

7/3 Recap

$$\begin{aligned} &\text{Karatsuba}(12, 34, 2) \\ &m = 1 \\ &12 = 10^1 \quad a = 1 \\ &\quad \quad \quad b = 2 \\ &\quad \quad \quad c = 3 \\ &\quad \quad \quad d = 4 \end{aligned}$$

Selection Sort $O(n^2)$

Merge Sort ~~$O(n^2)$~~ $O(n \log_2 n)$ from $T(n) = 2 \cdot T(n/2) + Cn$

Correctness of Mergesort? Lecture #5

Integer Multiplication w/ Karatsuba $O(n^{1.58}) > O(n^2)$

MASTER THEOREM for divide & conquer algo's

$$T(n) = a \cdot T(n/b) + Cn^d$$

$$\text{if } \frac{a}{b^d} > 1 \rightarrow T(n) = \Theta(n^{\log_b a})$$

$$= 1 \rightarrow \Theta(n^d \log n)$$

$$< 1 \rightarrow \Theta(n^d)$$

Binary Search

$$\Theta(\log n)$$

18 7 3 10 | 11 6 14 20

3 7 10 18 6 11 14 20

FSM

$O(n)$

$$a = 16 \quad b = 4 \quad d = 1$$

$$\frac{16}{4^1} = 4$$

$$\log_4 16$$