

Cosmic web correlations with the shape, spin and peculiar velocities of dark matter halos

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ABSTRACT

Key words: methods: N-body simulations, galaxies: haloes, cosmology: theory, dark matter, large-scale structure of Universe

Author Web Method Halo Finder Major Axis Correlation
SHAPE

1 INTRODUCTION

2 THEORETICAL ANTECEDENTS

... There is abundant literature on the issue of shape and angular momentum alignment of dark matter haloes with respect to the cosmic web.

... This alignment is often measured from the distribution of the $\cos\theta$ where θ is the angle between the two axes of interest.

... Table 1 and Table 2 summarize recent results found in the literature for shape and angular momentum alignment, respectively.

The tidal connection between voids in simulations (Platen et al. 2008), the alignment of observed galaxies with the inferred tidal field (Lee & Erdogdu 2007; Jones et al. 2010). There are other kind of alignment statistics based on modifications of the correlation (Paz et al. 2008; Faltenbacher et al. 2009) that go beyond a local computation and therefore are not reviewed in detail in this paper.

- (Libeskind et al. 2013) Studies shape and spin alignment with the cosmic web defined by the velocity shear tensor method described in this paper.

The simulation has 2048³ particles in a box of $250h^{-1}\text{Mpc}$, corresponding to a particles mass of $1.3 \times 10^8 h^{-1}\text{M}_\odot$. Halos are found using a FOF halo finder with $b = 0.17$. The catalog only include halos more massive than $3 \times 10^9 h^{-1}\text{M}_\odot$.

The shape is defined from the reduced inertia tensor. Results are reported for three mass bins $M_{\text{vir}} < 10^{11.5} h^{-1}\text{M}_\odot$, $11^{11.5} < M_{\text{vir}} < 12^{12.5} h^{-1}\text{M}_\odot$ and $M_{\text{vir}} > 12^{12.5} h^{-1}\text{M}_\odot$.

The identification of the cosmic web is done on a grid of 256^3 with a gaussian smoothing of $\sim 1h^{-1}\text{Mpc}$ over the velocity field. We define this velocity field as the ratio of a momentum density to the matter density field. The details of this approach are described in the Appendix.

The alignment signal of the spin is very weak while the

shape alignment signal is very strong. The shape alignment is such that the eigenvector corresponding to the smallest eigenvalue is aligned with the major axis. This effect is stronger for more massive halos. In other words the major axis of a halo is aligned with a filament, and lies on the plane that define a sheet. However the spin is anti-aligned with the filament for massive halos and weakly aligned for low mass halos.

- (Trowland et al. 2013)

The simulation is the millennium run, which has 2160³ particles in a volume of $500h^{-1}\text{Mpc}$ on a side. This corresponds to a particle mass of $8.6 \times 10^8 h^{-1}\text{M}_\odot$. The catalog uses both halos and subhalos which were identified with SUBFIND. Only halos with more than 500 particles were kept to get a robust computation for the spin. For each halo the spin is defined as the sum of the angular momentum of each particle with respect to the center of mass.

The method to define the filamentary structure is based on the eigenvalues of the hessian of the density. However the analysis are reported on a box of $300h^{-1}\text{Mpc}$ on a side. Four different gaussian smoothing scales are used: 2.0, 3.0 and $5.0h^{-1}\text{Mpc}$.

The authors report a slight alignment signal of spin against the principal filament axis. By fitting the following functional form to the $\cos(\theta)$ distribution

$$P(\cos\theta) = (1-c)\sqrt{1+\frac{c}{2}} \left[1 - c \left(1 - \frac{3}{2} \cos^2\theta \right) \right]^{-3/2}, \quad (1)$$

they are able to quantify the degree of alignment ($c < 0$) or anti-alignment ($c > 0$). This parameterization is based on theoretical expectations of Tidal Torque Theory (TTT) (Lee et al. 2005). At $z = 0$, the reported value is $c = 0.035 \pm 0.004$, where the uncertainty was calculated using bootstrapping and resampling.

When the halo sample is divided between low mass and high mass halos with a transition scale $M_* = 5.9 \times 10^{12}\text{M}_\odot$, there is an anti-alignment above this mass and an alignment below it.

