

Motivation  
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Persistent Path Spectral(PPS)  
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Protein-Ligand Binding Affinity Prediction  
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# Persistent Path-Spectral Based Machine Learning for Protein-Ligand Binding Affinity Prediction

Ran Liu

BUAA & BIMSA

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# Outline

## Motivation

## Persistent Path Spectral(PPS)

## Protein-Ligand Binding Affinity Prediction

## Motivation

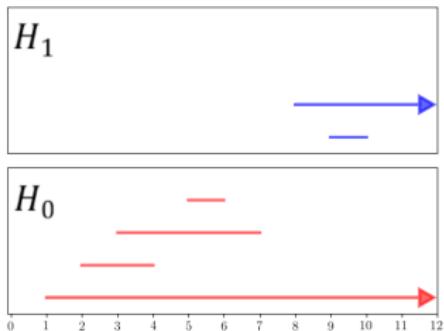
## Persistent Path Spectral(PPS)

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- Persistent homology, a key theory for TDA, has been applied to numerous data science fields with many achievements. Its essence is to provide topological features to the data.

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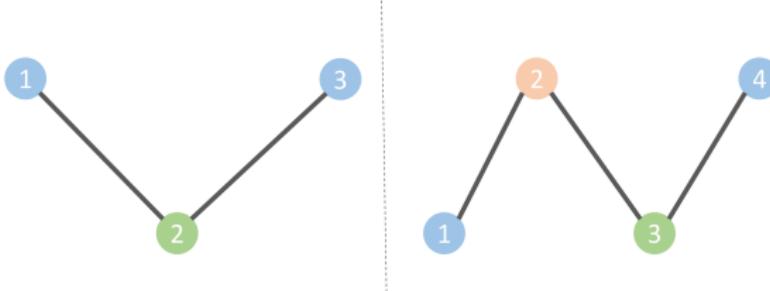


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- Recently, research Beyond TDA is being conducted.

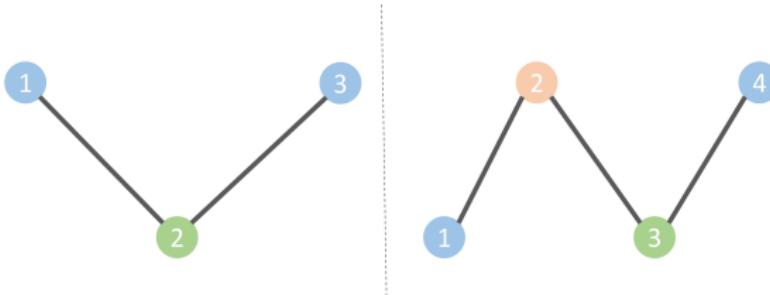
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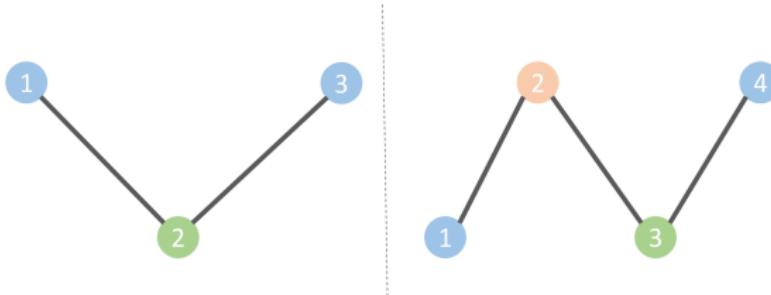
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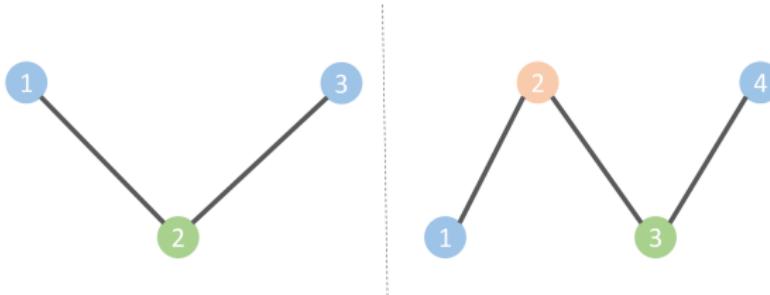
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- We introduce the idea of hopping into the high-dimensional plate, combine it with the filtering process, consider specifically the Laplacian matrix, feed its spectral information into machine learning to obtain the Persistent Path Spectral(PPS) model, which can give a quantitative description of the data.

