# 1 P-instructions

## 1.1 Expressions and Assignments

instruction	meaning	condition	result	comments	references
add N	$STORE[SP - 1] := STORE[SP - 1] +_N STORE[SP];$	(N,N)	(N)		tab. 2.1, p. 11
	SP := SP - 1				
$\operatorname{\mathbf{sub}} N$	STORE[SP - 1] := STORE[SP - 1]N STORE[SP];	(N,N)	(N)		tab. 2.1, p. 11
	SP := SP - 1				
$\mathbf{mul}\ N$	$STORE[SP - 1] := STORE[SP - 1] *_N STORE[SP];$	(N,N)	(N)		tab. 2.1, p. 11
	SP := SP - 1				
$\operatorname{\mathbf{div}} N$	$  STORE[SP - 1] := STORE[SP - 1] /_N STORE[SP];$	(N,N)	(N)		tab. 2.1, p. 11
	SP := SP - 1				
neg N	STORE[SP] :=N STORE[SP];	(N)	(N)		tab. 2.1, p. 11
and	STORE[SP - 1] := STORE[SP - 1] and $STORE[SP];$	(b,b)	(b)		tab. 2.1, p. 11
	SP := SP - 1				
or	STORE[SP - 1] := STORE[SP - 1]  or  STORE[SP];	(b,b)	(b)		tab. 2.1, p. 11
	SP := SP - 1				
not	STORE[SP] := note STORE[SP];	(b)	(b)		tab. 2.1, p. 11
equ $T$	$  STORE[SP - 1] := STORE[SP - 1] =_T STORE[SP];$	(T,T)	(b)		tab. 2.1, p. 11
	SP := SP - 1				
$\operatorname{\mathbf{geq}} T$	$  STORE[SP - 1] := STORE[SP - 1] \ge_T STORE[SP];$	(T,T)	(b)		tab. 2.1, p. 11
	SP := SP - 1				
leq T	$STORE[SP - 1] := STORE[SP - 1] \le_T STORE[SP];$	(T,T)	(b)		tab. 2.1, p. 11
	SP := SP - 1				
les $T$	$  STORE[SP - 1] := STORE[SP - 1] <_T STORE[SP];$	(T,T)	(b)		tab. 2.1, p. 11
	SP := SP - 1				
$\operatorname{\mathbf{grt}} T$	$  STORE[SP - 1] := STORE[SP - 1] >_T STORE[SP];$	(T,T)	(b)		tab. 2.1, p. 11
	SP := SP - 1				

instruction	meaning	condition	result	comments	references
$\mathbf{neq}\ T$	$STORE[SP - 1] := STORE[SP - 1] \neq_T STORE[SP];$	(T,T)	(b)		tab. 2.1, p. 11
	SP := SP - 1				

#### 1.2 Store and Load Instructions

instruction	meaning	condition	result	comments	references
$\operatorname{\mathbf{ldo}} T q$	SP := SP + 1;	$q \in [0, maxstr]$	(T)	load location given by absolute	tab. 2.2, p. 12
	STORE[SP] := STORE[Q]			address on top of stack	
$\operatorname{\mathbf{ldc}} T q$	SP := SP + 1;	type(q) = T	(T)	load constant q	tab. 2.2, p. 12
	STORE[SP] := q			on top of stack	
ind $T$	STORE[SP] := STORE[STORE[SP]]	(a)	(T)	load indirectly using	tab. 2.2, p. 12
				highest stack location	
$\mathbf{sro}\ T\ q$	STORE[q] := STORE[SP];	(T)		stores in location addressed	tab. 2.2, p. 12
	SP := SP - 1	$q \in [0, maxstr]$		by absolute address	
sto $T$	STORE[STORE[SP - 1]] := STORE[SP];	(a, T)		stores in location addressed	tab. 2.2, p. 12
	SP := SP - 2			by $2^{nd}$ highest stack location	