Author	Web Method	Spatial Scale	Along	Alignment	Mass dependence
Libeskind et al. (2013)	V-Web	$1h^{-1}\text{Mpc}$	filament	++	$> 10^{12}h^{-1}\text{M}_\odot$
			filament	+	$< 10^{12}h^{-1}\text{M}_\odot$
			wall	++	all masses
Zhang et al. (2009)	Hessian density field	$2.1h^{-1}\text{Mpc}$	filament	++	$> 10^{12}h^{-1}\text{M}_\odot$
			filament	+	$< 10^{12}h^{-1}\text{M}_\odot$
Aragón-Calvo et al. (2007)	Hessian density field	-	wall	++	$> 10^{12}h^{-1}\text{M}_\odot$
			wall	+	$< 10^{12}h^{-1}\text{M}_\odot$
			filament	++	$> 10^{12}h^{-1}\text{M}_\odot$
			filament	+	$< 10^{12}h^{-1}\text{M}_\odot$

Table 1. Summary of previous theoretical results. Shape. Indicates the alignment of the halo's major axis along a filament or a sheet.

Author	Web Method	Spatial Scale	Along	Alignment	Mass dependence
Libeskind et al. (2013)	V-Web	$1h^{-1}\text{Mpc}$	filament	—	$> 10^{12}h^{-1}\text{M}_\odot$
			filament	+	$< 10^{12}h^{-1}\text{M}_\odot$
			wall	++	all masses
Trowland et al. (2013)	Hessian density	$2 - 5h^{-1}\text{Mpc}$	filament	—	$> 5 \times 10^{12}h^{-1}\text{M}_\odot$
			filament	+	$< 5 \times 10^{12}h^{-1}\text{M}_\odot$
Codis et al. (2012)	Morse Theory & Tidal Web	$1 - 5h^{-1}\text{Mpc}$	filament	--	$> 10^{12}h^{-1}\text{M}_\odot$
			filament	++	$< 10^{12}h^{-1}\text{M}_\odot$
			wall	++	all masses
Zhang et al. (2009)	Hessian density field	$2.1h^{-1}\text{Mpc}$	filament	++	only if anticorrelated with shape
			filament	--	only if correlated with shape
Aragón-Calvo et al. (2007)	Hessian density field	-	wall	++	$> 10^{12}h^{-1}\text{M}_\odot$
			wall	+	$< 10^{12}h^{-1}\text{M}_\odot$
			filament	—	$> 10^{12}h^{-1}\text{M}_\odot$
			filament	+	$< 10^{12}h^{-1}\text{M}_\odot$
Hahn et al. (2007)	Tidal Web	$2.1h^{-1}\text{Mpc}$	filament	—	none
		$2.1h^{-1}\text{Mpc}$	wall	++	stronger $> 10^{12}h^{-1}\text{M}_\odot$

Table 2. Summary of previous theoretical results. Angular Momentum

• (Codis et al. 2012) Studies the alignment of the spin of dark matter halos relative to the surrounding large scale structure and to the tidal tensor eigenvalues.

They use a dark matter simulation with 4096^3 DM particles in a cubic periodic box of $2000h^{-1}\text{Mpc}$ on a side, which corresponds to a particle mass of $7.7 \times 10^9\text{M}_\odot$. Halos are identified using a FoF algorithm with a linking length of 0.2 keeping all halos with more than 40 particles, which sets the minimum halo mass to be $3 \times 10^{11}\text{M}_\odot$. In their work the particles were sampled on a 2048^3 grid and the density field was smoothed with a gaussian filter over a scale of $5h^{-1}\text{Mpc}$ corresponding to a mass of 1.9×10^{14} . The skeleton was computed over 6^3 overlapping subcubes and then reconnected.

The filament finder algorithm is based on Morse theory and defines a Skeleton to be the set of critical lines joining the maxima of the density field through saddle points following the gradient. They also compute the hessian of the potential over the smoothed density field to get their eigenvectors.

The spin of the halo is defined as $m_p \sum_i (r_i - \bar{r}) \times (v_i - \bar{v})$ where \bar{r} is the center of mass of the halo and \bar{v} is the average velocity.

They measure the spin alignment with each one of the eigenvectors. With respect to the minor eigenvector e_1 there is antialignment for masses $M > 5 \times 10^{12}\text{M}_\odot$ and alignment for masses $< 5 \times 10^{12}\text{M}_\odot$. With respect to the intermediate

eigenvector e_2 there is a strong alignment at high masses and no alignment for low masses, with respect to the major eigenvector e_3 there is an anti-alignment signal at all masses. The results from the Skeleton algorithm are in perfect agreement with the results from the Tidal web. The transitional mass is weakly dependent on the smoothing scale, varying between $1 - 5 \times 10^{12}h^{-1}\text{M}_\odot$ for smoothing scales between $1.0 - 5.0h^{-1}\text{Mpc}$.

• (Zhang et al. 2009) Study the spin and shape alignment against filaments.

