

MEHR ALS LINEAR ODER LOGISTISCH?

QUANTILS REGRESSIONEN UND ADAPTIVE SPLINES IN SAS

MIHAI PAUNESCU

QUANTILS- REGRESSION

QUANTILE



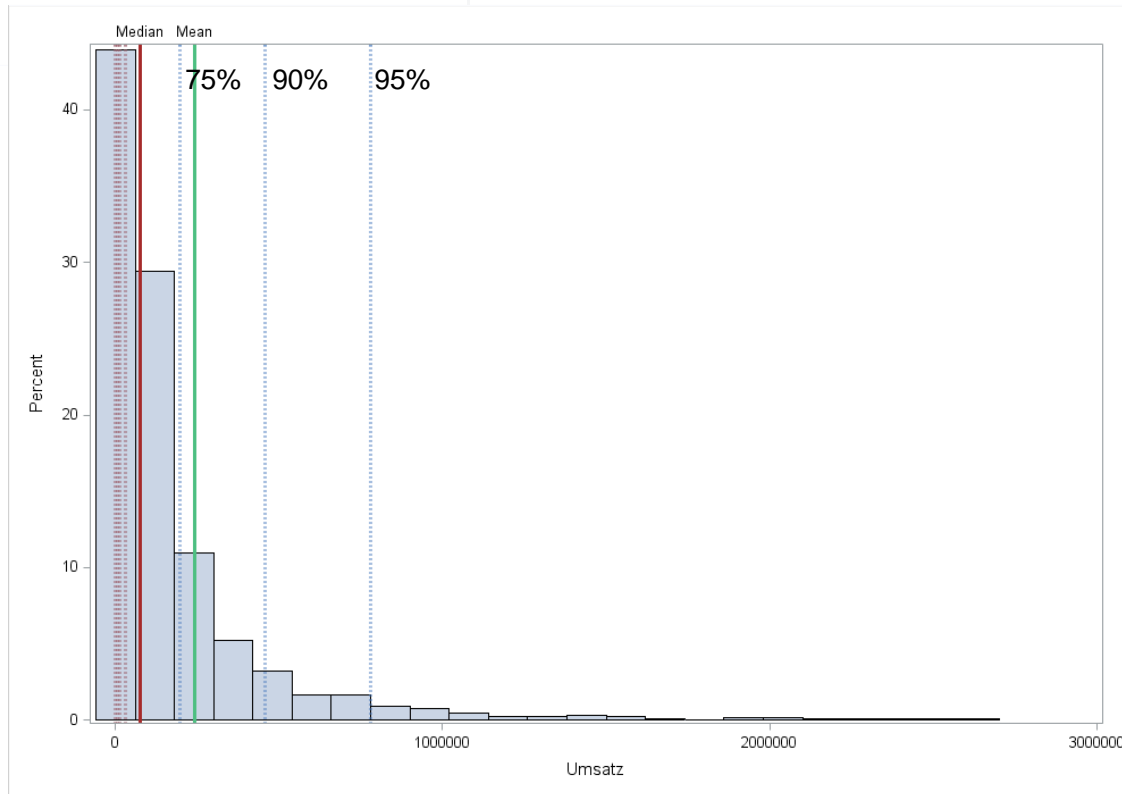
```
proc univariate data=dat;
ods select moments quantiles;
var sales;
run;
```

| Basic Statistical Measures | | | |
|----------------------------|----------|---------------------|----------|
| Location | | Variability | |
| Mean | 241825.8 | Std Deviation | 823581 |
| Median | 75875.1 | Variance | 6,78E+16 |
| Mode | . | Range | 18605198 |
| | | Interquartile Range | 168416 |

| Quantiles (Definition 5) | |
|--------------------------|-------------|
| Level | Quantile |
| 100% Max | 18605230.40 |
| 99% | 2699730.30 |
| 95% | 779877.70 |
| 90% | 458327.90 |
| 75% Q3 | 198564.00 |
| 50% Median | 75875.10 |
| 25% Q1 | 30147.60 |
| 10% | 13607.10 |
| 5% | 5598.60 |
| 1% | 500.75 |
| 0% Min | 32.55 |

QUANTILS- REGRESSION

QUANTILE IM HISTOGRAMM



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```
ods graphics on / width=1000px height=700px;
proc sgplot data=dat;
  where sales < 2699730.30;
  histogram sales;
  refline 779877.70 458327.90 198564.00 / axis=x lineattrs=(color=bigb pattern=dot thickness=3);
  refline 30147.60 13607.10 5598.60 500.75 /axis=x lineattrs=(color=dapk pattern=dot thickness=3);
  refline 75875.10 /axis=x label='Median' lineattrs=(color=brown thickness=3);
  refline 241825.8 /axis=x label='Mean' lineattrs=(color=big thickness=3);
run;
```