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- We introduce the idea of hopping into the high-dimensional plate, combine it with the filtering process, consider specifically the Laplacian matrix, feed its spectral information into machine learning to obtain the Persistent Path Spectral(PPS) model, which can give a quantitative description of the data.
- And test our model on issue of protein-ligand binding affinity prediction, PPS model can achieve competitive results.

## Motivation 000

## Persistent Path Spectral(PPS)

## Protein-Ligand Binding Affinity Prediction

## Motivation

## Persistent Path Spectral(PPS)

## Definition (Simplicial Complex)

An (abstract) simplicial complex  $C$  is a pair  $(V, C_V)$  where  $V$  is a vertex set and  $C$  is a simplex set, such that every  $\sigma \in C_V$  is a nonempty subset of vertex set , and every nonempty subset of  $\sigma$  is also  $\in C_V$ .

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## Definition (n-simplex walk,path)

A series of  $n$ -simplices  $\sigma_1^n, \sigma_2^n, \dots, \sigma_l^n, \sigma_{l+1}^n$  (not must diverse) is called an  **$n$ -simplex walk** from  $\sigma_1^n$  to  $\sigma_{l+1}^n$  while  $\sigma_i^n$  and  $\sigma_{i+1}^n$  share an  $(n+1)$ -simplex for each  $i = 1, 2, \dots, l$ .

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Under another additional condition that these  $n$ -simplices are different from each other, this  **$n$ -simplex walk** turns into an  **$n$ -simplex path**.

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Among all the  $n$ -simplex paths between  $\sigma_i^n$  and  $\sigma_j^n$ , the ones having the minimum number of  $(n+1)$ -simplexes are called **the shortest  $n$ -simplex paths** (may more than one).

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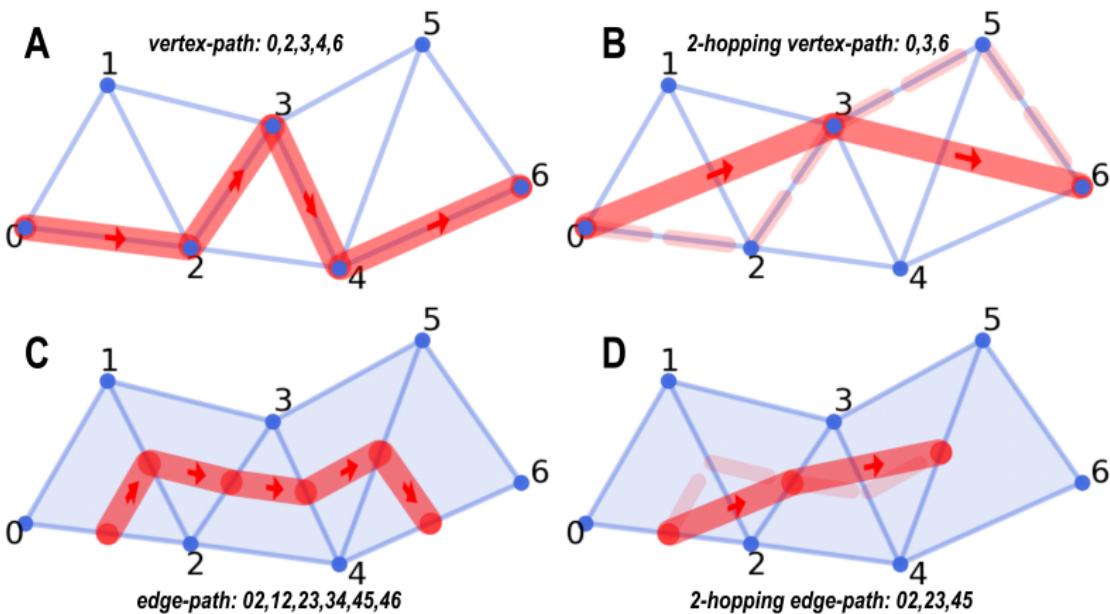
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When these  $n$ -simplices are different from each other, this  **$k$ -hopping  $n$ -simplex walk** turns into a  **$k$ -hopping  $n$ -simplex path**.

