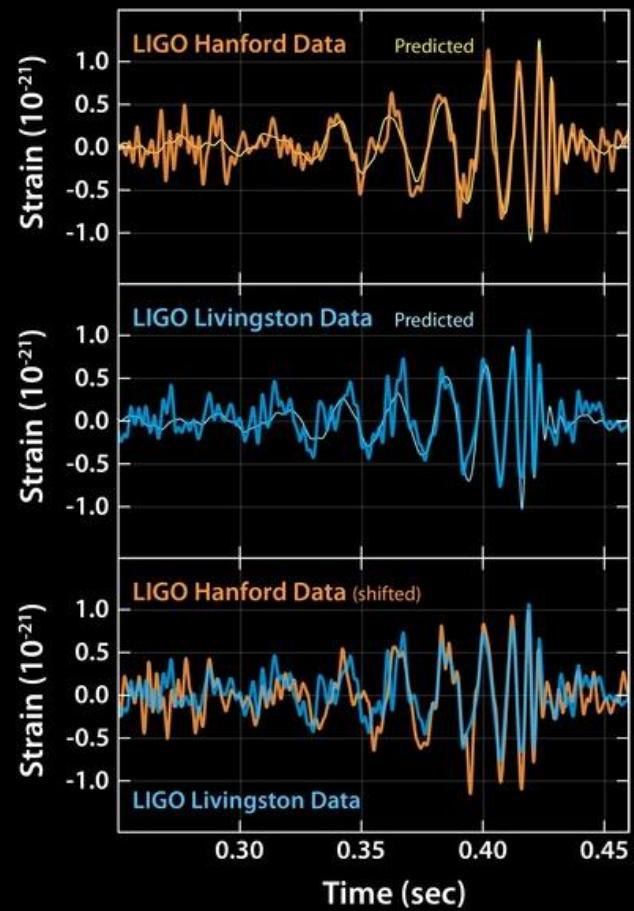
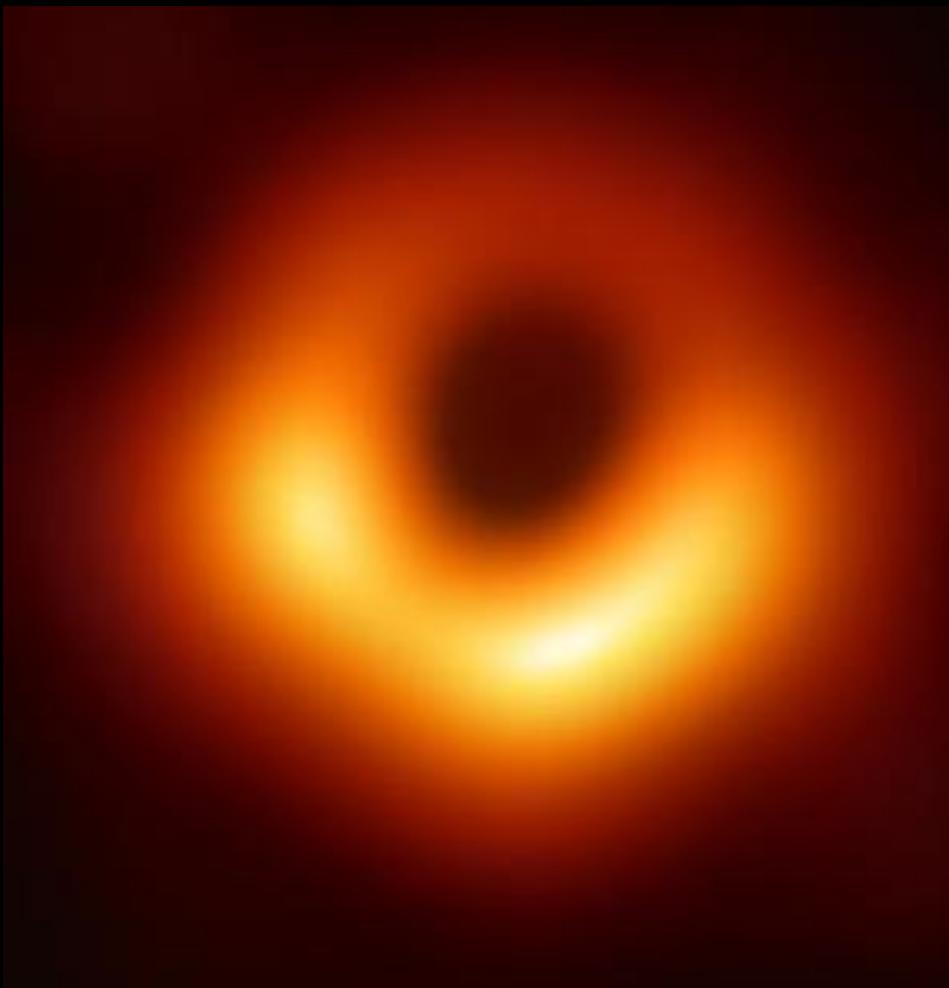
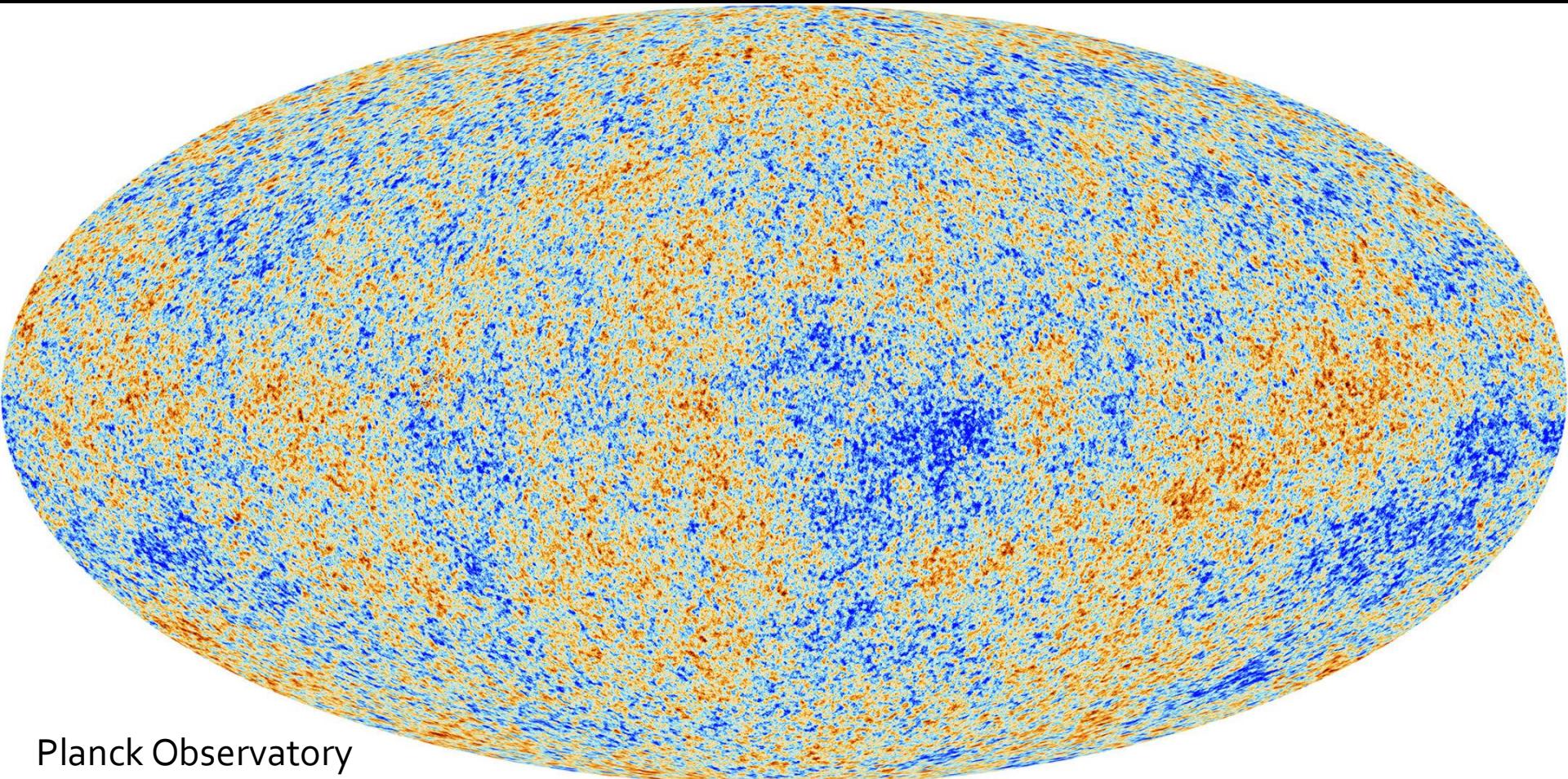


