

## Conversione da decimale a floating point

- Convert 2.625 to our 8-bit floating point format.
  - A. The integral part is easy,  $2_{10} = 10_2$ . For the fractional part:
 

|                         |             |  |
|-------------------------|-------------|--|
| $0.625 \times 2 = 1.25$ | $\boxed{1}$ | Generate 1 and continue with the rest. |
| $0.25 \times 2 = 0.5$   | $\boxed{0}$ | Generate 0 and continue.               |
| $0.5 \times 2 = 1.0$    | $\boxed{1}$ | Generate 1 and nothing remains.        |

 So  $0.625_{10} = 0.101_2$ , and  $2.625_{10} = 10.101_2$ .
  - B. Add an exponent part:  $10.101_2 = 10.101_2 \times 2^0$ .
  - C. Normalize:  $10.101_2 \times 2^0 = 1.0101_2 \times 2^1$ .
  - D. Mantissa: 0101
  - E. Exponent:  $1 + 3 = 4 = 100_2$ .
  - F. Sign bit is 0.
 The result is  $\boxed{0} \boxed{100} \boxed{0101}$ . Represented as hex, that is  $45_{16}$ .
- Convert -4.75 to our 8-bit floating point format.
  - a. The integral part is  $4_{10} = 100_2$ . The fractional:
 

|                       |             |  |
|-----------------------|-------------|--|
| $0.75 \times 2 = 1.5$ | $\boxed{1}$ | Generate 1 and continue with the rest. |
| $0.5 \times 2 = 1.0$  | $\boxed{1}$ | Generate 1 and nothing remains.        |

 So  $4.75_{10} = 100.11_2$ .
  - b. Normalize:  $100.11_2 = 1.0011_2 \times 2^2$ .
  - c. Mantissa is 0011, exponent is  $2 + 3 = 5 = 101_2$ , sign bit is 1.
 So -4.75 is  $\boxed{1} \boxed{101} \boxed{0011} = d3_{16}$

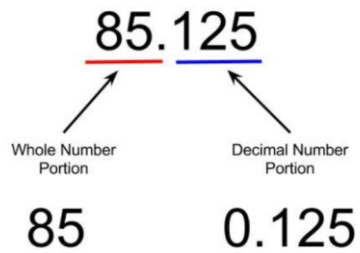
## Conversione da formato floating point a decimale

- Convert the 8-bit floating point number e7 (in hex) to decimal.
  - A. Convert:  $e7_{16} = 11100111_2$ .
  - B. Separate:  $\boxed{1} \boxed{110} \boxed{0111}$
  - C. Mantissa: 1.0111
  - D. Exponent:  $110_2 = 6_{10}$ ;  $6 - 3 = 3$ .
  - E. De-normalize:  $1.0111_2 \times 2^3 = 1011.1$
  - F. Convert:
 

|              |       |       |       |       |              |
|--------------|-------|-------|-------|-------|--------------|
| Exponents    | $2^3$ | $2^2$ | $2^1$ | $2^0$ | $2^{-1}$     |
| Place Values | 8     | 4     | 2     | 1     | 0.5          |
| Bits         | 1     | 0     | 1     | 1     | . 1          |
| Value        | 8     |       | + 2   | + 1   | + 0.5 = 11.5 |
  - G. Sign: negative.
 Result: e7 is -11.5
- Convert the 8-bit floating point number 26 (in hex) to decimal.
  - a. Convert and separate:  $26_{16} = \boxed{0} \boxed{010} \boxed{0110}_2$
  - b. Exponent:  $010_2 = 2_{10}$ ;  $2 - 3 = -1$ .
  - c. Denormalize:  $1.011_2 \times 2^{-1} = 0.1011$ .
  - d. Convert:
 

|              |       |          |          |          |                   |
|--------------|-------|----------|----------|----------|-------------------|
| Exponents    | $2^0$ | $2^{-1}$ | $2^{-2}$ | $2^{-3}$ | $2^{-4}$          |
| Place Values | 1     | 0.5      | 0.25     | 0.125    | 0.0625            |
| Bits         | 0     | . 1      | 0        | 1        | 1                 |
| Value        |       | 0.5      |          | + 0.125  | + 0.0625 = 0.6875 |
  - e. Sign: positive
 Result: 26 is 0.6875.

## Decimale a floating point IEEE 754 (step by step)

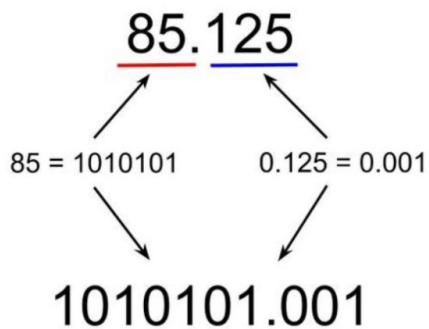


| Whole Number Division | Result | Remainder |
|-----------------------|--------|-----------|
| 85/2                  | 42     | 1         |
| 42/2                  | 21     | 0         |
| 21/2                  | 10     | 1         |
| 10/2                  | 5      | 0         |
| 5/2                   | 2      | 1         |
| 2/2                   | 1      | 0         |
| 1/2                   | 0      | 1         |

$$85 = 1010101$$

| Decimal Number Multiplication | Result | Number in front of decimal |
|-------------------------------|--------|----------------------------|
| 0.125 x 2                     | 0.25   | 0                          |
| 0.25 x 2                      | 0.5    | 0                          |
| 0.5 x 2                       | 1.0    | 1                          |
| 0.0 x 2                       | 0.0    | 0                          |

$$0.125 = 001$$



1010101.001

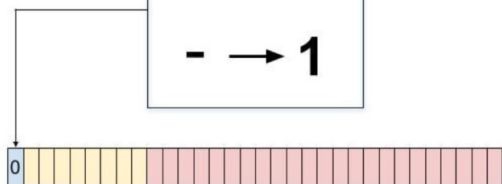
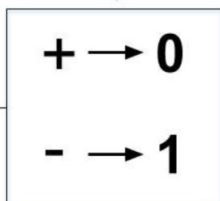


Move decimal 6 places

1.010101001 x 2<sup>6</sup>

step 1

Sign



1.010101001 x 2<sup>6</sup>

$$127 + 6 = 133$$

| Whole Number Division | Result | Remainder |
|-----------------------|--------|-----------|
| 133/2                 | 66     | 1         |
| 66/2                  | 33     | 0         |
| 33/2                  | 16     | 1         |
| 16/2                  | 8      | 0         |
| 8/2                   | 4      | 0         |
| 4/2                   | 2      | 0         |
| 2/2                   | 1      | 0         |
| 1/2                   | 0      | 1         |



133 = 10000101

Exponent



1.010101001 x 2<sup>6</sup>

Mantissa



85.125

