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## Automata Theory Quiz 1

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1. ~~Set~~ Consider a language  $L$  with  $i$  strings namely  $L = \{a_1, a_2, a_3, a_4, \dots, a_i\}$

We can write a regular expression of the form:

$$R = a_1 + a_2 + a_3 + a_4 + \dots + a_i$$

This regular expression accepts this language  $L$  and can be converted to a FSA.

$\therefore$  any language with only a finite number of strings ~~can be converted to~~ is a regular language.

2.

First consider a non-regular language  $N$  and let  $A$  be a regular language.

If  $N \subseteq A$  then  $A$  is no longer regular or  $N$  is, in fact, regular.

$\Rightarrow$  Non-regular languages cannot be a subset of regular languages.  $\rightarrow \textcircled{1}$

In the given case of  $B \subseteq C$

this language is always a subset of  $B$  or since it can only contain ~~large~~ strings that are in  $B$ .

So by  $\textcircled{1}$ , it follows that  $B \subseteq C$  is also regular.

3.  $AB \rightarrow a$  can be removed and any  
where  $A$  is present  $a$  can be replaced

Let  $B' \rightarrow b$

Now  $A \rightarrow B$  becomes

$A \rightarrow BB'$

and  $B \rightarrow Bb$  becomes

$B \rightarrow BB'$

Now  $\Sigma^*$  =

$\{ S \rightarrow AB$

$A \rightarrow BB'$

$A \rightarrow a$

$B' \rightarrow b$

$B \rightarrow BB' \}$  as

starting symbol is  $S$ . and total number  
of rules is 5.

4.

5. Assuming  $w^R$  is the reverse of  $w$ .

$$\Rightarrow |w^R| = |w|$$

Consider a pumping length  $p$ .

and a string in  $L$   $x^R C x^R$  such  
that  $|x| = |x^R| = p$ .

Assuming language  $L$  is regular,  
then a ~~finite~~ subset string of  $x^R C x^R$   
in the first  $\Sigma^*$  symbols can be  
pumped infinitely and ~~the~~ produce  
strings in  $L$ .

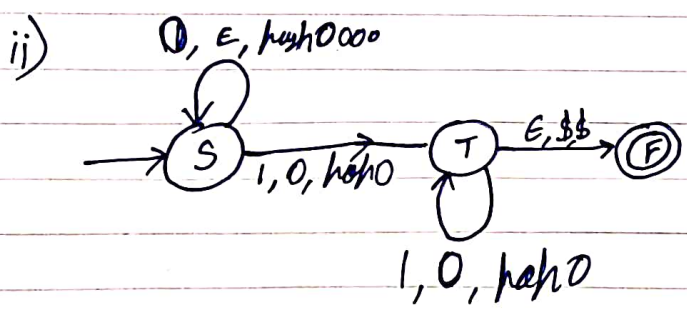
Notice that  $|xcl| \leq p$   
 On choosing any possible subset string from  $x$  and pumping it, we get a string such that  $|w| \neq |w^R|$

this means the new string will not be in  $L$  and hence  $L$  is not regular.

6. Yes  $L$  is context free

i)  $G$  such that  $L(G)$  is

$\{S, \epsilon\}$	// variables
$\{0, 1, \epsilon\}$	// terminals
$\{S \rightarrow 0S \mid 1S \mid \epsilon\}$	// productions
$\{S\}$	// starting



// Assuming first symbol pushed to stack is 0



4. Consider string  $x = aacbac$

it can be derived with

$S \rightarrow aS$	,	$aS$
$S \rightarrow aSbs$	,	$aasbs$
$S \rightarrow c$	,	$aacbc$

and

$S \rightarrow aSbs$	,	$aSbs$
$S \rightarrow aS$	,	$aasbs$
$S \rightarrow c$	,	$aacbc$

hence it is ambiguous.