They use a dark matter simulation with 1024^3 DM particles in a periodic box of $100h^{-1}\text{Mpc}$ on a side. The particle mass is $6.92 \times 10^7h^{-1}\text{M}_\odot$. Dark matter haloes are found using a FOF algorithm with a linking length of 0.2 times the interparticle distance. Only halos with more than 500 particles are retained for further analysis.

The angular momentum is measured with positions respect to the center of mass and the shape is determined using the non-normalized moment of inertia tensor.

The environment is found using the hessian of the density. The density field was interpolated over a 1024^3 grid and then smoothed with a Gaussian filter of scale $R_s = 2.1h^{-1}\text{Mpc}$. There are two methods to define the direction of a filament. The first method uses the eigenvalues of the hessian density, however they define the filament direction with the eigenvector corresponding to the single positive eigenvalue of

the hessian. The second method used a line that connects the two terminal halos in a filament segment.

The characterization of the alignment with the $\cos(\theta)$ statistic. For the method that uses the eigenvectors, they find that the strenght of the spin alignment decreases with halo mass. For the shape they study the alingment of the major axis with the filament. The find an alignment signal in all mass bins, with an stronger effect for more massive halos.

In a final experiment they measure the spin alignment in four different samples that separated by the strength of the shape alignment. They find that halos anticorrelated in shape, show a strong sping correlation going to the extreme where there is a strong spin anticorrelation for halos with a strong shape correlation. This means that the halos with strong spin alignment are not the same halos showing strong shape alignment.

- (Aragón-Calvo et al. 2007) The method is the Multi-scale Morphology Filter which is based on the Hessian matrix of the density field, where the density field is computed from the particle distribution using a Delaunay tessellation field estimator (DTFE), which is self-adaptive. This allows them to identify clusters, filaments and walls.

The simulation has 512^3 particles in a cubic box of $150h^{-1}\text{Mpc}$. The mass per particle is $2 \times 10^9 h^{-1}M_\odot$. Halo identification is done with the HOP algorithm. They keep halos with more than 50 partices and less than 5000, defining a mass range of $1 - 100 \times 10^{11} h^{-1}M_\odot$.

The principal axes of each halo are computed from the non-normalized inertia tensor. The inertian tensor and the angular momentum are computed with respect to the center of mass of the halo.

They compute two angles, one with respect to the direction defining the filaments and the other the walls. Their results make a distinction between halos of more massive and less massive than $10^{12} h^{-1}M_\odot$.

The halo spins tend to lie on the plane of the wall. This is stronger for massive halos. The effect for filaments is weaker: low mass halos tend to lie parallel to their host filament, while high mass halos tend to be perpendicular.

Theres is a very strong effect for the principal axes of halos in filaments to be strongly correlated with the direction of the filaments. The minor axis tend to be perpendicular to the filament. This effect is stronger for larger halos.

The effect in walls is less strong ,but still the minor axis tend to lie perpendicular to the wall, while the other axis then to lie over the wall. The effect is stronger for massive halos.

They find that spins and shapes of dark matter halos are significantly correlated with each other and with the orientation of their host structures.

- (Hahn et al. 2007) The method is the Tweb. They use three simulations each of 512^3 particles, with sizes $L_1 = 45h^{-1}\text{Mpc}$, $L_2 = 90h^{-1}\text{Mpc}$ and $L_3 = 180h^{-1}\text{Mpc}$, this corresponds to particle masses of 4.7, 38.0, $300 \times 10^7 h^{-1}M_\odot$. The normalization is $\sigma_8 = 0.9$. Halo identification was done with a FOF algorithm with 0.2 times the interparticle distance. They consider halos of at least 300 particles.

The web is obtained for a grid of 1024^3 cells, the density field is obtained with a CIC interpolation and smoothed using a Gaussian Kernel. In the rest of the paper all the

results correspond to a smoothing scale of $R_s = 2.1h^{-1}\text{Mpc}$.

They Report on the angle between the halo angular momentum vector and the eigenvector corresponding to perpendicular directions to the sheets and the direction of the filaments. This is divided in two halo populations: $5 \times 10^{10} - 1.0 \times 10^{12}$ and $> 10^{12}$. There is a weak antialignment in the case of the filaments and a stronger anti-alignment in the case of the sheets. For the sheets the effect is stronger for the massive bin. In the filaments the alignment is weak regardless of the mass. They do not report any other significan statistic, but recognize that they suffer from small-number statistics in voids).

They do not see any strong dependance of the environment in the shape. They do not measure the shape alinment.

- (Brunino et al. 2007) Uses a DM only N-body simulation (the Millennium Run) to study the shape and angular momentum alignment with respect to large cosmological voids.