```
proc quantreg data=dat;  
  model Sales= / quantile=(0.5);  
run;
```

| Parameter Estimates | | | | | | |
|---------------------|----|----------|----------------|-----------------------|------------|---------|
| Parameter | DF | Estimate | Standard Error | 95% Confidence Limits | | t Value |
| Intercept | 1 | 75875.10 | 2.654.220 | 70.670.691 | 81.079.509 | 28.59 |
| | | | | | | Pr > t |

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QUANTILS- REGRESSION

KLASSIFIKATIONSVARIABLEN



```
proc quantreg data=dat ci=resampling ;
  class cust_grp;
  model Sales=cust_grp / quantile=(0.5) seed=12345;
run;
```

| Parameter Estimates | | | | | | | | |
|---------------------|---|----|----------|----------------|-----------------------|------------|---------|---------|
| Parameter | | DF | Estimate | Standard Error | 95% Confidence Limits | | t Value | Pr > t |
| Intercept | | 1 | 47335.60 | 3.071.371 | 41.313.237 | 53.357.963 | 15.41 | <.0001 |
| Cust_grp | I | 1 | 88078.60 | 6.903.957 | 74.541.278 | 101615.92 | 12.76 | <.0001 |
| Cust_grp | O | 1 | 21870.35 | 5.324.410 | 11.430.214 | 32.310.486 | 4.11 | <.0001 |
| Cust_grp | N | 0 | 0.0000 | 0.0000 | 0.0000 | 0.0000 | . | . |

```
proc means data=dat P1 median P90;
  var sales;
  class Cust_grp;
run;
```

| Analysis Variable : Sales | | |
|---------------------------|-------|----------|
| Cust_grp | N Obs | Median |
| I | 793 | 135414.2 |
| O | 1024 | 69062.08 |
| N | 1004 | 47323.3 |

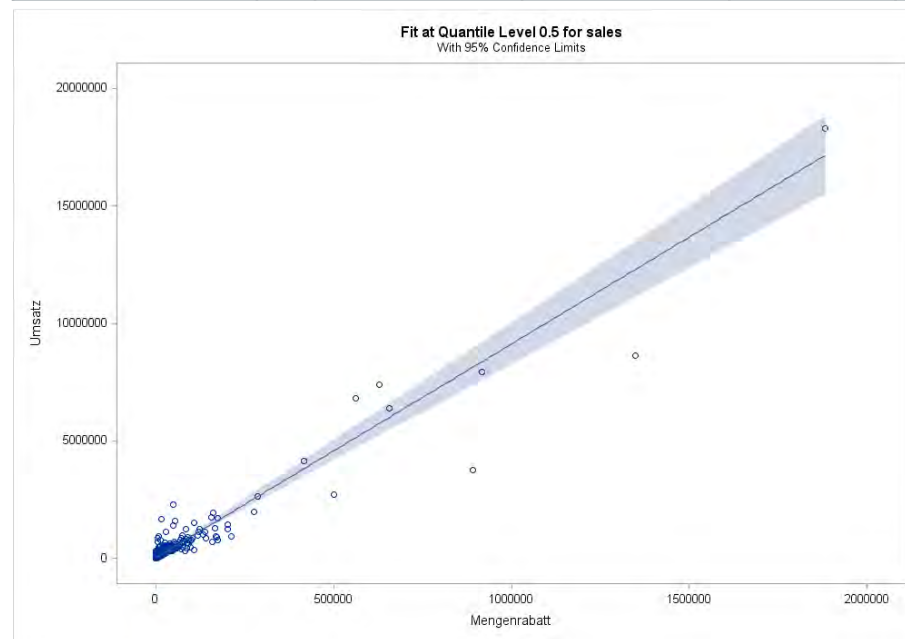
$$47335.6 + 88078.6 = 135414.2$$

QUANTILS- REGRESSION

MEDIAN SCHÄTZUNG FÜR INTERVALVARIABLE

