flower[b].begin() + 1, flower[b].end());
46
               return (int)flower[b].size() - pr;
47
           } else return pr;
48
       }
49
       inline void set_match(int u, int v){
50
           match[u]=g[u][v].v;
51
           if(u > n){
52
               edge e=g[u][v];
53
               int xr = flower_from[u][e.u], pr=get_pr(u, xr);
54
               for(int i = 0; i < pr; ++i)
55
                    set_match(flower[u][i], flower[u][i ^ 1]);
56
               set_match(xr, v);
57
               rotate(flower[u].begin(), flower[u].begin()+pr, flower[u].end());
58
           }
59
       }
60
61
       inline void augment(int u, int v){
           for(; ; ){
62
               int xnv=st[match[u]];
63
               set_match(u, v);
64
               if(!xnv)return;
65
               set_match(xnv, st[pa[xnv]]);
66
               u=st[pa[xnv]], v=xnv;
67
68
       }
69
       inline int get_lca(int u, int v){
70
           static int t=0;
71
72
           for(++t; u || v; swap(u, v)){
73
               if(u == 0)continue;
```

6.8. 带权带花树 53

```
if(vis[u] == t)return u;
74
                vis[u] = t;
75
                u = st[match[u]];
76
                if(u) u = st[pa[u]];
77
            }
78
79
            return 0;
80
       inline void add_blossom(int u, int lca, int v){
81
            int b = n + 1;
82
            while(b \leq n_x && st[b]) ++b;
83
            if(b > n_x) ++n_x;
84
            lab[b] = 0, S[b] = 0;
85
            match[b] = match[lca];
86
            flower[b].clear();
87
            flower[b].push_back(lca);
88
89
            for(int x = u, y; x != lca; x = st[pa[y]]) {
90
                flower[b].push_back(x),
                flower[b].push_back(y = st[match[x]]),
91
                q_push(y);
92
            }
93
            reverse(flower[b].begin() + 1, flower[b].end());
            for(int x = v, y; x != lca; x = st[pa[y]]) {
95
                flower[b].push_back(x),
96
                flower[b].push_back(y = st[match[x]]),
97
                q_push(y);
98
            }
99
            set_st(b, b);
100
            for(int x = 1; x \le n_x; ++x) g[b][x].w = g[x][b].w = 0;
101
            for(int x = 1; x \le n; ++x) flower_from[b][x] = 0;
102
            for(size_t i = 0 ; i < flower[b].size(); ++i){</pre>
103
                int xs = flower[b][i];
104
105
                for(int x = 1; x \le n_x; ++x)
                     if(g[b][x].w == 0 \mid\mid e_{delta}(g[xs][x]) < e_{delta}(g[b][x]))
106
                         g[b][x] = g[xs][x], g[x][b] = g[x][xs];
107
                for(int x = 1; x \le n; ++x)
108
                     if(flower_from[xs][x]) flower_from[b][x] = xs;
109
110
            set_slack(b);
111
       }
112
       inline void expand_blossom(int b){ // S[b] == 1
113
            for(size t i = 0; i < flower[b].size(); ++i)</pre>
114
                set_st(flower[b][i], flower[b][i]);
115
            int xr = flower_from[b][g[b][pa[b]].u], pr = get_pr(b, xr);
116
            for(int i = 0; i < pr; i += 2){
117
                int xs = flower[b][i], xns = flower[b][i + 1];
118
                pa[xs] = g[xns][xs].u;
119
                S[xs] = 1, S[xns] = 0;
120
121
                slack[xs] = 0, set_slack(xns);
122
                q_push(xns);
```

