A Solidity-to-CPN Approach Towards Formal Verification of Smart Contracts Extended Content

This document contains complementary content for the paper "A Solidity-to-CPN Approach Towards Formal Verification of Smart Contracts" in which we propose an algorithm for the transformation of a smart contract written in Solidity into a hierarchical Coloured Petri Net model over which temporal properties can be verified. In section 1, we remind the reader of the use case presented in the paper. Section 2 starts by a reminder of the different elements of the CPN model to be generated then presents the full algorithm with detailed descriptions of its different parts followed by an example of its application on the use case. More details on using CPN Tools and Helena for the verification of the model are presented in Section 3. Section 4 concludes the document.

1 Use Case: Blind Auction

The use case presented in this section is adapted from an example in [1]. Participants in a blind auction have a bidding window during which they can place their bids. A participant can place more than one bid as long as the bidding window is still open. The placed bid is blinded in the sense that only a hashed value is submitted at this stage, and yet it is still binding because the bidder has to make a deposit along the blinded bid, with a value that is supposedly greater than that of the real bid. Once the bidding window is closed, the revealing window is opened. During this stage of the auction, participants with at least one placed bid proceed to reveal them. Revealing a bid consists in the participant sending the actual value of the bid along with the key used in its hash, and the system verifying whether the sent values do correspond with the previously placed blinded bid and potentially updating the highest bid and bidder's values accordingly. If the revealed value of a bid does not correspond with its blinded value, or is greater than the deposit made previously along the blinded bid, the said bid is considered invalid. Once the revealing window is closed, every bid left unrevealed is discarded from the auction. Participants can then proceed to withdraw their deposits. A deposit made along a non-winning, invalid or unrevealed bid is wholly restored. In case of a winning bid, the difference between the deposit and the real value of the bid is restored. The auction is considered to be terminated when all participants withdraw their deposits. Figure 1 describes the workflow of the blind auction system and Listing 1.1 represents the Solidity smart contract implementing it.

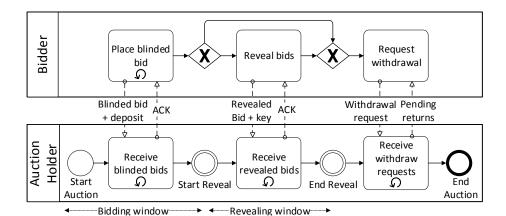


Fig. 1: Blind Auction Workflow

```
contract BlindAuction {
    struct Bid {
        bytes32 blindedBid;
        uint deposit;}
    uint public biddingEnd;
    uint public revealEnd;
    mapping(address => Bid[]) public bids;
    address public highestBidder;
    uint public highestBid;
    mapping(address => uint) pendingReturns;
    modifier onlyBefore(uint _time) {require(now<_time);_;}</pre>
    modifier onlyAfter(uint _time) {require(now>_time);_;}
    constructor(uint _biddingTime, uint _revealTime) public {
        biddingEnd = now + _biddingTime;
        revealEnd = biddingEnd + _revealTime;}
    function bid(bytes32 _blindedBid) public payable
       onlyBefore(biddingEnd) {
        bids[msg.sender].push(Bid({blindedBid: _blindedBid,
           deposit: msg.value}));}
    function reveal(uint[] values, bytes32[] secrets) public
       onlyAfter(biddingEnd) onlyBefore(revealEnd) {
        require (values.length == secrets.length);
        for(uint i = 0; i < values.length && i < bids[msg.</pre>
           sender].length; i ++) {
            var bid = bids[msg.sender][i];
            var (value, secret) = (values[i], secrets[i]);
            if(bid.blindedBid == keccak256(value, secret) &&
                bid.deposit >= value && value > highestBid) {
                highestBid = value;
                highestBidder = msg.sender;}}
    function withdraw() public onlyAfter
```

```
(revealEnd) {
  uint amount = pendingReturns[msg.sender];
  if (amount > 0) {
    if (msg.sender != highestBidder)
        msg.sender.transfer(amount);
    else
        msg.sender.transfer(amount - highestBid);
    pendingReturns [msg.sender] = 0;}}
```

Listing 1.1: Blind Auction smart contract in Solidity

2 Solidity-to-CPN Transformation

This section represents the core of our contribution. Herein we propose an algorithm that transforms a Solidity smart contract into a hierarchical CPN model over which CTL properties can be verified (cf. Section 3). The general idea here is to start from a CPN model representing the general workflow of the smart contract (we refer to this as the level-0 model) and then to build on it by embedding it with submodels representing the execution of the smart contract functions (we refer to these submodels as level-1 models). In a level-0 model, we distinguish 2 parts, namely the user's behaviour part which models the way users can interact with the system and the smart contract's behaviour part which represents the system. These two are linked via communication places. Figure 2 shows the level-0 model of the previously described blind auction use case. The submodels corresponding to the transitions represented in green will be detailed in Section 2.3.

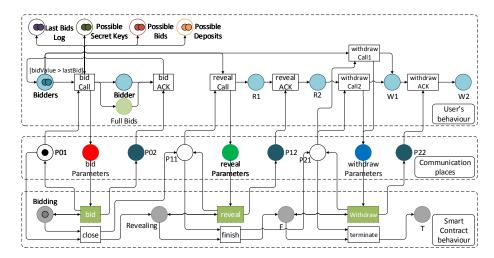


Fig. 2: Blind Auction - Level-0 Model

We lead off by setting some notations on the elements of the model in Section 2.1 before getting into the algorithm in Section 2.2 and applying it on the use case in Section 2.3.

2.1 Notations on the Model's Elements

Places P

- In the Smart Contract's Behaviour part, we define state places P_S as places that hold the state of the smart contract, namely the contract's balance and the values of the state (global) variables. Their colour is as follows [uint: contractBalance, type₁: stateVariable₁, ..., type_n: stateVariable_n]
- Among communication places, we distinguish:
 - parameter places P_P : that convey potential inputs of function calls along with the caller's information and the transferred value. Their colour is as follows [address: sender, uint: balance, uint: value, type₁: inputParameter₁, ..., type_n: inputParameter_n]
 - return places P_R : that communicate potential returned data from functions along with the caller's updated information. Their colour is as follows [address: sender, uint: balance, type_R: returnParameter]
 - interface places P_I : that handle handovers between the function calls and their execution. They are uncoloured (basic) places.
- On level 1 (a transition's detailed sub-model), we distinguish 2 types of places:
 - control flow places P_{cf} . Their colour is a metaColour defined at each transition of level 0 as the concatenation of the colour of its input control flow place • $t[cf] \in P_S$ and the colour of its input parameters place • $t[input] \in P_P$.
 - data places P_{data} (for internal local variables) where each place is of a colour corresponding to the represented variable's type.
- For a place $p \in P$, we can access its identifier (p.name) and its colour (p.colour)

