

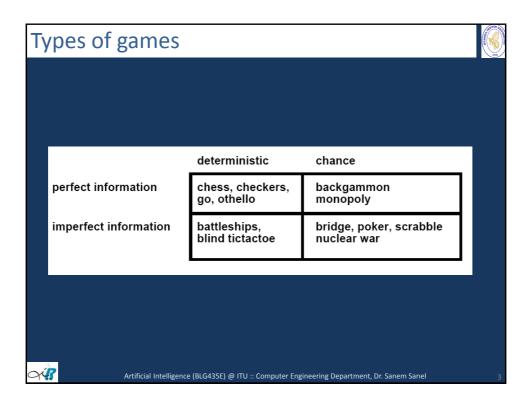
### Al Games



- Agents' goals are in conflict
- Two players: MAX and MIN
- MAX moves first and they take turns until the game is over
- At the end of the game
  - points are awarded to the winner
  - penalties are given to the loser
- Zero-sum games

OU!

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# Deep Blue



- Against Garry Kasparov
  - 1996, in 1997 won
  - Massively parallel, P2SC-based system with 30-nodes
    - each node containing a 120 MHz P2SC microprocessor
    - Written in C and ran under the AIX OP.
    - · Capable of evaluating 200 million positions per second
    - search to a depth of 14 moves, to a maximum of twenty or even more moves in some situations
- · Junior is the last champion
  - International Computer Chess Tournament



OUR

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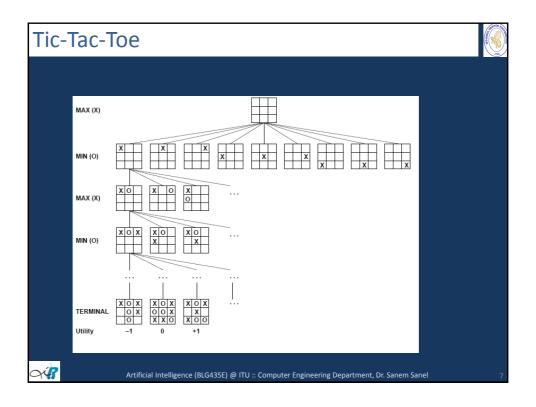
### Game formulation

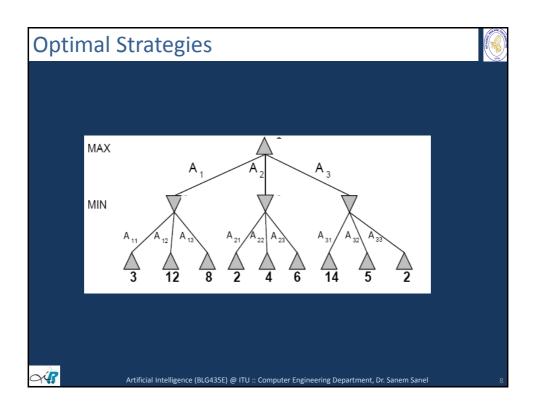


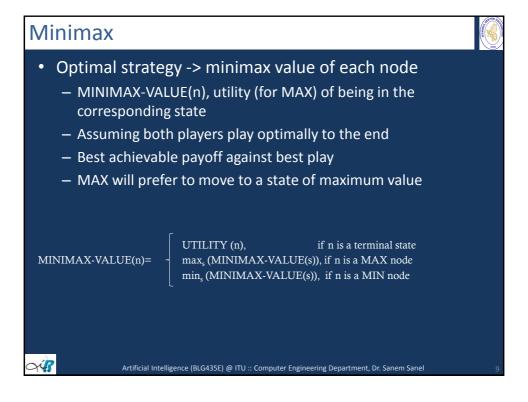
- A game is formally defined
  - initial state
  - successor function
  - terminal test (terminal state)
  - utility function (objective, payoff)
- Game tree: the initial state and the legal moves
- ply: the depth of the search tree (ply of lookahead)