```
123
124
            S[xr] = 1, pa[xr] = pa[b];
            for(size_t i = pr + 1;i < flower[b].size(); ++i){</pre>
125
                int xs = flower[b][i];
126
127
                S[xs] = -1, set_slack(xs);
128
            }
            st[b] = 0;
129
       }
130
       inline bool on_found_edge(const edge &e){
131
            int u = st[e.u], v = st[e.v];
132
            if(S[v] == -1){
133
                pa[v] = e.u, S[v] = 1;
134
                int nu = st[match[v]];
135
                slack[v] = slack[nu] = 0;
136
                S[nu] = 0, q_push(nu);
137
138
            else if(S[v] == 0){
139
                int lca = get_lca(u, v);
                if(!lca) return augment(u, v), augment(v, u), true;
140
                else add_blossom(u, lca, v);
141
            }
142
143
            return false;
       }
144
       inline bool matching(){
145
            memset(S + 1, -1, sizeof(int) * n_x);
146
            memset(slack + 1, 0, sizeof(int) * n_x);
147
            q = queue<int>();
148
149
            for(int x = 1; x \le n_x; ++x)
                if(st[x] == x && !match[x]) pa[x]=0, S[x]=0, q_push(x);
150
            if(q.empty())return false;
151
            for(;;){
152
                while(q.size()){
153
154
                     int u = q.front();q.pop();
                     if(S[st[u]] == 1)continue;
155
                     for(int v = 1; v \le n; ++v)
156
                         if(g[u][v].w > 0 && st[u] != st[v]){
157
                             if(e_delta(g[u][v]) == 0){
158
159
                                  if(on_found_edge(g[u][v]))return true;
                             }else update_slack(u, st[v]);
160
                         }
161
                }
162
                int d = INF;
163
                for(int b = n + 1; b \le n_x; ++b)
164
                     if(st[b] == b \&\& S[b] == 1)d = min(d, lab[b]/2);
165
                for(int x = 1; x \le n_x; ++x)
                     if(st[x] == x && slack[x]){
167
                         if(S[x] == -1)d = min(d, e_delta(g[slack[x]][x]));
168
                         else if(S[x] == 0)d = min(d, e_delta(g[slack[x]][x])/2);
169
170
171
                for(int u = 1; u \le n; ++u){
```

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```
if(S[st[u]] == 0){
172
                         if(lab[u] <= d)return 0;</pre>
173
                         lab[u] -= d;
174
                     }else if(S[st[u]] == 1)lab[u] += d;
175
                }
176
177
                for(int b = n+1; b \le n_x; ++b)
                     if(st[b] == b){
178
                         if(S[st[b]] == 0) lab[b] += d * 2;
179
                         else if(S[st[b]] == 1) lab[b] -= d * 2;
180
                     }
181
                q=queue<int>();
182
                for(int x = 1; x \le n_x; ++x)
183
                     if(st[x] == x && slack[x] && st[slack[x]] != x && e_delta(g[slack[x]][x]) == 0)
184
                         if(on_found_edge(g[slack[x]][x]))return true;
185
                for(int b = n + 1; b \le n_x; ++b)
186
                     if(st[b] == b && S[b] == 1 && lab[b] == 0)expand_blossom(b);
187
188
            }
            return false;
189
       }
190
        inline pair<long long, int> solve(){
191
            memset(match + 1, 0, sizeof(int) * n);
192
            n_x = n;
193
            int n_matches = 0;
194
            long long tot_weight = 0;
195
            for(int u = 0; u \le n; ++u) st[u] = u, flower[u].clear();
196
            int w_max = 0;
197
            for(int u = 1; u <= n; ++u)
198
                for(int v = 1; v \le n; ++v){
199
                     flower_from[u][v] = (u == v ? u : 0);
200
                     w_{max} = max(w_{max}, g[u][v].w);
201
202
203
            for(int u = 1; u <= n; ++u) lab[u] = w_max;</pre>
            while(matching()) ++n_matches;
            for(int u = 1; u \le n; ++u)
205
                 if(match[u] && match[u] < u)</pre>
206
                     tot_weight += g[u][match[u]].w;
207
208
            return make_pair(tot_weight, n_matches);
       }
209
       inline void init(){
210
            for(int u = 1; u \le n; ++u)
211
                for(int v = 1; v \le n; ++v)
212
                     g[u][v]=edge(u, v, 0);
213
       }
214
215 | };
```

6.9 Dominator Tree

```
vector<int> prec[N], succ[N];
2 vector<int> ord;
3 int stamp, vis[N];
4 int num[N];
5 int fa[N];
6 void dfs(int u) {
       vis[u] = stamp;
7
8
       num[u] = ord.size();
       ord.push_back(u);
9
       for (int i = 0; i < (int)succ[u].size(); ++i) {</pre>
10
           int v = succ[u][i];
11
12
           if (vis[v] != stamp) {
13
               fa[v] = u;
               dfs(v);
14
           }
15
       }
16
  }
17
  int fs[N], mins[N], dom[N], sem[N];
18
  int find(int u) {
19
20
       if (u != fs[u]) {
           int v = fs[u];
21
           fs[u] = find(fs[u]);
22
           if (mins[v] != -1 \&\& num[sem[mins[v]]] < num[sem[mins[u]]]) {
23
               mins[u] = mins[v];
24
           }
25
       }
26
27
       return fs[u];
28 }
void merge(int u, int v) { fs[u] = v; }
30 vector<int> buf[N];
31 | int buf2[N];
32 void mark(int source) {
       ord.clear();
33
       ++stamp;
34
       dfs(source);
35
       for (int i = 0; i < (int)ord.size(); ++i) {</pre>
36
           int u = ord[i];
37
           fs[u] = u, mins[u] = -1, buf2[u] = -1;
38
39
       for (int i = (int)ord.size() - 1; i > 0; --i) {
40
           int u = ord[i], p = fa[u];
41
           sem[u] = p;
42
           for (int j = 0; j < (int)prec[u].size(); ++j) {</pre>
43
               int v = prec[u][j];
44
               if (use[v] != stamp) continue;
45
               if (num[v] > num[u]) {
46
                    find(v); v = sem[mins[v]];
47
```

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```
48
                if (num[v] < num[sem[u]]) {</pre>
49
                     sem[u] = v;
50
                }
51
            }
52
53
            buf[sem[u]].push_back(u);
            mins[u] = u;
54
            merge(u, p);
55
            while (buf[p].size()) {
56
                int v = buf[p].back();
57
                buf[p].pop_back();
58
                find(v);
59
                if (sem[v] == sem[mins[v]]) {
60
                     dom[v] = sem[v];
61
                } else {
62
                     buf2[v] = mins[v];
63
64
            }
65
       }
66
       dom[ord[0]] = ord[0];
67
       for (int i = 0; i < (int)ord.size(); ++i) {</pre>
68
69
            int u = ord[i];
            if (~buf2[u]) {
70
                dom[u] = dom[buf2[u]];
71
72
            }
       }
73
74
  |}
```

6.10 树 hash

