Computer practical 1-cont: Topics in Statistics III/IV, Term 1

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Aim

- To check some descriptive statistics:
 - Fourfold Plots and Mosaic Plots

Contigency table: data manipulation

Below we load a table where refers to a 1992 survey by the Wright State University School of Medicine and the United Health Services in Dayton, Ohio. The survey asked 2276 students in their final year of high school in a nonurban area near Dayton, Ohio whether they had ever used alcohol, cigarettes, or marijuana. Denote the variables in this $2 \times 2 \times 2$ table by A for alcohol use, C for cigarette use, and M for marijuana use.

Load the observed counts in a data frame obs.frame and print the result. Use commands:

- data.frame(): as in SC2
- factor(): to encode a vector as a factor (aka category)
- expand.grid(): to produce all combinations of the supplied vectors or factors.

```
##
     count marijuana cigarette alcohol
## 1
       911
                  Yes
                                      Yes
                              Yes
## 2
       538
                   No
                              Yes
                                       Yes
## 3
        44
                               No
                                      Yes
                  Yes
## 4
       456
                   No
                               No
                                      Yes
## 5
         3
                  Yes
                              Yes
                                        No
## 6
        43
                   No
                              Yes
                                        No
## 7
         2
                   Yes
                               No
                                        No
## 8
       279
                   No
                               No
                                        No
```

Create 3 dimentional contingency table from obs.frame. Use command:

• xtabs(), to create a contingency table from cross-classifying factors in a dara.frame

```
# this is me again
obs.xtabs <- xtabs(count ~ marijuana+cigarette+alcohol, data=obs.frame)
## print
obs.xtabs
   , , alcohol = No
##
##
            cigarette
## marijuana No Yes
##
         No
            279
         Yes
                2
##
##
   , , alcohol = Yes
##
##
##
            cigarette
## marijuana No Yes
##
         No 456 538
##
         Yes 44 911
     Compute the marginal contigency table of marijuana and cigarette.
```

- Use command margin.table(, margin =) and obs.xtabs.
- Save it in obs.mc.xtabs.

```
obs.mc.xtabs <- margin.table(obs.xtabs, margin=c(1,2))
obs.mc.xtabs

## cigarette
## marijuana No Yes
## No 735 581
## Yes 46 914</pre>
```

Odds ratio calculations

Code an R function, named 'odds.ratio' with:

- Inputs:
 - x: a 2 by 2 matrix whose elements are the observed counts of a 2 by 2 contigency table
 - conf.level: with default input value 0.95 representing the confidence level
 - theta0: with default value 1 representing a null hypothesis value of the odds ratio test
- Outputs:
 - estimator: representing mle of odds satio
 - log.estimator : representing the mle of log odds ratio
 - asympt. SE : representing the standard error / standard deviation of the mle of odds ratio
 - conf.interval: representing confidence interval of mle of odds ratio at sig level conf.level (from the inputs)
 - conf.level =representing confidence level
 - Ztest: representing the test statistic for the odds ratio test (2 tails)

- p.value : representing the p value of the odds ratio test (2 tails)
- log.conf.interval : representing in log scale the confidence interval of mle of odds ratio at sig level conf.level (from the inputs)

```
odds.ratio <- function(x,conf.level=0.95,theta0=1)</pre>
  if (any(x==0)) x <- x+0.5
  theta <- x[1,1] *
    x[2,2]/(x[1,2] *
               x[2,1])
  SE \leftarrow sqrt(sum(1/x))
  Za2 \leftarrow qnorm(0.5 *
                  (1+conf.level))
  Low <- exp(log(theta)-Za2 * SE)
  Up <- exp(log(theta)+Za2 *
               SE)
  CI <- c(Low, Up)
  Z=(log(theta)-log(theta0))/SE
  pv=2
    pnorm(-abs(Z))
  logCI <- log(CI)</pre>
  list (estimator=theta,
        log.estimator=log(theta),
        asympt.SE=SE,
        conf.interval=CI,
        conf.level=conf.level,
        Ztest=Z,
        p.value=pv,
        log.conf.interval=logCI
}
```