## Example: hopping path of simplicial complex

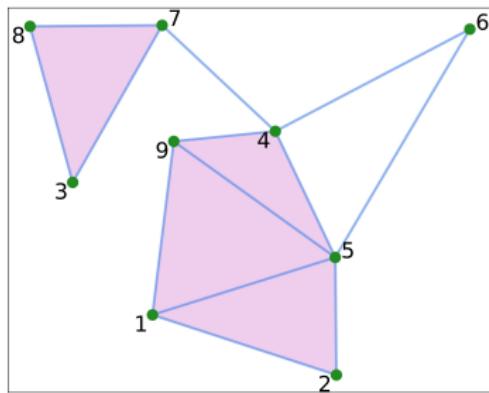


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*Given a simplicial complex  $C$ , which can be represented by  $\{C_n\}_{n \geq 0}$ , here  $C_n$  is the collection of all  $n$ -simplices. For a subset of  $C_n$ , denoted as  $X_n$ , if there is a  $k$ -hopping  $n$ -simplex walk visiting every  $n$ -simplices of  $X_n$  at least, the subset  $X_n$  is defined as a  **$k$ -hopping  $n$ -simplex connected component** of  $C$ , which denoted by  **$(k,n)$  connected component** for simplicity.*

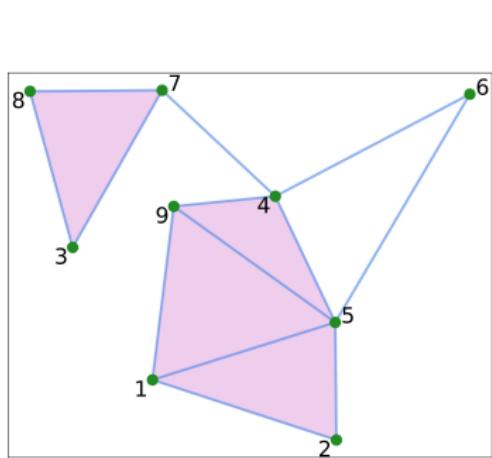
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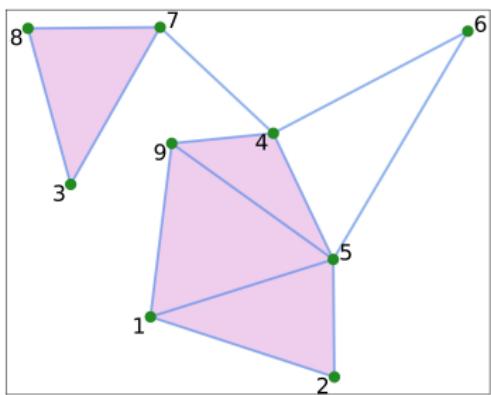
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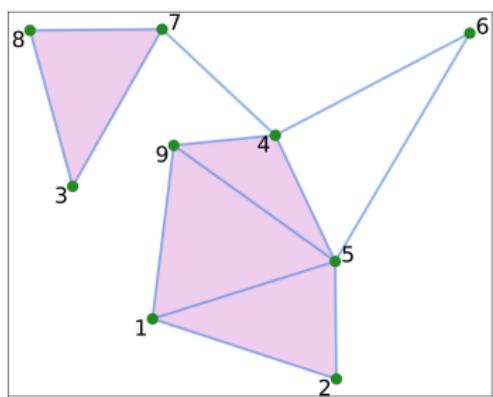
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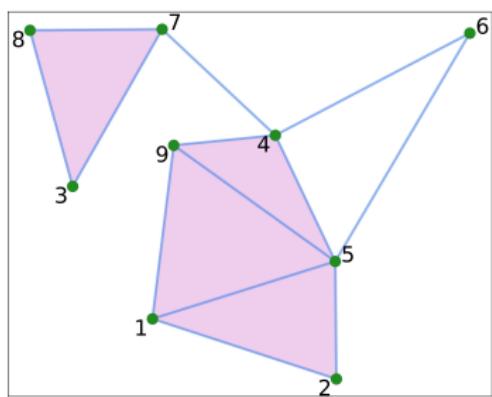
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- seven (2,1) connected components, ten (3,1) connected components

## Definition (k-path degree)

**k-path degree**  $\delta_k(\sigma_i^n)$  of  $\sigma_i^n$  is defined as the count of n-simplices  $\sigma_j^n$  such that the path-distance between  $\sigma_i^n$  and  $\sigma_j^n$  is k.