```
const unsigned long long MAGIC = 4423;
2
3 unsigned long long magic[N];
  std::pair<unsigned long long, int> hash[N];
5
  void solve(int root) {
6
       magic[0] = 1;
7
       for (int i = 1; i \le n; ++i) {
8
9
           magic[i] = magic[i - 1] * MAGIC;
       }
10
       std::vector<int> queue;
11
       queue.push_back(root);
12
       for (int head = 0; head < (int)queue.size(); ++head) {</pre>
13
           int x = queue[head];
14
           for (int i = 0; i < (int)son[x].size(); ++i) {</pre>
15
               int y = son[x][i];
16
17
               queue.push_back(y);
18
```

```
}
19
       for (int index = n - 1; index >= 0; --index) {
           int x = queue[index];
21
           hash[x] = std::make_pair(0, 0);
22
23
24
           std::vector<std::pair<unsigned long long, int> > value;
           for (int i = 0; i < (int)son[x].size(); ++i) {</pre>
25
               int y = son[x][i];
26
               value.push_back(hash[y]);
27
           }
28
           std::sort(value.begin(), value.end());
29
30
           hash[x].first = hash[x].first * magic[1] + 37;
31
           hash[x].second++;
32
           for (int i = 0; i < (int)value.size(); ++i) {</pre>
33
34
               hash[x].first = hash[x].first * magic[value[i].second] + value[i].first;
35
               hash[x].second += value[i].second;
           }
36
           hash[x].first = hash[x].first * magic[1] + 41;
37
           hash[x].second++;
38
       }
39
40
  }
```

6.11 无向图最小割

```
int cost[maxn] [maxn], seq[maxn], len[maxn], n, m, pop, ans;
  bool used[maxn];
2
  void Init(){
3
       int i,j,a,b,c;
4
       for(i=0;i<n;i++) for(j=0;j<n;j++) cost[i][j]=0;</pre>
5
6
       for(i=0;i<m;i++){</pre>
7
           scanf("%d %d %d",&a,&b,&c); cost[a][b]+=c; cost[b][a]+=c;
8
9
       pop=n; for(i=0;i<n;i++) seq[i]=i;
  }
10
  void Work(){
11
       ans=inf; int i,j,k,l,mm,sum,pk;
12
       while(pop > 1){
13
14
           for(i=1;i<pop;i++) used[seq[i]]=0; used[seq[0]]=1;</pre>
           for(i=1;i<pop;i++) len[seq[i]]=cost[seq[0]][seq[i]];</pre>
15
           pk=0; mm=-inf; k=-1;
16
           for(i=1;i<pop;i++) if(len[seq[i]] > mm){ mm=len[seq[i]]; k=i; }
17
18
           for(i=1;i<pop;i++){</pre>
                used[seq[l=k]]=1;
19
                if(i==pop-2) pk=k;
20
                if(i==pop-1) break;
21
22
                mm = -inf;
                for(j=1;j<pop;j++) if(!used[seq[j]])</pre>
23
```

6.12. ISAP 最大流 59

```
if((len[seq[j]]+=cost[seq[l]][seq[j]]) > mm)
24
25
                         mm=len[seq[j]], k=j;
           }
26
           sum=0;
28
           for(i=0;i<pop;i++) if(i != k) sum+=cost[seq[k]][seq[i]];</pre>
29
           ans=min(ans,sum);
30
           for(i=0;i<pop;i++)</pre>
                cost[seq[k]][seq[i]]=cost[seq[i]][seq[k]]+=cost[seq[pk]][seq[i]];
31
           seq[pk]=seq[--pop];
32
       }
33
       printf("%d\n",ans);
34
  }
35
```

6.12 ISAP 最大流

```
const unsigned long long MAGIC = 4423;
2
3 unsigned long long magic[N];
  std::pair<unsigned long long, int> hash[N];
6
  void solve(int root) {
       magic[0] = 1;
7
       for (int i = 1; i <= n; ++i) {
8
9
           magic[i] = magic[i - 1] * MAGIC;
       }
10
       std::vector<int> queue;
11
       queue.push_back(root);
12
       for (int head = 0; head < (int)queue.size(); ++head) {</pre>
13
           int x = queue[head];
14
           for (int i = 0; i < (int)son[x].size(); ++i) {</pre>
15
               int y = son[x][i];
16
               queue.push_back(y);
17
           }
18
       }
19
       for (int index = n - 1; index >= 0; --index) {
20
           int x = queue[index];
21
           hash[x] = std::make_pair(0, 0);
22
23
24
           std::vector<std::pair<unsigned long long, int> > value;
           for (int i = 0; i < (int)son[x].size(); ++i) {</pre>
25
               int y = son[x][i];
26
               value.push_back(hash[y]);
27
           }
28
           std::sort(value.begin(), value.end());
29
30
           hash[x].first = hash[x].first * magic[1] + 37;
31
           hash[x].second++;
32
           for (int i = 0; i < (int)value.size(); ++i) {</pre>
33
```

```
hash[x].first = hash[x].first * magic[value[i].second] + value[i].first;
hash[x].second += value[i].second;
}
hash[x].first = hash[x].first * magic[1] + 41;
hash[x].second++;
}
hash[x].second++;
}
```

6.13 重口味费用流