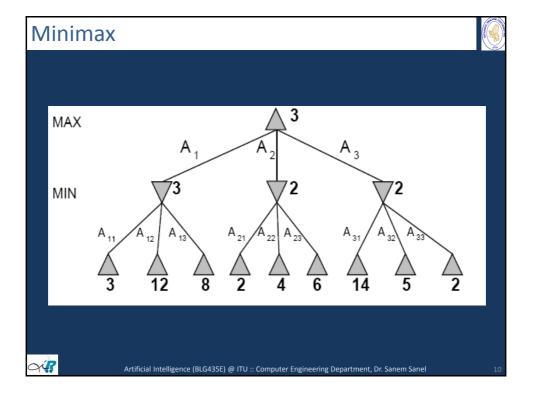


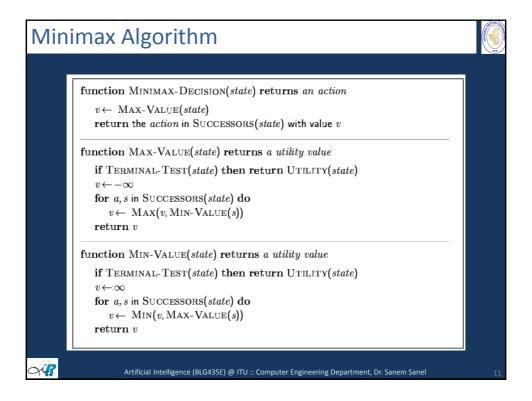
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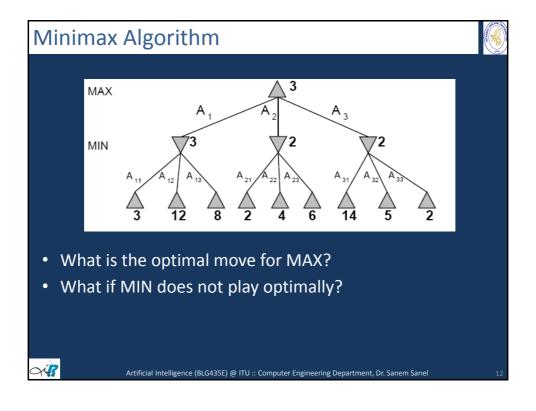












# **Properties of Minimax**



- Complete?
- Optimal?
- Time complexity?
- Space complexity?



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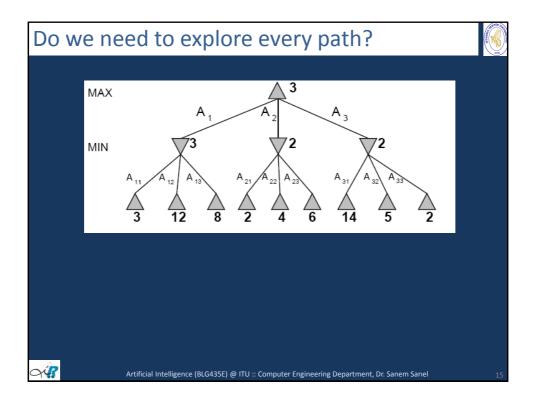
# **Properties of Minimax**

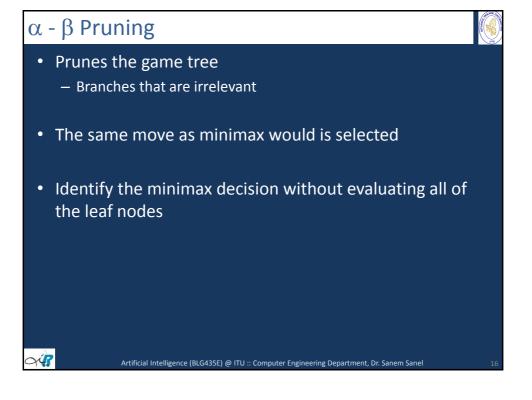


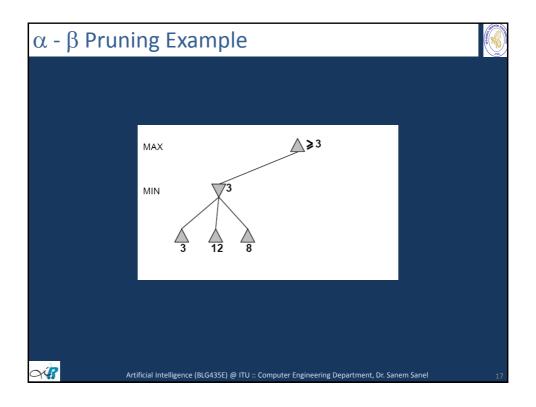
- Complete? Yes, if tree is finite (chess has specific rules for this)
- Optimal? Yes, against an optimal opponent. Otherwise??
- Time complexity? O(b<sup>m</sup>)
- Space complexity? O(bm)
- For chess,  $b \approx 35$ ,  $m \approx 100$  for "reasonable" games
  - exact solution completely infeasible
- Do we need to explore every path?