Gravity and black holes



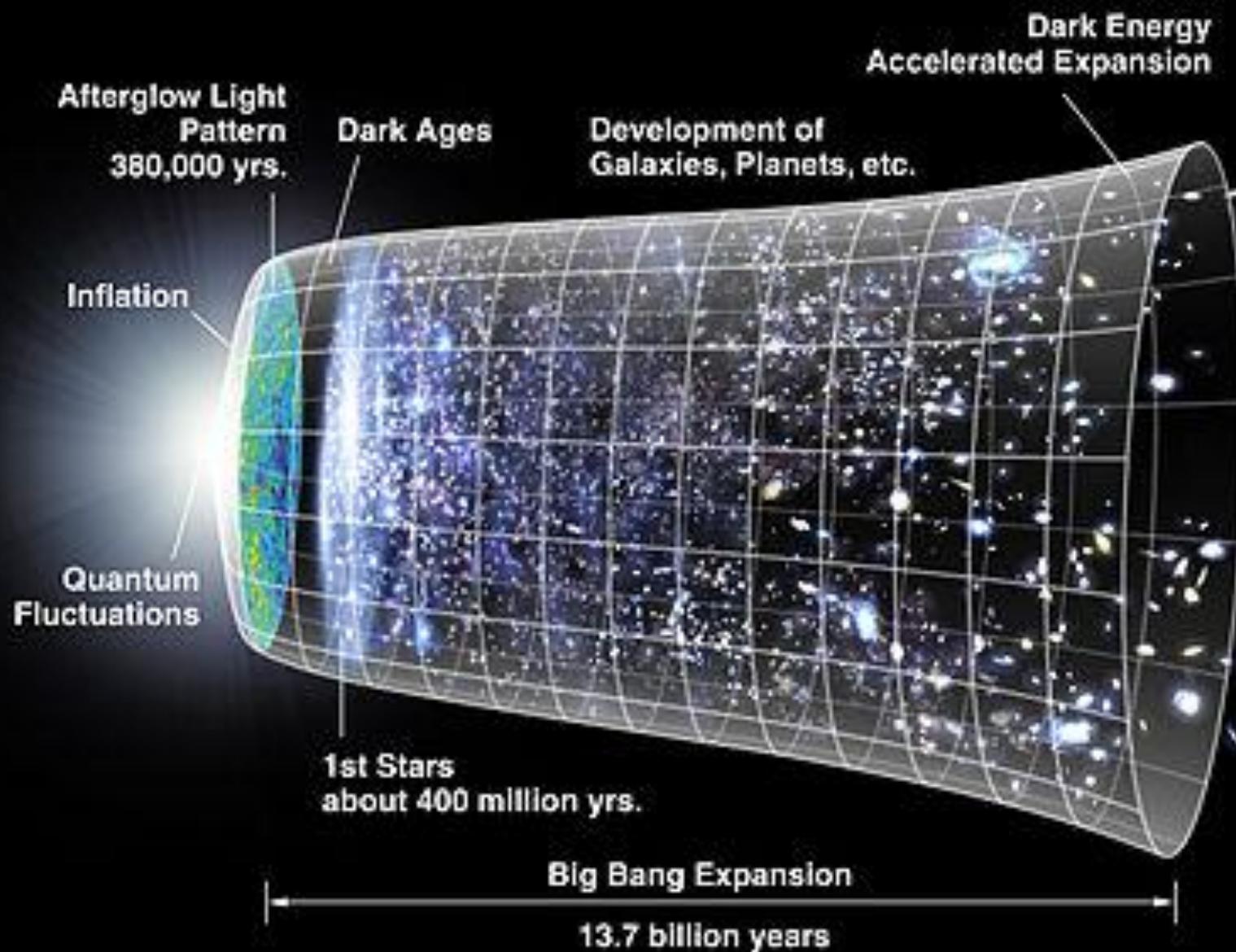
Big Bang: Cosmic Microwave Background



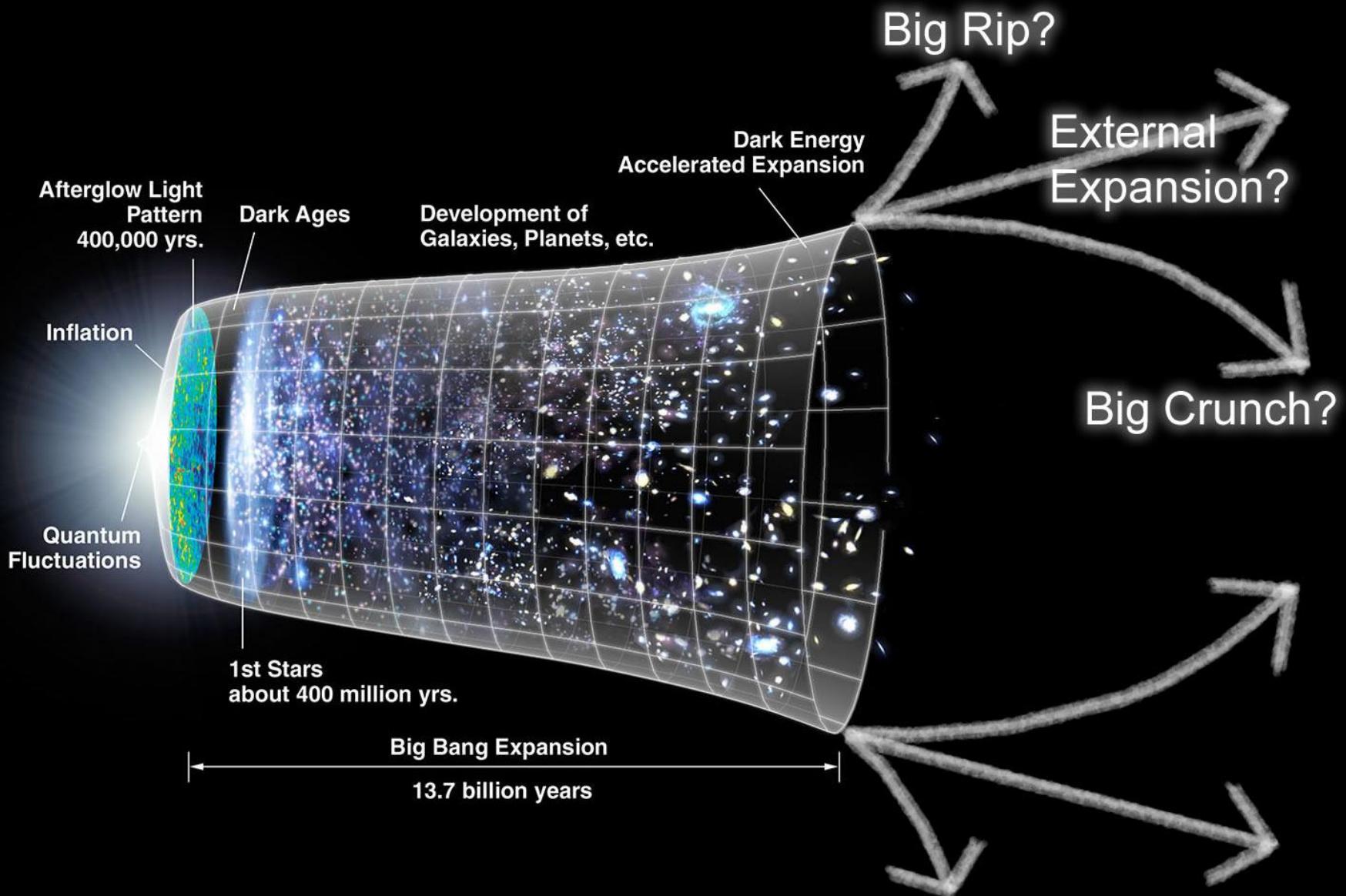
Planck Observatory

Universe was smooth at 1 part in 10,000

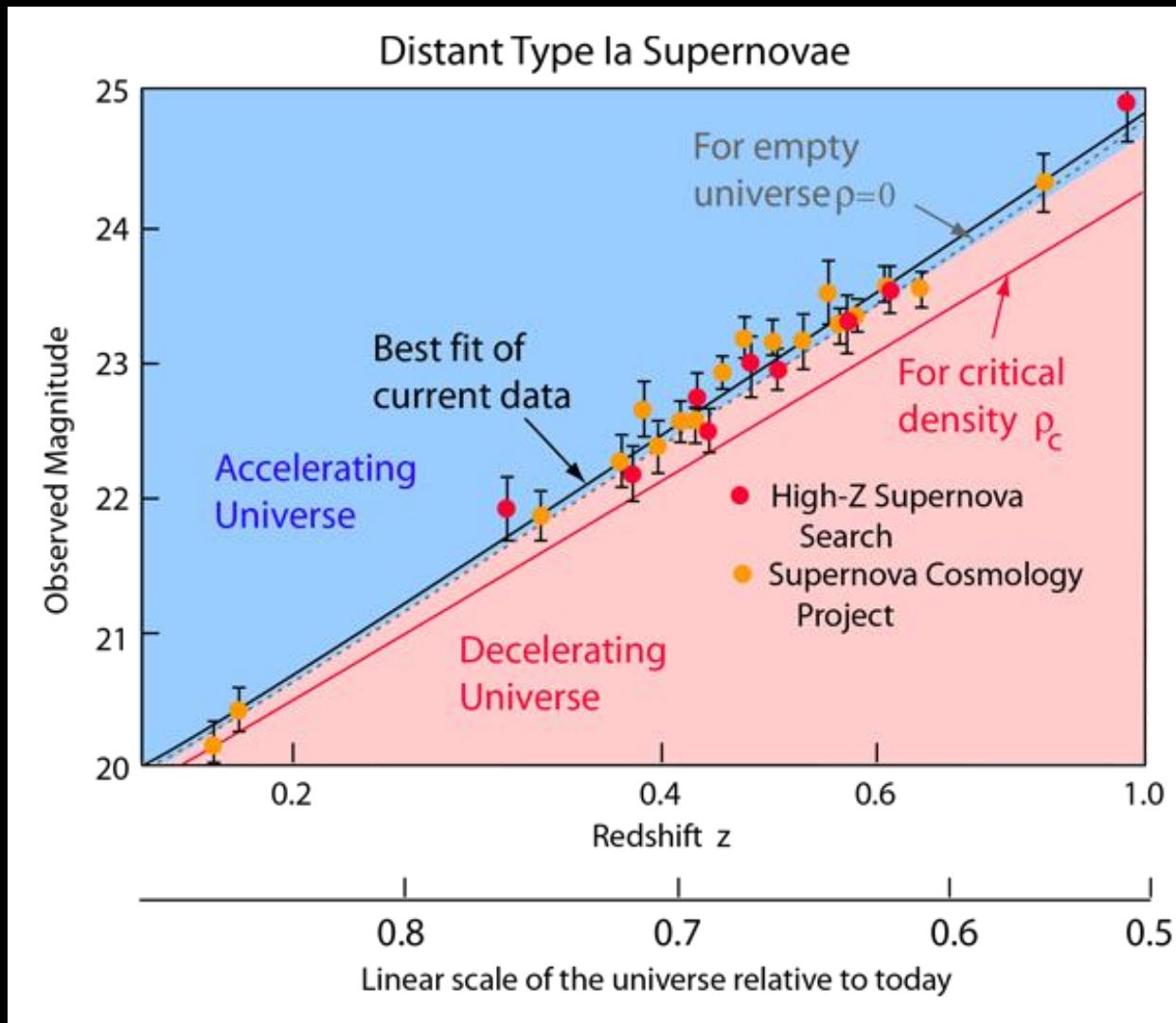
Cosmology in a single plot



Cosmological Future



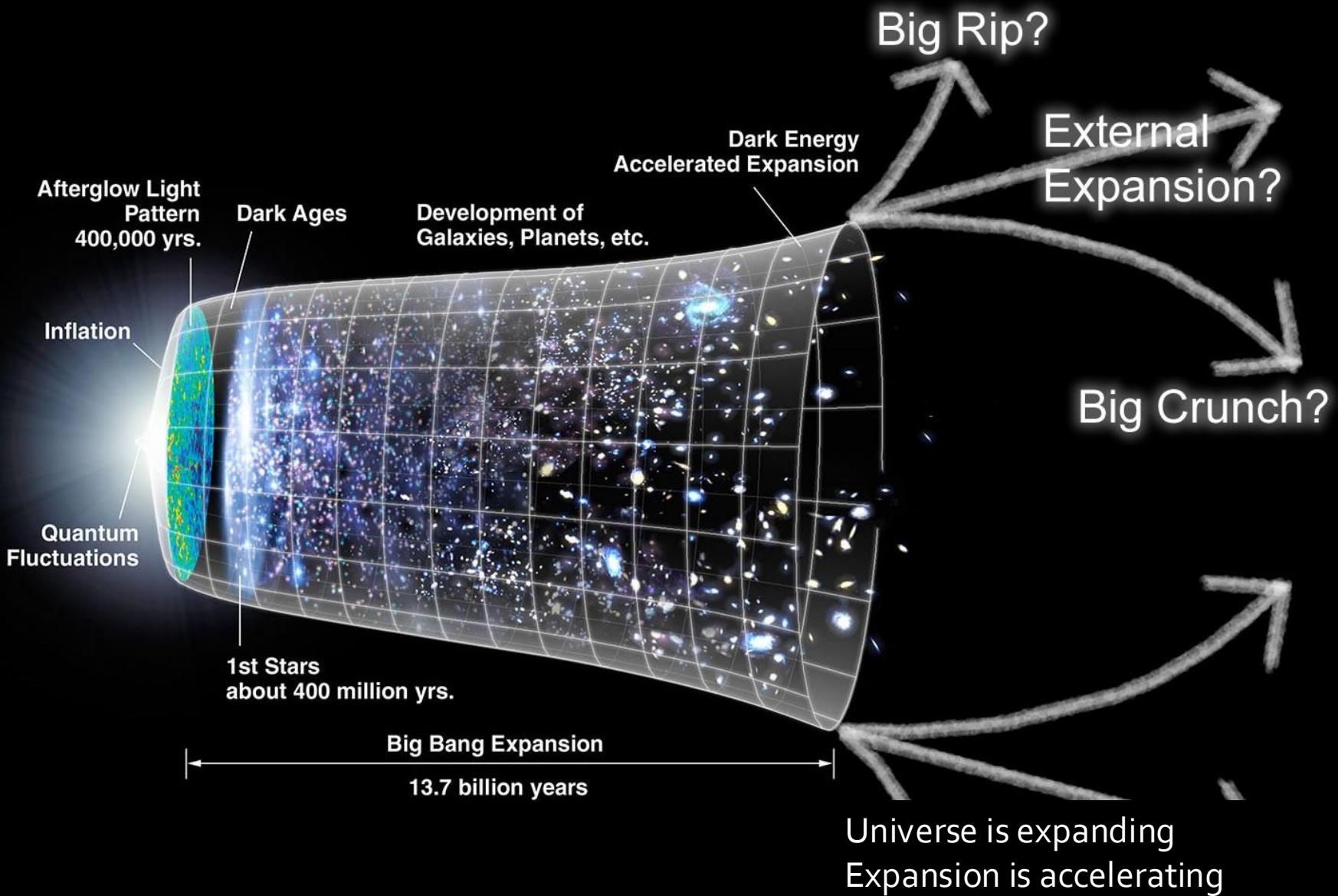
Universe expansion is accelerating



Type 1a supernova:
standard candles
(always the same
brightness)

Distance versus
redshift allows us to
see that expansion is
accelerating

Cosmological Future



Big Rip (Big Chill/Heat Death): the far-future of the universe

If expansion continues to accelerate

-13.5 billion years: Big Bang

-5 billion years: Sun formed

2 billion years: people better leave Earth

5 billion years: sun evolves off main sequence

4-8 billion years: Andromeda Galaxy, Milky Way merge

100-1,000 billion years: Local Group galaxies merge

150 billion years: galaxies beyond local subcluster will pass beyond cosmological horizon (no causal interactions)

800 billion years: stars burn out, little star formation; luminosities diminish

2 trillion years: galaxies outside local supercluster not detectable

1-100 trillion years: star formation ends

1e20 years: galaxies ripped apart; stars flung out or eaten by black holes

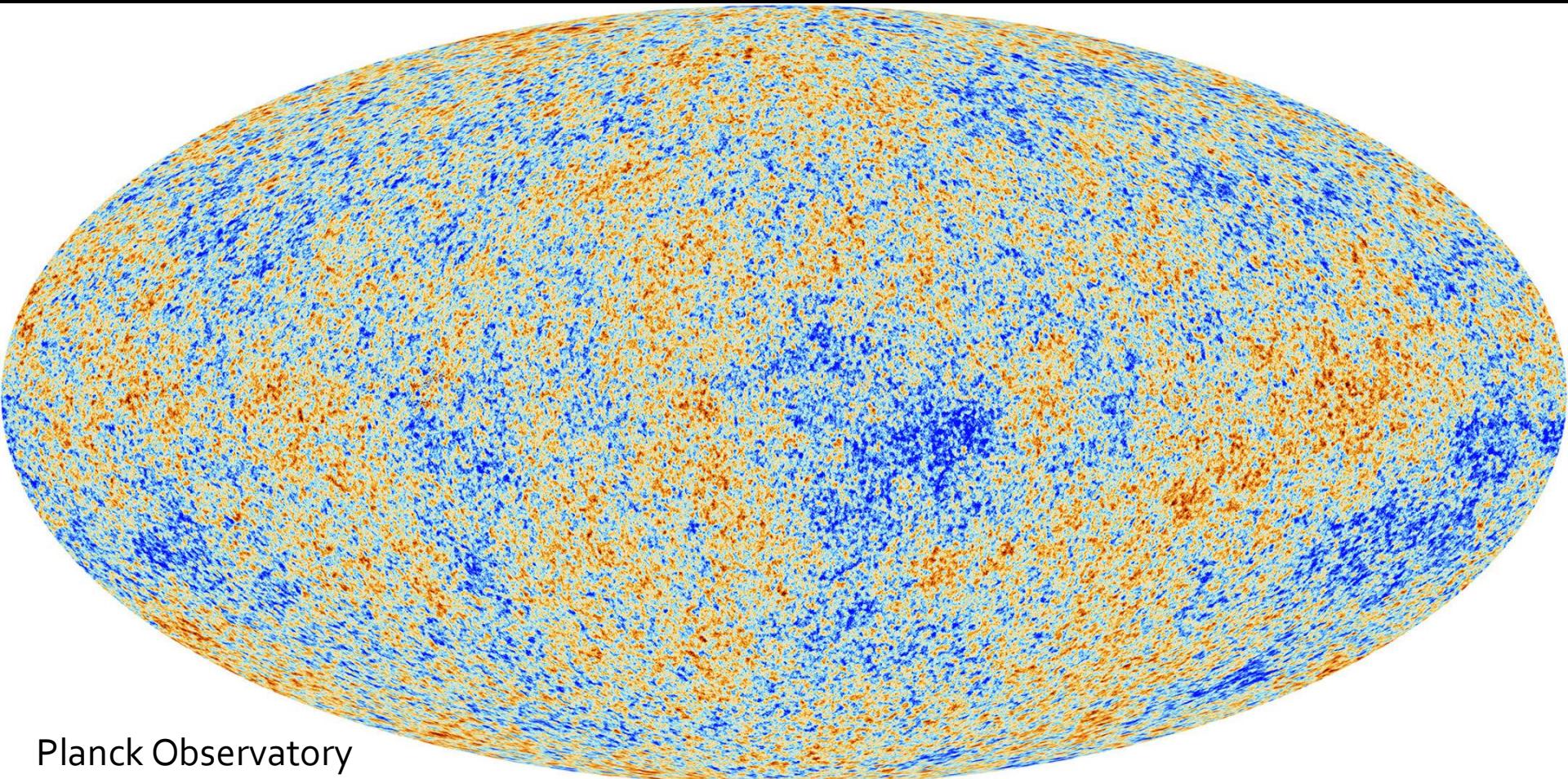
1e50 years: protons decay, normal matter no longer exists

