

→ Question 1:

$$P(RRGG|z)$$

$$= \alpha_1(u_1) + \alpha_2(u_2) + \alpha_3(u_3)$$

$$\alpha_1(u_1) = 0.33 \times P(R|u_1)$$

$$= 0.33 \times 0.3 = 0.1$$

$$\alpha_1(u_2) = 0.33 \times 0.1$$

$$= 0.033$$

$$\alpha_1(u_3) = 0.33 \times 0.6$$

$$= 0.2$$

$$\alpha_2(u_1) = 0.1 \times 0.1 \times 0.3 + 0.033 \times 0.3 \times 0.3 + 0.2 \times 0.3 \times 0.3$$

$$= 0.02694$$

$$\alpha_2(u_2) = 0.1 \times 0.1 \times 0.1 + 0.033 \times 0.2 \times 0.1 + 0.2 \times 0.4 \times 0.1 = 0.01266$$

$$\alpha_2(u_3) = 0.1 \times 0.5 \times 0.6 + 0.033 \times 0.2 \times 0.6 + 0.2 \times 0.3 \times 0.6 = 0.06996$$

$$\alpha_3(u_1) = 0.02694 \times 0.1 \times 0.3 + 0.01266 \times 0.6 \times 0.3 + 0.06996 \times 0.3 \times 0.5 = 0.015639$$

$$\alpha_3(u_2) = 0.0165168, \alpha_3(u_3) = 0.003699$$

$$\alpha_4(u_1) = 6.29184 \times 10^{-3}, \alpha_4(u_2) = 4.415424 \times 10^{-3}$$

$$\alpha_4(u_3) = 1.223256 \times 10^{-3}$$

$$\therefore P(RRGG|z) = 0.01193052$$