$$-rac{\mathrm{d}^2 y_n}{\mathrm{d}oldsymbol{x}^2} + oldsymbol{x} y_n = \lambda_n y_n$$

on 
$$0 \le x \le \infty$$
, with  $y(0) = y(\infty) = 0$ .

To this equation the solution is:

$$y_n = C_1 \operatorname{Ai}(x + \lambda_n)$$

Where  $C_1$  is an arbitrary constant, and  $\lambda_n$  are the zeros of the Airy function,  $\operatorname{Ai}(x)$ , on the negative x axis (e.g.  $\lambda_1 \approx -2.338$ ).

To numerically integrate this solution let us use a Chebyshev spectral method. If  $t_m$  comprises points on the Chebyshev extrema grid, that is:

$$t_m = -\cos(\frac{\pi m}{N}), \qquad n \in [0, 1, 2, ..., N]$$

then:

$$x_m = L\left(\frac{1+t_m}{1-t_m}\right)$$

.

This is a rational transformation from the Chebyshev extrema grid to the semi-infinite domain.