1e70 years: black holes evaporate

1e100 years: supermassive black holes evaporate

1e1000 years to eternity: dark era, heat death

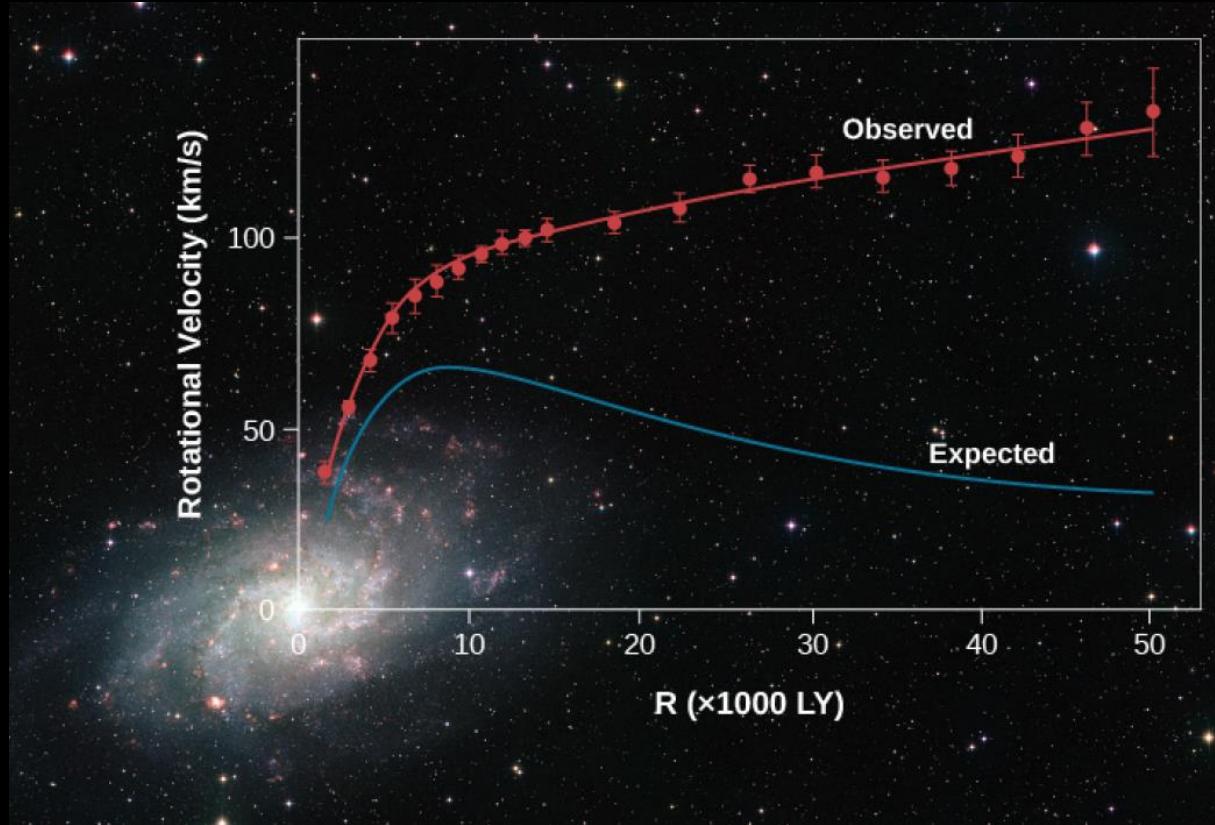
Big Bang: Cosmic Microwave Background



Planck Observatory

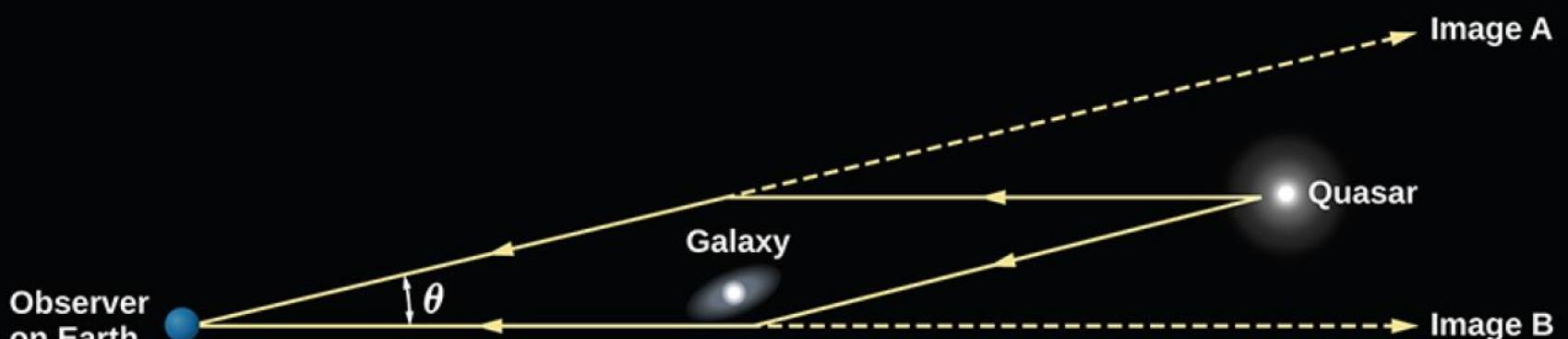
Universe was smooth at 1 part in 10,000

Measuring masses of large structures

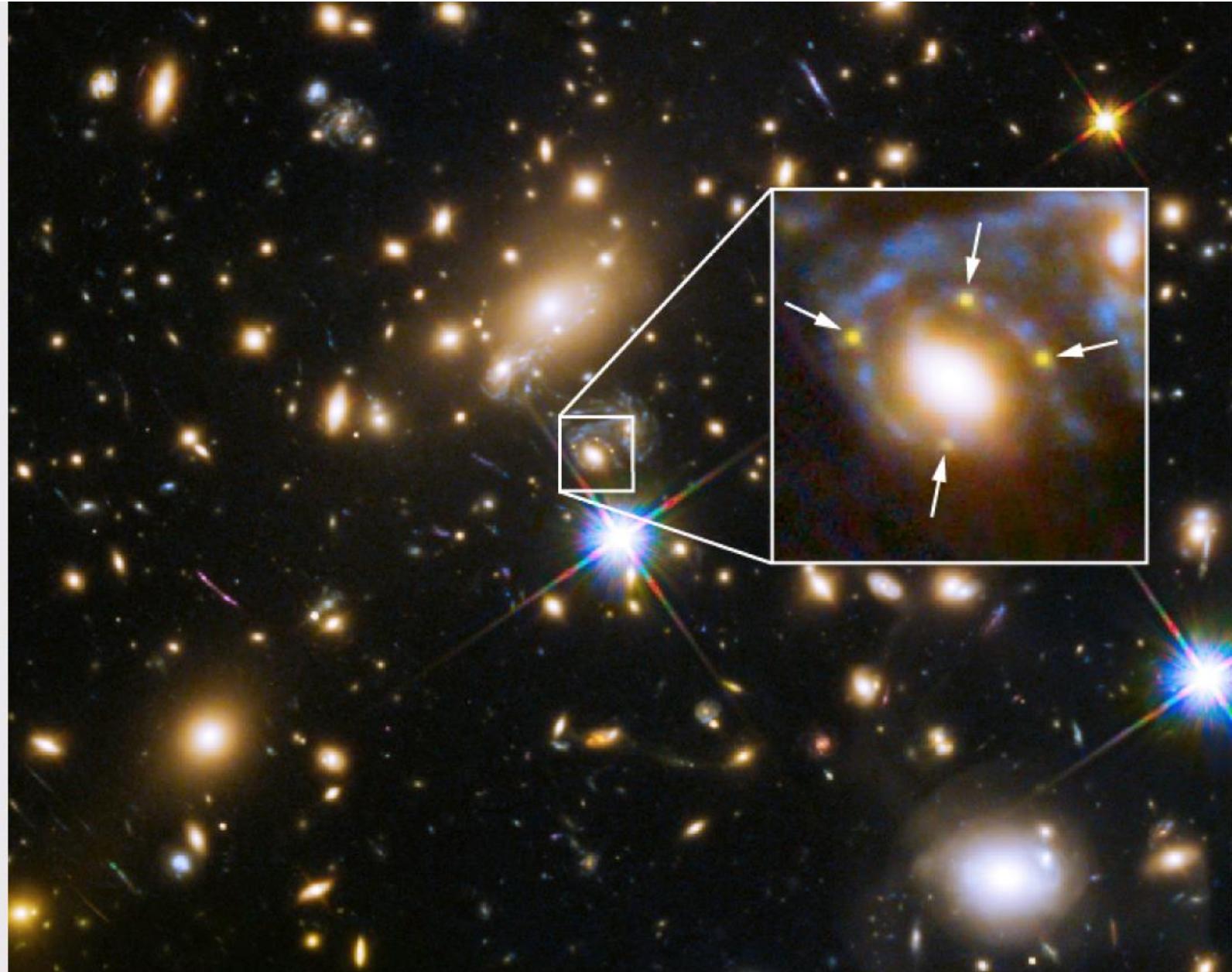


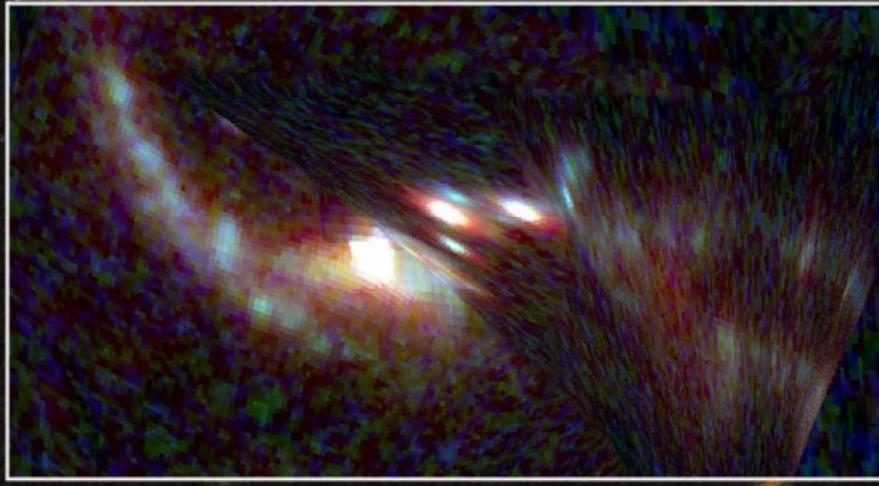
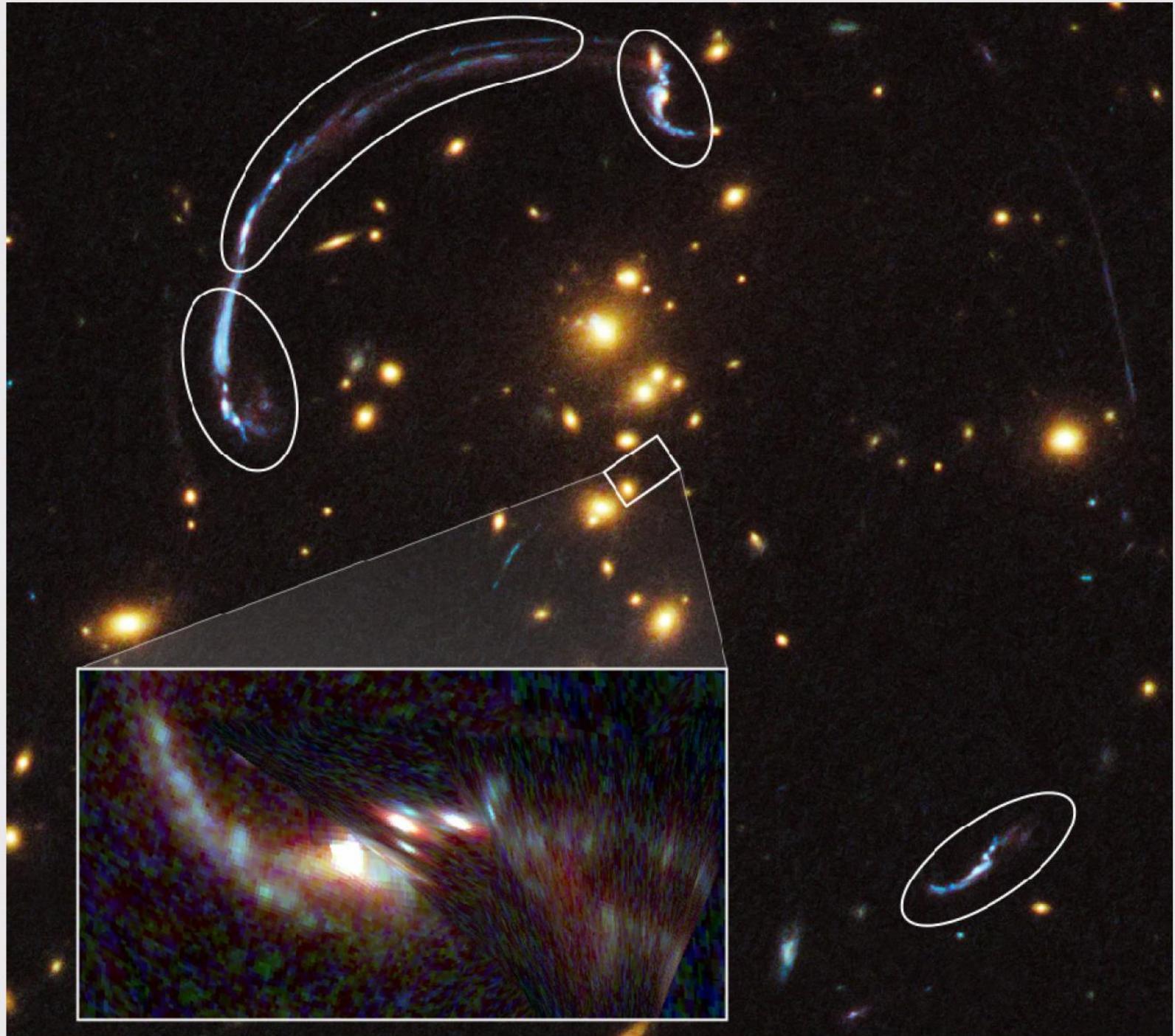
Galaxy rotation curve:
evidence for dark matter

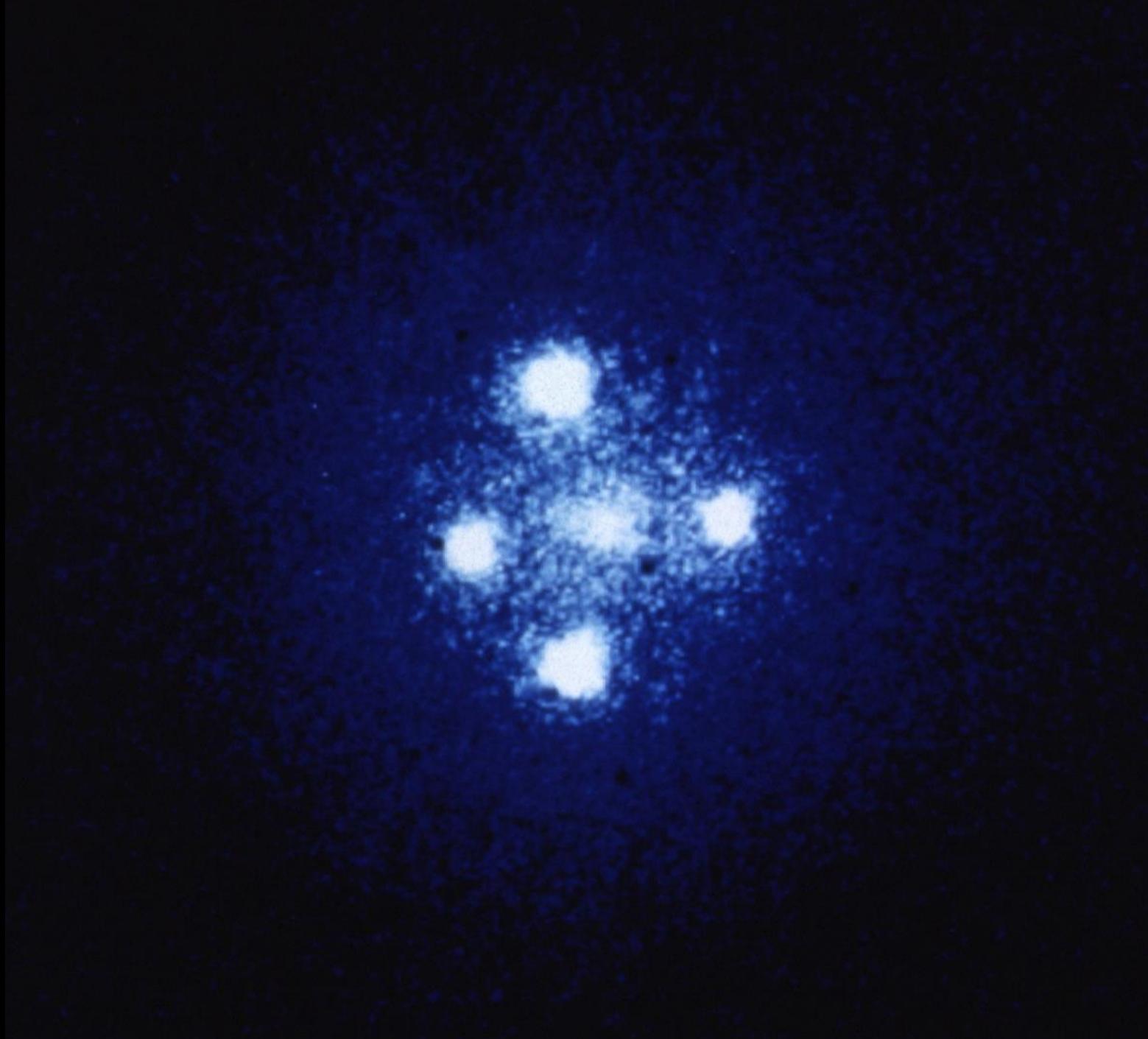
Masses and dark matter: gravitational lensing