Transitions T For a transition $t \in T$ we distinguish:

- $\bullet t[cf] \in P_{cf} \cup P_S$, the input control flow place of t
- $-\bullet t[input] \in P_P$, the input parameters place of t
- $\bullet t[com] \in P_C$, the input communication place of t
- $-\bullet t^{[}data] \subseteq P_{data}$, the input data places of t (in case of a submodel transition) item $t \bullet [cf] \in P_{cf} \cup P_S$, the output control flow place of t
- $-t \bullet [output] \in P_R$, the output return place of t
- $-t \bullet [data] \subseteq P_{data}$, the output data places of t (in case of a submodel transition)
- $-t \bullet [com] \in P_C$, the output communication place
- $-t^{action} \in S$: action of t (the function's body)

Statements S A statement $st \in \mathbb{S}$ can be either a compound statement $\{st[1]; st[2]; \ldots; st[N]\}$, where st[i] is a statement, or a simple statement (st_{LHS}, st_{RHS}) , or a control statement. A simple statement can be:

- an assignment statement, where we can access:
 - the assigned variable $st_{LHS}.var$
 - the set of variables used in the assignment expression $st_{RHS}.vars$ (can be empty)
- a variable declaration statement, with:
 - the declared variable $st_{LHS}.var$
 - the type of the variable $st_{LHS}.type$
 - the set of variables used in the variable initialization $st_{RHS}.vars$ (can be empty if no initialization is given)
- a sending statement, where we can access:
 - the destination account $st_{LHS}.var$
 - the set of variables in the expression of the value sent $st_{RHS}.vars$ (can be empty)
- a returning statement (st_{LHS} is empty), with:
 - the variables in the expression of the returned value $st_{RHS}.vars$ (can be empty)

A control statement can be:

- a requirement statement of the form require(c)
- a selection statement which can have:
 - a single-branching form: if(c) then st_T
 - a double-branching form: if(c) then st_T
- a looping statement which can be:
 - a for loop: for(init; c; inc) st_T
 - a while loop: $while(c) st_T$

where c is a boolean expression in which we can access the set of used variables c.variables.

2.2 Transformation Algorithm

The goal of our proposed algorithm is to generate a hierarchical CPN model that extends the level-0 model by level-1 submodels that correspond to the functions of the smart contract in question. To do so, EXTENDMODEL is applied on the level-0 model.

extendModel

```
1: procedure EXTENDMODEL(P_{CPN} = (P,T,A,\Sigma,V,C,G,E,I))
        Input: level-0 CPN model
 2:
 3:
        Output: hierarchical level-0 CPN model extended with level-1 sub-models
        for transition t \in T do
 4:
            metaColour \leftarrow [\bullet t[cf].colour, \bullet t[input].colour]
 5:
 6:
            P_{data} \leftarrow \emptyset
            getLocalVariables(t^{action}, P_{data})
 7:
            insertSubModel(t, P_{CPN})
 8:
        end for
 9:
10: end procedure
```

Extending the initial model with the submodel of a transition t comprises 3 main steps:

- defining a colour metaColour that is the concatenation of the colour of the state places in the global model with that of the input parameters place of transition t (line 5)
- creating the set of places corresponding to local var-iables in the function of transition t (lines 6 and 7)
- inserting the submodel of transition t into the level-0 model model (line 8)

getLocalVariables

```
1: procedure GETLOCALVARIABLES(st, P<sub>data</sub>)
 2:
       Input: statement st
       Output: P_{data} set of places corresponding to local variables in the state-
 3:
       ment st
 4:
       if st is a variable declaration statement then
 5:
           create place p with p.name \leftarrow st_{LHS}.variable and p.colour \leftarrow st_{LHS}.type
           P_{data}.add(p)
 6:
       else if st is a selection statement then
 7:
           getLocalVariables(st_T, P_{data})
 8:
 9:
           if st is a selection statement: if(c) then st_T else st_F then
10:
               getLocalVariables(st_F, P_{data})
           end if
11:
       else if st is a looping statement then
12:
           if st is a for statement: for(init; c; inc)st_T then
13:
               getLocalVariables(init, P_{data})
14:
               getLocalVariables(st_T, P_{data})
15:
16:
           else if st is a while statement: while(c)st_T then
17:
               getLocalVariables(st_T, P_{data})
           end if
18:
       else if st is a compound statement \{st[1]; st[2]; \ldots; st[N]\} then
19:
20:
           for i = 1..N do
21:
               getLocalVariables(st[i], P_{data})
22:
           end for
```

23: end if24: end procedure

GETLOCALVARIABLES creates a set of places to be used in the submodel of a transition t, corresponding to the local variables used in its function. To do so, the statements in the function's body are recursively investigated in search for variable declaration statements. For each variable declaration statement found, a place bearing the name of the variable and its type as its name and colour is created and added to the set P_{data} (lines 5 and 6). In addition to standalone variable declarations, we note that we can also find variables declared in the initialization of a For loop.

We opt for the construction of this set of places beforehand, as opposed to on the fly during the construction of the submodel, for the following reason. In Solidity, a variable can be used before its declaration (as long as a declaration does exist). Creating its corresponding place on the fly while creating the submodel of a transition would consequently require testing for its existence every time the variable is used in a statement, as the creation of the place in question may have to happen prior to the declaration statement, in any other statement using it (as part of st_{LHS} or st_{RHS}) for the first time. On this account, we judge it more efficient to sweep the code first for the construction of P_{data} .

insertSubModel

- hiding t (line 4)

model (lines 6-16) by:

- creating the submodel for t (line 5)

```
1: procedure insertSubModel(t, P<sub>CPN</sub>)
 2:
        Input: transition t and CPN model P_{CPN}
 3:
        Output: CPN model embedded with the level-1 submodel for t
        hide transition t
 4:
        subModel = CREATESUBMODEL(t; t^{action}; \bullet t[cf]; t \bullet [cf]; P_{data}; metaColour)
 5:
        for t' \in subModel.T do
 6:
 7:
            if \bullet t'[cf] = \bullet t[cf] then
                create arc from \bullet t[input] to t'
 8:
 9:
            end if
            if t' \bullet [cf] = t \bullet [cf] then
10:
                create arc from t' to t \bullet [com]
11:
                if t'^{action} is not a returning statement then
12:
                   create arc from t' to t \bullet [output] (with inscription [inInsc.sender],
13:
                    inInsc.balance
                end if
14:
15:
            end if
        end for
16:
17: end procedure
Replacing a transition t by its corresponding submodel comprises 3 main steps:
```

