

Office

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Question

JT2012XXX asked on May 14, 2012

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How can I add in a hyperbolic regression curve in Excel 2010?

Original Title: "hyperbolic curve"

In addition to Linear, Polynomial selections in Excel - we would like the option to add-in a Hyperbolic regression curve.

Is there a Template that exists with this option? or other instructions welcome!

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Answer

E.J. GUN replied on May 14, 2012

★ [Community Star](#)

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A hyperbolic curve of the form $y = (m \cdot x) / (k + x)$ has a discontinuity at $x = -k$. This prevents a "traditional" curve fitting of the entire curve, but you can easily fit the curve if you transform the equation into a linear version, solve for the linearized coefficients, and then use those coefficients to fit the non-linear data. Steps to take:

1. Instead of fitting $y = (m \cdot x) / (k + x)$, you will transform the equation into $(1/y) = (1/m) + (k/m) \cdot (1/x)$.
2. Now you have two new coefficients, $A = (1/m)$ and $B = (k/m)$, and two new variables $(1/y)$ and $(1/x)$.
3. The new equation becomes $(1/y) = A + B \cdot (1/x)$. You can run a linear regression on this equation, using the (x, y) set of data you are trying to fit, to solve for the coefficients A and B.
4. Once you have A and B, you can solve for m and k:
 $m = 1/A$
 $k = m \cdot B$
5. Use the coefficients m and k to calculate the fitted curve.

You have to watch for and handle discontinuities ($x = 0$, $y = 0$, $x = k$, etc).

HTH,
Eric

P.S. - this can all be done with equations on a worksheet, or with VBA

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Answer

Gary's Student replied on May 14, 2012

MVP ★ [Community Star](#)

0 Found this helpful
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While not a template, here is an example of GUN's solution. Say the x values are in column A (A1 thru A10) and the y values are in column B (B1 thru B10):

```
1 0.500000
2 0.933333
3 1.312500
4 1.647059
5 1.944444
```

In C1 enter:
 =1/A1 and copy down
 In D1 enter:
 =1/B1 and copy down
 Cols C & D display:
 1.000000 2.000000
 0.500000 1.071429
 0.333333 0.761905
 0.250000 0.607143
 0.200000 0.514286
 0.166667 0.452381
 0.142857 0.408163
 0.125000 0.375000
 0.111111 0.349206
 0.100000 0.328571

To do a linear fit to cols C & D, in E1 enter:
 =SLOPE(D1:D10,C1:C10)
 In E2 enter:
 =INTERCEPT(D1:D10,C1:C10)
 This displays:
 1.857143
 0.142857

Finally to calculate m and k, in F1 enter:
 =1/E2
 and in F2 enter:
 =F1*E1
 F1 and F2 display
 7
 13

The fit is then

$$y = (7 * x) / (13 + x)$$

GSNU201305

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Answer

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EJ. GUN replied on May 14, 2012 ▼

★ Community Star

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```
1 0.500000
2 0.933333
3 1.312500
4 1.647059
5 1.944444
6 2.210526
7 2.450000
8 2.666667
9 2.863636
10 3.043478
```

In C1 enter:

=1/A1 and copy down

In D1 enter:

=1/B1 and copy down

Cols C & D display:

```
1.000000 2.000000
0.500000 1.071429
0.333333 0.761905
0.250000 0.607143
0.200000 0.514286
0.166667 0.452381
0.142857 0.408163
0.125000 0.375000
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7
13
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