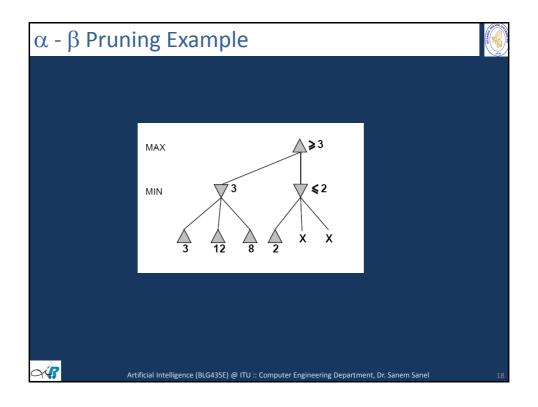


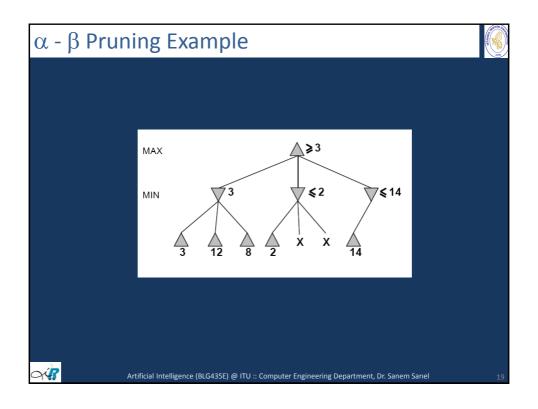
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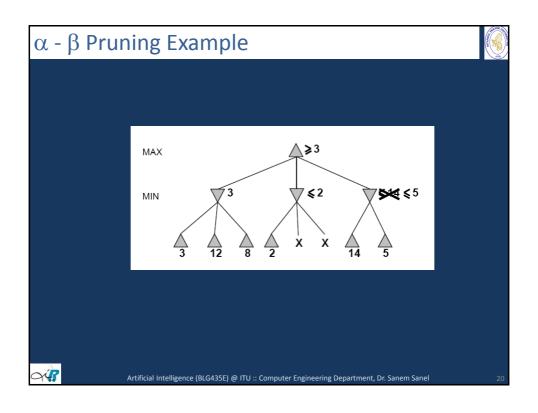