The voids are found with a spherical void finder. This algorithm first looks for potential void centers in the underdense regions of the simulation. These positions define the centers of spheres that are empty of halos above a given mass threshold. Only voids with radius larger than $10h^{-1}\text{Mpc}$ were considered for further analysis.

Halos were identified by linking particles with density exceeding 900 times the background density in order to keep the analysis of shape and angular momentum on the core of the halo. Only halos with masses in the range $8.6 \times 10^{11} h^{-1}M_\odot < M_h < 8.6 \times 10^{12} h^{-1}M_\odot$ were included analized to measure their angular momentum and the inertia tensor, both in a non-normalized way.

For the purpose of measuring alignments a second cut is imposed whereby only halos within a shell of radius $R_{void} < r < 1.05R_{void}$. The alignment is then measured between the vector connecting the center of the void to the halo in question and the vector of interest.

The results show that there is a strong alignment of halo shape in such a way that the major axis is parallel to the shell surrounding the void. In the case of angular momentum there is not a significant signal for alignment.

- (Basilakos et al. 2006) Use a cosmological SPH+N-body simulation to measure the alignment of cluster halos with their parent supercluster. For both the cluster halos and parent super-cluster they define the shape via the non-normalized inertia tensor. The find that strenght of the alignments increases with the degree of filamentarity of the supercluster.

The simulation has 2×512^3 particles in a box of side $500h^{-1}\text{Mpc}$. The dark matter particle mass is $6.6 \times 10^{10} h^{-1}M_\odot$ while for SPH particles is $1.2 \times 10^{10} h^{-1}M_\odot$. The halo finding is done with a FOF algorithm with a linking length of 0.17 and keep objects with more than 100 particles.

- (Lee & Pen 2002) Observational measurement for the alignment of galaxy spin axes with the local tidal shear field. For the measurement of shear, we have used the Point Source Catalog Redshift (PSCz) survey (a complete redshift survey from the IRAS Point Source Catalog) data. This was done down to a radial comoving distance of $\sim 150h^{-1}\text{Mpc}$.

- (Hatton & Ninin 2001) DM matter only simulation. 256^3 particles, $100h^{-1}\text{Mpc}$, particle mass. Look for align-

ment of angular momentum vectors with neighboring structures or other massive structures. They match halos using close pair statistics. They do not find any evidence for a statistically significant mutual alignment of halos on any scale.

3 N-BODY SIMULATION AND HALO FINDING

In this paper we use the Bolshoi volume. This is a simulation that follows the non-linear evolution of a dark matter density field on cosmological scales. The volume is a cubic box with $250h^{-1}\text{Mpc}$ on a side, the matter density field is sampled with 2048^3 particles. The cosmological parameters in the simulation correspond to the results inferred from WMAP5 data, which are also consistent with the more recent results of WMAP9. These parameters are $\Omega_m = 0.27$, $\Omega_\Lambda = 0.73$, $\sigma_8 = 0.82$, $n_s = 0.95$ and $h = 0.70$ for the matter density, cosmological constant, normalization of the power spectrum, the slope in the spectrum of the primordial matter fluctuation and the dimensionless Hubble constant. With this conditions the mass of each dark matter particle in the simulation corresponds to $m_p = 1.4 \times 10^8 h^{-1} \text{M}_\odot$.

In this paper we use groups found with a Friends-Of-Friends (FOF) halo finder using a linking length of $b = 0.17$ times the mean interparticle separation. This choice translates into halos with a density of 570 times the mean density at $z = 0$. The measurements for the shape, angular momentum and peculiar velocity are done using the set of particles in each dark matter halo. The definition we use in this paper for the shape comes from the diagonalization of the reduced inertia tensor.

$$\mathcal{I}_{lm} = \sum_i \frac{x_{i,l}x_{i,m}}{R_i^2}, \quad (2)$$

where i is the particle index in the halo and l, m run over the three spatial indexes and $R_i^2 = x_{i,1}^2 + x_{i,2}^2 + x_{i,3}^2$, where the positions are measured with respect to the center of mass.

The spin is calculated as

$$\vec{J} = \sum_i m_p R_i \vec{v}_i, \quad (3)$$

where the velocities are also measured with respect to the center of mass velocity. Finally the peculiar velocity of a halo is computed as the center of mass velocity.

4 THE COSMIC WEB ALGORITHMS

We use two algorithms to define the cosmic web on cosmological N-body simulations. Both are based on the same algorithmic principle, which is determining locally a symmetric tensor which can be diagonalized to yield three real eigenvalues $\lambda_1 > \lambda_2 > \lambda_3$ and their corresponding eigenvectors \mathbf{e}_1 , \mathbf{e}_2 and \mathbf{e}_3 . This allows for a local classification into one of the following four categories: void, sheet, filament and peak depending whether the number of eigenvalues larger than a given threshold λ_{th} is 3, 2, 1 or 0, respectively.