```
int S, T, totFlow, totCost;
2
  int dis[N], slack[N], visit[N];
3
4
5 int modlable () {
      int delta = INF;
6
7
      for (int i = 1; i <= T; i++) {
           if (!visit[i] && slack[i] < delta) delta = slack[i];</pre>
8
           slack[i] = INF;
9
10
11
      if (delta == INF) return 1;
      for (int i = 1; i <= T; i++)
12
           if (visit[i]) dis[i] += delta;
13
14
      return 0;
15 }
16
  int dfs (int x, int flow) {
17
       if (x == T) {
18
           totFlow += flow;
19
           totCost += flow * (dis[S] - dis[T]);
20
21
           return flow;
      }
22
      visit[x] = 1;
23
      int left = flow;
24
      for (int i = e.last[x]; ~i; i = e.succ[i])
25
           if (e.cap[i] > 0 && !visit[e.other[i]]) {
26
               int y = e.other[i];
               if (dis[y] + e.cost[i] == dis[x]) {
28
29
                   int delta = dfs (y, min (left, e.cap[i]));
                   e.cap[i] -= delta;
30
                   e.cap[i ^ 1] += delta;
31
                   left -= delta;
32
                   if (!left) { visit[x] = 0; return flow; }
33
34
                    slack[y] = min (slack[y], dis[y] + e.cost[i] - dis[x]);
35
36
37
           }
      return flow - left;
38
```

6.14. 2-SAT 61

```
39 }
40
  pair <int, int> minCost () {
41
       totFlow = 0; totCost = 0;
42
       fill (dis + 1, dis + T + 1, 0);
43
44
45
           do {
               fill (visit + 1, visit + T + 1, 0);
46
           } while (dfs (S, INF));
47
       } while (!modlable ());
48
       return make_pair (totFlow, totCost);
49
50 | }
```

6.14 2-SAT

```
int S, T, totFlow, totCost;
3 int dis[N], slack[N], visit[N];
  int modlable () {
5
6
      int delta = INF;
      for (int i = 1; i <= T; i++) {</pre>
7
           if (!visit[i] && slack[i] < delta) delta = slack[i];</pre>
8
9
           slack[i] = INF;
      }
10
      if (delta == INF) return 1;
11
      for (int i = 1; i <= T; i++)
12
           if (visit[i]) dis[i] += delta;
13
      return 0;
14
15 }
16
17
  int dfs (int x, int flow) {
       if (x == T) {
18
           totFlow += flow;
19
           totCost += flow * (dis[S] - dis[T]);
20
           return flow;
21
22
      visit[x] = 1;
23
24
      int left = flow;
      for (int i = e.last[x]; ~i; i = e.succ[i])
25
           if (e.cap[i] > 0 && !visit[e.other[i]]) {
26
               int y = e.other[i];
27
               if (dis[y] + e.cost[i] == dis[x]) {
28
                    int delta = dfs (y, min (left, e.cap[i]));
29
                   e.cap[i] -= delta;
30
                   e.cap[i ^ 1] += delta;
31
                   left -= delta;
32
                   if (!left) { visit[x] = 0; return flow; }
33
```

```
} else {
34
                    slack[y] = min (slack[y], dis[y] + e.cost[i] - dis[x]);
36
           }
37
38
      return flow - left;
39
40
  pair <int, int> minCost () {
41
      totFlow = 0; totCost = 0;
42
43
      fill (dis + 1, dis + T + 1, 0);
      do {
44
           do {
45
               fill (visit + 1, visit + T + 1, 0);
46
           } while (dfs (S, INF));
47
      } while (!modlable ());
48
49
      return make_pair (totFlow, totCost);
50 }
```

6.15 欧拉遍历

```
1 //从一个奇度点 dfs, sqn 即为回路/路径
2 //first 存点, second 存边的编号, 正反边编号一致
  |//清空 cur、used 数组
4
  void getCycle(int u)
5
  {
      for(int &i=cur[u]; i < (int)adj[u].size(); ++ i){</pre>
6
7
          int id = adj[u][i].second;
8
          if (used[id]) continue;
          used[id] = true;
9
          getCycle(adj[u][i].first);
10
      }
11
12
      sqn.push_back(u);
13 }
```

6.16 最大团搜索

```
1 /*
  |Int g[][] 为图的邻接矩阵。
2
      MC(V) 表示点集 V 的最大团
3
      令 Si={vi, vi+1, ..., vn}, mc[i] 表示 MC(Si)
4
      倒着算 mc[i], 那么显然 MC(V)=mc[1]
5
      此外有 mc[i]=mc[i+1] or mc[i]=mc[i+1]+1
6
7
  */
  void init(){
8
9
      int i, j;
      for (i=1; i<=n; ++i) for (j=1; j<=n; ++j) scanf("%d", &g[i][j]);
10
11 }
```

6.17. 线性规划 63

```
12 void dfs(int size){
13
       int i, j, k;
       if (len[size] == 0) {
14
            if (size>ans) {
15
                ans=size; found=true;
16
17
           }
18
           return;
       }
19
       for (k=0; k<len[size] && !found; ++k) {</pre>
20
            if (size+len[size]-k<=ans) break;</pre>
21
            i=list[size][k];
22
            if (size+mc[i]<=ans) break;</pre>
23
            for (j=k+1, len[size+1]=0; j<len[size]; ++j)</pre>
24
            if (g[i][list[size][j]]) list[size+1][len[size+1]++]=list[size][j];
25
            dfs(size+1);
26
       }
27
28
  }
  void work(){
29
       int i, j;
30
       mc[n]=ans=1;
31
       for (i=n-1; i; --i) {
32
33
           found=false;
           len[1]=0;
34
           for (j=i+1; j<=n; ++j) if (g[i][j]) list[1][len[1]++]=j;
35
            dfs(1);
36
           mc[i]=ans;
37
       }
38
  }
39
  void print(){
40
       printf("%d\n", ans);
41
42 }
```

6.17 线性规划