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The **k-path n-simplex Laplacian matrix**  $L_k^n$  of simplicial complex  $C$  is a  $N(C_n)$  order square symmetric matrix whose entries is shown as follows, denoted by **(k,n) path-Laplacian**.

$$L_k^n(C)(i, j) = \begin{cases} \delta_k(\sigma_i^n) & , i = j \\ -1 & , d_{i,j}^n = k \\ 0 & , otherwise \end{cases} \quad (1)$$

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## Theorem

The number of **k-hopping n-simplex connected components** is the multiplicity of zero eigenvalue of **(k,n) path-Laplacian**.

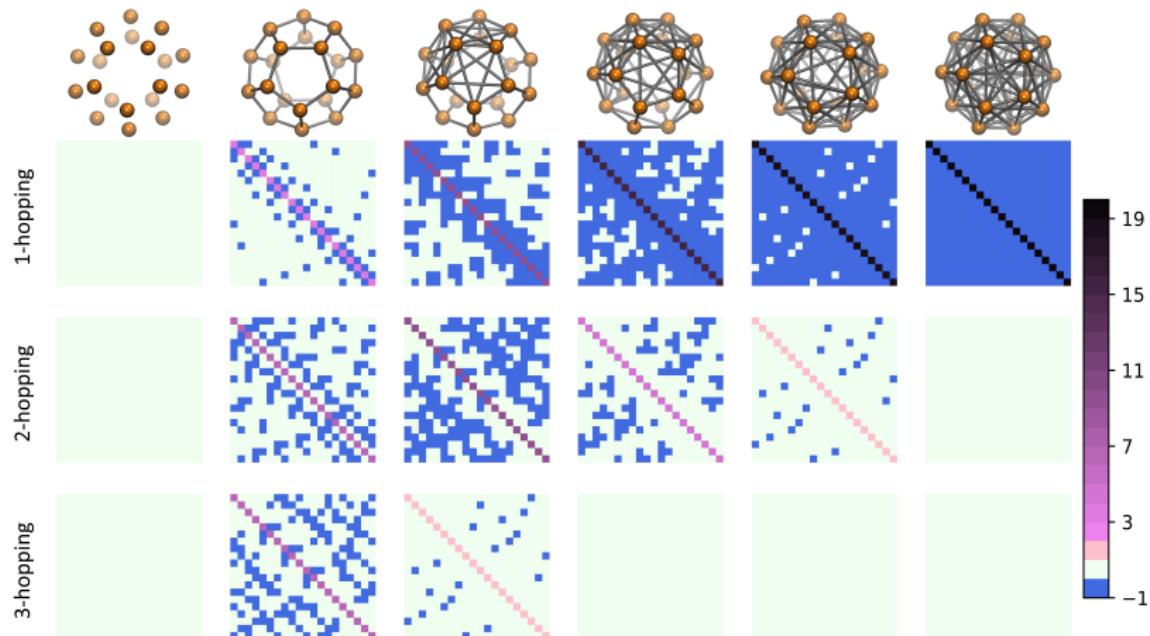
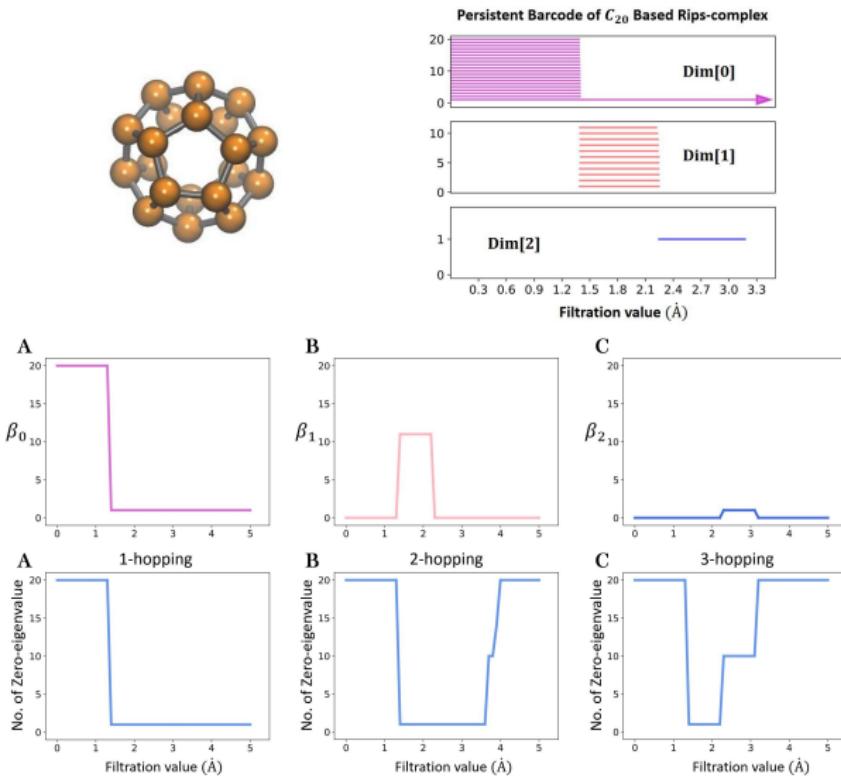
Example: Laplacian matrix of  $C_{20}$ 

