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## Worksheet 09

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## **Topics**

- Clustering Review
- Clustering Aggregation

## **Clustering Aggregation**

| Point | C | P |
|-------|---|---|
| Α     | 0 | а |
| В     | 0 | b |
| С     | 2 | b |
| D     | 1 | С |
| Е     | 1 | d |

a) Fill in the following table where for each pair of points determine whether C and P agree or disagree on how to cluster that pair.

| Pair | Disagreement |
|------|--------------|
| АВ   | 1            |
| АС   | 0            |
| A D  | 0            |
| ΑE   | 0            |
| ВС   | 1            |
| ВD   | 0            |
| ВЕ   | 0            |
| CD   | 0            |

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| Pair | Disagreement |  |  |  |
|------|--------------|--|--|--|
| C E  | 0            |  |  |  |
| DE   | 1            |  |  |  |

As datasets become very large, this process can become computationally challenging.

b) Given N points, what is the formula for the number of unique pairs of points one can create?

The formula is "n(n-1)/2"

Assume that clustering C clusters all points in the same cluster and clustering P clusters points as such:

| Point | P |
|-------|---|
| Α     | 0 |
| В     | 0 |
| С     | 0 |
| D     | 1 |
| Е     | 1 |
| F     | 2 |
| G     | 2 |
| Н     | 2 |
| I     | 2 |

c) What is the maximum number of disagreements there could be for a dataset of this size? (use the formula from b)?

$$(9*(9-1))/2 = 36$$

d) If we look at cluster 0. There are  $(3 \times 2) / 2 = 3$  pairs that agree with C (since all points in C are in the same cluster). For each cluster, determine how many agreements there are. How many total agreements are there? How many disagreements does that mean there are between C and P?

For cluster 0, there are 3 agreements (A, B, C). For cluster 1, (2x1)/2=1. For cluster 2, (4x3)/2=6. Hence the total agreement is 10. For total disagreement, we do 36-10=26 disagreements.

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e) Assuming that filtering the dataset by cluster number is a computationally easy operation, describe an algorithm inspired by the above process that can efficiently compute disagreement distances on large datasets.

Aggregate clustering, k-means

| In [ ]: |  |  |  |
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