- connecting the created submodel to the places connected to t in the level-0

- connecting the input parameters place of transition t to the input transitions of its submodel (lines 7-9)
- connecting the output transitions of the submodel of t to its output communication place and its output return place in case t^{action} does not include a returning statement (lines 10-15). We note that otherwise the connection to the output return place is established as part of the execution of CREATESUBMODEL.

createSubModel

```
1: procedure CREATESUBMODEL(t; st; p<sub>in</sub>; p<sub>out</sub>; P<sub>data</sub>; metaColour)
        Input: transition t, statement st, control flow input place p_{in}, cont-
        rol flow output place p_{out}, set of internal data places P_{data}, meta colour
        metaColour
        Output: submodel of transition t
 3:
 4:
        set default place colour to metaColour
       if st is a compound statement \{st[1]; st[2]; ...; st[N]\} then
 5:
            for i = 1..N - 1 do
 6:
 7:
               create place p_i
 8:
            end for
 9:
            CREATESUBMODEL (t; st[1]; p_{in}; p_1; P_{data}; meta-Colour)
            for i = 2..N - 1 do
10:
               CREATESUBMODEL(t;st[i];p_{i-1};p_i;P_{data}; metaColour)
11:
12:
            end for
13:
            CREATESUBMODEL (t; st[N]; p_{N-1}; p_{out}; P_{data}; metaColour)
        else if st is a simple statement then
14:
15:
            if st is an assignment statement then
               create transition t'
16:
17:
               create arc from p_{in} to t'
               for v \in st_{RHS}.variables \setminus \{st_{LHS}.variable\} do
18:
                   create arc from P_{data}[v] to t'
19:
                   create arc from t' to P_{data}[v]
20:
21:
               end for
               if st_{LHS}.variable is a local variable then
22:
23:
                   create arc from P_{data}[st_{LHS}.variable] to t'
                   create arc from t' to P_{data}[st_{LHS}.variable] with inscription
24:
                   st_{RHS}
                   create arc from t' to p_{out}
25:
               else
26:
27:
                   create arc from t' to p_{out} with inscription outInsc \leftarrow inInsc in
                   which the variable corresponding to st_{LHS}.variable is replaced
                   by st_{RHS}
               end if
28:
29:
            else if st is a variable declaration statement then
30:
               create transition t'
               create arc from p_{in} to t'
31:
```

```
32:
                for v \in st_{RHS}.variables do
                    create arc from P_{data}[v] to t'
33:
                    create arc from t' to P_{data}[v]
34:
                end for
35:
                create arc from t' to P_{data}[st_{LHS}.variable] with inscription st_{RHS}
36:
37:
                create arc from t' to p_{out}
            else if st is a sending statement then
38:
                create transition t'
39:
40:
                create arc from p_{in} to t'
                for v \in st_{RHS}.variables do
41:
                    create arc from P_{data}[v] to t'
42:
                    create arc from t' to P_{data}[v]
43:
44:
                create arc from t' to p_{out} with inscription outInsc \leftarrow inInsc in
45:
                which the variable corresponding to the sender's (respectively the
                contract's) balance is incremented (respectively decremented) by
                st_{RHS}
            else if st is a returning statement then
46:
                create transition t'
47:
                create arc from p_{in} to t'
48:
                for v \in st_{RHS}.variables do
49:
                    create arc from P_{data}[v] to t'
50:
51:
                    create arc from t' to P_{data}[v]
                end for
52:
                create arc from t' to t \bullet [cf]
53:
                create arc from t' to t \bullet [output] with inscription outInsc \leftarrow [inInsc.sender],
54:
                inInsc.balance, st_{RHS}
55:
            end if
        else if st is a control statement then
56:
57:
            if st is a requirement statement: require(c) then
                create transition t_{revert} with guard !c
58:
                create arc from p_{in} to t_{revert}
59:
                create arc from t_{revert} to \bullet t[cf]
60:
                for v \in c.variables do
61:
                    create arc from P_{data}[v] to t_{revert}
62:
                    create arc from t_{revert} to P_{data}[v]
63:
                end for
64:
                create transition t_{!revert} with guard \boldsymbol{c}
65:
                create arc from p_{in} to t_{!revert}
66:
67:
                create arc from t_{!revert} to p_{out}
                for v \in c.variables do
68:
                    create arc from P_{data}[v] to t_{!revert}
69:
                    create arc from t_{!revert} to P_{data}[v]
70:
71:
                end for
            else if st is a selection statement then
72:
```

```
73:
               create place p_T
               create transition t_T with guard c
74:
               create arc from p_{in} to t_T
75:
               create arc from t_T to p_T
76:
               for v \in c.variables do
77:
                   create arc from P_{data}[v] to t_T
78:
                   create arc from t_T to P_{data}[v]
79:
               end for
80:
81:
               CREATESUBMODEL (t; st_T; p_T; p_{out}; P_{data}; metaColour)
82:
               create transition t_F with guard !c
               create arc from p_{in} to t_F
83:
84:
               for v \in c.variables do
                   create arc from P_{data}[v] to t_F
85:
                   create arc from t_F to P_{data}[v]
86:
               end for
87:
               if st is a selection statement: if(c) then st_T then
88:
                   create arc from t_F to p_{out}
89:
               else if st is a selection statement: if(c) then st_T else st_F then
90:
                   create place p_F
91:
                   create arc from t_F to p_F
92:
                   CREATESUBMODEL(t; st_F; p_F; p_{out}; P_{data}; metaColour)
93:
               end if
94:
95:
            else if st is a looping statement then
               if st is a for statement: for(init; c; inc)st_T then
96:
                   create place p_{init}
97:
98:
                   create place p_c
99:
                   create place p_T
100:
                    CREATESUBMODEL (t;init;p_{in};p_{init};P_{data}; metaColour)
101:
                    create transition t_T with guard c
102:
                    create arc from p_{init} to t_T
                    for v \in c.variables do
103:
                        create arc from P_{data}[v] to t_T
104:
                        create arc from t_T to P_{data}[v]
105:
                    end for
106:
                    create arc from t_T to p_c
107:
                    create transition t_F with guard !c
108:
109:
                    create arc from p_{init} to t_F
110:
                    for v \in c.variables do
                        create arc from P_{data}[v] to t_F
111:
112:
                        create arc from t_F to P_{data}[v]
                    end for
113:
                    create arc from t_F to p_{out}
114:
115:
                    CREATESUBMODEL (t; st_T; p_c; p_T; P_{data}; metaColour)
116:
                    CREATESUBMODEL(t;inc;p_T;p_{init};P_{data}; metaColour)
                else if st is a while loop statement: while(c) st<sub>T</sub> then
117:
```

```
118:
                    create place p_T
                    create transition t_T with guard c
119:
120:
                    create arc from p_{in} to t_T
                    for v \in c.variables do
121:
                        create arc from P_{data}[v] to t_T
122:
                        create arc from t_T to P_{data}[v]
123:
                    end for
124:
                    create arc from t_T to p_T
125:
126:
                    create transition t_F with guard !c
127:
                    create arc from p_{in} to t_F
128:
                    for v \in c.variables do
129:
                        create arc from P_{data}[v] to t_F
                        create arc from t_F to P_{data}[v]
130:
                    end for
131:
132:
                    create arc from t_F to p_{out}
                    CREATESUBMODEL (t; st_T; p_T; p_{in}; P_{data}; metaColour)
133:
134:
                end if
135:
             end if
         end if
136:
137: end procedure
```