#### 1.3 Conditional and Iterative Statements

instruction	meaning	condition	result	comments	references
<b>ujp</b> q	PC := q	$q \in [0, codemax]$		unconditional branch	tab. 2.4, p. 14
fjp q	if STORE[SP] = false	(b)		conditional branch	tab. 2.4, p. 14
	then $PC := q$	$q \in [0, codemax]$			
	fi				
	SP := SP - 1				

instruction	meaning	condition	result	comments	references
ixj q	PC := STORE[SP] + q;		(i)	indexed branch (switch)	tab. 2.5, p. 17
	SP := SP - 1				
ixa q	STORE[SP - 1] := STORE[SP - 1] + STORE[SP] * q;	(a, i)	(a)	indexed address computation: start	tab. 2.6, p. 22
	SP := SP - 1			address in STORE[SP - 1], index of	
				selected subarray in STORE[SP],	
				$q = g \cdot d^{(j)}$ subarray size	
inc $T$	STORE[SP] := STORE[SP] + q	(T) and $type(q) = i$	(T)		tab. 2.7, p. 23
$\operatorname{\mathbf{dec}} T$	STORE[SP] := STORE[SP] - q	(T) and $type(q) = i$	(T)		tab. 2.7, p. 23

#### 1.4 Array Indexation

instruction	meaning	condition	result	comments	references
$\mathbf{chk}\ p\ q$	if $(STORE[SP] < p)$ or $(STORE[SP] > q)$	(i,i)	(i)	check array boundaries	tab. 2.8, p. 23
	then error('value out of range')				
	fi				
dpl T	SP := SP + 1;	(T)	(T,T)	copies highest stack entry	tab. 2.9, p. 27
	STORE[SP] := STORE[SP - 1]				tab. 2.9, p. 27
$\operatorname{\mathbf{Idd}} T$	SP := SP + 1;	$(a, T_1, T_2)$	$(a, T_1, T_2, i)$	indirect access to descriptor arrays	tab. 2.9, p. 27
	STORE[SP] := STORE[STORE[SP - 3] + q]				tab. 2.9, p. 27
sli $T_2$	STORE[SP - 1] := STORE[SP];	$(T_1, T_2)$	$(T_2)$	move highest stack entry	tab. 2.9, p. 27
	SP := SP - 1			in $2^{nd}$ highest position	

## 1.5 Dynamic Memory Allocation

instruction	meaning	condition	result	comments	references
new	if NP - STORE[SP] $\leq$ EP	(a,i)			tab. 2.10, p. 29
	then error('store overflow')			object size at top of stack	fig. 2.7, p. 30
	else $NP := NP - STORE[SP];$				
	STORE[STORE[SP - 1]] := NP;			address of pointer just below	
	SP := SP - 2;			$ptr \rightarrow object start address$	
	fi				

#### 1.6 Procedure Calls and Frames on the Stack

## 1.6.1 Loading and Storing Bound and Free Variables

instruction	meaning	condition	result	comments	references	
lod T p q	SP := SP + 1;		(T)	load a value of type $T$	tab. 2.11, p. 42	
	STORE[SP] := STORE[base(p, MP) + q]			nesting depth $p$ , relative address $q$		
lda p q	SP := SP + 1;		(a)	loads addresses	tab. 2.11, p. 42	
	STORE[SP] := base(p, MP) + q			nesting depth $p$ , relative address $q$		
str T p q	STORE[base(p, MP) + q] := STORE[SP];		(T)	storing values	tab. 2.11, p. 42	
	SP := SP - 1			nesting depth $p$ , relative address $q$		
!!!	base(p,a) = if p = 0 then a else base(p-1, STORE[a+1]) fix e.g. $base(d, MP)$ follows SL chain d times to return MP of the predecessor frame (Fig. 2.12, p. 42)					

#### 1.6.2 Instructions for Calling and Entering Procedures (Caller)

instruction	meaning	condition	result	comments	references
mst p	STORE[SP + 2] := base(p, MP);		stack marked with	set SL to point to static predecessor's MP	tab. 2.12, p. 47
			organisational block	p nrof times to follow SL-chain	Fig. 2.12, p. 42
	STORE[SP + 3] := MP;			set DL to pint to start of caller's frame	Fig. 2.11, p. 40
	STORE[SP + 4] := EP;			save EP	
	SP := SP + 5;			location for return address reserved; params	
				can now be evaluated from $STORE[SP + 1]$	
$\operatorname{\mathbf{cup}} p q$	MP := SP - (p+4);		call user procedure	p: params storage requirement	tab. 2.12, p. 47
	STORE[MP + 4] := PC;			save return address	
	PC := q;			proc. init. routine start address $q$ in CODE	
!!!	base(p, a) = <b>if</b> $p = 0$ <b>then</b> $a$ <b>else</b> $base(p - 1)$	STORE[a+1] fi: e	g. $base(d, MP)$ follows	SL chain $d$ times (Fig. 2.12, p. 42)	!!!