```
proc quantreg data=dat ci=resampling plots=(fitplot);
  where cust_grp='n';
  model Sales=Rabatt_Menge / quantile=(0.5) seed=12345;
run;
```

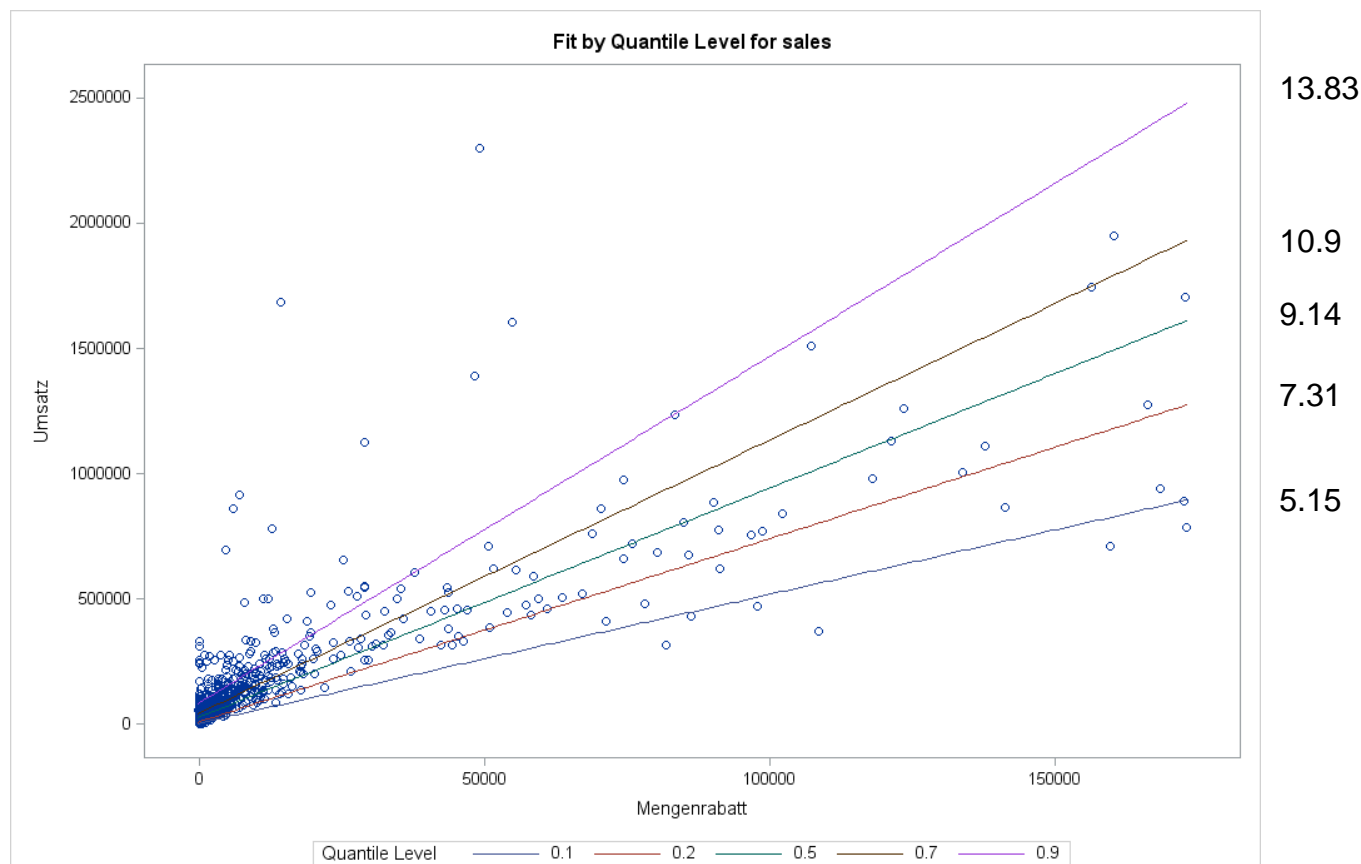
| Parameter Estimates | | | | | | | |
|---------------------|----|----------|----------------|-----------------------|-----------|---------|---------|
| Parameter | DF | Estimate | Standard Error | 95% Confidence Limits | | t Value | Pr > t |
| Intercept | 1 | 28552.1 | 5873.371 | 17026.581 | 40077.615 | 4.86 | <.0001 |
