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## End Term (Odd) Semester Examination November 2025

Roll no

Name of the Course: **B.Tech. (CSE)**

Semester: **III**

Name of the Paper: **Probability and Random Processes**

Paper Code: **TCS-344**

Time: 3 Hour

Maximum Marks: 100

### Note:

- All the questions are compulsory.
- Answer any two sub questions from a, b and c in each main question.
- Total marks for each question is 20 (twenty).
- Each sub-question carries 10 marks.

Q1.

(2X10=20 Marks) (CO1)

a. Define conditional probability and Baye's theorem. Further, from a city population, the probability of selecting (i) a male or a smoker is  $7/10$ , (ii) a male smoker is  $2/5$ , and (iii) a male if a smoker is already selected is  $2/3$ . Find the probability of selecting:

- a non-smoker,
- a male,
- a smoker if a male is first selected.

b. Define the following events with suitable examples:

- Equally likely events
- Mutually exclusive events
- Independent events
- Dependent events
- Exhaustive events.

c. (i) A room has three electric lamps. From a collection of 10 electric bulbs, of which 6 are good, 3 are selected at random and put in the lamp. Find the probability that the room is lighted.

(ii) A sample space contains three sample points with associated probabilities given by  $2p$ ,  $p^2$  and  $4p - 1$ . Find the value of  $p$ .

(2X10=20 Marks) (CO2)

Q2.

a. Define random variable and its types with suitable examples. Let  $X$  be a continuous random variable with probability density function:

$$f(x) = \begin{cases} ax, & 0 \leq x \leq 1 \\ a, & 1 \leq x \leq 2 \\ -ax + 3a, & 2 \leq x \leq 3 \\ 0, & \text{elsewhere} \end{cases}$$

(i) Determine the constant  $a$  and (ii) compute  $P(X \leq 1.5)$ .

b. A random variable  $X$  has the following probability function:

$X = x$	0	1	2	3	4	5	6	7
$p(x)$	0	$k$	$2k$	$2k$	$3k$	$k^2$	$2k^2$	$7k^2 + k$

- Find  $k$
- Find  $P(X < 6)$ ,  $P(X \geq 6)$  and  $P(0 < X < 5)$
- If  $P(X \leq a) > 0.5$ , find the minimum value of  $a$ , and
- Determine the distribution function of  $X$ .



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c. Define binomial distribution and also, prove that mean of binomial distribution is  $np$  and variance of binomial distribution is  $npq$

(2X10=20 Marks) (CO3)

Q3.

a. Define correlation and its types. Also, check that the two variables  $x$  and  $y$  are correlated or not in the following table:

$x$	65	66	67	67	68	69	70	72
$y$	67	68	65	68	72	72	69	71

b. Write some applications for regression analysis and obtain regression coefficients from the following data:

$x$	1	2	3	4	5	6	7	8
$y$	3	7	10	12	14	17	20	24

Hence, find regression lines.

c. Describe exponential distribution with real life application. Also, derive mean and variance of exponential distribution.

Q4.

(2X10=20 Marks) (CO4)

a. Explain random process with examples and its classification. Also, compare between random variable and random process.

b. Prove that random process  $X(t) = A \sin(\omega t + \theta)$ , where  $A$  and  $\omega$  are constants;  $\theta$  is random variable uniformly distributed in interval  $(0, 2\pi)$  is stationary random process.

c. Define wide-sense stationary random process. Also, show that stationary first order-random process has constant a mean and a constant variance.

Q5.

(2X10=20 Marks) (CO5)

a. Define autocorrelation function and cross correlation function with properties. Also, show that random process  $X(t) = A \cos(\omega t + \theta)$ , where  $A$  and  $\omega$  are constants;  $\theta$  is a random variable uniformly distributed in interval  $[0, 2\pi]$  is wide-sense stationary process.

b. Describe power density spectrum and its properties. Prove that average power of the random process  $X(t) = A_0 \cos(\omega_0 t + \theta)$  is  $A_0^2/2$ , where  $A_0$  and  $\omega_0$  are real constants, and  $\theta$  is a random variable uniformly distributed on the interval  $(0, \pi/2)$ .

c. Define the following:

- Linear system with example
- Stable linear system
- Linear time-invariant system
- Autocorrelation function of response
- Cross-correlation function of input and output.

Also, prove that mean value of system response  $Y(t)$  is equal to the mean value of  $X(t)$  times the area under network's impulse response.