```
void sieve(){
       f[1]=mu[1]=phi[1]=1;
2
       for(int i=2;i<maxn;i++){</pre>
3
            if(!minp[i]){
4
5
                minp[i]=i;
                minpw[i]=i;
6
                mu[i]=-1;
7
                phi[i]=i-1;
8
                f[i]=i-1;
9
                p[++p[0]]=i;//Case 1 prime
10
11
           for(int j=1;j<=p[0]&&(LL)i*p[j]<maxn;j++){</pre>
12
13
                minp[i*p[j]]=p[j];
                if(i\%p[j]==0){
14
```

```
//Case 2 not coprime
15
                    minpw[i*p[j]]=minpw[i]*p[j];
16
                    phi[i*p[j]]=phi[i]*p[j];
17
                    mu[i*p[j]]=0;
18
                    if(i==minpw[i]){
19
                        f[i*p[j]]=i*p[j]-i;//Special Case for <math>f(p^k)
20
21
                    }else{
                        f[i*p[j]]=f[i/minpw[i]]*f[minpw[i]*p[j]];
22
                    }
23
                    break;
24
                }else{
25
                    //Case 3 coprime
26
                    minpw[i*p[j]]=p[j];
27
                    f[i*p[j]]=f[i]*f[p[j]];
28
                    phi[i*p[j]]=phi[i]*(p[j]-1);
29
                    mu[i*p[j]]=-mu[i];
30
31
                }
32
           }
       }
33
34 | }
```

Chapter 7

其他

7.1 Dancing Links

```
1 struct Node {
2
       Node *1, *r, *u, *d, *col;
       int size, line_no;
3
       Node() {
           size = 0; line_no = -1;
5
6
           l = r = u = d = col = NULL;
7
  } *root;
8
9
  void cover(Node *c) {
10
      c->l->r = c->r; c->r->l = c->l;
11
       for (Node *u = c->d; u != c; u = u->d)
12
           for (Node *v = u->r; v != u; v = v->r) {
13
                v->d->u = v->u;
14
                v->u->d = v->d;
15
16
                -- v->col->size;
           }
17
18 }
19
  void uncover(Node *c) {
20
       for (Node *u = c->u; u != c; u = u->u) {
21
           for (Node *v = u->1; v != u; v = v->1) {
22
                ++ v->col->size;
23
24
                v->u->d = v;
                v \rightarrow d \rightarrow u = v;
25
26
       }
27
       c->l->r = c; c->r->l = c;
28
29
30
31 std::vector<int> answer;
32 bool search(int k) {
      if (root->r == root) return true;
```

66 CHAPTER 7. 其他

```
Node *r = NULL;
34
       for (Node *u = root->r; u != root; u = u->r)
           if (r == NULL || u->size < r->size)
36
               r = u;
37
       if (r == NULL || r->size == 0) return false;
38
39
       else {
40
           cover(r);
           bool succ = false;
41
           for (Node *u = r->d; u != r && !succ; u = u->d) {
42
               answer.push_back(u->line_no);
43
               for (Node *v = u->r; v != u; v = v->r) // Cover row
44
                    cover(v->col);
45
               succ \mid = search(k + 1);
46
               for (Node *v = u \rightarrow 1; v != u; v = v \rightarrow 1)
47
                    uncover(v->col);
48
               if (!succ) answer.pop_back();
49
50
           }
           uncover(r);
51
           return succ;
52
       }
53
  }
54
55
56 bool entry[CR][CC];
Node *who[CR][CC];
58 int cr, cc;
59
60
  void construct() {
       root = new Node();
61
62
       Node *last = root;
       for (int i = 0; i < cc; ++ i) {
63
           Node *u = new Node();
64
65
           last->r = u; u->l = last;
           Node *v = u; u->line_no = i;
66
           last = u;
67
           for (int j = 0; j < cr; ++ j)
68
               if (entry[j][i]) {
69
70
                    ++ u->size;
71
                    Node *cur = new Node();
                    who[j][i] = cur;
72
73
                    cur->line_no = j;
                    cur->col = u;
74
                    cur->u = v; v->d = cur;
75
                    v = cur;
76
77
           v->d = u; u->u = v;
78
79
80
       last->r = root; root->l = last;
81
       for (int j = 0; j < cr; ++ j) {
82
           Node *last = NULL;
```

```
for (int i = cc - 1; i \ge 0; -- i)
83
                if (entry[j][i]) {
                     last = who[j][i];
85
                     break;
86
                }
87
88
            for (int i = 0; i < cc; ++ i)
89
                if (entry[j][i]) {
                     last->r = who[j][i];
90
                     who[j][i]->1 = last;
91
92
                     last = who[j][i];
                }
93
       }
94
   }
95
96
   void destruct() {
97
       for (Node *u = root->r; u != root; ) {
98
99
            for (Node *v = u->d; v != u; ) {
                Node *nxt = v->d;
100
                delete(v);
101
                v = nxt;
102
            }
103
104
            Node *nxt = u->r;
            delete(u); u = nxt;
105
       }
106
107
       delete root;
108 }
```

7.2 Dancing Links 可重覆盖

```
1 struct Node {
2
      Node *1, *r, *u, *d, *col;
3
      int size, line_no;
      Node() {
           size = 0; line_no = -1;
5
           l = r = u = d = col = NULL;
6
7
8
  } *root;
9
10
  void cover(Node *c) {
      c->l->r = c->r; c->r->l = c->l;
11
      for (Node *u = c->d; u != c; u = u->d)
12
           for (Node *v = u->r; v != u; v = v->r) {
13
               v->d->u = v->u;
14
               v->u->d = v->d;
15
               -- v->col->size;
16
           }
17
18 }
19
```

68 CHAPTER 7. 其他