| Rabatt_Menge | 1 | 9.1 | 0.4522 | 8.2082 | 9.9829 | 20.12 | <.0001 |



QUANTILS- REGRESSION

QUANTILSCHÄTZUNG FÜR INTERVALVARIABLE

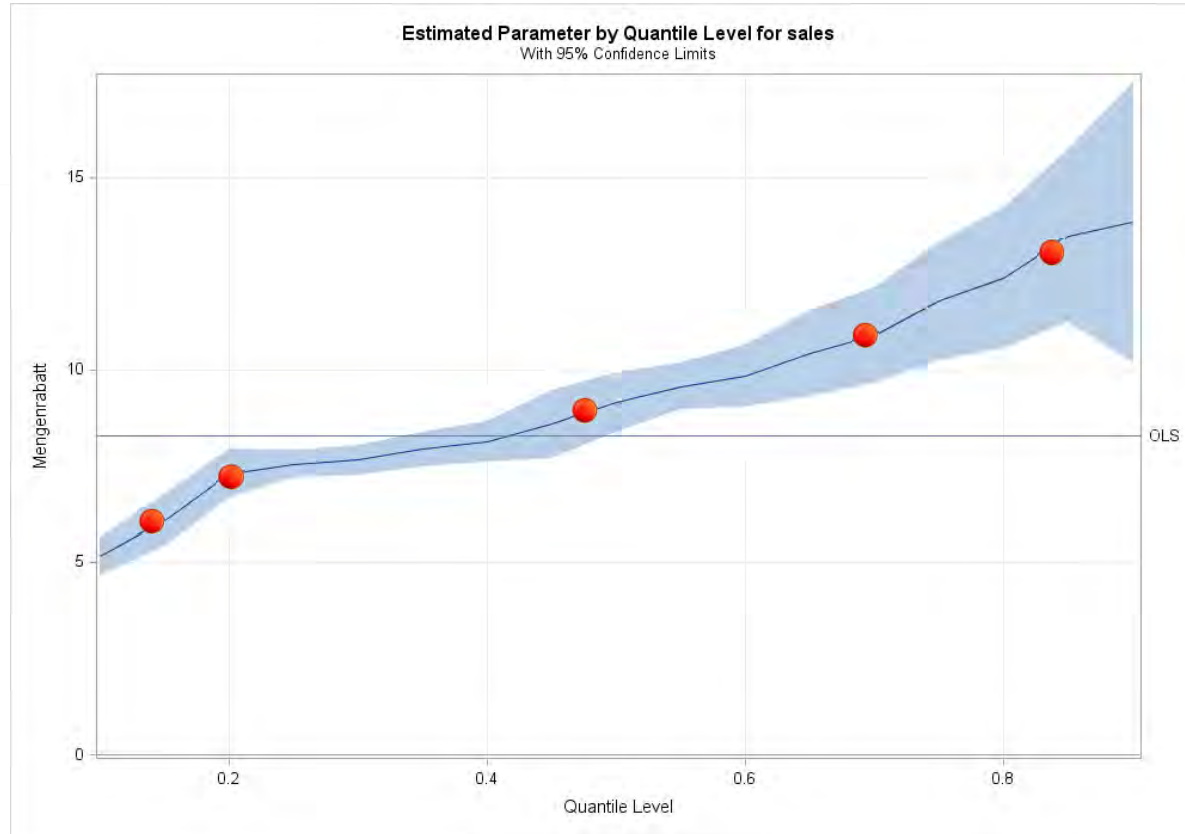
```
proc quantreg data=dat ci=resampling plots=(fitplot);  
ods select fitplot;  
where cust_grp='n' and Rabatt_Menge < 200000;  
model Sales=Rabatt_Menge / quantile=(0.1 0.2 0.5 0.7 0.9) seed=12345;  
run;
```



QUANTILS- REGRESSION

QUANTILE PROZESS PLOT