#### 1.6.3 Instructions for Returning

instruction	meaning	condition	result	comments	references
retf	SP := MP;		leaves result at	function result in local stack	tab. 2.13, p. 48
	PC := STORE[MP + 4];		top of stack	return branch	
	EP := STORE[MP + 3];			restore EP	
	$ifEP \ge NP$				
	thenerror('storeoverflow')fi				
	MP := STORE[MP +2]			release current stack frame	
				revert via DL ptr	
retp	SP := MP - 1;			procedure w/o results	tab. 2.13, p. 48
	PC := STORE[MP + 4];			return branch	
	EP := STORE[MP + 3];			restore EP	
	$ifEP \ge NP$				
	thenerror('storeoverflow')fi				
	MP := STORE[MP +2]			release current stack frame	
				revert via DL ptr	

## 1.6.4 Instructions for Calling and Entering Procedures (Callee)

instruction	meaning	condition	result	comments	references
ssp p	SP := MP + p - 1			set stack pointer	tab. 2.12, p. 47
				p size of static part data area	
sep p	EP := SP + p;			set extreme pointer	tab. 2.12, p. 47
	$ifEP \ge NP$			p max. depth of local stack	
	then error('store overflow') fi;			collision check stack, heap	
!!!	base(p, a) = <b>if</b> $p = 0$ <b>then</b> $a$ <b>else</b> $base(p - 1, STORE)$	$\overline{E[a+1]}$ fi: e.g. $base(a$	d, MP) follows SL ch	nain d times (Fig. 2.12, p. 42)	!!!

## 1.6.5 Block Copy Instructions

instruction	meaning	condition	result	comments	references
movs q	for $i := q - 1$ down to 0 do STORE[SP + $i$ ] := STORE[STORE[SP] + $i$ ]	(a)		STORE[SP] holds begin addresss structured type (backward copying;	tab. 2.14, p. 50
	$\mathbf{od};$			begin address TOS overwritten)	
	SP := SP + q - 1				
movd q	for $i := 1$ to $STORE[MP + q + 1]$ do				tab. 2.14, p. 50
	STORE[SP + i] := STORE[STORE[MP + q]]				
	+ STORE[MP + q + 2] + i - 1]				
	od;				
	SP := SP + STORE[MP + q + 1]				