CREATESUBMODEL browses the body of the transition's corresponding function recursively, statement by statement, and creates snippets of a CPN model according to the type of the processed statement (cf. figures 3-11) that interconnect to create the transition's submodel. In the following we give the corresponding CPN patterns corresponding to each of the statement types:

- Compound statement $\{st[1]; st[2]; \ldots; st[N]\}$ (lines 5-13): the algorithm is re-executed on each component statement st[i], after creating N-1 control flow places (of the metaColour colour) to interconnect the resulting CPN snippets while merging the entering point of the snippet of st[1] with the entering point of the snippet of st and the exiting point of st[N] to that of the snippet of st.

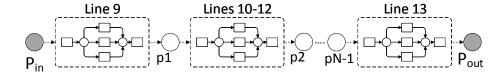


Fig. 3: Compound Statement Pattern

- Assignment statement (st_{LHS}, st_{RHS}) (lines 15-28): to represent such a statement, a transition t' is created with input and output links to, respectively, the input (p_{in}) and output (p_{out}) places passed as parameters.

t' is also connected to the places in P_{data} that correspond to the variables used in the statement's RHS with input/output links (to read the data). In case of a local variable assignment (Figure 4 (a)), an input/output link is created with the place corresponding to the assigned variable in the statement's LHS with the new value (st_{RHS}) inscribed on the output link. In case of a state variable assignment (Figure 4 (b)), the new value (st_{RHS}) is given in the variable's corresponding placement in the inscription on the link to the output (p_{out}) place.

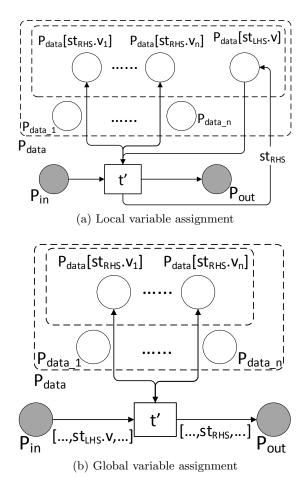


Fig. 4: Assignment statement pattern

- Variable Declaration statement (st_{LHS} , st_{RHS}) (lines 29-37): the algorithm creates a transition t' with input and output links to, respectively, the input (p_{in}) and output (p_{out}) places passed as parameters. Input/output links are

created from and to the places corresponding to the variables used in the statement's RHS. An output link is also created to the place representing the declared variable with st_{RHS} as inscription.

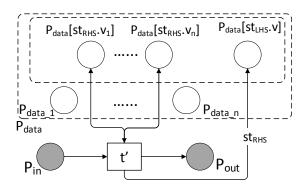


Fig. 5: Variable Declaration Statement Pattern

– Sending statement (st_{LHS}, st_{RHS}) (lines 38-45): the CPN snippet for a sending statement is generated in a way that is similar to that of the case of a global variable assignment, except that instead of updating the assigned variable's counterpart on the output link to p_{out} the algorithm updates the contractBalance and balance values from the input of t' by decreasing the first and increasing the second by st_{RHS} .

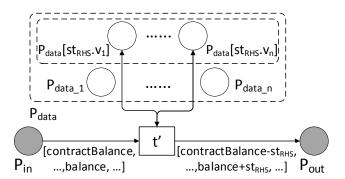


Fig. 6: Sending Statement Pattern

- Returning statement $(-, st_{RHS})$ (lines 46-55): this is also treated similarly to a global variable assignment statement, but with the following differences. t' is linked to $t \bullet [cf]$ instead of p_{out} with the same inscription of its input link with p_{in} , and has an additional output link with the output return place

 $t \bullet [output]$ with the return value set to st_{RHS} in its inscription, with the same sender's address and balance from its input inscription.

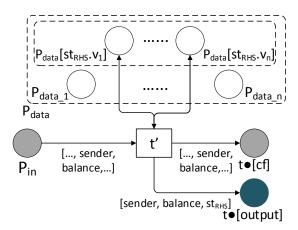


Fig. 7: Returning Statement Pattern

- Requirement statement require(c) (lines 57-71): such a statement is transformed by creating two transitions t_{revert} and $t_{!revert}$, with !c and c as respective guards, input links with p_{in} and input/output links with the places representing local variables used in c. Transition t_{revert} has $\bullet t[cf]$ as output place whereas p_{out} is the output place of $t_{!revert}$. We note that, as a requirement statement is often placed at the beginning of the function, p_{in} and $\bullet t[cf]$ are usually the same.

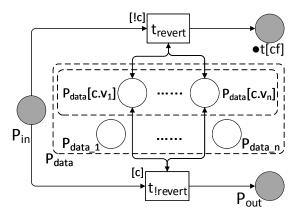
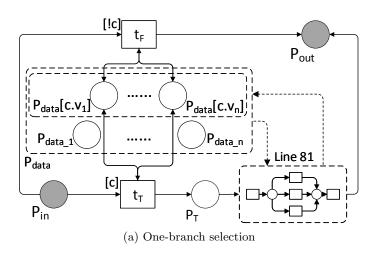


Fig. 8: Requirement Statement Pattern

- Selection statement if(c) then st_T [else st_F] (lines 72-94): the algorithm creates two transitions, t_T with guard c and t_F with guard !c, that respectively represent the activation of the true and false (or default) branches of the selection statement. Both transition are linked to the input place p_{in} and any places representing local variables used in c. CREATESUBMODEL is then recursively called for the true-branch statement. In case of a one-branch selection, t_F is linked directly to the output place p_{out} . In case of a double-branch selection, a new place p_F is created to be the output place of t_F and the input place in a recursive call for CREATESUBMODEL on the false-branch statement.