Figure: Vertex(0-simplex) path-Laplacian matrices with filtration values  $1.0\text{\AA}$ ,  $1.5\text{\AA}$ ,  $2.3\text{\AA}$ ,  $3.3\text{\AA}$ ,  $3.7\text{\AA}$ ,  $4.0\text{\AA}$ .

# Example: Persistent feature of $C_{20}$



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Assume we have a filtration of simplicial complexes, which is a sequence of nested simplicial complexes

$$O_1 \subset O_2 \subset \dots \subset O_t$$

where  $O_i$  is a sub-complex of  $O_{i+1}$  ( $0 < i < t$ ). For each  $O_i$ , we consider its  $(k, n)$  path-Laplacian matrix  $L_k^n(O_i)$ , then we get a sequence of path-Laplacian matrixes for each pair  $(k, n)$

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*The persistence and variance of the path-spectral information through the sequence of path-Laplacian matrixes is called the **persistent path-spectral** of the sequence of simplicial complexes.*

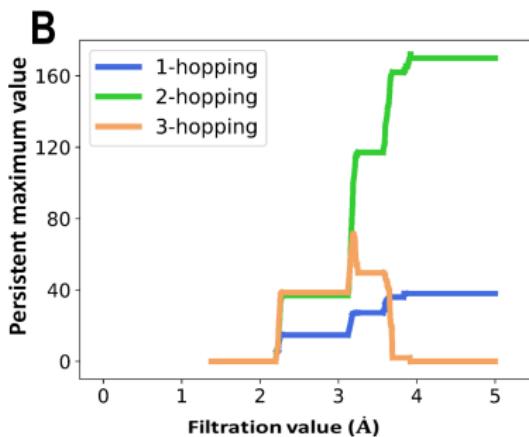
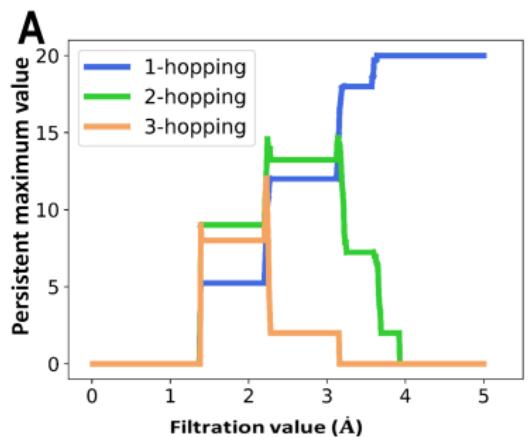
Example: Persistent path-spectral of  $C_{20}$ 

Figure: Persistent attribute curves from persistent path-spectral for  $C_{20}$ . Left is based on vertex, right is based on edge.