We use two different symmetric tensors. The first is the shear tensor, defined as the hessian of the gravitational potential, normalized in such a way as to be dimensionless:

$$T_{\alpha\beta} = \frac{\partial^2 \phi}{\partial r_\alpha \partial r_\beta}, \quad (4)$$

where ϕ is the gravitational potential rescaled by a factor $4\pi G \bar{\rho} = 3/2 \Omega_m H_0^2$ in such a way that the Poisson equation can be written as:

$$\nabla^2 \phi = \delta, \quad (5)$$

where δ is the matter overdensity, $\bar{\rho}$ is the average matter density, H_0 is the Hubble constant at present time and Ω_m is the matter density parameter.

The second tensor is the velocity shear:

$$\Sigma_{\alpha\beta} = -\frac{1}{2H_0} \left(\frac{\partial v_\alpha}{\partial r_\beta} + \frac{\partial v_\beta}{\partial r_\alpha} \right) \quad (6)$$

4.1 Numerical considerations

In this paper we compute the cosmic web on grids of two different resolutions 256^3 and 512^3 . In the case for the Tweb we interpolate

5 RESULTS

5.1 Interweb Alignment

... We compute the pair-wise alignment between the eigenvectors in the two web finders.

... We also compute the alignment between the eigenvectors in cells occupied by dark matter halos. This will be a key element in the interpretation of the results for halo-based alignments in the next sections: shape, angular momentum and peculiar velocities.

...

5.2 Shape Alignment

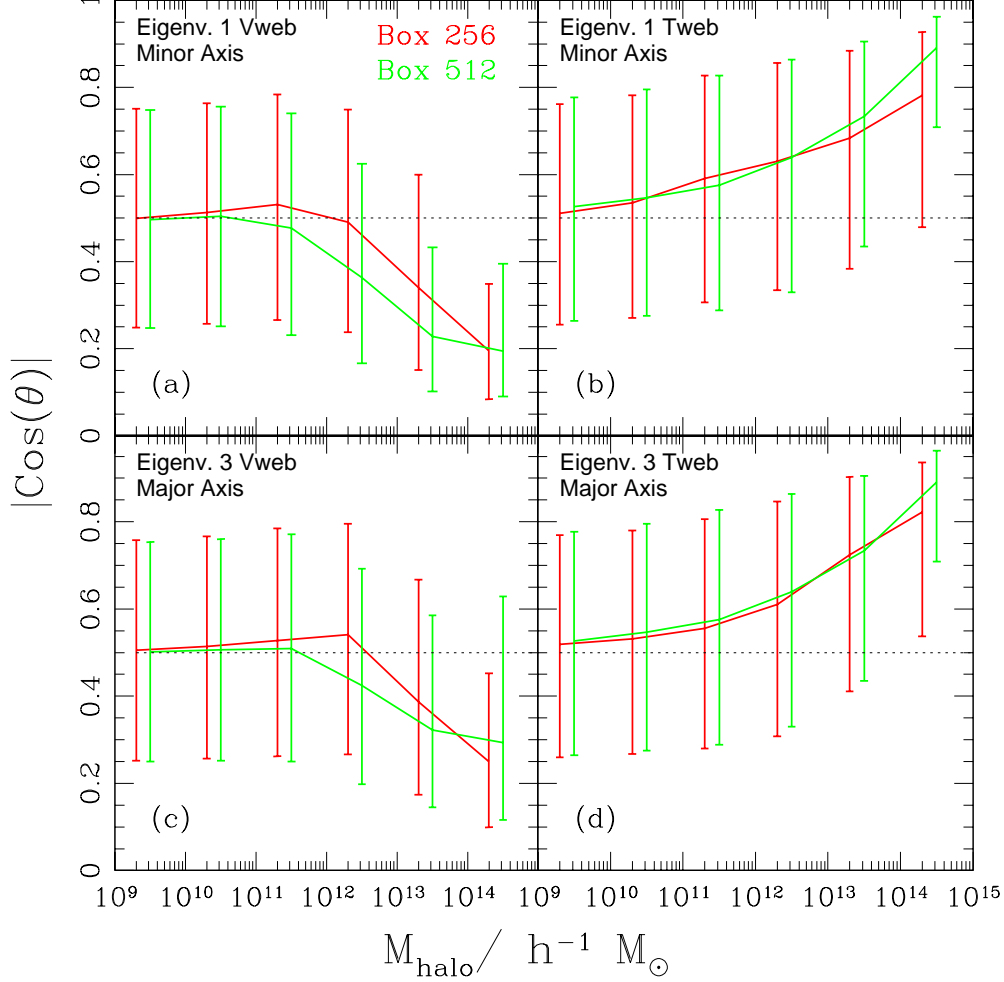


Figure 2. Median of $\cos \theta$ quantifying the shape alignment for the Vweb (left) and the Tweb (right) at two different grid resolutions. In the upper (lower) panels the angle θ is measured between the halo minor (major) axis and the first (third) eigenvector.