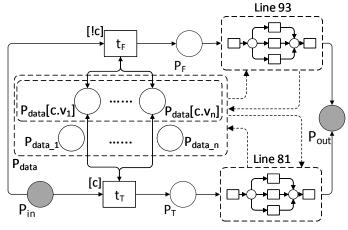


Fig. 9: Selection Statement Pattern

(b) Double-branch selection

– For Looping statement for(init;c;inc) st_T (lines 96-116): three places, p_{init} , p_c and p_T , are created to respectively represent initialization, increments and one pass of the loop's body. Transitions t_T with guard c and t_F with guard !c are created and linked to the input place p_{in} and any places representing local variables used in c. t_T is linked to p_c as output to trigger a counter increment while t_F is linked to p_out as output to leave the loop. CREATESUBMODEL is recursively called with three statements: init which is usually a variable declaration statement with initialization, st_T to develop the CPN snippet for one run of the loop, and inc which is usually an assignment to a local variable type of statement.

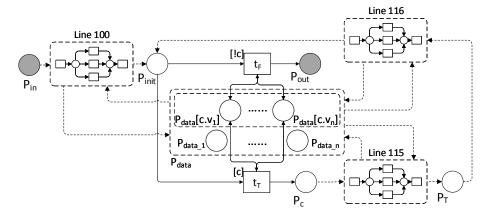


Fig. 10: For Looping Statement Pattern

- While Looping statement while(c) st_T (lines 117-134): for this loop the algorithm proceeds by creating one new place p_T which will be the output for a new transition t_T with guard c. Another transition t_F is also created with !c as guard and p_{out} as output place. Both transition are linked to the input place p_{in} and any places representing local variables used in c. A recursive call to CREATESUBMODEL on st_T with p_T for input and p_{in} for output places is responsible for the generation of the loop's body corresponding CPN snippet.

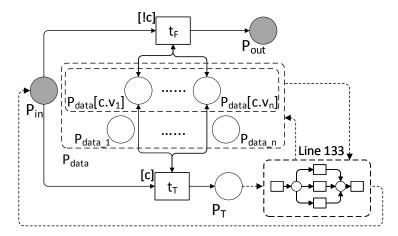


Fig. 11: While Looping Statement Pattern

2.3 Application on the Use Case

The application of the algorithm on the level-0 model of the Blind Auction use case (Figure 2) presented in Section 1 yields a hierarchical CPN model whose level-1 submodels are shown in Figures 12-14. These submodels correspond to the transitions representing functions in the Blind Auction smart contract (Listing 1.1), namely bid, reveal and withdraw. For each submodel, the light-grey-coloured places represent control flow places P_{cf} of a metaColour specific to the submodel in question, whereas places of other colours inside the dashed-line box are places of the relative P_{data} . Places outside the box are the input/output places of the corresponding level-0-transition, among which the dark grey places are state places in P_S , uncoloured places are interface places in P_I , dark blue places are return places in P_R and the others (red, green and blue) are parameter places in P_P . The submodels inside the dashed-line boxes are the product of CREATESUBMODEL, and the links with the input/output places of level 0 are generated by INSERTSUBMODEL.

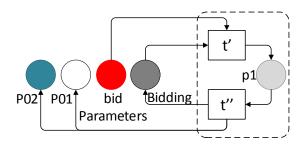


Fig. 12: SubModel of transition bid

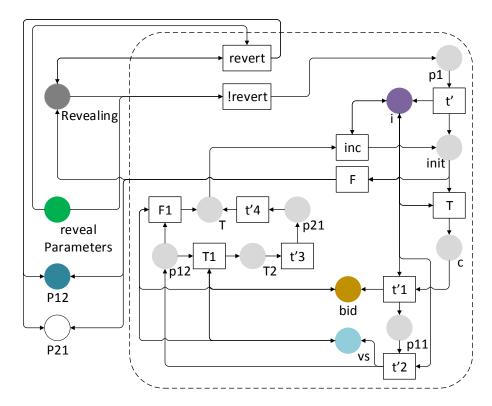


Fig. 13: SubModel of transition reveal

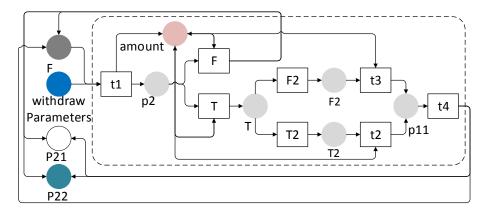


Fig. 14: SubModel of transition withdraw

3 Smart Contract Verification

Having established the CPN model for a smart contract, verifying properties of the latter would come down to verifying properties on the corresponding CPN model. In the following, we present the analysis and verification results rendered by two model checking tools, namely *CPN Tools* and *Helena*, and compare their performances in terms of execution time.

In addition to its editing capabilities, *CPN Tools* also offers the possibility to analyze the state space of a CPN model through its *State Space* palette as well as its associated *ASK-CTL* library [2]. The latter uses a CTL-like temporal logic interpretation over the state space of the model and leverages explicit model checking techniques for the verification of behavioural properties.

Helena is a High LEvel Nets Analyzer available as a command line tool. It offers explicit model checking support for an on-the-fly verification of state properties as well as LTL properties over CPN models described in Helena's specification language.

We have manually designed the CPN model for our use case using *CPN Tools* and written it in *Helena*'s specification language. We have then used both tools to generate its state space and test the verification of temporal properties with the aim of investigating their potential in the verification of behavioural and contract-specific properties.

3.1 State Space Analysis Results

In the following, we present state space analysis statistics for different initial marking values. Table 1 shows the evolution of the state space generation time, as well as the number of nodes, arcs and dead markings while varying the number of bidders, possible bids, possible secret kevs and possible deposits in the system. Every line is subdivided into two sub-lines, the upper one representing the analysis results for the model extended with the level-1 submodels (i.e., the hierarchical model), and the bottom one representing the results for the level-0 model (i.e., non-hierarchical model). In the line corresponding to the state space generation time, cells highlighted in grey represent the results obtained using Helena while non-highlighted cells represent results obtained by CPN Tools. We note that the state space generated for each scenario by both tools has the same size, which validates the conformance of the model written in Helena's specification language with that which we visually designed using CPN Tools. However, we can clearly see that Helena (the highlighted columns) outperforms CPN Tools (the non-highlighted columns) with a considerably shorter execution time. We also note that for 5 bidders (while fixing the other variables at 1), as well as for 1 bidder (while fixing the other variables at 4), the state space generation had not finished after several hours of execution using CPN Tools, which is why we do not report corresponding results.