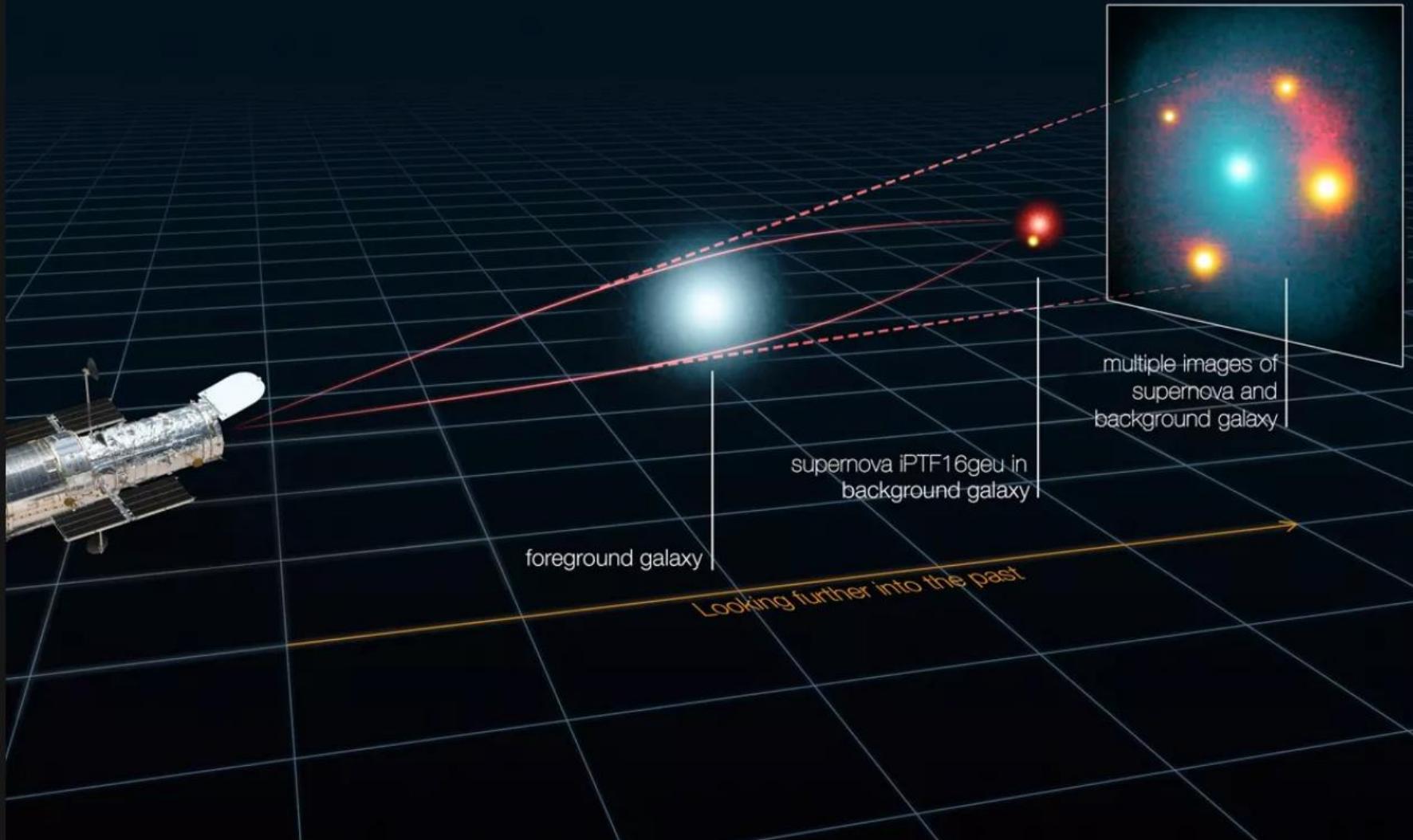


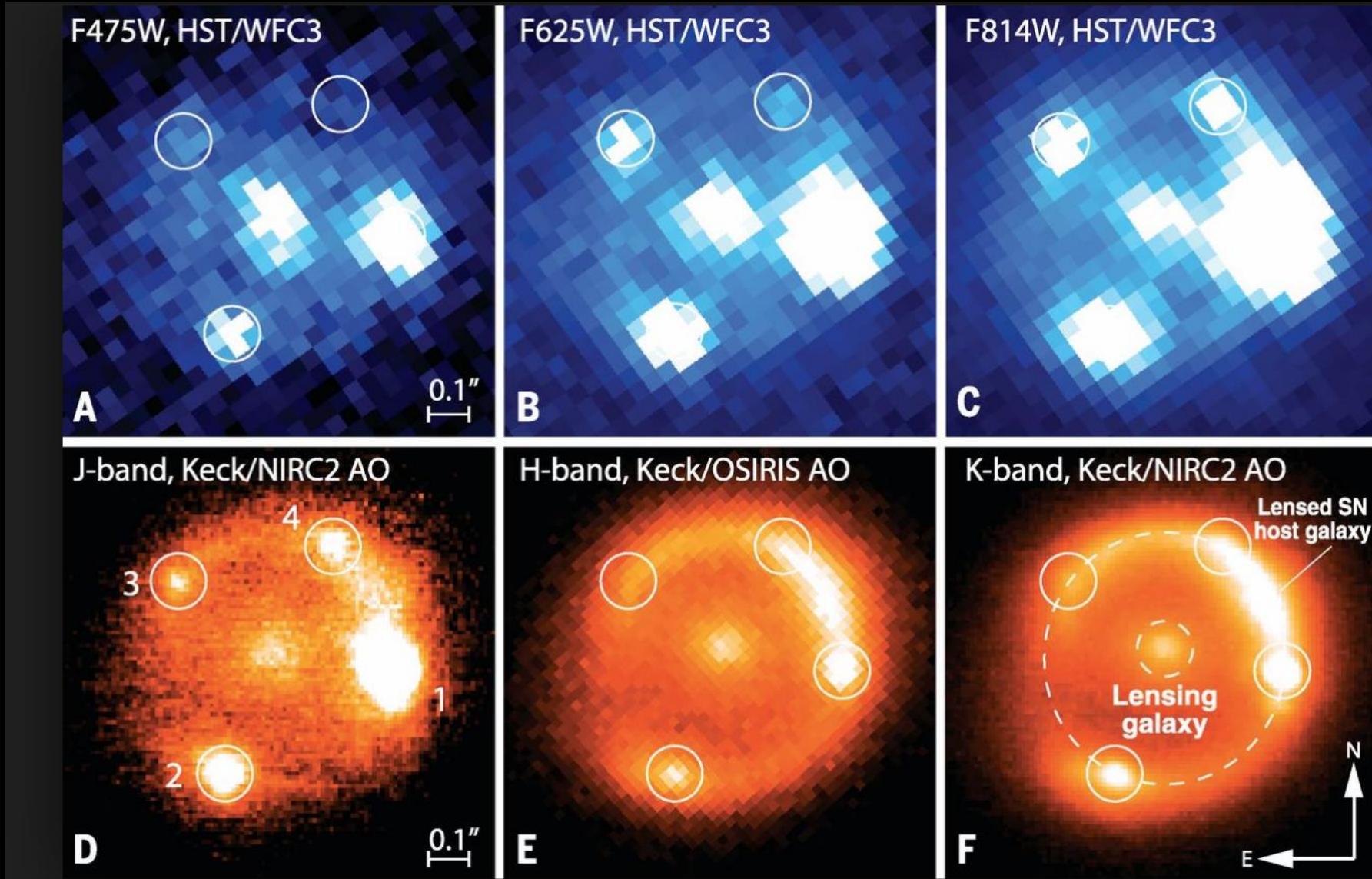
Gravitational lensing

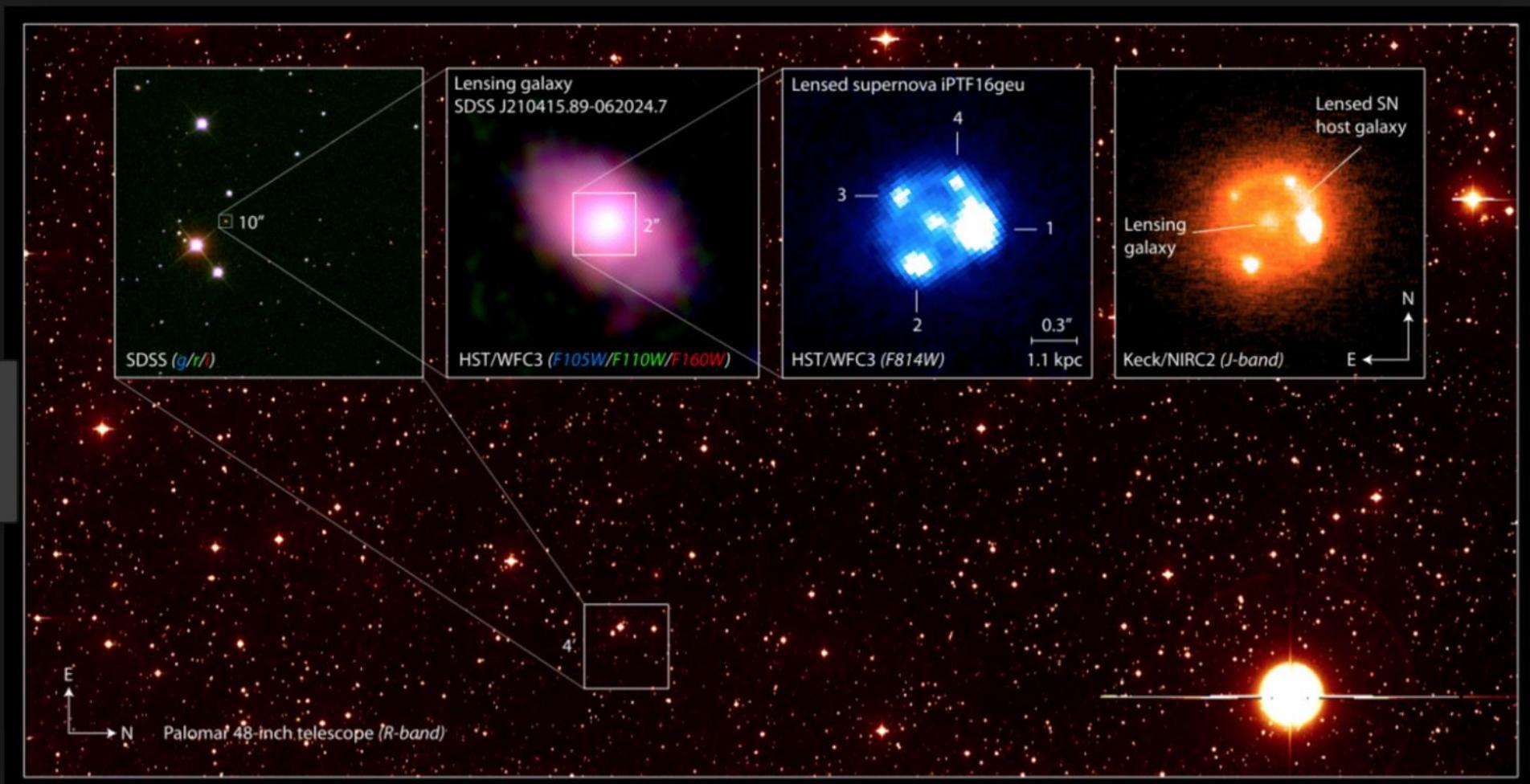


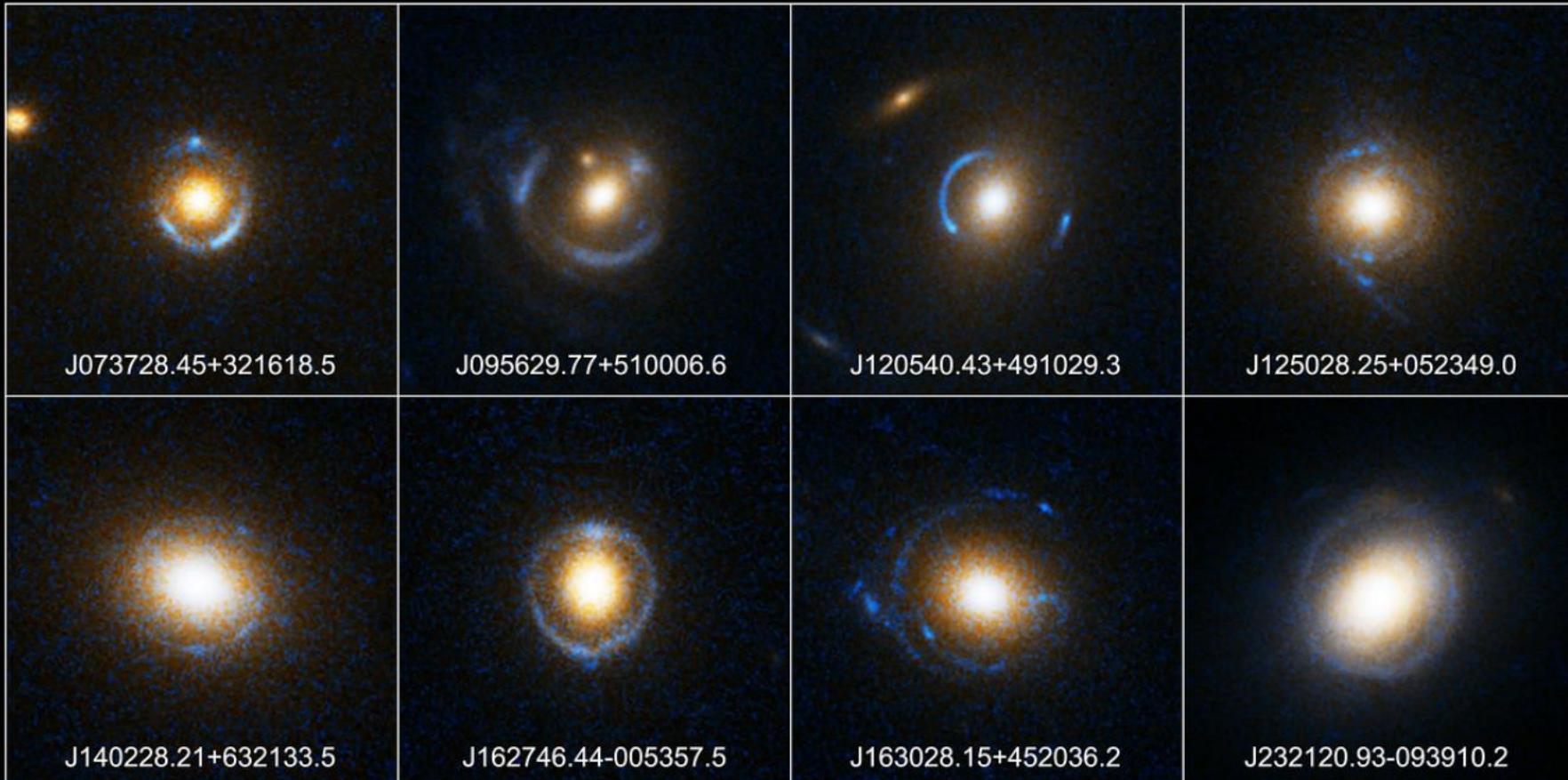








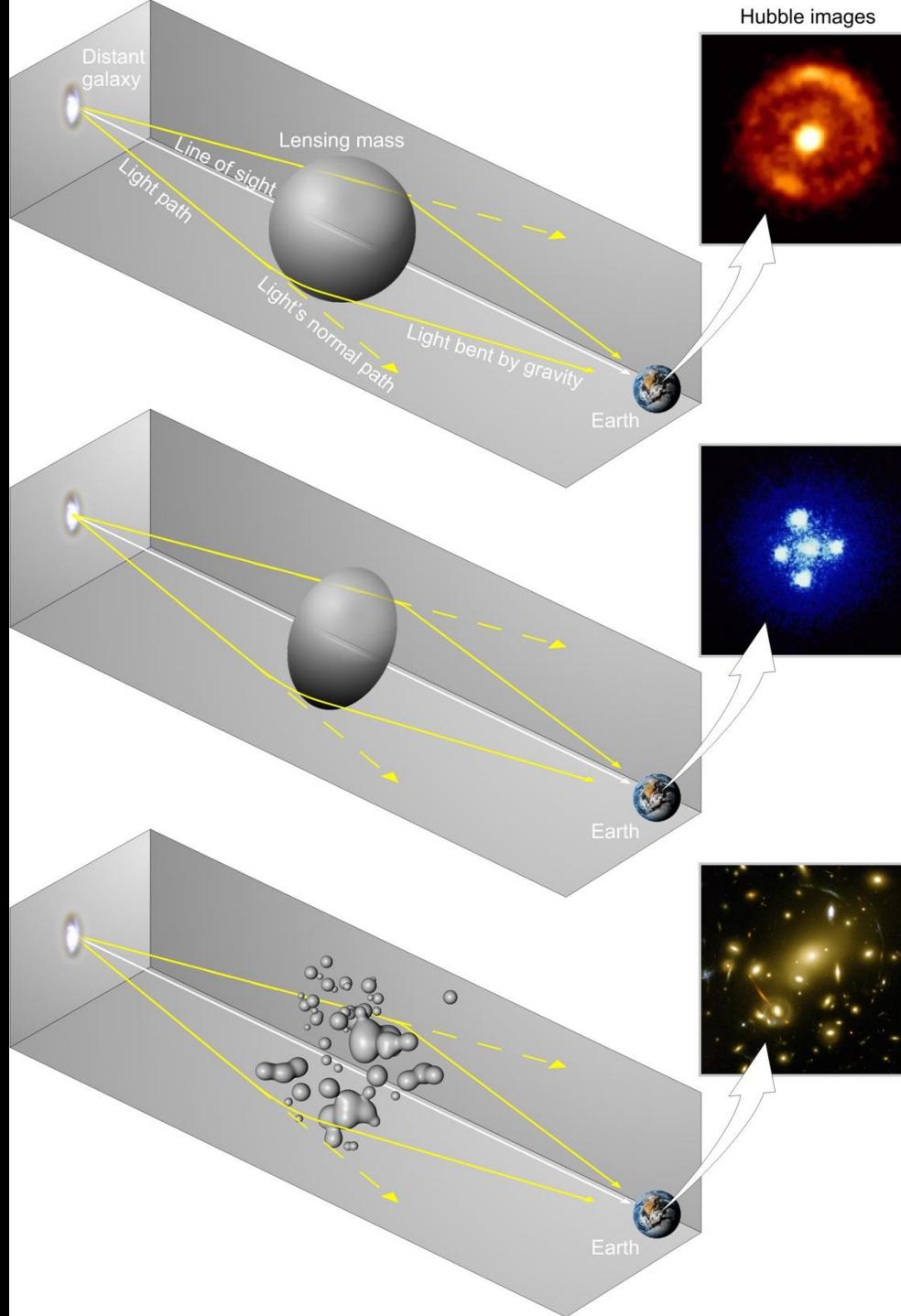




Einstein Ring Gravitational Lenses
Hubble Space Telescope • Advanced Camera for Surveys

NASA, ESA, A. Bolton (Harvard-Smithsonian CfA), and the SLACS Team

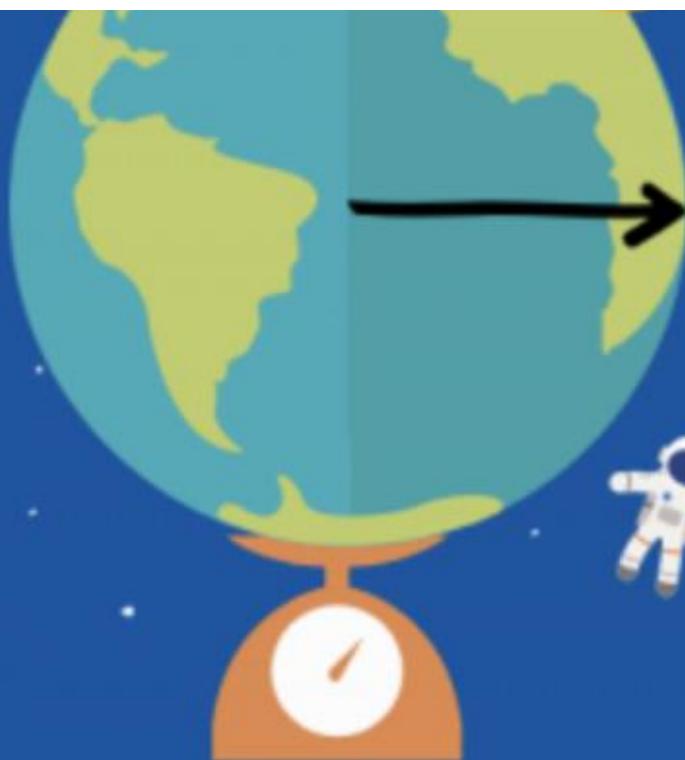
STScI-PRC05-32



Escape Velocity

What happens when escape velocity is faster than c (speed of light)?