5.3 Angular Momentum Alignment

5.4 Peculiar velocity Alignment

Possible conclusion. Prolateness follow concentration. In the Tweb Angular momentum alignment is influenced by spin at higher masses. In the Vweb angular momentum alignment is influenced by all factors. In the peculiar velocity alignment only spin seems to have an effect.

5.5 What drives the alignment

We wish to understand what other selection criteria on halo properties can produce a stronger local alignment for the shape, spin and peculiar velocities. We split the halo population into low and high mass halos imposing a cut at $M_{\text{halo}} = 10^{11} h^{-1} M_{\odot}$. This allows us to have robust statistics on the high mass end. We have also computed these results for a cut at $M_{\text{halo}} = 10^{12} h^{-1} M_{\odot}$ and checked that the results we report below are not affected by this change.

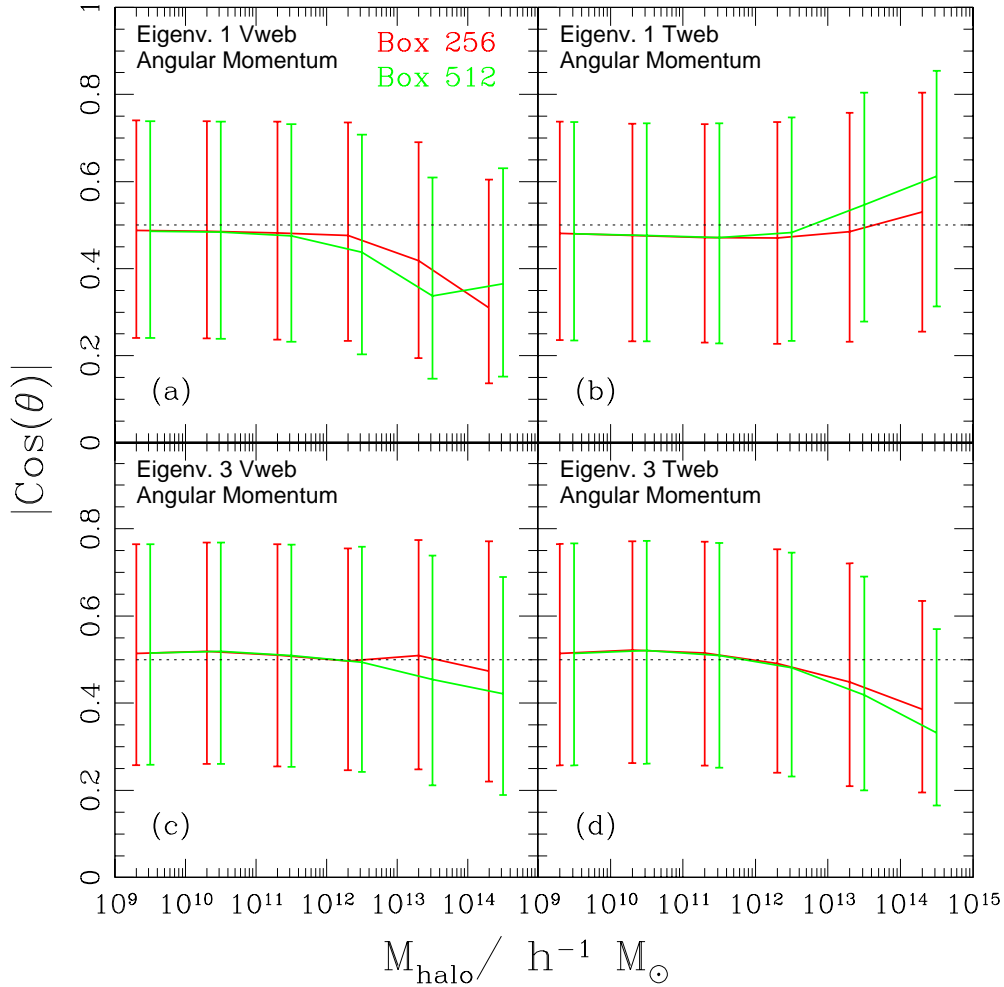


Figure 3. Median of $\cos \theta$ quantifying the angular momentum alignment for the Vweb (left) and the Tweb (right) at two different grid resolutions. In the upper (lower) panels the angle θ is measured between the first (third) eigenvector and the angular momentum vector.

