

## Quiz navigation



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### Question 1

Not yet  
answered

Points out of  
3.00

Find the unit vector  $\mathbf{u} = [u_1 \ u_2 \ u_3]^T$  in the same direction as  $\mathbf{v} = [3 \ 4 \ 0]^T$ .

$u_1 =$    $u_2 =$    $u_3 =$

### Question 2

Not yet  
answered

Points out of  
4.00

Determine which pairs of vectors are orthogonal.

Select one or more:

☐ a.  $\left\{ \begin{bmatrix} 3 \\ 2 \\ -5 \\ 0 \end{bmatrix}, \begin{bmatrix} -4 \\ 1 \\ -2 \\ 6 \end{bmatrix} \right\}$

☐ b.  $\left\{ \begin{bmatrix} 8 \\ -5 \end{bmatrix}, \begin{bmatrix} -2 \\ -2 \end{bmatrix} \right\}$

☐ c.  $\left\{ \begin{bmatrix} -3 \\ 7 \\ 4 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 \\ -8 \\ 15 \\ -7 \end{bmatrix} \right\}$

☐ d.  $\left\{ \begin{bmatrix} 12 \\ 3 \\ -5 \end{bmatrix}, \begin{bmatrix} 2 \\ -3 \\ 3 \end{bmatrix} \right\}$

## Question 3

Not yet  
answeredPoints out of  
4.00

Let  $\mathbf{y} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$  and  $\mathbf{u} = \begin{bmatrix} 4 \\ -7 \end{bmatrix}$ . Write  $\mathbf{y}$  as the sum of two orthogonal vectors, such that  $\mathbf{y} = \hat{\mathbf{y}} + \mathbf{z}$ , where  $\hat{\mathbf{y}} = \begin{bmatrix} \hat{y}_1 \\ \hat{y}_2 \end{bmatrix}$  is in  $\text{Span}\{\mathbf{u}\}$  and  $\mathbf{z} = \begin{bmatrix} z_1 \\ z_2 \end{bmatrix}$  is orthogonal to  $\mathbf{u}$ .

$$\hat{y}_1 = \boxed{\phantom{000}} \quad \hat{y}_2 = \boxed{\phantom{000}}$$

$$z_1 = \boxed{\phantom{000}} \quad z_2 = \boxed{\phantom{000}}$$

## Question 4

Not yet  
answeredPoints out of  
3.00

Let  $\mathbf{y} = \begin{bmatrix} 6 \\ 3 \\ -2 \end{bmatrix}$ ,  $\mathbf{u}_1 = \begin{bmatrix} 3 \\ 4 \\ 0 \end{bmatrix}$ ,  $\mathbf{u}_2 = \begin{bmatrix} -4 \\ 3 \\ 0 \end{bmatrix}$ . Find the orthogonal projection of  $\mathbf{y}$  onto  $\text{Span}\{\mathbf{u}_1, \mathbf{u}_2\}$ , i.e. find  $\hat{\mathbf{y}} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$ .

$$x_1 = \boxed{\phantom{000}} \quad x_2 = \boxed{\phantom{000}} \quad x_3 = \boxed{\phantom{000}}$$

## Question 5

Not yet  
answeredPoints out of  
4.00

Compute the orthogonal projection,  $\begin{bmatrix} x \\ y \end{bmatrix}$ , of  $\begin{bmatrix} 1 \\ 7 \end{bmatrix}$  onto the line through  $\begin{bmatrix} -4 \\ 2 \end{bmatrix}$ .

$$x = \boxed{\phantom{000}}$$

$$y = \boxed{\phantom{000}}$$

## Question 6

Not yet  
answeredPoints out of  
7.00

Let  $\mathbf{y} = \begin{bmatrix} 3 \\ -1 \\ 1 \\ 13 \end{bmatrix}$ ,  $\mathbf{v}_1 = \begin{bmatrix} 1 \\ -2 \\ -1 \\ 2 \end{bmatrix}$ ,  $\mathbf{v}_2 = \begin{bmatrix} -4 \\ 1 \\ 0 \\ 3 \end{bmatrix}$ .

a. Find the closest point  $(x_1, x_2, x_3, x_4)$  to  $\mathbf{y}$  in the subspace  $W$  spanned by  $\mathbf{v}_1$  and  $\mathbf{v}_2$ .

$$x_1 = \boxed{\phantom{000}} \quad x_2 = \boxed{\phantom{000}} \quad x_3 = \boxed{\phantom{000}} \quad x_4 = \boxed{\phantom{000}}$$

b. Find the shortest distance from  $\mathbf{y}$  to the subspace of  $\mathbb{R}^4$  spanned by  $\mathbf{v}_1$  and  $\mathbf{v}_2$ :  $\boxed{\phantom{000}}$