```
proc quantreg data=dat ci=resampling;  
ods select quantplot;  
where cust_grp='n' and Rabatt_Menge < 200000;  
model Sales=Rabatt_Menge  
/quantile=(0.1 to 0.9 by 0.05) plot=(quantplot /unpack ols) seed=1268 ;  
run;
```



13.83

10.9

9.14

7.31

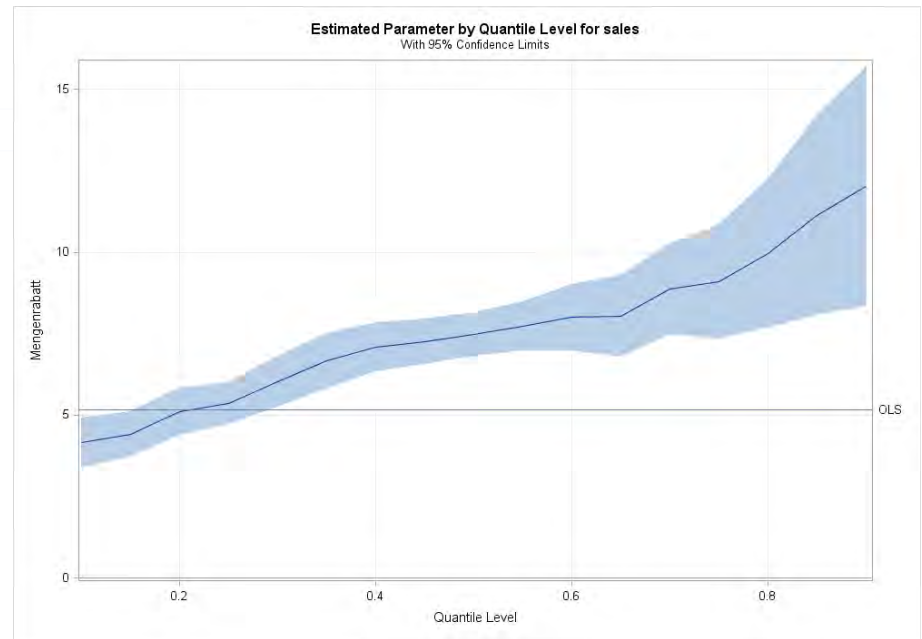
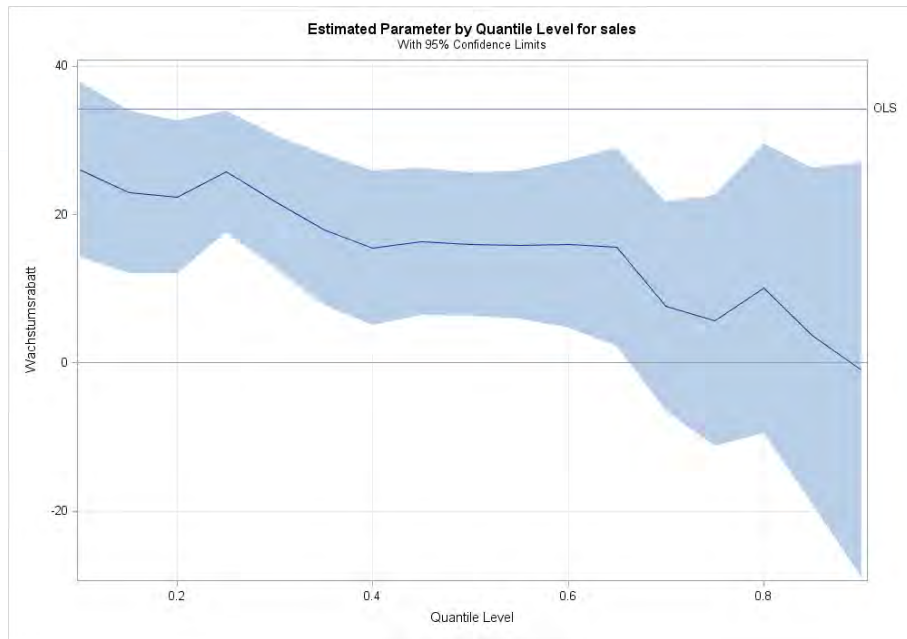
5.15

QUANTILS- REGRESSION

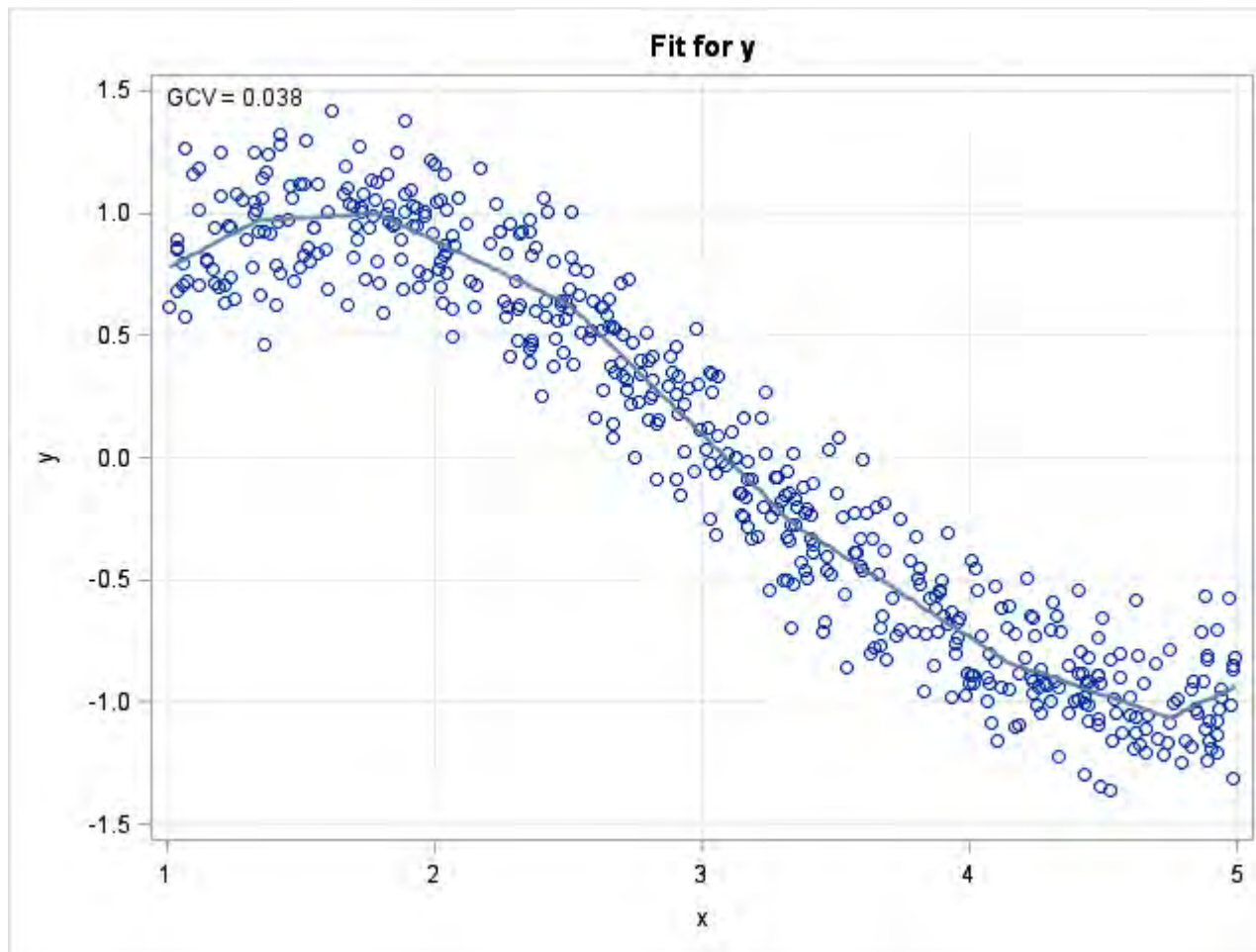
MULTIVARIATE QUANTILSREGRESSION



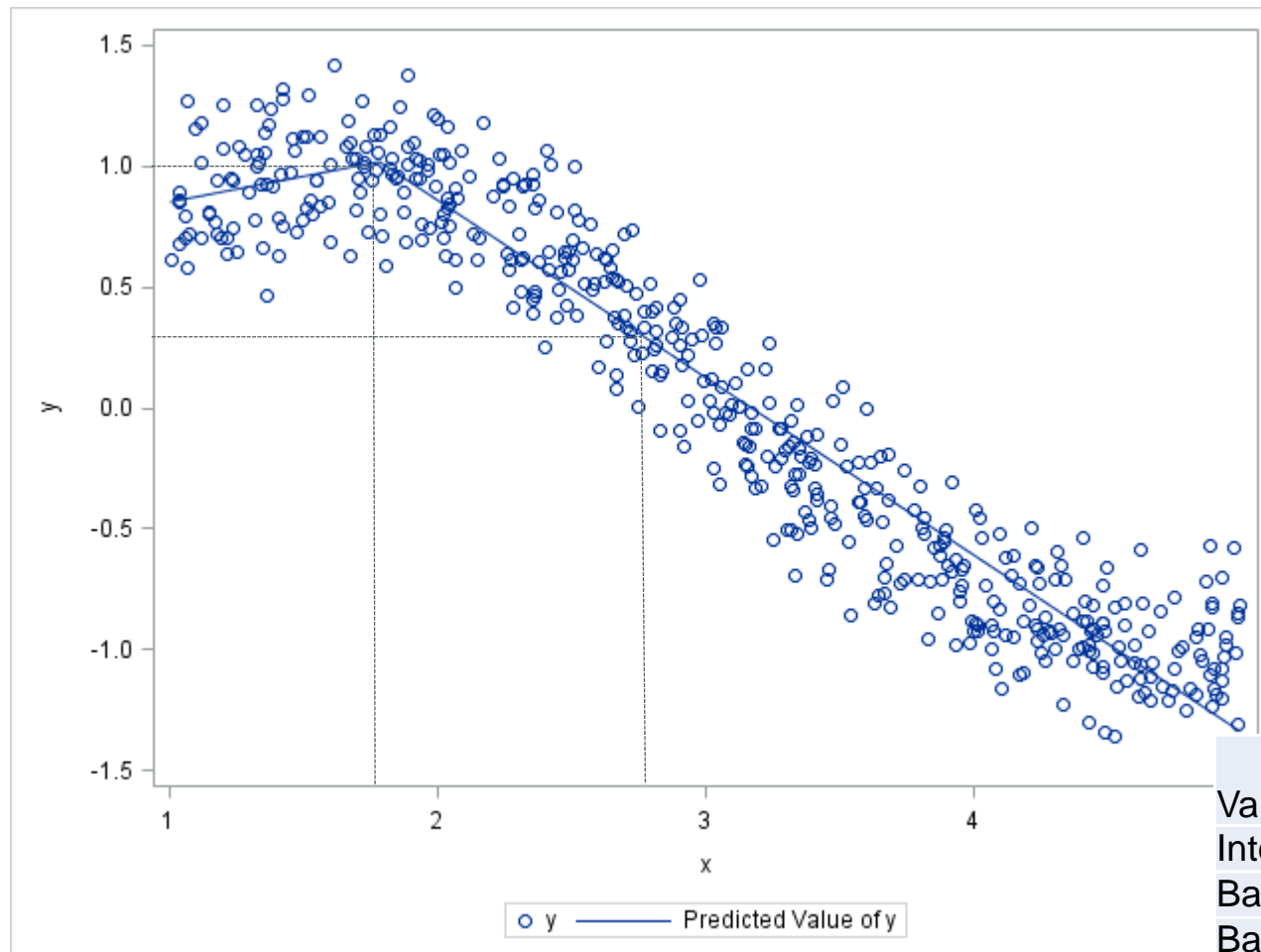
```
proc quantreg data=dat ci=resampling;  
where cust_grp='n';  
model Sales=Rabatt_Wachstum Rabatt_Menge /  
quantile=(0.1 to 0.9 by 0.05) plot=(quantplot /unpack ols) seed=1268 ;  
run;
```



- Verwendung:
 - Zusammenhänge entdecken für extreme Bereiche der Zielvariable
 - Robuste Medianschätzung gegenüber Ausreißer, ohne Verteilungsannahmen
- Hinweise:
 - Ist nicht äquivalent zu linearen Regressionen für Segmente von Beobachtungen
 - Schneller: HPQUANTSELECT ab SAS/STAT 13.2



