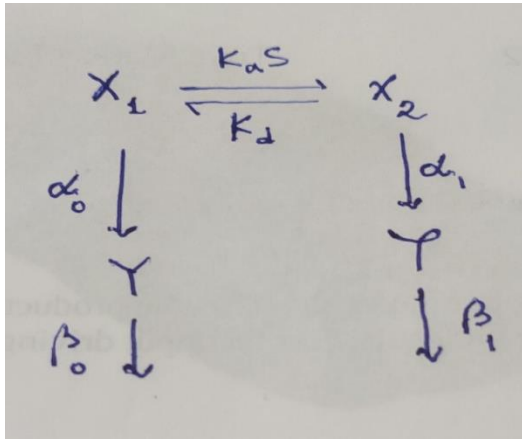


## Exam

(Time 24 hours)

For the following reaction scheme



$$X_1 + X_2 = X_T$$

1. Write down the differential equation and calculate the steady state.
2. Write down the power spectrum of  $\Delta X_1$ ,  $\Delta X_2$  and  $\Delta Y$ .
3. Calculate the variance  $\sigma^2 = \langle \Delta Y^2 \rangle$ .
4. Write down the expression for fisher information.

$$\left\langle \frac{\partial}{\partial S} [\log(Y : S)]^2 \right\rangle \simeq 1/\sigma^2 \left( \frac{\partial}{\partial S} \langle Y \rangle \right)^2$$

5. Write down the expression for entropy production rate.
6. Perform the Gillespie simulation with  $k_a = 1$ ,  $k_d = 1$ ,  $\alpha_1 = 0.5$ ,  $\alpha_0 = 0.05$ ,  $\beta_1 = 0.05$ ,  $\beta_0 = 0.01$

$X_1 + X_2 = X_T$ , by vary  $S$  from 1 to 10.