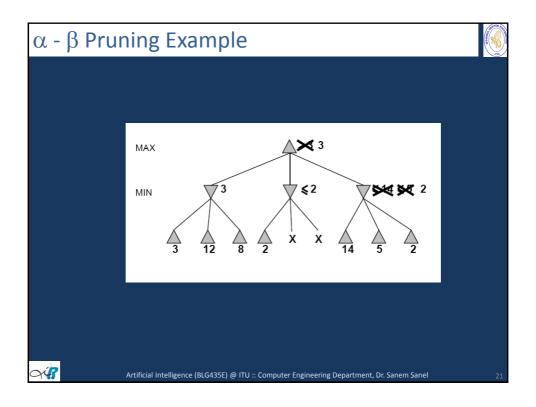


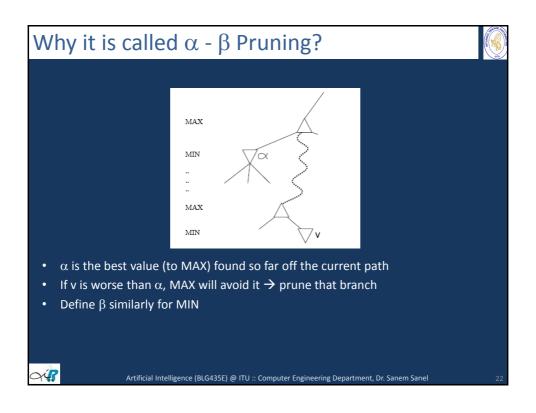


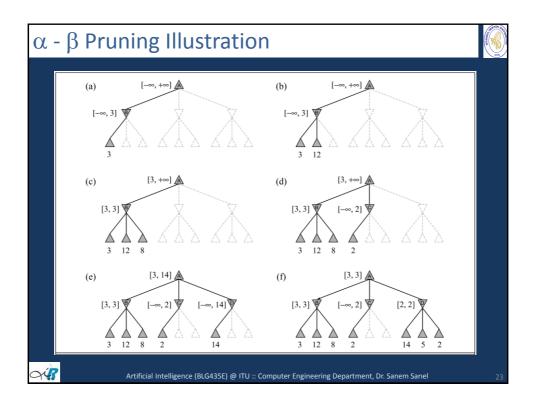


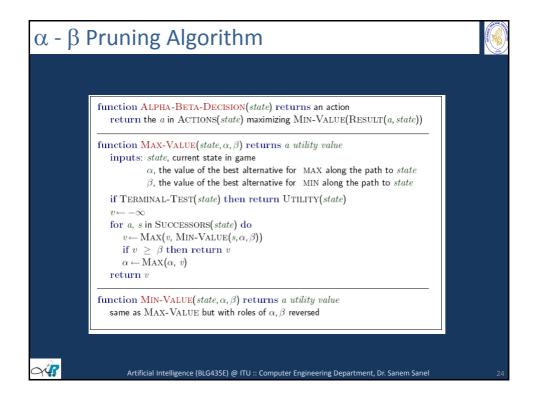












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function Min-Value(state, \alpha, \beta) returns a utility value inputs: state, current state in game \alpha, the value of the best alternative for Max along the path to state \beta, the value of the best alternative for Min along the path to state if Terminal-Test(state) then return Utility(state) v \leftarrow +\infty for a, s in Successors(state) do v \leftarrow \text{Min}(v, \text{Max-Value}(s, \alpha, \beta)) if v \leq \alpha then return v \beta \leftarrow \text{Min}(\beta, v) return v
```

# Properties of $\alpha$ - $\beta$ Algorithm



- · Pruning does not affect the final result
- Good move ordering improves effectiveness of pruning
- With "perfect ordering", time complexity : O(bm/2)
  - doubles solvable depth
- Unfortunately, 35<sup>50</sup> is still impossible!

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### **Resource Limits**



- Shannon's 1950 paper: Programming a computer for playing chess
  - Use CUTOFF-TEST instead of TERMINAL-TEST
    - · depth limit
  - Use EVAL instead of UTILITY
    - evaluation function that estimates desirability of position



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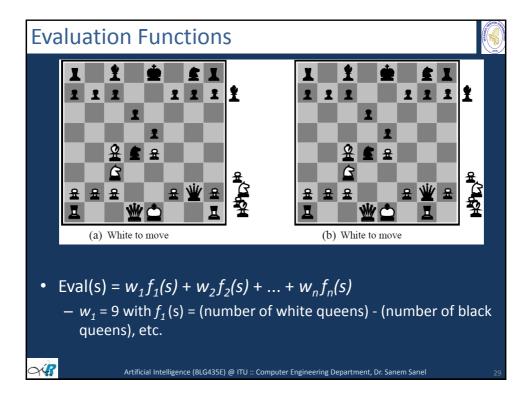
### **Evaluation Functions**

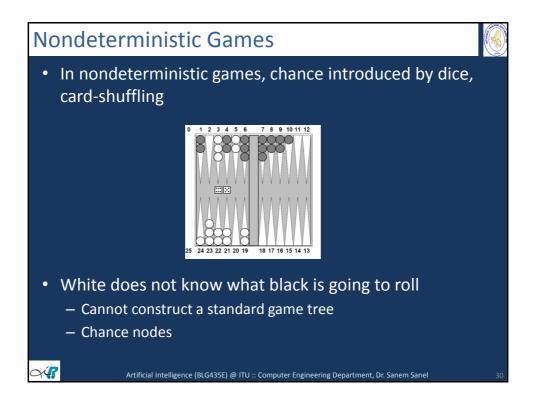


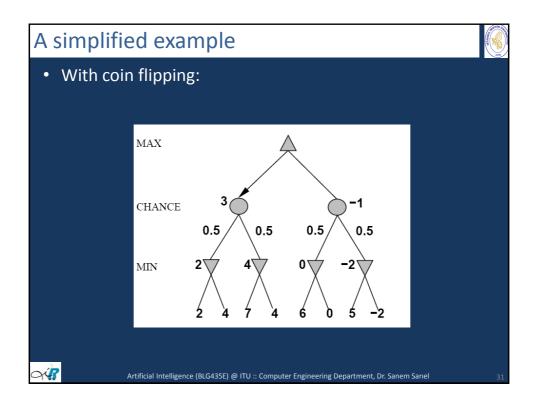
- Estimate of the expected utility of the game
- The performance is dependent on the quality of the evaluation function
- The evaluation function
  - Should give higher scores to better positions
  - Should order the terminal states as the utility function
  - Computation must not take too long
  - For non-terminal states the evaluation function should be correlated with the actual chances of winning

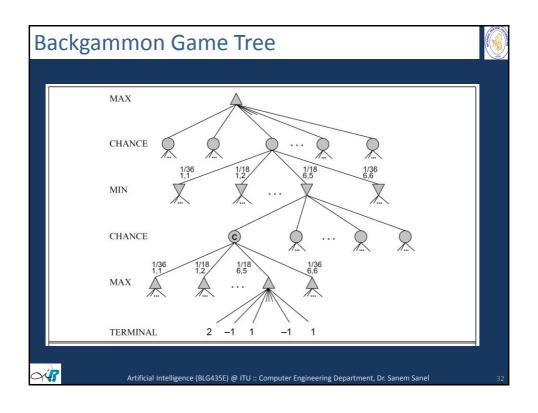


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# Algorithm for nondeterministic games EXPECTIMINIMAX gives perfect play Just like MINIMAX, except we must also handle chance nodes: if state is a MAX node then return the highest EXPECTIMINIMAX-Value of SUCCESSORS(state) if state is a MIN node then return the lowest EXPECTIMINIMAX-Value of SUCCESSORS(state) if state is a chance node then return average of EXPECTIMINIMAX-Value of SUCCESSORS(state)