```
proc adaptivereg  
plots=all  
details=bases;  
  
model y = x;  
  
run;
```

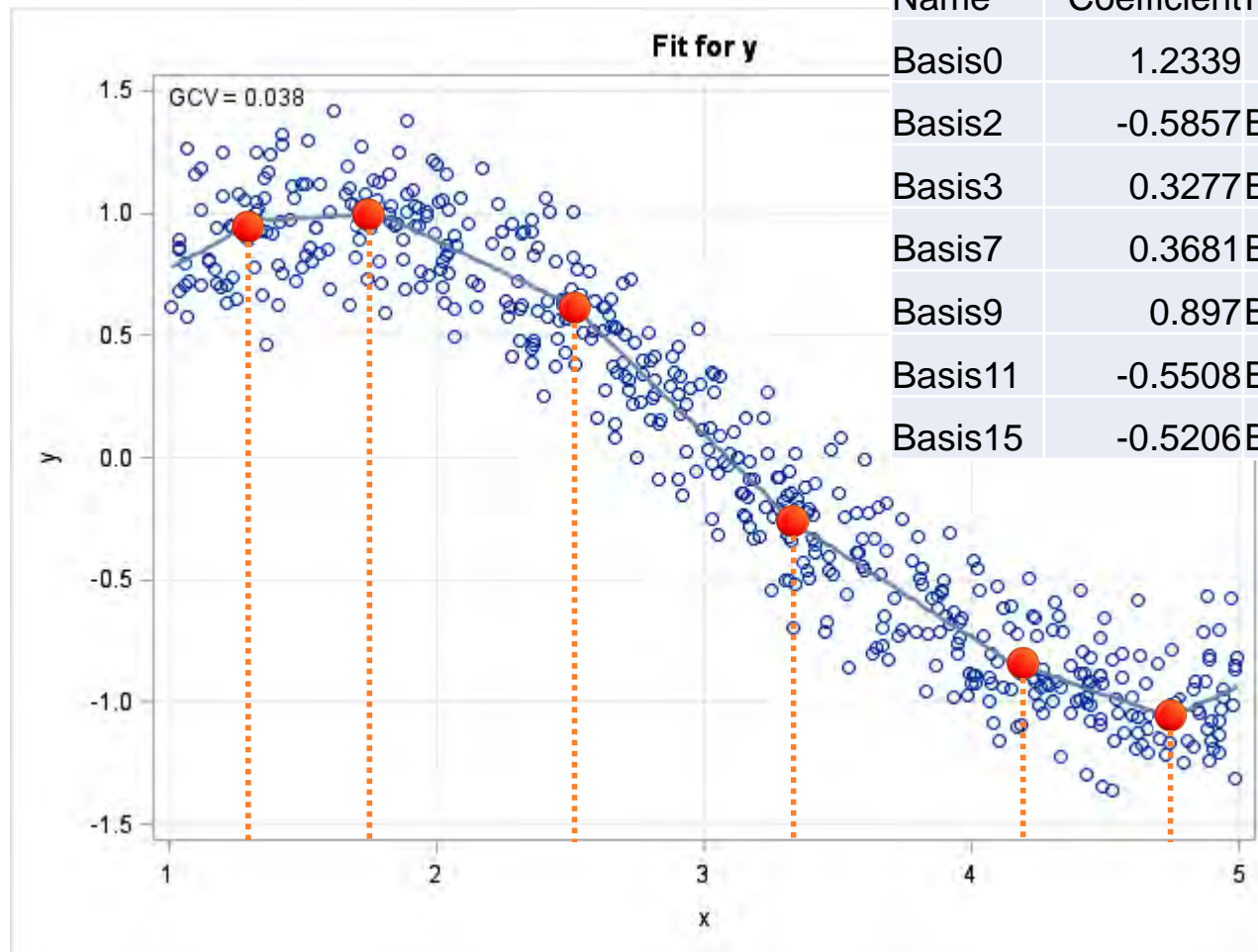


| | |
|--------|--------------------------|
| Basis1 | $\text{MAX}(x - 1.8, 0)$ |
|--------|--------------------------|

| | |
|--------|--------------------------|
| Basis2 | $\text{MAX}(1.8 - x, 0)$ |
|--------|--------------------------|

```
data ds2;  
set ds;  
Basis1 = max(x-1.8, 0);  
Basis2 = max(1.8 - x, 0);  
run;  
  