# 2 Generating P-code Instruction Sequences: Compilation Schemes

## 2.1 Schemata for Expression Evaluation, Assignment and Statement Sequences

	Function	$(\rho: Var \mapsto \mathbb{N}_0; \text{ maps variable to relative address})$	Condition	References
1	$code_R(e_1 = e_2) \rho$	$= code_R \ e_1 \ \rho; code_R \ e_2 \ \rho; \mathbf{equ} \ T$	$type(e_1) = type(e_2) = T$	p. 13
2	$code_R(e_1 \neq e_2) \ \rho$	$= code_R \ e_1 \ \rho; code_R \ e_2 \ \rho; \mathbf{neq} \ T$	$type(e_1) = type(e_2) = T$	p. 13
*				tab. 2.1, p. 11
3	$code_R(e_1+e_2) \rho$	$= code_R \ e_1 \ \rho; code_R \ e_2 \ \rho; $ add $N$	$type(e_1) = type(e_2) = N$	p. 13
4	$code_R(e_1 - e_2) \rho$	$= code_R \ e_1 \ \rho; code_R \ e_2 \ \rho; \mathbf{sub} \ N$	$type(e_1) = type(e_2) = N$	p. 13
5	$code_R(e_1*e_2) \rho$	$= code_R \ e_1 \ \rho; code_R \ e_2 \ \rho; \mathbf{mul} \ N$	$type(e_1) = type(e_2) = N$	p. 13
6	$code_R(e_1/e_2) \rho$	$= code_R \ e_1 \ \rho; code_R \ e_2 \ \rho; \mathbf{div} \ N$	$type(e_1) = type(e_2) = N$	p. 13
7	$code_R(-e) \rho$	$= code_R \ e \ \rho; \mathbf{neg} \ N$	type(e) = N	p. 13
8	$code_R(x) \rho$	$= code_L \ x \ \rho; \mathbf{ind} \ T$	x variable identifier of type $T$	p. 13
9	$code_R(c) \rho$	$= \mathbf{ldc} \ T \ c$	c constant of type $T$	p. 13
10	$code(x := e) \rho$	$= code_L \ x \ \rho; code_R \ e \ \rho; sto \ T$	x variable identifier	p. 13
11	$code_L \ x \ \rho$	$= \mathbf{ldc} \ a \ \rho(x)$	x variable identifier	p. 13
12	$code(\mathbf{if}\ e\ \mathbf{then}\ st_1\ \mathbf{else}\ st_2\ \mathbf{fi})\ \rho$	= $code_R \ e \ \rho$ ; <b>fjp</b> $l_1$ ; $code \ st_1 \ \rho$ ; <b>ujp</b> $l_2$ ; $l_1$ : $code \ st_2 \ \rho$ ; $l_2$ :	e boolean expression	p. 14
13	$code(\mathbf{if}\ e\ \mathbf{then}\ st\ \mathbf{fi})\ \rho$	$= code_R \ e \ \rho; \mathbf{fjp} \ l; code \ st \ \rho; l:$	e boolean expression	p. 14
14	$code(\mathbf{while}\ e\ \mathbf{do}\ st\ \mathbf{od})\ \rho$	= $l_1$ : $code_R \ e \ \rho$ ; $\mathbf{fjp} \ l_2$ ; $code \ st \ \rho$ ; $\mathbf{ujp} \ l_1$ ; $l_2$ :	e boolean expression	p. 14
15	$code(\mathbf{repeat}\ st\ \mathbf{until}\ e)\ \rho$	= $l$ : $code st \rho;code_R e \rho;\mathbf{fjp} l$	e boolean expression	p. 14
16	$code(st_1; st_2) \rho$	$= code \ st_1 \ \rho; code \ st_2 \ \rho$		p. 15