For each mass interval we perform cuts in the following properties: spin, concentration, triaxiality, circularity and density. We measure the web alignments in two sets, each one including the 30% of halos in the lower/higher end of the corresponding property.

6 DISCUSSION

7 CONCLUSIONS

ACKNOWLEDGMENTS

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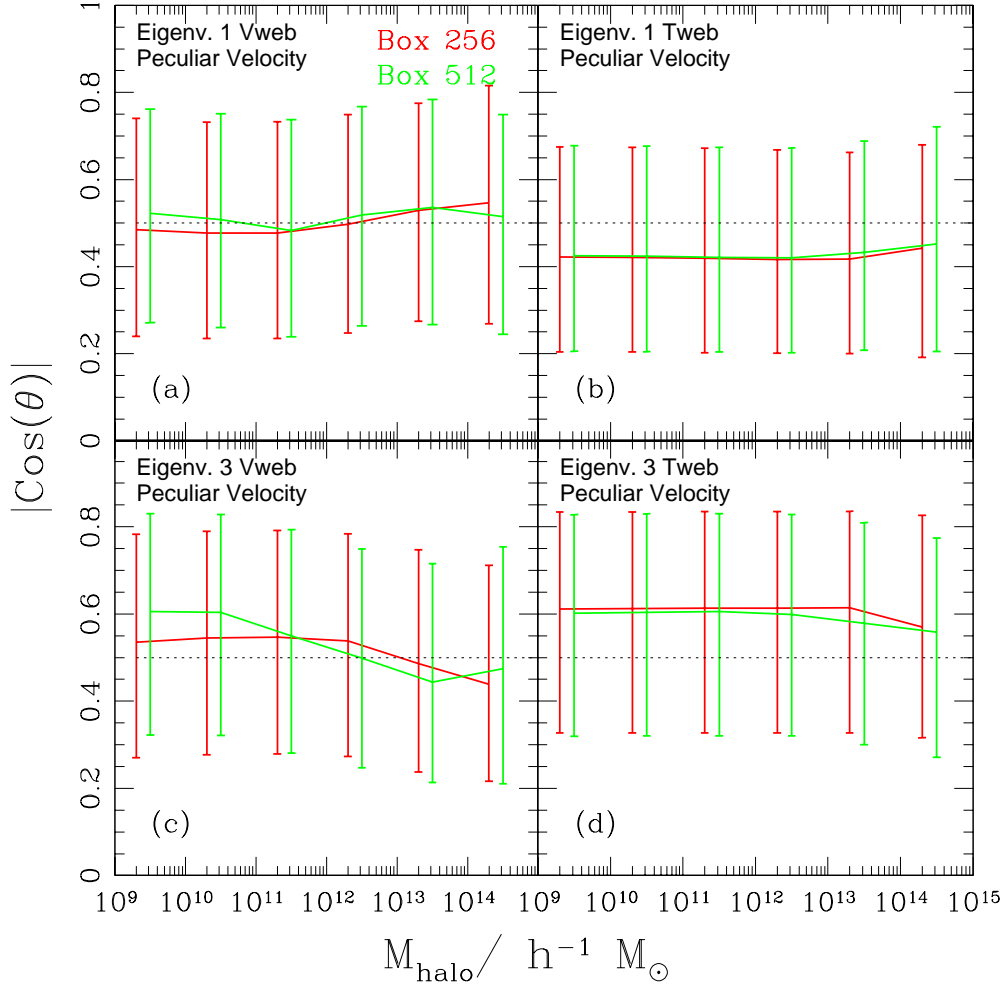


Figure 4. Median of $\cos \theta$ quantifying the peculiar velocity alignment with the Vweb (left) and the Tweb (right) at two different grid resolutions. In the upper (lower) panels the angle θ is measured between the first (third) eivenvector and a halo’s peculiar velocity.