$$v_e = \sqrt{\frac{2GM}{r}}$$



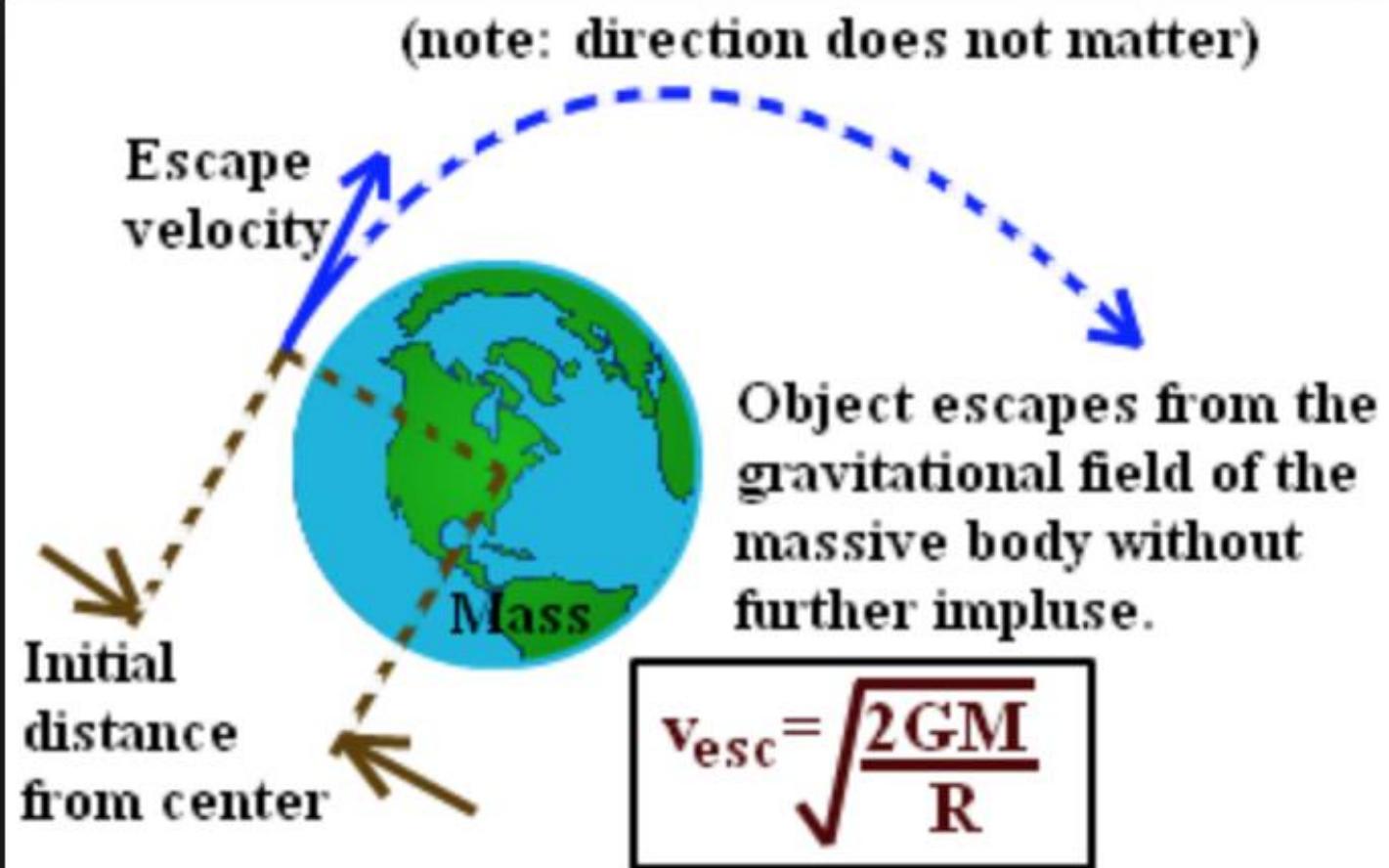
r = Radius of the planet*



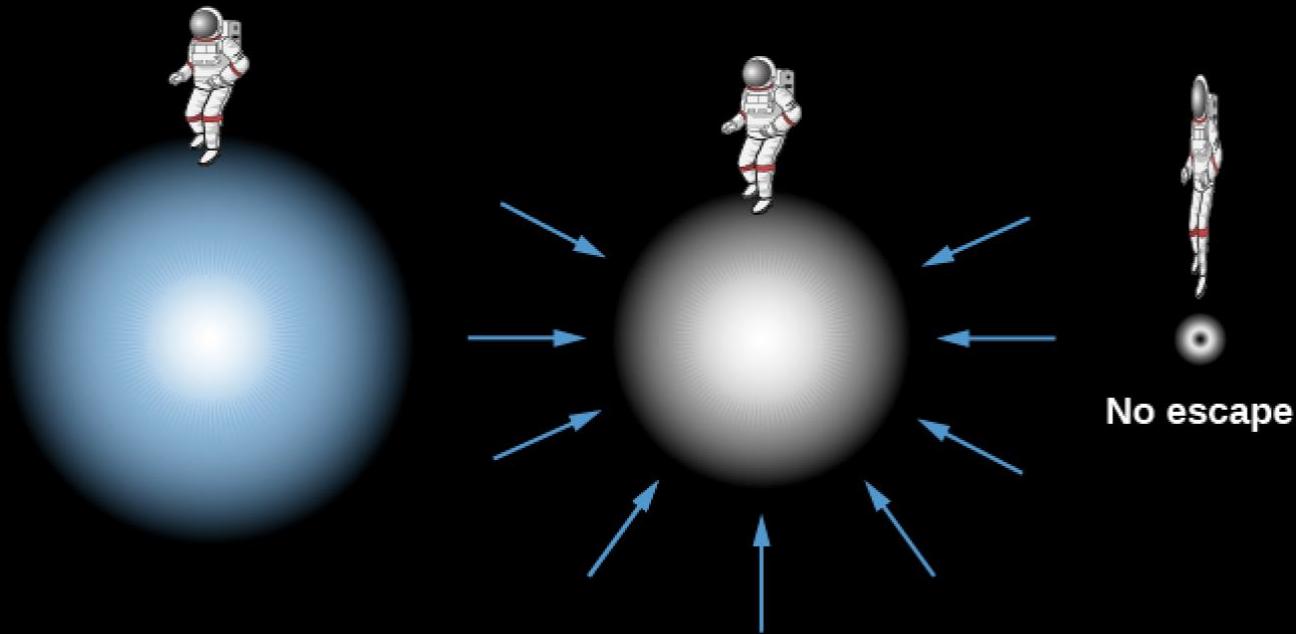
G = Newton's universal constant of gravity

M = Mass of the planet

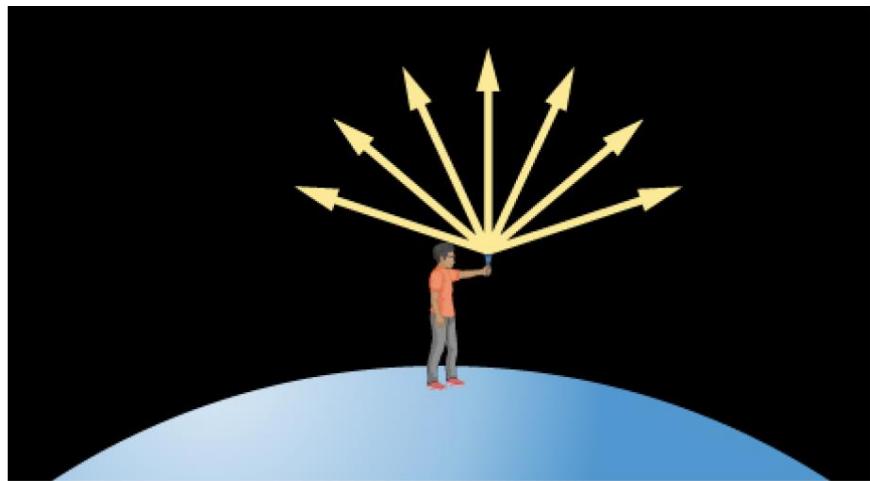
Black holes: gravity high enough (large mass, small volume) that light cannot escape



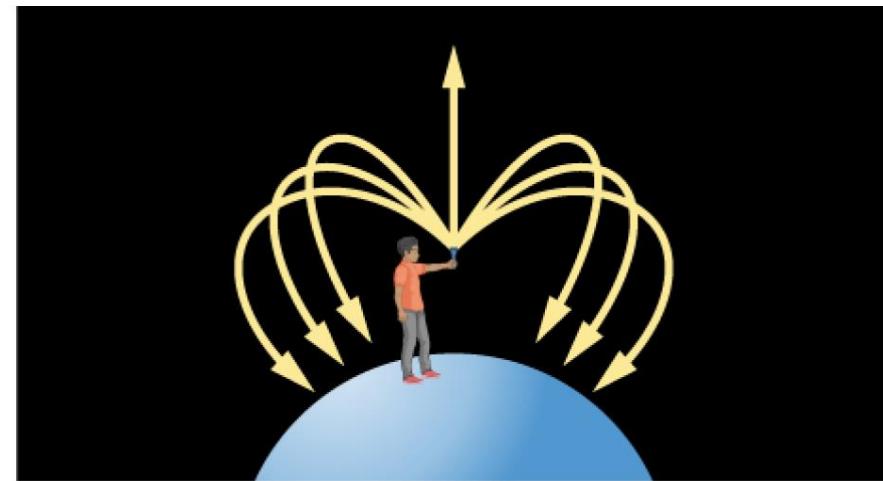
Black holes: gravity high enough (large mass, small volume) that light cannot escape



Black holes: event horizon defines radius where light can no longer escape



(a)