```
20 void uncover(Node *c) {
       for (Node *u = c->u; u != c; u = u->u) {
            for (Node *v = u -> 1; v != u; v = v -> 1) {
22
                 ++ v->col->size;
23
24
                 v \rightarrow u \rightarrow d = v;
25
                 v \rightarrow d \rightarrow u = v;
            }
26
       }
27
       c \rightarrow 1 \rightarrow r = c; c \rightarrow r \rightarrow 1 = c;
28
  |}
29
30
  std::vector<int> answer;
31
   bool search(int k) {
32
       if (root->r == root) return true;
33
       Node *r = NULL;
34
       for (Node *u = root->r; u != root; u = u->r)
35
36
            if (r == NULL \mid | u \rightarrow size < r \rightarrow size)
                 r = u;
37
       if (r == NULL || r->size == 0) return false;
38
       else {
39
40
            cover(r);
41
            bool succ = false;
            for (Node *u = r->d; u != r && !succ; u = u->d) {
42
                 answer.push_back(u->line_no);
43
                 for (Node v = u-r; v != u; v = v-r) // Cover row
                      cover(v->col);
45
                 succ \mid = search(k + 1);
46
                 for (Node *v = u->1; v != u; v = v->1)
47
                      uncover(v->col);
48
                 if (!succ) answer.pop_back();
49
            }
50
51
            uncover(r);
            return succ;
52
       }
53
  |}
54
55
56
  |bool entry[CR][CC];
Node *who[CR][CC];
58 int cr, cc;
59
   void construct() {
60
       root = new Node();
61
       Node *last = root;
62
       for (int i = 0; i < cc; ++ i) {
63
            Node *u = new Node();
64
            last->r = u; u->l = last;
65
            Node *v = u; u->line_no = i;
66
67
            last = u;
68
            for (int j = 0; j < cr; ++ j)
```

7.3. 蔡勒公式 69

```
if (entry[j][i]) {
69
70
                     ++ u->size;
                     Node *cur = new Node();
71
                     who[j][i] = cur;
73
                     cur->line_no = j;
74
                     cur->col = u;
75
                     cur->u = v; v->d = cur;
                     v = cur;
76
                }
77
            v->d = u; u->u = v;
78
79
       last->r = root; root->l = last;
80
       for (int j = 0; j < cr; ++ j) {
81
            Node *last = NULL;
82
            for (int i = cc - 1; i >= 0; -- i)
83
84
                if (entry[j][i]) {
85
                     last = who[j][i];
                     break;
86
                }
87
            for (int i = 0; i < cc; ++ i)
88
                if (entry[j][i]) {
89
90
                     last->r = who[j][i];
                     who[j][i]->l = last;
91
                     last = who[j][i];
92
                }
93
       }
94
   }
95
96
97
   void destruct() {
       for (Node *u = root->r; u != root; ) {
98
            for (Node *v = u->d; v != u; ) {
99
100
                Node *nxt = v->d;
                delete(v);
101
                v = nxt;
102
            }
103
            Node *nxt = u->r;
104
105
            delete(u); u = nxt;
106
       delete root;
107
108 }
```

7.3 蔡勒公式

0 for Sunday. Day and month is 1-based.

```
int zeller(int y,int m,int d) {
   if (m<=2) y--,m+=12; int c=y/100; y%=100;
   int w=((c>>2)-(c<<1)+y+(y>>2)+(13*(m+1)/5)+d-1)%7;
```

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```
4   if (w<0) w+=7; return(w);
5 }</pre>
```

7.4 蔡勒公式 new

0 for Sunday. Day and month is 1-based.

```
int zeller(int y,int m,int d)
  {
2
       if (m<=2)</pre>
3
                     y--,m+=12;
4
       int c=y/100;
5
       y%=100;
       int w;
6
       if (y<1582 \mid | (y==1582 \&\& (m<10 \mid | (m==10 \&\& d<=4))))
7
           w=((c/4)-2*c+y+(y/4)+(13*(m+1)/5)+d-1)\%7;
8
9
           w=y+(y/4)+(c/4)-2*c+(13*(m+1)/5)+d+2;
10
11
       retur w;
12 }
```

Chapter 8

技巧

8.1 真正的释放 STL 容器内存空间

```
template <typename T>
__inline void clear(T& container) {
    container.clear(); // 或者删除了一堆元素
    T(container).swap(container);
}
```

8.2 无敌的大整数相乘取模

Time complexity O(1).

```
// 需要保证 x 和 y 非负
long long mult(long long x, long long y, long long MODN) {
   long long t = (x * y - (long long)((long double)x / MODN * y + 1e-3) * MODN) % MODN;
   return t < 0 ? t + MODN : t;
}
```

8.3 无敌的读入优化

```
|// getchar() 读入优化 << 关同步        cin << 此优化
  |// 用 isdigit() 会小幅变慢
3 // 返回 false 表示读到文件尾
 namespace Reader {
      const int L = (1 << 15) + 5;
5
      char buffer[L], *S, *T;
6
      __inline bool getchar(char &ch) {
7
          if (S == T) {
8
              T = (S = buffer) + fread(buffer, 1, L, stdin);
9
              if (S == T) {
10
                  ch = EOF;
11
12
                  return false;
13
```

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```
}
14
           ch = *S++;
15
           return true;
16
       }
17
       __inline bool getint(int &x) {
18
19
           char ch; bool neg = 0;
20
           for (; getchar(ch) && (ch < '0' || ch > '9'); ) neg \hat{} ch == '-';
           if (ch == EOF) return false;
21
           x = ch - '0';
22
           for (; getchar(ch), ch >= '0' && ch <= '9'; )</pre>
23
               x = x * 10 + ch - '0';
24
           if (neg) x = -x;
25
           return true;
26
       }
27
28 }
```

8.4 梅森旋转算法

High quality pseudorandom number generator, twice as efficient as rand() with -02. C++11 required.