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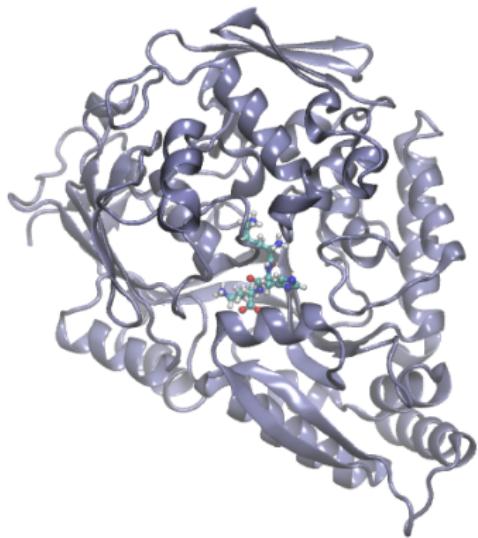
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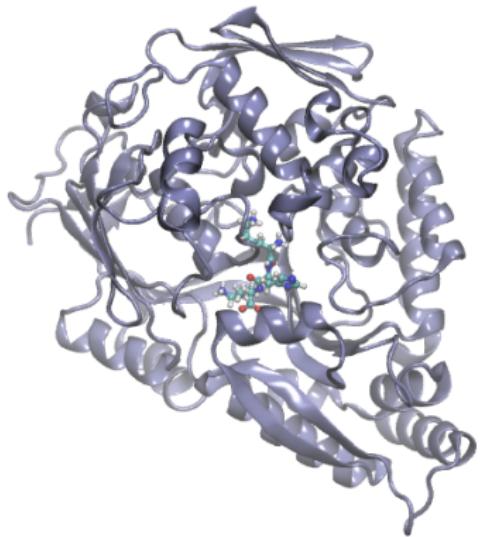
# Protein-Ligand Complex and Affinity



- A protein-ligand complex is a complex of a protein bound with a ligand that is formed following molecular recognition between proteins that interact with each other or with various other molecules.

**Figure:** Protein-ligand complex ID: 1b3f.

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- A protein-ligand complex is a complex of a protein bound with a ligand that is formed following molecular recognition between proteins that interact with each other or with various other molecules.
- The highest possible affinity from a protein towards the ligand, or target molecule, can be observed when the protein has a perfect mirror image of the shape of the target surface together with a charge distribution that complements perfectly the target surface.

# Protein-ligand binding affinity prediction

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- However, this is extremely costly in the first screening of a compound, which requires a prohibitively enormous search space.
- To narrow the search space, there is an urgent need to develop more efficient computational approaches.

## Computational approaches

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1. One is the classical methods which usually use linear functions to model the relationship between experimental data and features.

Classical methods can be divided into three groups:

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2. The other is artificial intelligence (AI) based methods which can capture nonlinear relationship between features and experimental data. AI based models can be grouped into two categories:
  - Machine learning models
  - Deep learning models

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- For each protein-ligand complex, 36 atom combinations are generated with protein atoms C, N, O, S and ligand atoms C, N, O, S, P, F, Cl, Br, I. And a filtered bipartite graph is constructed from every atom-combination where the distance is used as the filtration value for each edge.

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- For electrostatic interactions, H atoms are also taken into consideration and a total of 50 atom combinations are generated from electrostatic interactions.

## Featurization

- For the topological representation of a protein-ligand complex, use PPS to obtain feature, which can be combined with machine learning model.

## Featurization

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- We use persistent median value curve and persistent mean value curve of the persistent spectral with hopping 1, 2 and 3 as the features.
- The size of features based distance-model is **21600 = 36(atom-combinations) × 100(persistence) × 3(hopping) × 2**, the size of features based electrostatic function is **15000 = 50(atom-combinations) × 50(persistence) × 3(hopping) × 2**. Combined model's feature size is **36600 = 21600 + 15000**.

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No. of estimators	Maximum features	Learning rate	Loss function
40000	Square root	0.001	Least square
Minimum sample split	Subsample size	Maximum depth	Repetition
3	0.7	6	10

Table: Detailed parameters of GBT

## Datasets

- The PDBbind database is a collection of the experimentally measured binding affinities exclusively for the protein-ligand complexes available in the Protein Data Bank(PDB).
- This type of knowledge is the much needed basis for many computational and statistical studies on molecular recognition.