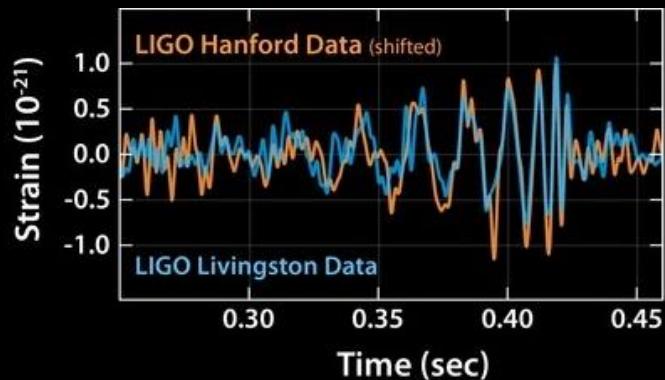
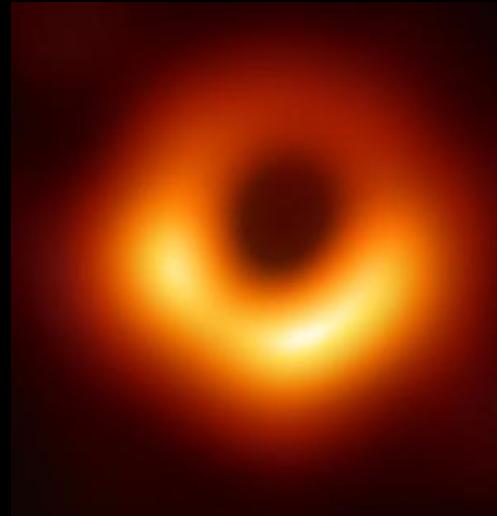


(b)

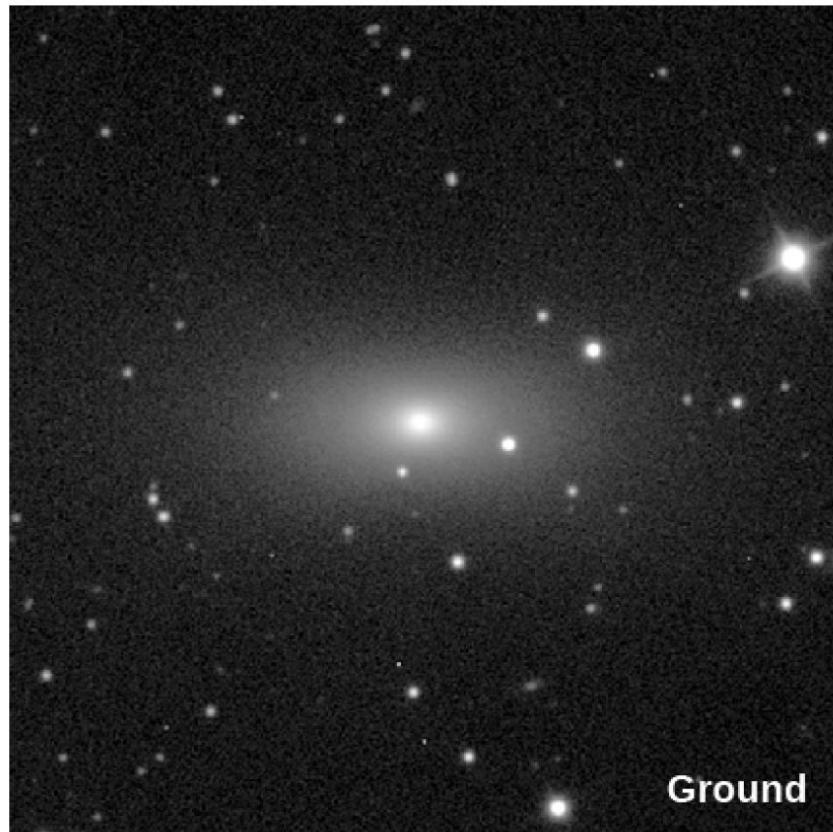
Figure 24.14 Light Paths near a Massive Object. Suppose a person could stand on the surface of a normal star with a flashlight. The light leaving the flashlight travels in a straight line no matter where the flashlight is pointed. Now consider what happens if the star collapses so that it is just a little larger than a black hole. All the light paths, except the one straight up, curve back to the surface. When the star shrinks inside the event horizon and becomes a black hole, even a beam directed straight up returns.

Types of black holes

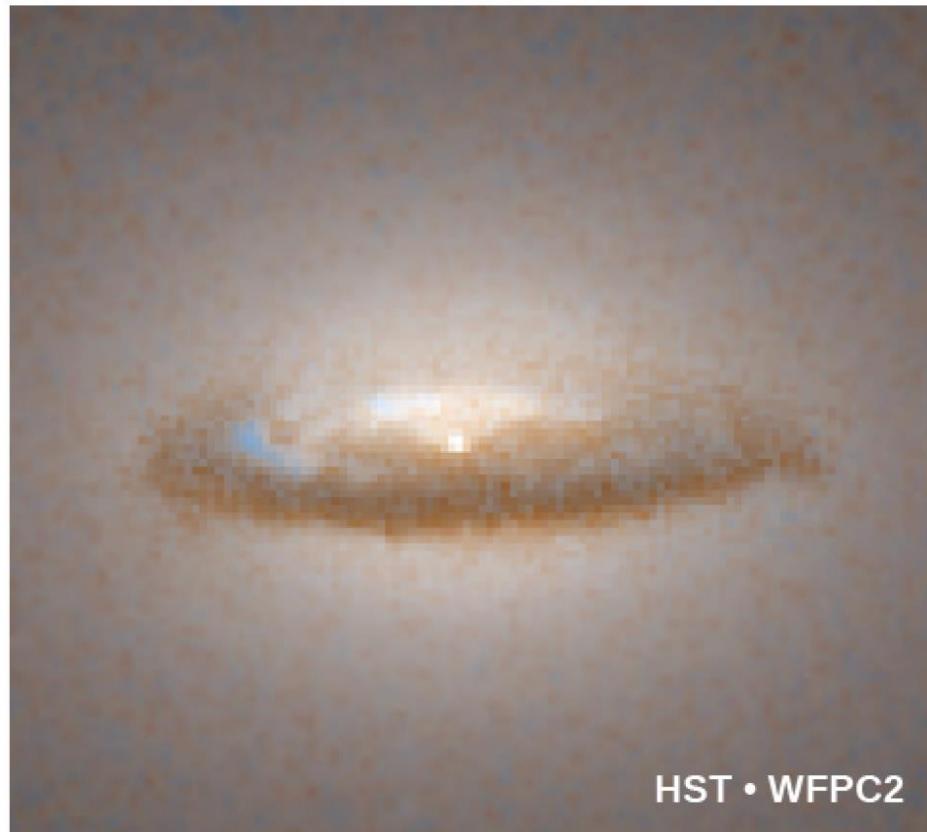
- Supermassive black holes
 - Centers of galaxies
- Stellar mass black holes
 - Remnant of a dead stars
- Primordial black holes?
 - Speculative, no idea whether they exist
 - They would be tiny



Imaging: usually can't resolve the black hole

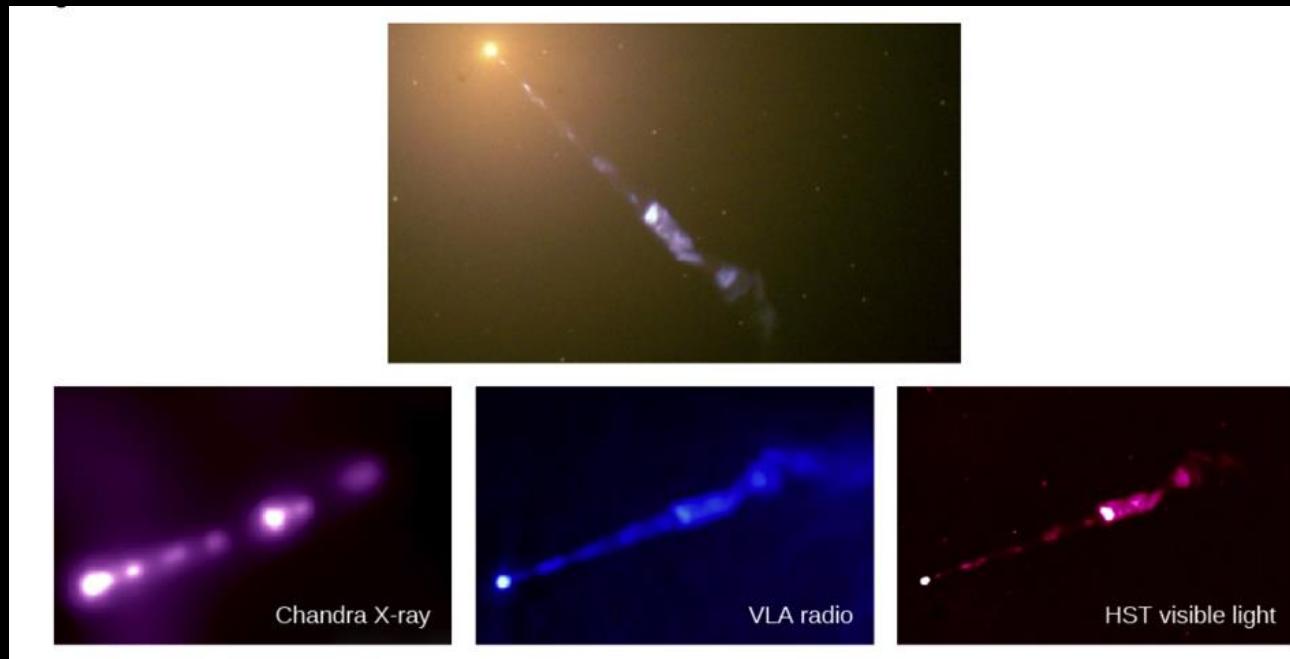
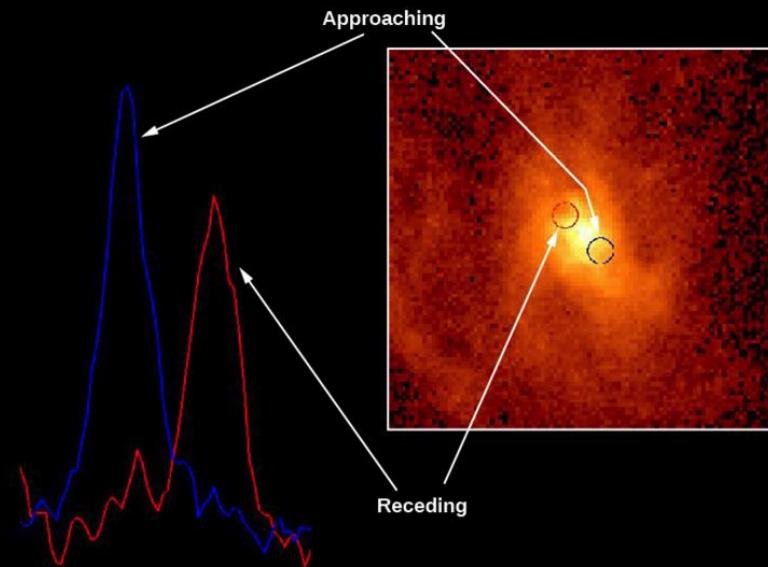


Ground



HST • WFPC2

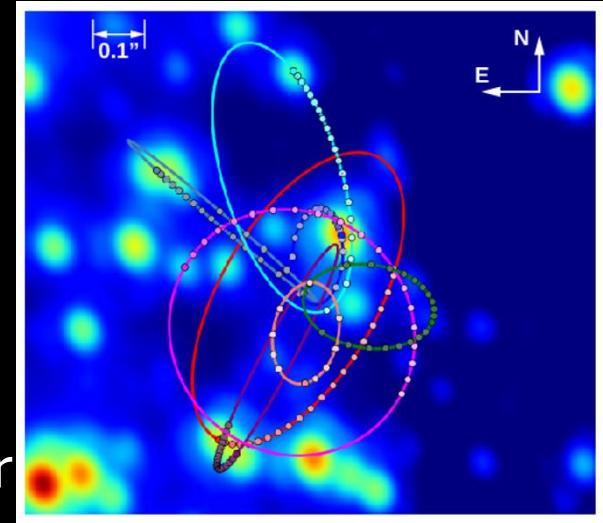
Indirect evidence: accretion disks, jets