# 2.2 Array-Related Schemata

	Function	$(\rho: Var \mapsto \mathbb{N}_0; \text{ maps variable to relative address})$	Condition	References
17	$code_L \ c[i_1, \ldots, i_k] \ \rho$	= $\mathbf{ldc} \ a \ \rho(c); code_I \ [i_1, \dots, i_k] \ g \ \rho$	array components of type $T$ ; $g = size(T)$	p. 23
			$type(i_1) = \dots = type(i_k) = N$	
18a	$code_I [i_1, \ldots, i_k] g \rho$	$= code_R i_1 \rho; \mathbf{ixa} \ g \cdot d^{(1)};$	array components of type $T$ ; $g = size(T)$	pp. 22–23
		$code_R \ i_2 \ \rho$ ; <b>ixa</b> $g \cdot d^{(2)}$ ;	$type(i_1) = \dots = type(i_k) = N$	
		:	$d = \sum_{j=1}^{k} u_j \cdot d^{(j)}; d^{(j)} = \prod_{l=j+1}^{k} d_l$	
		$code_R i_k \rho; \mathbf{ixa} \ g \cdot d^{(k)};$	$d_l$ ranges of array dimensions	
		$\operatorname{\mathbf{dec}}\ a\ g\cdot d$		
18b	$code_I [i_1, \ldots, i_k] arr \rho$	= $code_R i_1 \rho$ ; <b>chk</b> $u_1 o_1$ ; <b>ixa</b> $g \cdot d^{(1)}$ ;	array components of type $T$ ; $g = size(T)$	pp. 22–23
		$code_R \ i_2 \ \rho$ ; <b>chk</b> $u_2 \ o_2$ ; <b>ixa</b> $g \cdot d^{(2)}$ ;	$type(i_1) = \dots = type(i_k) = N$	
		<b>:</b>	$d = \sum_{j=1}^{k} u_j \cdot d^{(j)}; d^{(j)} = \prod_{l=j+1}^{k} d_l$	
		$code_R i_k \rho$ ; <b>chk</b> $u_k o_k$ ; <b>ixa</b> $g \cdot d^{(k)}$ ;	$d_l$ ranges of array dimensions	
		$\operatorname{\mathbf{dec}}\ a\ g\cdot d$	$arr = (g; u_1, o_1, \dots, u_k, o_k)$	
19	$code_{Ld} \ b[i_1,\ldots,i_k] \ \rho$	= $\mathbf{ldc} \ a \ \rho(b);$	load descriptor address	p. 26
		$code_{Id} [i_1, \ldots, i_k] g \rho$	(static) component size $g$	
20	$code_{Id} [i_1, \ldots, i_k] g \rho$	$= \mathbf{dpl} \; i;$	duplicate highest stack entry (descriptor address)	p. 26
		$\mathbf{ind}\ i;$	load fictitious start address via upper duplicate	
		$\mathbf{ldc}\ i\ 0;$		
		$code_R i_1 \rho$ ; add $i$ ; ldd $2k + 3$ ; mul $i$ ;	Horner scheme; retrieve and account for $d_2$	p. 25
		$code_R i_2 \rho$ ; add $i$ ; ldd $2k + 4$ ; mul $i$ ;	Horner scheme; retrieve and account for $d_3$	p. 25
		:		
		$code_R i_{k-1} \rho$ ; add $i$ ; ldd $3k + 1$ ; mul $i$ ;	Horner scheme; retrieve and account for $d_{k-1}$	p. 25
		$code_R i_k \rho; \mathbf{add} i;$	Horner scheme; account for last term	p. 25
		ixa $g$ ;	indexed address: add offset to fictitious address	p. 25
		sli $a$ ;	pop redundant address value ( $2^{nd}$ highest stack entry)	

## 2.3 Record- and Pointer-Related Schemata

	Function	$(\rho: Var \mapsto \mathbb{N}_0; \text{ maps variable to relative address})$	Condition	References
21	$code_L c_i v \rho$	= $\mathbf{ldc} \ a \ \rho(v); \mathbf{inc} \ a \ \rho(c_i)$	$type(c_i) = T; c_i \text{ component in record } v;$	p. 28
			$\rho(c_i) = \sum_{j=1}^{i-1} size(t_j)$ for sizes	
22	$code(\mathbf{new}(x)) \rho$	= $\mathbf{ldc} \ a \ \rho(x); \mathbf{ldc} \ i \ size(t); \mathbf{new}$	if $x$ is a variable of type $\uparrow t$	p. 30
			cf. P-instruction <b>new</b> for upper 2 stack entries	
23	$code_L(xr) \rho$	= $\mathbf{ldc} \ a \ \rho(x); code_M(r) \ \rho$	for name $x$ (variable reference)	p. 31
24	$code_M(.xr) \rho$	= inc $a \rho(x)$ ; $code_M(r) \rho$	for name $x$ (record field section)	p. 31
25	$code_M(\uparrow r) \rho$	= ind $a$ ; $code_M(r) \rho$	(pointer dereferencing)	p. 31
26	$code_M([i]r) \rho$	$= code_{I(d)} [i] g \rho; code_{M}(r) \rho$	component size $g$ of array (array indexing)	p. 31
27	$code_M(\epsilon)$	$=\epsilon$	(empty statement)	p. 31