```
#include <random>
int main() {
    std::mt19937 g(seed); // std::mt19937_64
    std::cout << g() << std::endl;
}</pre>
```

Chapter 9

提示

9.1 控制 cout 输出实数精度

```
std::cout << std::fixed << std::setprecision(5);
```

9.2 vimrc

```
set nu
set sw=4
set sts=4
set ts=4
syntax on
set cindent
```

9.3 让 make 支持 c + 11

```
In .bashrc or whatever:
export CXXFLAGS='-std=c++11 -Wall'
```

9.4 tuple 相关

9.5 线性规划转对偶

```
\begin{array}{l} \text{maximize } \mathbf{c}^T \mathbf{x} \\ \text{subject to } \mathbf{A} \mathbf{x} \leq \mathbf{b}, \mathbf{x} \geq 0 \\ \end{array} \Longrightarrow \begin{array}{l} \text{minimize } \mathbf{y}^T \mathbf{b} \\ \text{subject to } \mathbf{y}^T \mathbf{A} \geq \mathbf{c}^T, \mathbf{y} \geq 0 \end{array}
```

74 CHAPTER 9. 提示

9.6 32-bit/64-bit 随机素数

32-bit	64-bit
73550053	1249292846855685773
148898719	1701750434419805569
189560747	3605499878424114901
459874703	5648316673387803781
1202316001	6125342570814357977
1431183547	6215155308775851301
1438011109	6294606778040623451
1538762023	6347330550446020547
1557944263	7429632924303725207
1981315913	8524720079480389849

9.7 NTT 素数及其原根

Prime	Primitive root
1053818881	7
1051721729	6
1045430273	3
1012924417	5
1007681537	3

9.8 Java Hints

```
1 import java.io.*;
2 import java.lang.*;
3 import java.math.*;
  import java.util.*;
5
6
        Regular usage:
           Slower IO :
7
8
               Scanner in = new Scanner (System.in);
9
               Scanner in = new Scanner (new BufferedInputStream (System.in));
10
                   in.nextInt () / in.nextBigInteger () / in.nextBigDecimal () / in.nextDouble ()
11
                   in.nextLine () / in.hasNext ()
12
               Output :
13
                   System.out.print (...);
14
                   System.out.println (...);
15
16
                   System.out.printf (...);
           Faster IO:
17
               Shown below.
18
           BigInteger :
19
               BigInteger.valueOf (int) : convert to BigInteger.
20
               abs / negate () / max / min / add / subtract / multiply /
21
                   divide / remainder (BigInteger) : BigInteger algebraic.
22
               gcd (BigInteger) / modInverse (BigInteger mod) /
23
                   modPow (BigInteger ex, BigInteger mod) / pow (int ex) : Number Theory.
24
               not () / and / or / xor (BigInteger) / shiftLeft / shiftRight (int) : Bit operation.
25
```

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```
compareTo (BigInteger) : comparation.
26
               intValue () / longValue () / toString (int radix) : converts to other types.
27
               isProbablePrime (int certainty) / nextProbablePrime () : checks primitive.
28
          BigDecimal:
29
30
               consists of a BigInteger value and a scale.
31
               The scale is the number of digits to the right of the decimal point.
               divide (BigDecimal) : exact divide.
32
               divide (BigDecimal, int scale, RoundingMode roundingMode) :
33
                   divide with roundingMode, which may be:
34
                       CEILING / DOWN / FLOOR / HALF_DOWN / HALF_EVEN / HALF_UP / UNNECESSARY / UP.
35
               BigDecimal setScale (int newScale, RoundingMode roundingMode) :
36
                   returns a BigDecimal with newScale.
37
               doubleValue () / toPlainString () : converts to other types.
38
39
           Arrays :
               Arrays.sort (T [] a);
40
41
               Arrays.sort (T [] a, int fromIndex, int toIndex);
               Arrays.sort (T [] a, int fromIndex, int toIndex, Comperator <? super T> comperator);
42
43
               addFirst / addLast (E) / getFirst / getLast / removeFirst / removeLast () :
44
                   deque implementation.
45
               clear () / add (int, E) / remove (int) : clear, add & remove.
46
47
               size () / contains / removeFirstOccurrence / removeLastOccurrence (E) :
                   deque methods.
48
               ListIterator <E> listIterator (int index) : returns an iterator :
49
                   E next / previous () : accesses and iterates.
50
                   hasNext / hasPrevious () : checks availablity.
51
                   nextIndex / previousIndex () : returns the index of a subsequent call.
52
                   add / set (E) / remove () : changes element.
53
           PriorityQueue <E> (int initcap, Comparator <? super E> comparator) :
               add (E) / clear () / iterator () / peek () / poll () / size () :
55
                   priority queue implementations.
56
57
           TreeMap <K, V> (Comparator <? super K> comparator) :
               Map.Entry <K, V> ceilingEntry / floorEntry / higherEntry / lowerEntry (K):
58
                   getKey / getValue () / setValue (V) : entries.
59
               clear () / put (K, V) / get (K) / remove (K) : basic operation.
60
               size () : size.
61
62
           StringBuilder:
               Mutable string.
63
               StringBuilder (string) : generates a builder.
64
               append (int, string, ...) / insert (int offset, ...) : adds objects.
65
               charAt (int) / setCharAt (int, char) : accesses a char.
66
               delete (int, int) : removes a substring.
67
               reverse () : reverses itself.
68
               length (): returns the length.
69
               toString (): converts to string.
70
           String:
71
72
               Immutable string.
73
               String.format (String, ...) : formats a string. i.e. sprintf.
74
               toLowerCase / toUpperCase () : changes the case of letters.
```