Table 1. State Space Analysis Results for different initial markings									
Possible Bidders		1	2	3	4	5		1	1
Possible Bids		1	1	1	1	1		2	3
Possible Secret Keys		1	1	1	1	1		2	3
Possible Deposits		1	1	1	1	1		2	3
State Space	Η	$0 \mid 0$	0 0	0 2	2 622	42	-	0 0	1 87
Generation	NH	0 0	0 0	0 1	0 152	11	-	0 0	0 16
Number of	Н	44	583	9166	156117	2714288	-	1288	79584
Nodes	NH	24	235	3118	47621	766548	-	484	19984
Number of	Η	46	900	19784	446326	9948298	-	1411	97463
Arcs	NH	26	378	7106	145062	3002038	-	555	22980
Number of	Н	3	10	35	124	437	-	65	3695
Dead Markings	NH	3	10	35	124	437	-	65	3695

Table 1: State Space Analysis Results for different initial markings

3.2 Properties from State Space Reports

Both *CPN Tools* and *Helena* are able to generate similar state space reports. Such reports allow the deduction of several general behavioural properties.

- Boundedness: The state space reports show that all of the places of our model are bounded. A place is bounded when the number of tokens it contains does not exceed some finite number for any marking reachable from the initial marking.
- Reversibility: In order to derive this property in our case, we modify the model as to obtain a short-circuited version. To do so, we added a transition that restores the model to its initial state once it reaches a final one. The state space report of the modified version indicates that all of the markings are home markings, hence the model is reversible.
- Liveness/Deadlock-freedom: The concept of liveness is closely related to the complete absence of deadlocks in operating systems. In fact, a live Petri net guarantees a deadlock-free operation, regardless of the firing sequence. The resulting state space analysis report for our modified model (the short-circuited version) indicates that all of our model's transitions are live, which means that every transition remains fireable for any firing sequence.

3.3 Temporal Properties Verification

Using *CPN Tools* More specific properties can be verified by elaborating CTL properties. In the following we give a few examples of contract-specific properties that can be verified on our Blind Auction use case.

- The system always terminates in a well-defined state (never terminates in an unexpected state):

We can formulate a *termination* property to check that all the dead markings in the state space actually correspond to final markings of the model,

and therefore checks that the model is deadlock-free. To do so, we give a characterization of the *termination* property as the model's capability to always reach a terminal state (a dead marking) where the following conditions are met:

• (C1) in the Smart Contract's Behaviour part, all places have to be empty except for the place T that must contain one token

```
fun C1  n = size (Mark.System'T 1 n) = 1
  andalso size (Mark.System'Bidding 1 n) = 0
  andalso size (Mark.System'Revealing 1 n) = 0
  andalso size (Mark.System'F 1 n) = 0
```

• (C2) all Communication places must be empty

```
fun C2 n = size (Mark.System'P01 1 n) = 0
   andalso size (Mark.System'P11 1 n) = 0
   andalso size (Mark.System'P21 1 n) = 0
   andalso size (Mark.System'bidParameters 1 n) = 0
   andalso size (Mark.System'revealParameters 1 n) = 0
   andalso size (Mark.System'withdrawParameters 1 n) = 0
   andalso size (Mark.System'P12 1 n) = 0
   andalso size (Mark.System'P12 1 n) = 0
   andalso size (Mark.System'P22 1 n) = 0
```

- (C3) in the User's Behaviour part:
 - * (C31) the markings of places PossibleSecretKeys, PossibleBids and PossibleDeposits must be the same as their initial markings

```
fun C31 n = Mark.System'PossibleSecretKeys 1 n = Mark.
   System'PossibleSecretKeys 1 InitNode
   andalso Mark.System'PossibleBids 1 n = Mark.System'
   PossibleBids 1 InitNode
   andalso Mark.System'PossibleDeposits 1 n = Mark.
   System'PossibleDeposits 1 InitNode
```

* (C32) tokens in W2 must correspond to the users who have actually placed bids

```
fun bidderExists adr n = List.find(fn {bidder, ...} =>
   adr = bidder) (Mark.System'W2 1 n) <> NONE
(* allBiddersExist: checks that all bidders in a list (
   1) exist in W2 *)
fun allBiddersExist l n = case l of {bidder,bidValue}::
    bidderExists bidder n andalso allBiddersExist t n
    | [] => true
(* C32: checks that the tokens in W2 correspond to the
   users who have actually placed bids (i.e., bidders
   with a bidding value different from 0 in
   LastBidsLog*)
fun C32 n = sameNumberOfBidders n
   andalso allBiddersExist (biddersWithBids n) n
 * (C33) the union of the sets of users who have not placed bids and
   those who have must correspond to the set of initial bidders
(* getBiddersBidder: returns the list of bidder
   addresses in Bidders *)
fun getBiddersInBidders n = remdupl(List.map(fn e:
   FULL_BIDDER => #bidder e)(Mark.System'Bidders 1 n))
(* getBiddersInW2: returns the list of bidder addresses
    in W2 *)
fun getBiddersInW2 n = remdupl(List.map(fn e:
   FULL_BIDDER => #bidder e) (Mark.System'W2 1 n))
(* C33: checks that the union of users who have not
   placed bids and those who have corresponds to the
   set of initial bidders *)
fun C33 n = size(Mark.System', Bidders 1 n) + size(Mark.
   System'W2 1 n)=size(Mark.System'Bidders 1 InitNode)
    andalso contains (remdupl((getBiddersInBidders n)
    ^^(getBiddersInW2 n))) (remdupl(getBiddersInBidders
    InitNode)) andalso contains (remdupl(
    getBiddersInBidders InitNode)) (remdupl((
    getBiddersInBidders n)^^(getBiddersInW2 n)))
 * (C34) every other place must be empty
fun C34 n = size (Mark.System'Bidders2 1 n) = 0
    andalso size (Mark.System'B1 1 n) = 0
    andalso size (Mark.System'R1 1 n) = 0
    andalso size (Mark.System'R2 1 n) = 0
```

The code for the *termination* property would look like this:

andalso size (Mark.System'W1 1 n) = 0

```
fun Termination n = Terminal n andalso C1 n andalso C2 n
    andalso C31 n andalso C32 n andalso C33 n andalso C34 n
val terminationFormula = INV(EV(NF("termination", Termination
    )));
eval_node terminationFormula InitNode;
```

where C1, C2, C31, C32, C33 and C34 are functions that check the corresponding aforementioned conditions on a node n. The evaluation of this property on our model returns true which confirms that all dead markings in the state space do correspond to final markings and that consequently the model contains no deadlocks.