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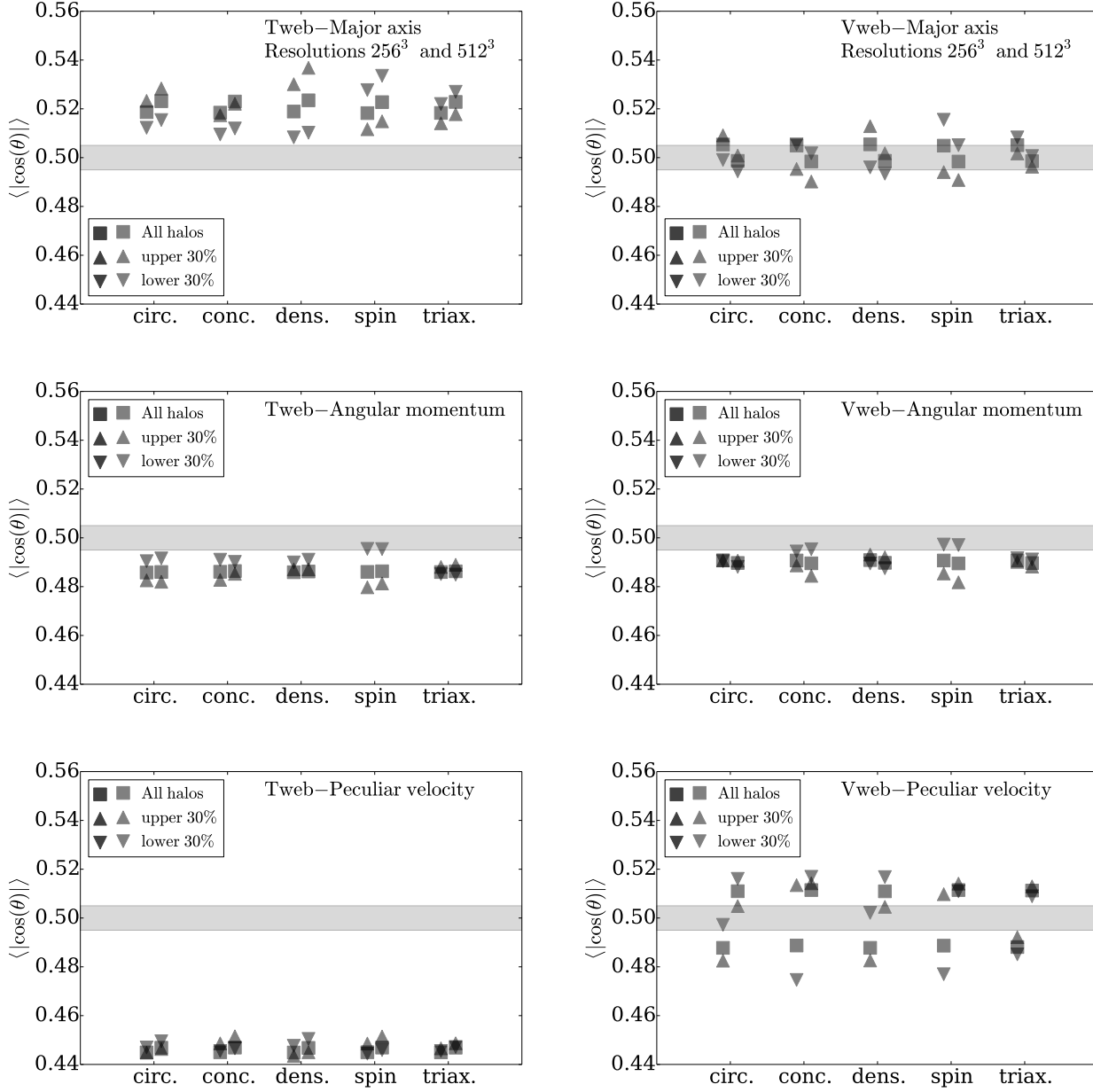


Figure 5. The alignment is always taken with respect to the first eigenvector.

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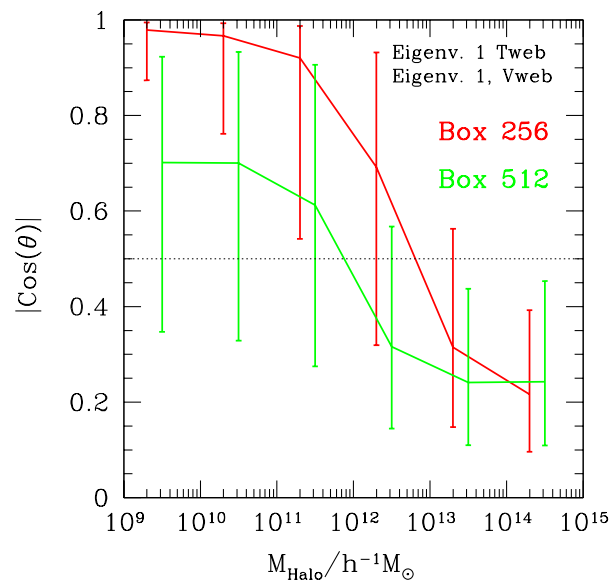


Figure 1. Median of the interweb alignment for the two grid resolutions as a function of the dark matter mass corresponding to the halos where the measurement was made. The error bars indicate the lower and upper quartiles (Figure in color in the web version).