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```
75 */
76
   /* Examples on Comparator :
77
   public class Main {
78
       public static class Point {
79
80
            public int x;
81
            public int y;
            public Point () {
82
                x = 0;
83
                y = 0;
85
            public Point (int xx, int yy) {
86
87
                x = xx;
88
                y = yy;
89
90
       };
91
       public static class Cmp implements Comparator <Point> {
            public int compare (Point a, Point b) {
92
                if (a.x < b.x) return -1;
93
                if (a.x == b.x) {
94
                     if (a.y < b.y) return -1;
95
96
                     if (a.y == b.y) return 0;
97
                return 1;
98
            }
99
100
101
       public static void main (String [] args) {
            Cmp c = new Cmp ();
102
            TreeMap <Point, Point> t = new TreeMap <Point, Point> (c);
103
            return;
104
       }
105
106
   };
107
108
          Another way to implement is to use Comparable.
109
       However, equalTo and hashCode must be rewritten.
110
111
       Otherwise, containers may fail.
112
       Example:
       public static class Point implements Comparable <Point> {
113
            public int x;
114
            public int y;
115
            public Point () {
116
                x = 0;
117
                y = 0;
118
119
            public Point (int xx, int yy) {
120
121
                x = xx;
122
                y = yy;
123
            }
```

9.8. JAVA HINTS

```
public int compareTo (Point p) {
124
                if (x < p.x) return -1;
125
                if (x == p.x) {
126
                    if (y < p.y) return -1;
127
                    if (y == p.y) return 0;
128
129
                return 1;
130
            }
131
            public boolean equalTo (Point p) {
132
                return (x == p.x \&\& y == p.y);
133
134
            public int hashCode () {
135
136
                return x + y;
137
       };
138
139
140
   //Faster IO :
141
142
   public class Main {
143
144
       static class InputReader {
145
            public BufferedReader reader;
146
            public StringTokenizer tokenizer;
147
            public InputReader (InputStream stream) {
148
                reader = new BufferedReader (new InputStreamReader (stream), 32768);
149
                tokenizer = null;
150
            }
151
            public String next() {
152
                while (tokenizer == null || !tokenizer.hasMoreTokens()) {
153
                     try {
154
155
                         String line = reader.readLine();
                         tokenizer = new StringTokenizer (line);
156
                    } catch (IOException e) {
157
                         throw new RuntimeException (e);
158
159
                }
160
                return tokenizer.nextToken();
161
162
            public BigInteger nextBigInteger() {
163
                return new BigInteger (next (), 10);
                                                           //
                                                                  customize the radix here.
164
165
            public int nextInt() {
166
                return Integer.parseInt (next());
167
            }
168
            public double nextDouble() {
169
                return Double.parseDouble (next());
170
171
172
       }
```

78 CHAPTER 9. 提示

```
173
      public static void main (String[] args) {
           InputReader in = new InputReader (System.in);
175
176
          //
177
                Put your code here.
178
      }
179
  |}
180
181
182 // Arrays
183 int a[];
184 .fill(a[, int fromIndex, int toIndex],val) | .sort(a[, int fromIndex, int toIndex])
185 // String
186 String s;
.charAt(int i) | compareTo(String) | compareToIgnoreCase () | contains(String) |
length () | substring(int 1, int len)
189 // BigInteger
190 .abs() | .add() | bitLength () | subtract () | divide () | remainder () | divideAndRemainder ()
     \rightarrow | modPow(b, c) |
191 | pow(int) | multiply () | compareTo () |
192 gcd() | intValue () | longValue () | isProbablePrime(int c) (1 - 1/2^c) |
193 nextProbablePrime () | shiftLeft(int) | valueOf ()
194 // BigDecimal
195 ROUND_CEILING | ROUND_DOWN_FLOOR | ROUND_HALF_DOWN | ROUND_HALF_EVEN | ROUND_HALF_UP | ROUND_UP
.divide(BigDecimal b, int scale , int round_mode) | doubleValue () | movePointLeft(int) |
     → pow(int) |
| setScale(int scale(精度) , int round_mode) | stripTrailingZeros ()
  // StringBuilder
198
  StringBuilder sb = new StringBuilder ();
200 | sb.append(elem) | out.println(sb)
201 // Collection
→ .remove()
203 for (Object o: s) {}
204 // Set
205 | Set s = new HashSet () | TreeSet ();
206 // List
207 List s = new LinkedList () | ArrayList ();
208 .add([int index,] E e) | .get (int index) | .indexOf (Object o) | .set (int index, E e) |
     → .subList (int 1, int r) | .remove (int index)
```