Dataset	Refined set	Training set	Test set (Core set)
PDBbind-v2007	1300	1105	195
PDBbind-v2013	2959	2764	195
PDBbind-v2016	4057	3772	285

**Table:** Detailed information of the three PDBbind datasets, i.e., PDBbind-v2007, PDBbind-v2013, PDBbind-v2016.

# Result

PDBbind-v2016	Dist	Charg	Dist+Charg
<b>1-hopping</b>	0.793(1.393)	0.808(1.359)	0.823(1.322)
<b>2-hopping</b>	0.792(1.392)	0.798(1.374)	0.810(1.347)
<b>3-hopping</b>	0.781(1.436)	0.800(1.375)	0.811(1.354)
<b>(1,2,3)-hopping</b>	0.829(1.287)	0.832(1.269)	0.843(1.248)

PDBbind-v2013	Dist	Charg	Dist+Charg
<b>1-hopping</b>	0.746(1.561)	0.760(1.534)	0.775(1.503)
<b>2-hopping</b>	0.753(1.535)	0.759(1.518)	0.767(1.497)
<b>3-hopping</b>	0.733(1.584)	0.725(1.606)	0.745(1.560)
<b>(1,2,3)-hopping</b>	0.778(1.478)	0.778(1.473)	0.791(1.444)

PDBbind-v2007	Dist	Charg	Dist+Charg
<b>1-hopping</b>	0.791(1.534)	0.800(1.509)	0.804(1.509)
<b>2-hopping</b>	0.793(1.500)	0.766(1.559)	0.791(1.497)
<b>3-hopping</b>	0.781(1.540)	0.776(1.547)	0.799(1.499)
<b>(1,2,3)-hopping</b>	0.818(1.142)	0.827(1.399)	0.827(1.399)

Table: PCCs and RMSEs of PPS-ML models on three datasets.

# Result

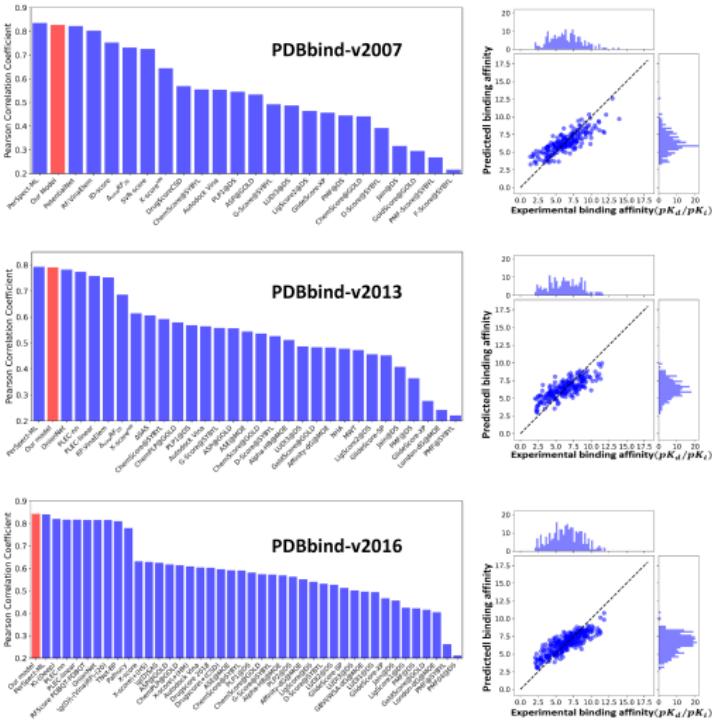


Figure: Performance of PPS-ML model on three datasets.

# Result

- In our model, the feature size is 36600, which is much larger than the data size of three PDBbind datasets we used.
- We expanded the parameter step by 5 times for feature generation to do regression to alleviate overfitting problem.

Dataset	Original size(36600)	Adjusted size(7320)
PDBbind-v2016	0.843(1.248)	0.839(1.257)
PDBbind-v2013	0.791(1.444)	0.790(1.447)
PBDbind-v2007	0.827(1.399)	0.830(1.390)

**Table:** PCCs and RMSEs of PPS-ML model on three datasets based on different feature size.

Motivation  
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Persistent Path Spectral(PPS)  
oooooooooooo

Protein-Ligand Binding Affinity Prediction  
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# Thank You!