No bid calls can be made once the bidding window is closed.

```
fun bidCallArcs () : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'bidCall (1, {...}) => true
| _ => false);
fun bidCallNodes () : Node list
= List.map(fn a => DestNode(a)) (bidCallArcs());
fun bidCall node = List.exists(fn a => a = node) (
   bidCallNodes ());
fun closeArcs (): Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'close (1, {...}) => true
| _ => false);
fun closeNodes () : Node list
= List.map(fn a => DestNode(a)) (closeArcs());
fun close node = List.exists(fn a => a = node) (closeNodes ()
val prop1 = INV(OR(NOT(NF("close",close)),NOT(EV(NF("bidCall"
   ,bidCall))));
eval_node prop1 InitNode
```

- No reveal calls can be made once the revealing window is closed.

```
fun revealCallArcs () : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'revealCall (1, {...}) => true
```

```
| _ => false);
fun revealCallNodes () : Node list
= List.map(fn a => DestNode(a)) (revealCallArcs());
fun revealCall node = List.exists(fn a => a = node) (
   revealCallNodes ());
fun finishArcs (): Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'finish (1, {...}) => true
| _ => false);
fun finishNodes () : Node list
= List.map(fn a => DestNode(a)) (finishArcs());
fun finish node = List.exists(fn a => a = node) (finishNodes
   ());
val prop2 = INV(OR(NOT(NF("finish",finish)),NOT(EV(NF("
   revealCall", revealCall)))));
eval_node prop2 InitNode
```

- No withdraw calls can be made once the withdrawing window is closed.

```
fun withdrawCall1Arcs () : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'withdrawCall1 (1, {...}) => true
| _ => false);
fun withdrawCall1Nodes () : Node list
= List.map(fn a => DestNode(a)) (withdrawCall1Arcs());
fun withdrawCall2Arcs () : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'withdrawCall2 (1, {...}) => true
| _ => false);
fun withdrawCall2Nodes () : Node list
= List.map(fn a => DestNode(a)) (withdrawCall2Arcs());
fun withdrawCall1 node = List.exists(fn a => a = node) (
   withdrawCall1Nodes());
fun withdrawCall2 node = List.exists(fn a => a = node) (
  withdrawCall2Nodes());
```

```
fun terminateArcs (): Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'terminate (1, {...})=> true
| _ => false);

fun terminateNodes (): Node list
= List.map(fn a => DestNode(a)) (terminateArcs());

fun terminate node = List.exists(fn a => a = node) (
    terminateNodes());

val prop3 = INV(OR(NOT(NF("terminate",terminate)),NOT(EV(OR(
    NF("withdrawCall1",withdrawCall1),NF("withdrawCall2",
    withdrawCall2))))));

eval_node prop3 InitNode
```

- Every call is followed by an acknowledgment.
 - bid:

```
fun bidCallArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'bidCall (1, {flb=x,...}) => #bidder x =
| _ => false);
fun bidCallNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (bidCallArcs(adr));
fun bidACKArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'bidACK (1, {flb=x,...}) => #bidder x =
| _ => false);
fun bidACKNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (bidACKArcs(adr));
fun bidCall adr node = List.exists(fn a => a = node) (
   bidCallNodes (adr));
fun bidACK adr node = List.exists(fn a => a = node) (
   bidACKNodes (adr));
```

```
fun prop41 (m : ADDRESS ms) : A = if size m = 1 then INV(OR(
   NOT(NF("bidCall",bidCall(ADDRESS.col(size m - 1)))),EV(NF
   ("bidACK",bidACK(ADDRESS.col(size m - 1)))))
else AND(INV(OR(NOT(NF("bidCall",bidCall(ADDRESS.col(size m -
   1)))),EV(NF("bidACK",bidACK(ADDRESS.col(size m - 1)))))
   , prop41(m--1'ADDRESS.col(size m - 1)));
eval_node (prop41(ADDRESS.all())) InitNode
```

• reveal:

```
fun revealCallArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'revealCall (1, {flb=x,...}) => #bidder x
| _ => false);
fun revealCallNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (revealCallArcs(adr));
fun revealACKArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'revealACK (1, {flb=x,...}) => #bidder x =
    adr
| _ => false);
fun revealACKNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (revealACKArcs(adr));
fun revealCall adr node = List.exists(fn a => a = node) (
   revealCallNodes (adr));
fun revealACK adr node = List.exists(fn a => a = node) (
   revealACKNodes (adr));
fun prop42 (m : ADDRESS ms) : A = if size m = 1 then INV(OR(
   NOT(NF("revealCall",revealCall(ADDRESS.col(size m - 1))))
   ,EV(NF("revealACK",revealACK(ADDRESS.col(size m - 1))))))
else AND(INV(OR(NOT(NF("revealCall",revealCall(ADDRESS.col(
   size m - 1)))),EV(NF("revealACK",revealACK(ADDRESS.col(
   size m - 1)))))), prop42(m--1'ADDRESS.col(size m - 1)));
eval_node (prop42(ADDRESS.all())) InitNode
```