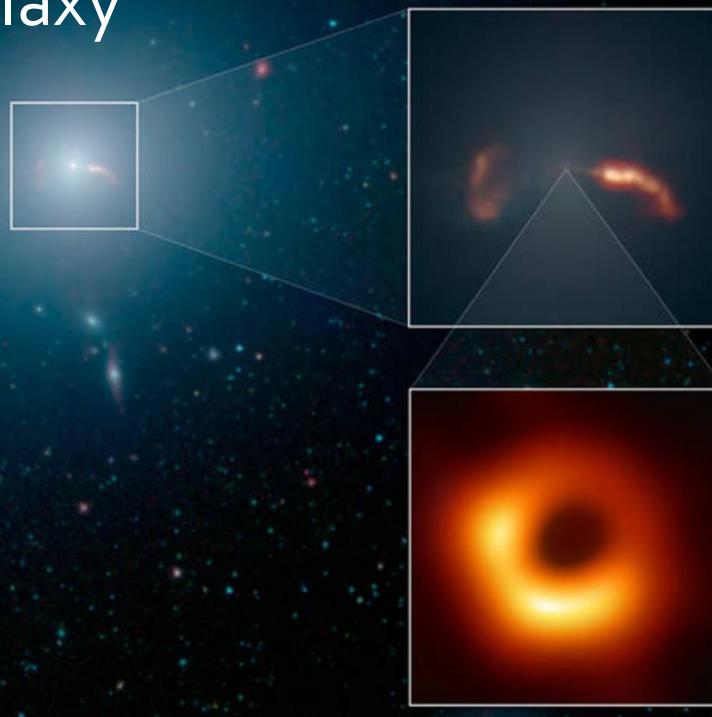
Supermassive black holes

Direct evidence

Milky Way:
galactic center

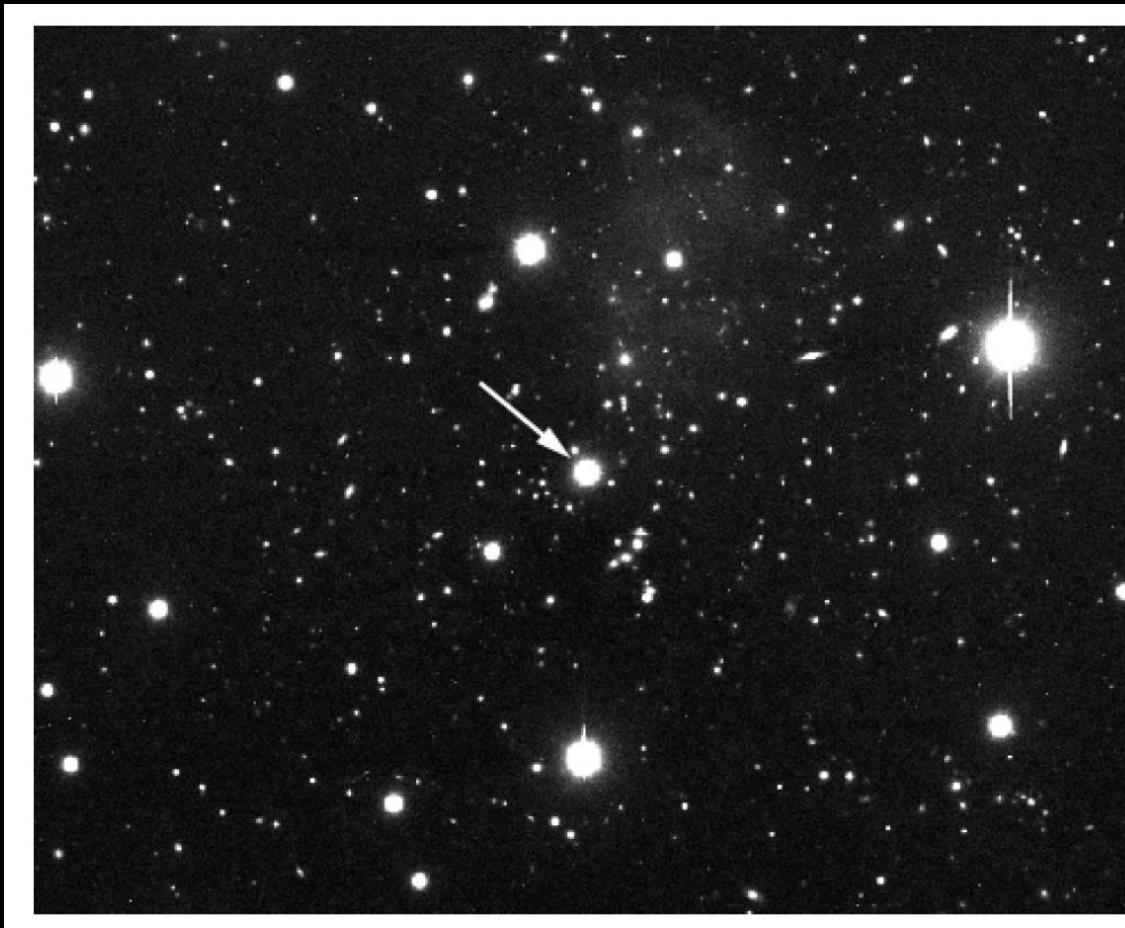


M87: nearby galaxy

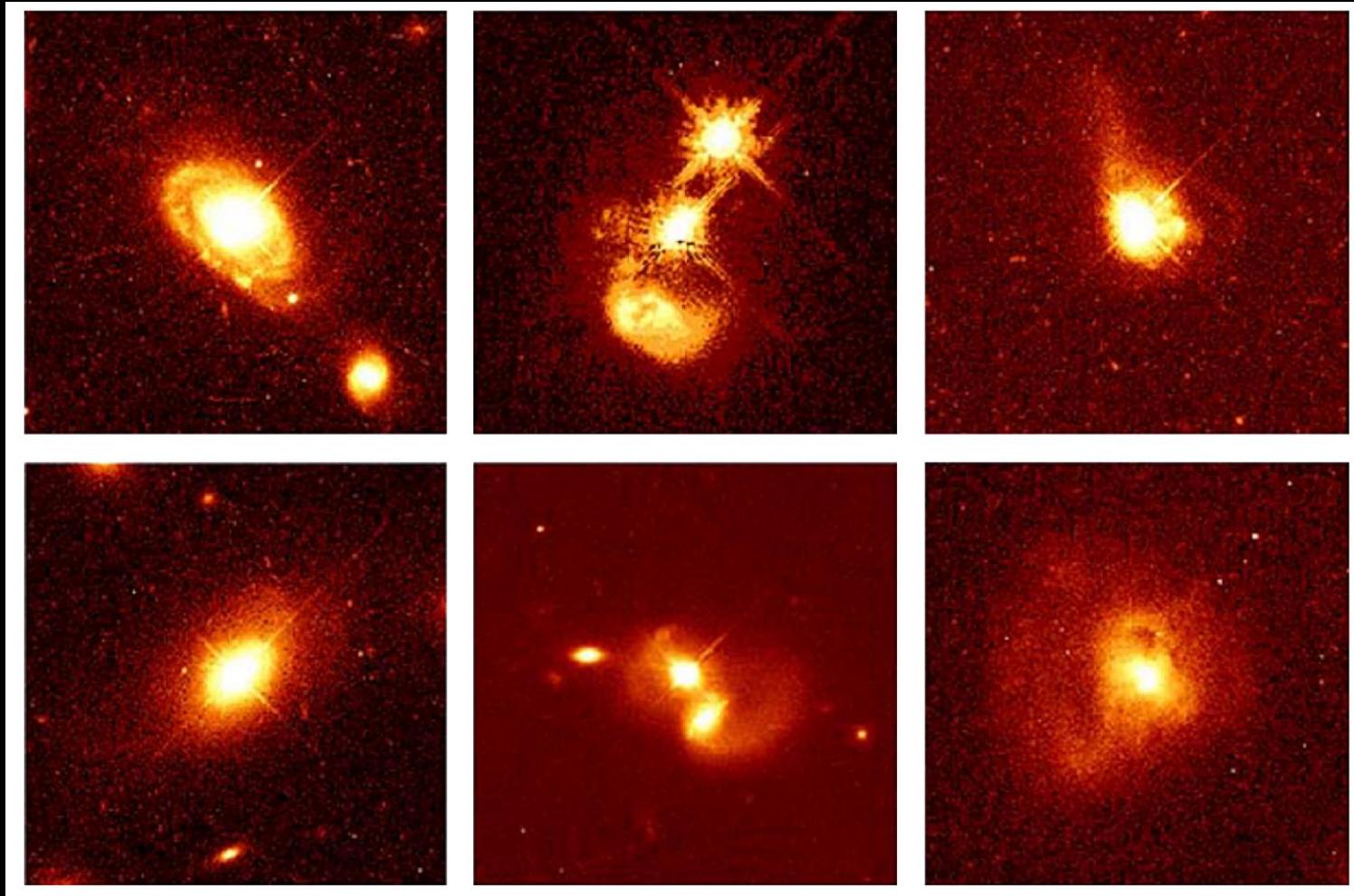


Supermassive black holes!

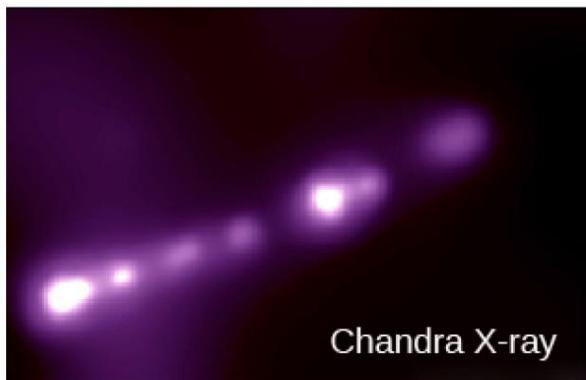
Quasars: quasi-stellar objects



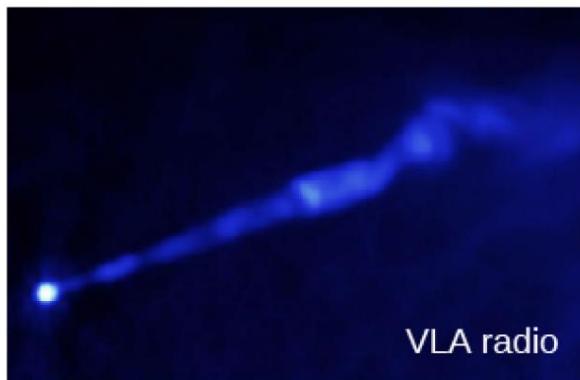
Quasars: accreting gas, outshines their host galaxies (but they do have host galaxies)



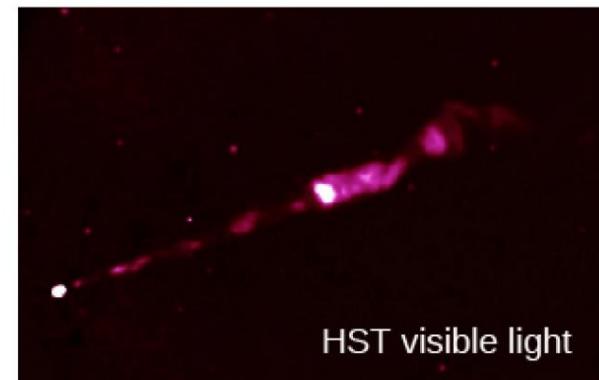
Jets from the central black hole



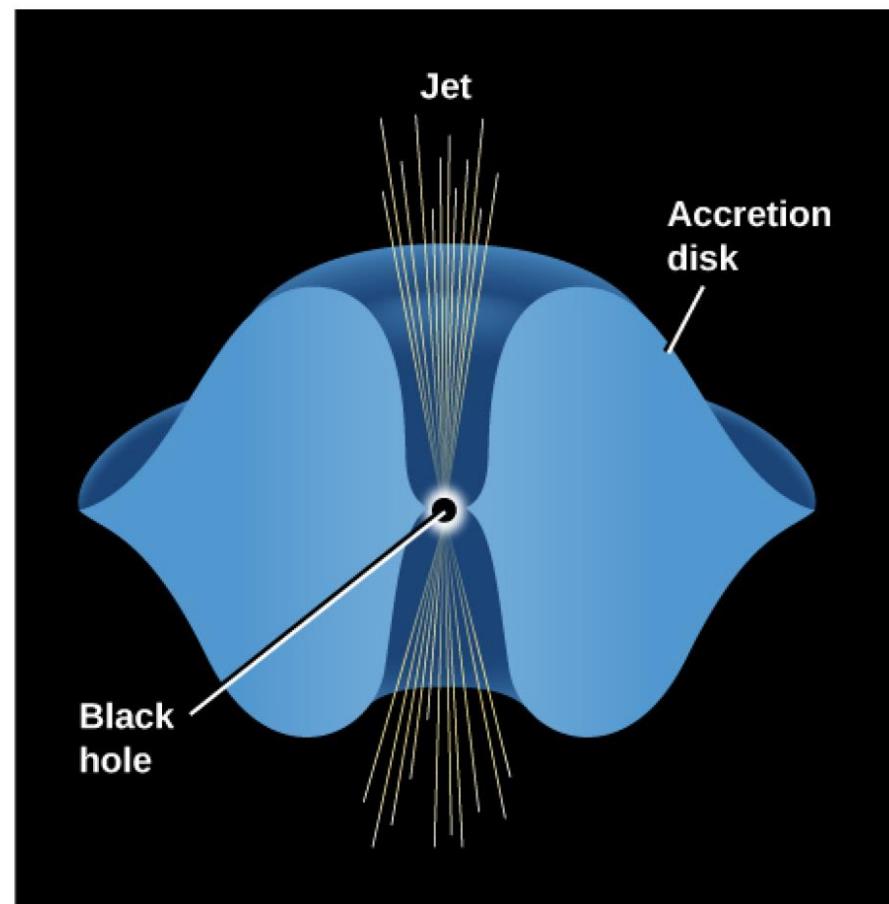
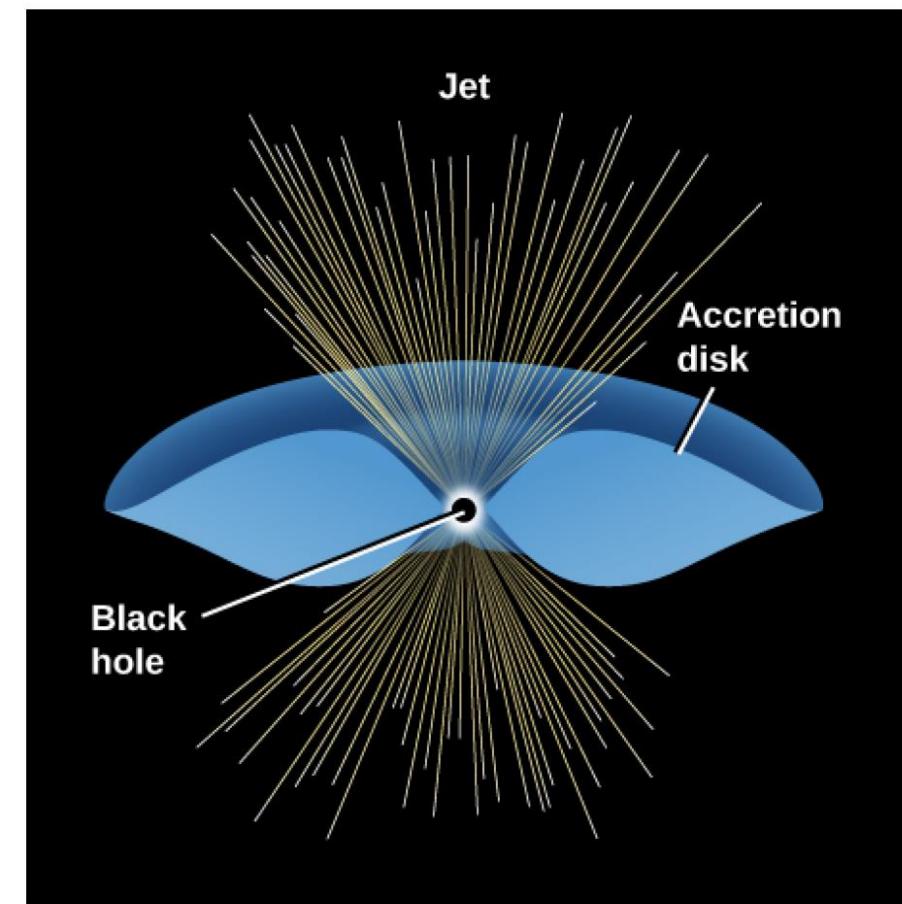
Chandra X-ray

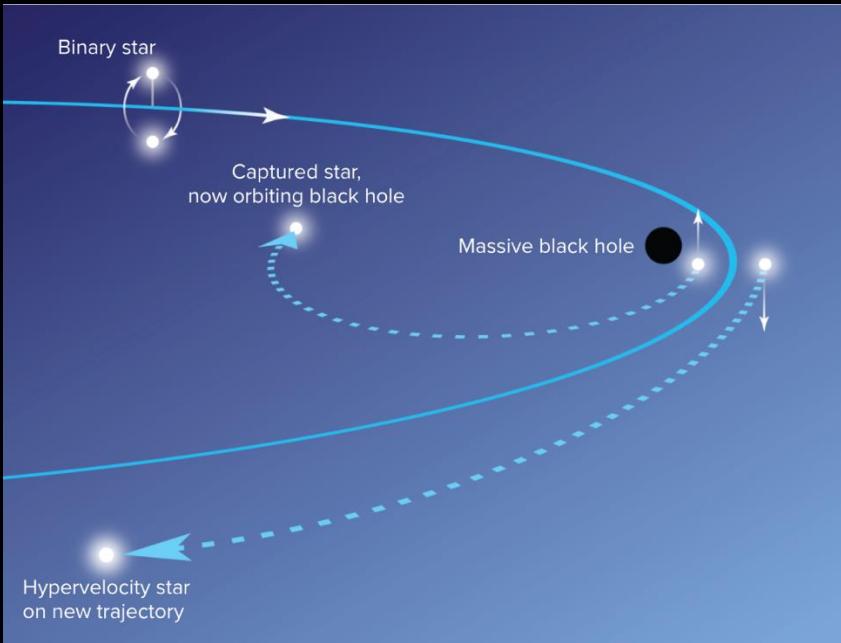


VLA radio



HST visible light

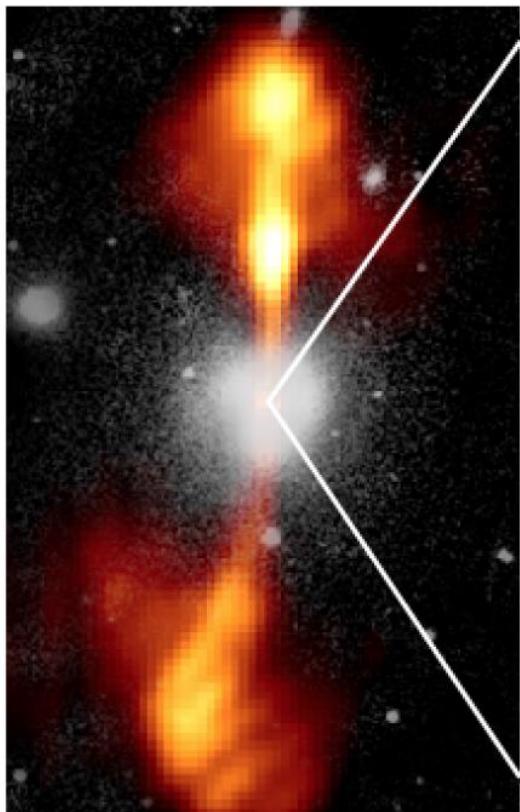




Hypervelocity stars:
Thrown out of galaxy by close encounter
with supermassive black hole