proc reg data=ds2;  
model y = basis1 basis2;  
run;
```

| Variable | Parameter Estimate | t Value | Pr > t |
|-----------|--------------------|---------|---------|
| Intercept | 1.02 | 52.04 | <.0001 |
| Basis1 | -0.73 | -67.82 | <.0001 |
| Basis2 | -0.21 | -3.31 | 0.001 |



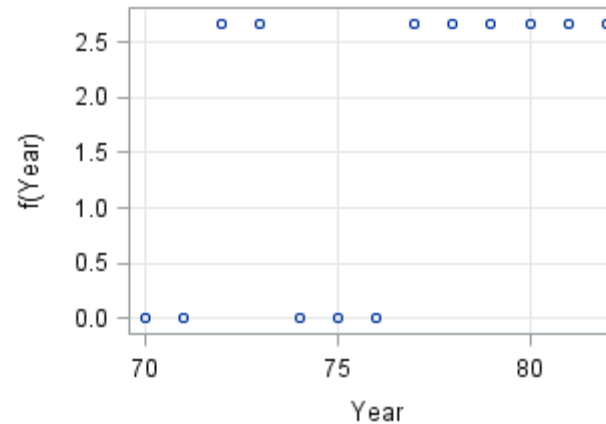
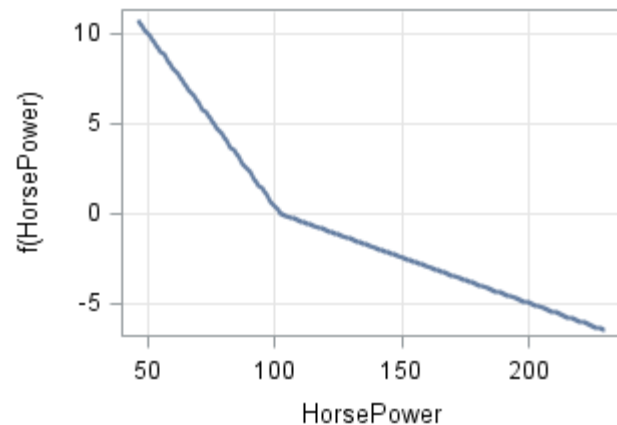
Regression Spline Model after Backward Selection

| Name | Coefficient | Parent | Variable | Knot |
|---------|-------------|--------|-----------|--------|
| Basis0 | 1.2339 | | Intercept | |
| Basis2 | -0.5857 | Basis0 | x | 1.7865 |
| Basis3 | 0.3277 | Basis0 | x | 4.1447 |
| Basis7 | 0.3681 | Basis0 | x | 3.3424 |
| Basis9 | 0.897 | Basis0 | x | 4.7489 |
| Basis11 | -0.5508 | Basis0 | x | 2.5061 |
| Basis15 | -0.5206 | Basis0 | x | 1.3345 |

```
proc adaptivereg data=autompg plots=all details=bases;
class cylinders year origin;
model mpg = cylinders displacement horsepower
weight acceleration year origin / additive;
run;
```

| Basis Information | |
|-------------------|--|
| Name | Transformation |
| Basis0 | 1 |
| Basis1 | Basis0*MAX(Weight - 3139,0) |
| Basis2 | Basis0*MAX(3139 - Weight,0) |
| Basis3 | Basis0*NOT(MISSING(HorsePower)) |
| Basis4 | Basis0*MISSING(HorsePower) |
| Basis5 | Basis3*MAX(HorsePower - 102,0) |
| Basis6 | Basis3*MAX(102 - HorsePower,0) |
| Basis7 | Basis0*(Year = 80 OR Year = 82 OR Year = 81 OR Year = 79 OR Year = 78 OR Year = 77 OR Year = 73 OR Year = 72) |
| Basis8 | Basis0*NOT(Year = 80 OR Year = 82 OR Year = 81 OR Year = 79 OR Year = 78 OR Year = 77 OR Year = 73 OR Year = 72) |
| Basis9 | Basis0*MAX(Displacement - 85,0) |
| Basis10 | Basis0*MAX(85 - Displacement,0) |
| Basis11 | Basis0*MAX(Displacement - 97,0) |
| Basis12 | Basis0*MAX(97 - Displacement,0) |
| Basis13 | Basis0*MAX(Acceleration - 21,0) |
| Basis14 | Basis0*MAX(21 - Acceleration,0) |
| Basis15 | Basis3*MAX(Displacement - 105,0) |
| Basis16 | Basis3*MAX(105 - Displacement,0) |

| Basis Information | | |
|-------------------|-------------|--|
| Name | Coefficient | Transformation |
| Basis3 | -4.03 | Basis0*NOT(MISSING(HorsePower)) |
| Basis4 | 0 | Basis0*MISSING(HorsePower) |
| Basis5 | -0.05 | Basis3*MAX(HorsePower - 102,0) |
| Basis6 | 0.19 | Basis3*MAX(102 - HorsePower,0) |
| Basis7 | 2.67 | Basis0*(Year = 80 OR Year = 82 OR Year = 81 OR Year = 79 OR Year = 78 OR Year = 77 OR Year = 73 OR Year = 72) |
| Basis8 | 0 | Basis0*NOT(Year = 80 OR Year = 82 OR Year = 81 OR Year = 79 OR Year = 78 OR Year = 77 OR Year = 73 OR Year = 72) |



PROC Adaptivereg

<http://support.sas.com/resources/papers/proceedings13/457-2013.pdf>

Weitere Nicht-Parametrische Regressionen: PROC GAM, PROC LOESS