For the marginal contigency table of marijuana and cigarette,

- compute the mle of the marginal odds ratio of marijuana and cigarette
- compute the 95% Confidence Interval of the marginal odds ratio of marijuana and cigarette
- perform a statiastical hypothesis test that marijuana and cigarette are independent at sig level 0.05

```
obs.mc.xtabs <- margin.table(obs.xtabs, margin=c(1,2))
odds.ratio.marijuana.cigarette <- odds.ratio(obs.mc.xtabs, conf.level=0.95, theta0=1)
odds.ratio.marijuana.cigarette

## $estimator
## [1] 25.1362
##
## $log.estimator
## [1] 3.224309
##
## $asympt.SE
## [1] 0.1609812</pre>
```

```
##
## $conf.interval
## [1] 18.33463 34.46093
##
## $conf.level
## [1] 0.95
##
## $Ztest
## [1] 20.02911
##
## $p.value
## [1] 3.071215e-89
##
## $log.conf.interval
## [1] 2.908792 3.539826
```

The MLE of the marginal odds ratio of marijuana and cigarette is 25.136197.

The 95% confidence interval of the marginal odds ratio of marijuana and cigarette is [18.33463, 34.4609298].

The hypothesis test with $H_0: \theta = 1$ versus $H_1: \theta \neq 1$ at sig. level 0.05 has a p-value $3.0712155 \times 10^{-89}$ Hence I reject $H_0: \theta = 1$ against $H_1: \theta \neq 1$ at sig. level 0.05.

Fourfold Plots

You can draw Fourfold Plots

Tables 2 x 2

It is a graphical expression visualizing the odds ratio

$$\theta = \frac{n_{11}n_{22}}{n_{12}n_{21}}$$

in 2×2 contingency tables.

It shows the departure from independence as measured by the sample odds ratio,

Each cell n_{ij} is represented as a quarter-circle with radius proportional to $\sqrt{n_{ij}}$ and area proportional to n_{ij} .

- If there is no association $\theta = 1$ between classification variables, the quarter-circles should form a circle.
- If there is positive association $\theta > 1$ between classification variables, the diagonal areas are greater than the off-diagonal areas
- If there is negative association $\theta < 1$ between classification variables, the diagonal areas are smaller than the off-diagonal areas

R provides a function to draw this kind of plots by using the function fourfoldplot' from the packageved'

• Install 'vcd' package and load it

install.packages('vcd') # IF NOT ALREADY INSTALLED ON YOUR PC, THEN UNCOMMENT AND RUN THIS COMMAND
library(vcd)

Loading required package: grid

Check in help the function fourfoldplot by usign the command '?fourfoldplot'

- Draw a Fourfold Plot for the marginal contigency table of marijuana and cigarette.
- Discuss what you can see

```
#
#
#
```

Note that:

- * The area of each shaded quadrant shows the observed counts.
- * Circular arcs show the limits of confidence interval for the odds ratio.

Tables $2 \times 2 \times K$

Fourfold Plots can be also used for 2 x 2 x K contigancy tables

- Draw a Fourfold Plot for the contigency table of marijuana cigarette, and alcohol by controlling on the alcohol levels.
- inspect the plots

```
#
#
#
```

Mosaic plot

Mosaic plot display graphically the cells of a contingency table as rectangular areas of size proportional to the corresponding observed frequencies.

When the classification variables are independent the areas tend to be perfectly aligned in rows and columns.

The greater the deviation is, the worse the aforesaid alignment is.

Furthermore, specific locations of the table that deviate from independence the most can be identified and thus the pattern of underlying association can be explained.

The strength of individual cells contribution to divergence from independence as well as the direction of the divergence are reflected in the magnitude and sign of the corresponding independence model's residuals that can be incorporated in a mosaic plot.

R provides a function to draw this kind of plots by using the function mosaic' from the packageved'

• Install 'vcd' package and load it

install.packages('vcd') # IF NOT ALREADY INSTALLED ON YOUR PC, THEN UNCOMMENT AND RUN THIS COMMAND
library(vcd)

• Check the command 'mosaic' in help by typing '?mosaic'

For the I x J case:

- Draw a Mosaic Plot for the marginal contigency table of marijuana cigarette.
- in particular use use mosaic(x,residuals_type="deviance",gp=shading_hcl) where x is the contigency table of interest
- Interpretet the plots

For the I x J x K case:

- Draw a Mosaic Plot for the contigency table of marijuana cigarette and alcohol.
- Interpretet the plots

```
#
#
#
```

Save me

Generate the document as a Notebook, PDF, Word, or HTML by choosing the relevant option (from the pop-up menu next to the Preview button). Then save your Markdown code by choosing the relevant option (from the task bar menu).

Save the *.Rmd script, so that you can edit it later.