#### 2.4 Schemata for Procedure and Function Calls

	Function	Condition	References
29	$code \ p(e_1,\ldots,e_k) \ \rho \ st = $ <b>mst</b> $st - st';$	st = nesting depth procedure call	p. 49
	$code_A \ e_1 \  ho \ st;$	st' = nesting depth procedure declaration	steps p. 46
	<u>:</u>	$\rho(p) = (l, st')$	
	$code_A \ e_k \ \rho \ st;$	s = storage requirements actual params	
	$\operatorname{\mathbf{cup}} s \ l;$	l = CODE address of <b>ssp</b> instr. rule $28/30$	
28	$code (proc \ p(specs); \ vdecls; \ pdecls; \ body) \ \rho \ st =$	st = nesting depth procedure declaration	p. 49
	$\operatorname{\mathbf{ssp}} n_{\text{-}}a'';$	storage requirements static part	steps p. 46
	$code_P \ specs \ \rho' \ st;$	storage requirements dynamic part	
	$code_P \ vdecls \ \rho'' \ st;$	create and initialise variables	
	$\operatorname{\mathbf{sep}} k;$	k max. depth local stack	
	$\mathbf{ujp}\ l;$	l = procedure start CODE address	
	$proc\_code;$	code for local procedures	
	$l: code body \rho''' st;$	code for procedure body	
	$\mathbf{ret}[\mathbf{f} \mathbf{p}]$	$(\rho', n_{-}a') = elab\_specs \ specs \ \rho \ 5 \ st$	
	,	$(\rho'', n_{-}a'') = elab\_vdecls\ vdecls\ \rho'\ n_{-}a'\ st$	
		$(\rho''', proc\_code) = elab\_pdecls \ pdecls \ \rho'' \ st$	
30	$code (program \ vdecls; \ pdecls; \ stats) \ \rho_0 =$	$\rho_0$ : all registers initialised to 0; SP to -1	p. 56
	$\operatorname{\mathbf{ssp}} n_{-a};$	SP after organisational block	steps p. 46
	$code_P \ vdecls \ \rho \ 1;$	generate code to fill array descriptors	
	$\operatorname{\mathbf{sep}} k;$	k max. depth local stack	
	$\mathbf{ujp}\ l;$	l = procedure start CODE address	
	$proc\_code;$	code for local procedures	
	$l: code \ stats \  ho' \ st;$	st = 1 nesting depth	
	$\operatorname{stp}$	stop P-machine	
		$(\rho, n_{-}a) = elab\_vdecls\ vdecls\ \rho_0\ 5\ 1$	
		$(\rho', proc\_code) = elab\_pdecls \ pdecls \ \rho \ 1$	
37	$code \text{ (return } [e x]) \rho st = code_R [e x] \rho st;$	T is type of expression $e$ or variable/parameter $x$	
	$\mathbf{str} \ T \ 0 \ 0;$		

#### 2.5 Schemata for Parameter Passing

	Function		Condition	References
31	$code_A \ x \ \rho \ st =$	$code_L \ x \ \rho \ st;$	parameter corresponding to $x$ is $var/reference$ parameter	p. 49
32	$code_A \ e \ \rho \ st =$	$code_R \ e \ \rho \ st;$	parameter corresponding to $e$ is value parameter of scalar type	p. 50
33	$code_A \ x \ \rho \ st =$	$code_L \ x \ \rho \ st;$	parameter corresponding to $e$ is of <b>structured</b> type $t$	p. 50
		movs s;	(record, descriptor) with static $size(t) = s$	
34	$code_P(\mathbf{value}\ x:\ \mathbf{array}[u_1o_1,\ldots,u_k,,o_k]\ \mathbf{of}\ t)\ \rho\ st =$	movd ra	copy the array	p. 52

#### 2.6 Schemata for Access to Variables and Formal Parameters

	Function		Condition	References
35	$code_L(x \ r) \ \rho \ st =$	lda d ra;	$\rho(x) = (ra, st'), d = st - st'$ is difference in nesting	p. 53
		$code_M \ r \ \rho \ st$	depths of applied and defining occurrences	steps p. 46
			local variable or formal value parameter $x$	
36	$code_L(x \ r) \ \rho \ st =$	$\mathbf{lod}\ a\ d\ ra;$	$\rho(x) = (ra, st'), d = st - st'$ is difference in nesting	p. 53
		$code_M \ r \ \rho \ st$	depths of applied and defining occurrences	steps p. 46
			formal var parameter $x$ (by reference)	
!!!	r is a word describing indexing, selection or dereferencing: $cf$ . 23 – 27			