• withrdaw:

```
fun withdrawCall1Arcs (adr : ADDRESS) : Arc list
= PredAllArcs(
```

```
fn a => case ArcToBE a of
Bind.Complete_System'withdrawCall1 (1, {flb=x,...}) => #bidder
    x = adr
| _ => false);
fun withdrawCall1Nodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (withdrawCall1Arcs(adr));
fun withdrawCall2Arcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System', withdrawCall2 (1, {flb=x,...}) => #bidder
    x = adr
| _ => false);
fun withdrawCall2Nodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (withdrawCall2Arcs(adr));
fun withdrawACKArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'withdrawACK (1, {flb=x,...}) => #bidder x
    = adr
| _ => false);
fun withdrawACKNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (withdrawACKArcs(adr));
fun withdrawCall1 adr node = List.exists(fn a => a = node) (
   withdrawCall1Nodes (adr));
fun withdrawCall2 adr node = List.exists(fn a => a = node) (
   withdrawCall2Nodes (adr));
fun withdrawACK adr node = List.exists(fn a => a = node) (
   withdrawACKNodes (adr));
fun prop43 (m : ADDRESS ms) : A = if size m = 1 then INV(OR(
   NOT(OR(NF("withdrawCall1",withdrawCall1(ADDRESS.col(size
   m - 1))), NF("withdrawCall2", withdrawCall2(ADDRESS.col(
   size m - 1))))), EV(NF("withdrawACK", withdrawACK(ADDRESS.
   col(size m - 1))))))
else AND(INV(OR(NOT(OR(NF("withdrawCall1", withdrawCall1(
   ADDRESS.col(size m - 1))), NF("withdrawCall2",
   withdrawCall2(ADDRESS.col(size m - 1))))), EV(NF("
   withdrawACK", withdrawACK(ADDRESS.col(size m - 1)))))),
   prop43(m--1'ADDRESS.col(size m - 1)));
eval_node (prop43(ADDRESS.all())) InitNode
```

- A bidder who has not revealed his bid cannot be the winner (highest bidder).

```
fun bidCallArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'bidCall (1, {flb=x,...}) => #bidder x =
| _ => false);
fun bidCallNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (bidCallArcs(adr));
fun revealCallArcs (adr : ADDRESS) : Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'revealCall (1, {flb=x,...}) => #bidder x
   = adr
| _ => false);
fun revealCallNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (revealCallArcs(adr));
fun terminateHighestBidderArcs (adr : ADDRESS): Arc list
= PredAllArcs(
fn a => case ArcToBE a of
Bind.Complete_System'terminate (1, {hbr=x,...}) => x = adr
| _ => false);
fun terminateHighestBidderNodes (adr : ADDRESS) : Node list
= List.map(fn a => DestNode(a)) (terminateHighestBidderArcs(
   adr));
fun bidCall adr node = List.exists(fn a => a = node) (
   bidCallNodes (adr));
fun revealCall adr node = List.exists(fn a => a = node) (
   revealCallNodes (adr));
fun terminateHighestBidder adr node = List.exists(fn a => a =
    node) (terminateHighestBidderNodes(adr))
fun prop5 (m : ADDRESS ms) : A = if size m = 1 then INV(OR(
   NOT(AND(NF("bidCall",bidCall(ADDRESS.col(size m - 1))),
   NOT(EV(NF("revealCall",revealCall(ADDRESS.col(size m - 1)
   )))))),NOT(NF("terminateHighestBidder",
   terminateHighestBidder(ADDRESS.col(size m - 1))))))
else AND(INV(OR(NOT(AND(NF("bidCall",bidCall(ADDRESS.col(size
    m - 1))), NOT(EV(NF("revealCall", revealCall(ADDRESS.col(
   size m - 1))))))), NOT(NF("terminateHighestBidder",
```

```
terminateHighestBidder(ADDRESS.col(size m - 1)))))),
prop5(m--1'ADDRESS.col(size m - 1)));
eval_node (prop5(ADDRESS.all())) InitNode
```

Using *Helena* The same result could be obtained using *Helena*:

```
ltl property termination: [] <> valid_termination;
```

with valid_termination representing the conjunction of the explained conditions:

```
proposition valid_termination :
//(C1)
                  T' card = 1
              and Bidding'card = 0
              and Revealing'card = 0
              and F' card = 0
//(C2)
              and P01'card = 0
              and P11'card = 0
              and P21' card = 0
              and Bid_Parameters'card = 0
              and Reveal_Parameters'card = 0
              and Withdraw_Parameters'card = 0
              and P02' card = 0
              and P12'card = 0
              and P22'card = 0
//(C31)
              and Possible_Secret_Keys'card = nPSK
              and Possible_Bids'card = nPB
              and Possible_Deposits'card = nPD
//(C32)
              and card(t in Last_Bids_Log|(t->1).bidValue!=0)
                   = W2'card
              and forall(t in W2 : exists(l in Last_Bids_Log
                  |(t->1).bidder = (1->1).bidder and (1->1).
                  bidValue!=0))
//(C33)
              and Bidders'card + W2'card = nBidders
              and forall(t in W2 : not exists(b in Bidders|(b
                  ->1).bidder = (t->1).bidder))
//(C34)
              and Bidder' card = 0
              and Full_Bids'card = 0
              and R1'card = 0
              and R2' card = 0
              and W1'card = 0;
```

Discussion Considering that *Helena* showed better results in terms of execution times, we decided to implement our prototype of the transformation algorithm targeting its specification language. Since our algorithm relies on the existence of a description of the intended workflow (as explained in Section 2) we manually create the elements corresponding to the level-0 model, based on which the different submodels are then automatically generated.

While some temporal properties can be expressed using both logics (LTL and CTL), like the aforementioned termination property, we note that some other properties can only be expressed using one logic and not the other. This, however, does not imply that either logic is a subset of the other. It is also worth mentioning that *Helena*'s verification is on-the-fly whereas *CPN Tools* requires the generation of the whole state space, which can constitute a considerable overhead for the verification process.

4 Conclusion

Being an important pillar for Blockchain technology, smart contracts need to provide certain guarantees in terms of correctness to support its foundation built on trust. Formal approaches for the verification of Solidity smart contracts have been proposed, but they are generally designed to target specific vulnerabilities known in the literature (e.g., reentrancy) which have been reported to be the root of some attacks or malfunctions. Checking the absence of such vulnerabilities in a smart contract does not guarantee its correctness as a faulty behaviour may stem from a flaw specific to that contract. Moreover, the need to verify contract-specific properties has proven increasingly necessary in the light of the expanding reach of smart contracts in many application fields.

In an effort to bring a solution to this problem, we propose a CPN-based formal verification approach for Solidity smart contracts. We implement a prototype of a transformation algorithm that generates a hierarchical CPN model representing a given Solidity smart contract, including both its control-flow and data aspects. Temporal properties are then verified on the CPN model to check corresponding properties on the smart contract, unrestrictedly to certain predefined vulnerabilities. At the time being, the proposed transformation supposes the existence of the level-0 model to be extended. Our next step is to fully automate this process by generating this model from an additional artifact that can provide a description of the intended workflow (e.g., a BP model). To further improve the tool's performance, we intend to work on *Helena*'s model checker by embedding it with an extension to an existing technique previously developed to deal with the state space explosion problem in regular PNs [3] and applying it on CPNs.

References

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