

# Linear regression

$$y_i \sim \text{Normal}(\mu_i, \sigma^2)$$

$$\mu_i = \beta_0 + \beta_1 * x_i$$

Where,

$y_i$  : response variable at site i

$\mu_i$  : mean of  $y_i$

$\sigma^2$  : variance of  $y_i$

$\beta_0$  : intercept

$\beta_1$  : slope

$x_i$  : covariate value at site i

# Logistic regression

$$y_i \sim \textit{Binomial}(\pi_i, N_i)$$

$$\textit{logit}(\pi_i) = \beta_0 + \beta_1 * x_i$$

Where,

$y_i$  : response variable (0 or 1) at site i

$\pi_i$  : probability of observing a 1 at site i

$N_i$  : number of trials (*eg*, coin tosses [=1 in typical logistic reg.])

$\beta_0$  : intercept – on logit scale

$\beta_1$  : slope – on logit scale

$x_i$  : covariate value at site i

# Poisson regression

$$y_i \sim \text{Poisson}(\lambda_i)$$

$$\log(\lambda_i) = \beta_0 + \beta_1 * x_i$$

Where,

$y_i$  : response variable (integer value) at site i

$\lambda_i$  : Poisson mean at site i

$\beta_0$  : intercept – on log scale

$\beta_1$  : slope – on log scale

$x_i$  : covariate value at site i

## Single-season occupancy

$$y_{ij} \sim \text{Binomial}(p_{ij}, Z_i)$$

$$Z_i \sim \text{Binomial}(\psi_i, 1)$$

$$\text{logit}(p_{ij}) = \beta_0 + \beta_1 * x_{ij}$$

$$\text{logit}(\psi_i) = \alpha_0 + \alpha_1 * v_i$$

Where,

$y_{ij}$  : observed presence/absence at site i on occasion j

$Z_i$  : state variable: actual presence/absence at site i

$p_{ij}$  : detection probability at site i on occasion j

$\psi_i$  : probability of occurrence at site i

$\beta_0$  : intercept – on logit scale

$\beta_1$  : slope – on logit scale

$x_{ij}$  : covariate value at site i on occasion j

$\alpha_0$  : intercept – on logit scale

$\alpha_1$  : slope – on logit scale

$v_i$  : covariate value at site i

## *N*-mixture model (aka Binomial mixture model)

$$y_{ij} \sim \text{Binomial}(p_{ij}, N_i)$$

$$N_i \sim \text{Poisson}(\lambda_i)$$

$$\text{logit}(p_{ij}) = \beta_0 + \beta_1 * x_{ij}$$

$$\log(\lambda_i) = \alpha_0 + \alpha_1 * v_i$$

Where,

$y_{ij}$  : observed abundance at site  $i$  on occasion  $j$

$N_i$  : state variable: actual abundance at site  $i$

$p_{ij}$  : detection probability at site  $i$  on occasion  $j$

$\lambda_i$  : mean abundance at site  $i$

$\beta_0$  : intercept – on logit scale

$\beta_1$  : slope – on logit scale

$x_{ij}$  : covariate value at site  $i$  on occasion  $j$

$\alpha_0$  : intercept – on log scale

$\alpha_1$  : slope – on log scale

$v_i$  : covariate value at site  $i$