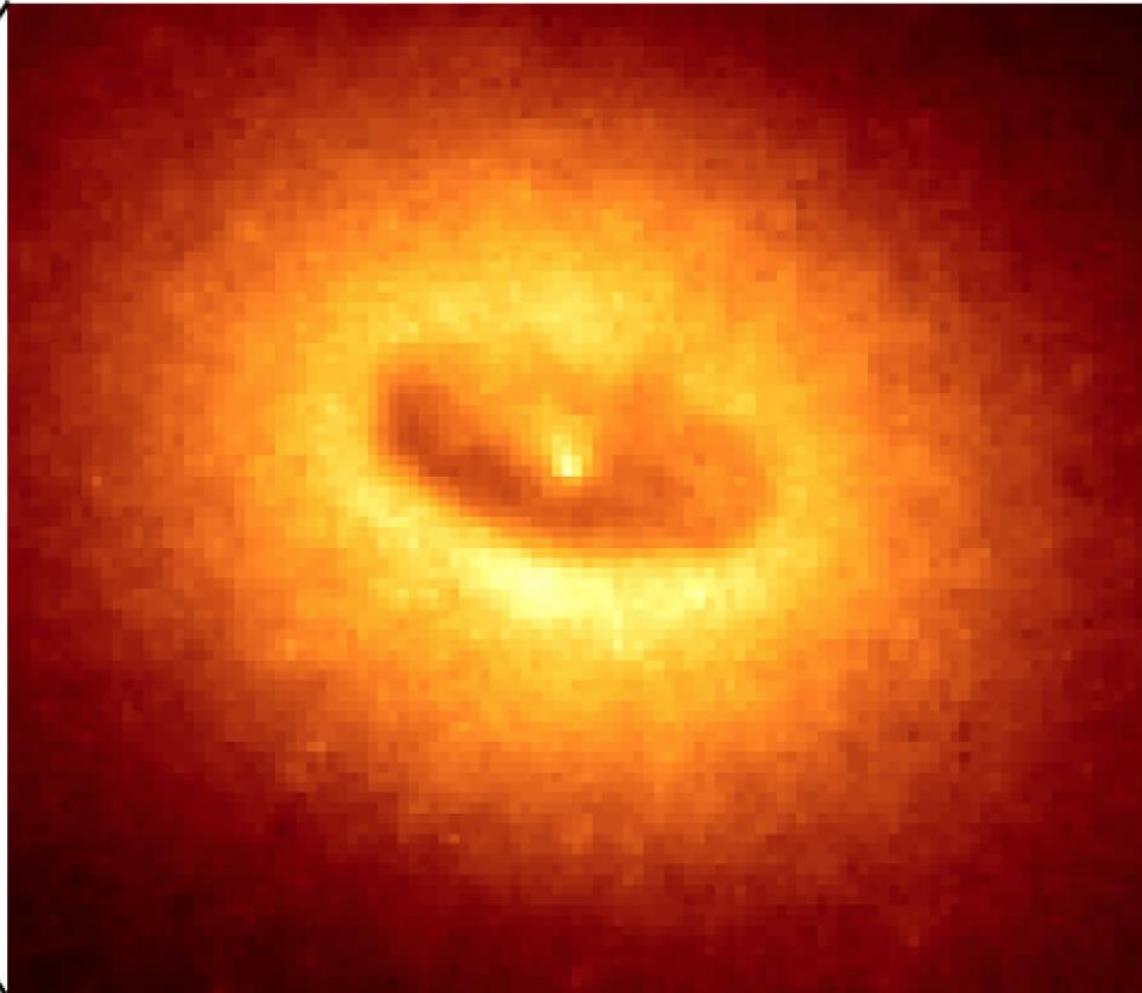


Tidal disruption events:
sometimes black hole eats a star!



380 arc seconds

88,000 LY



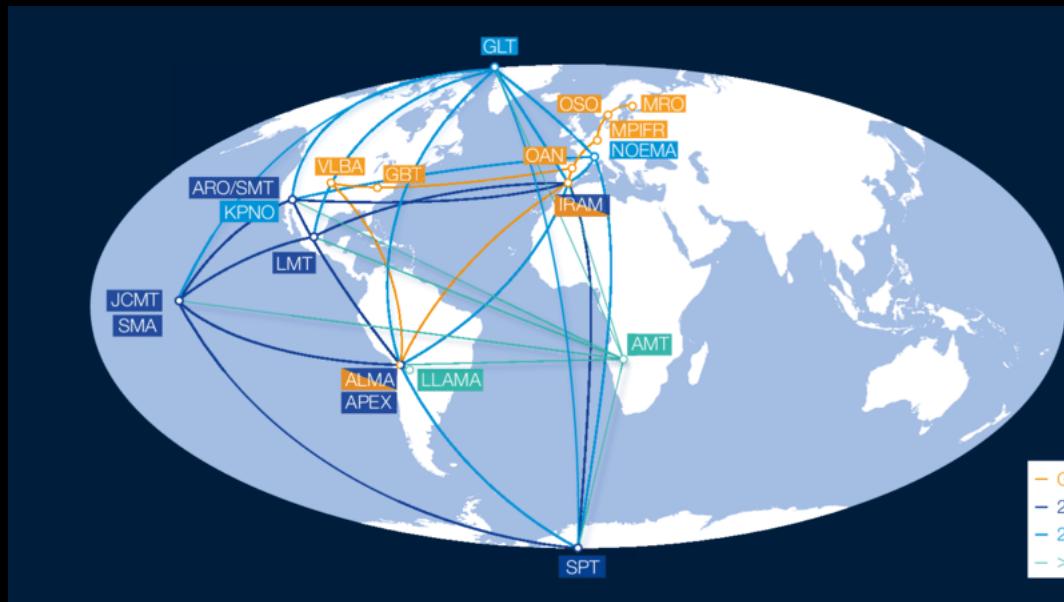
17 arc seconds

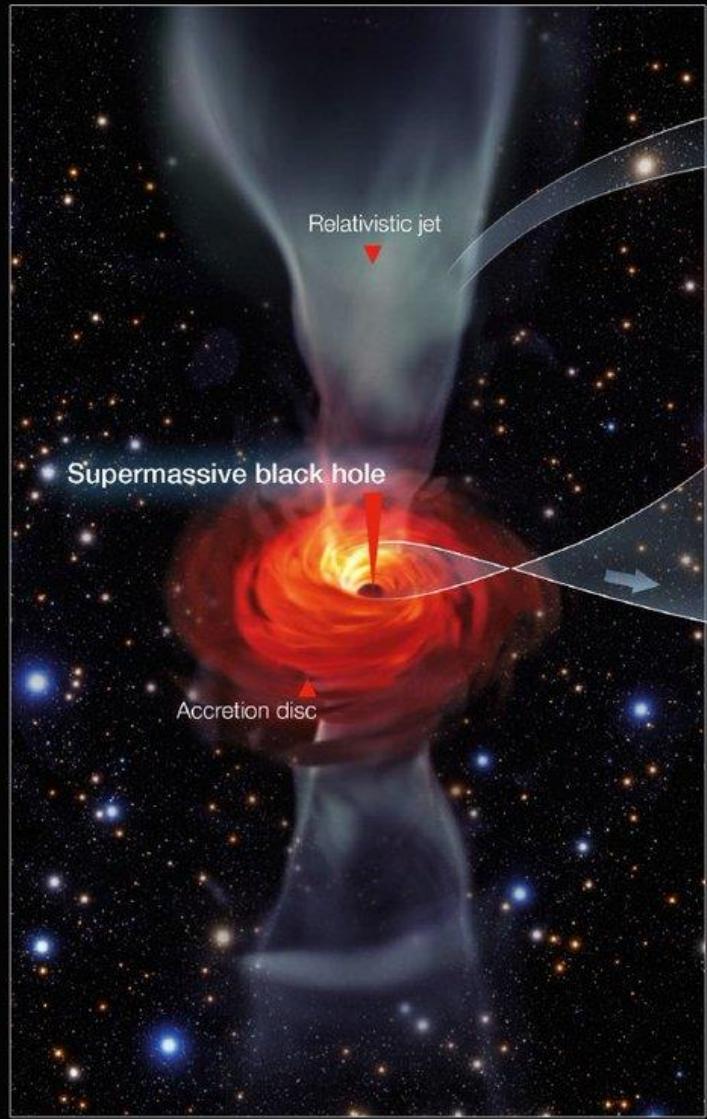
400 LY

Event Horizon Telescope:

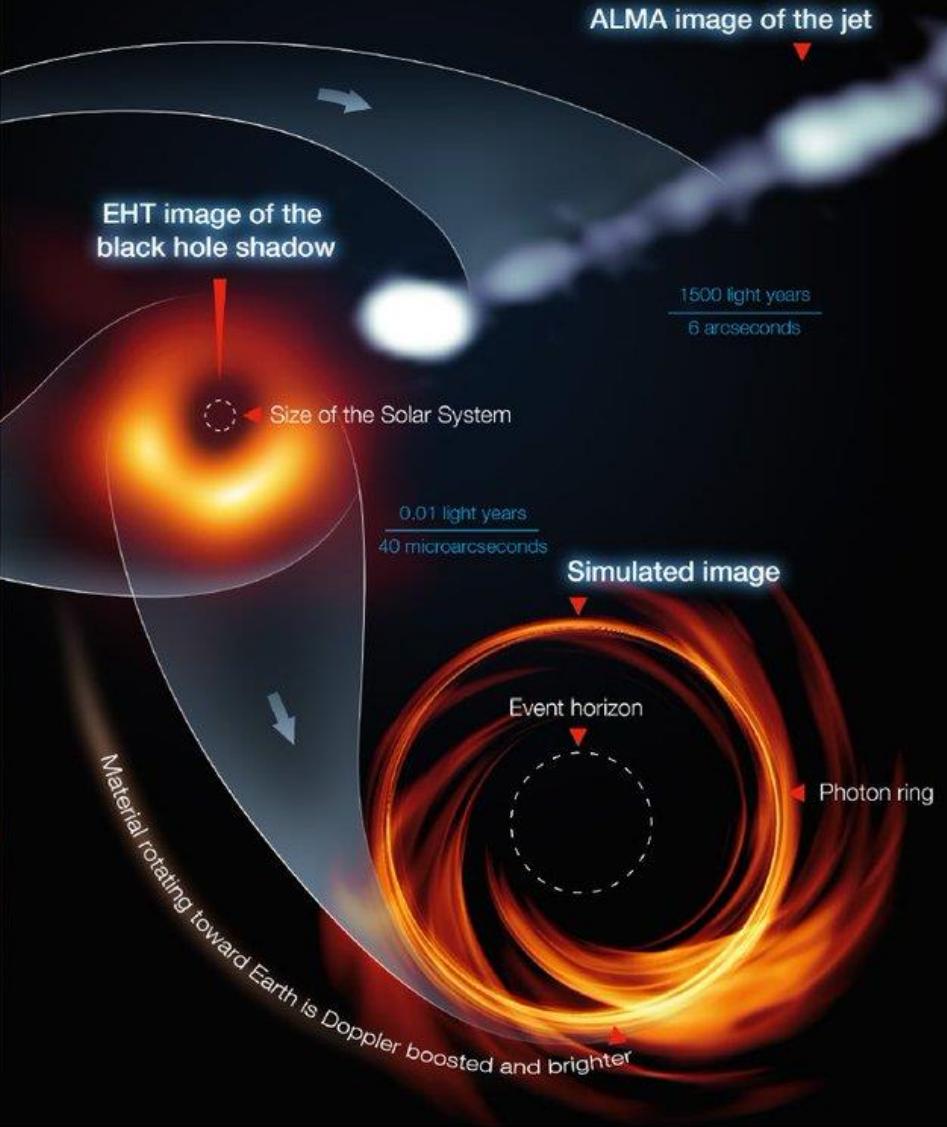
Uses radius of earth

spatial resolution = wavelength/diameter



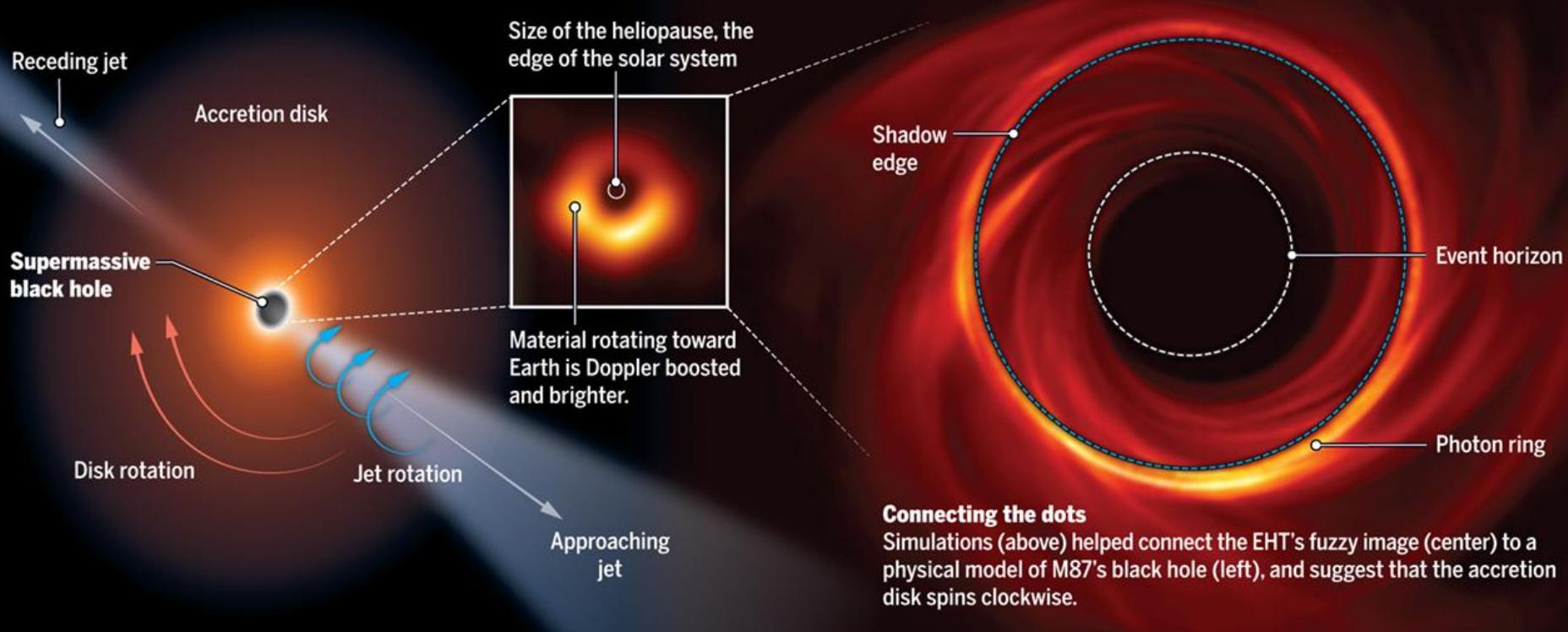


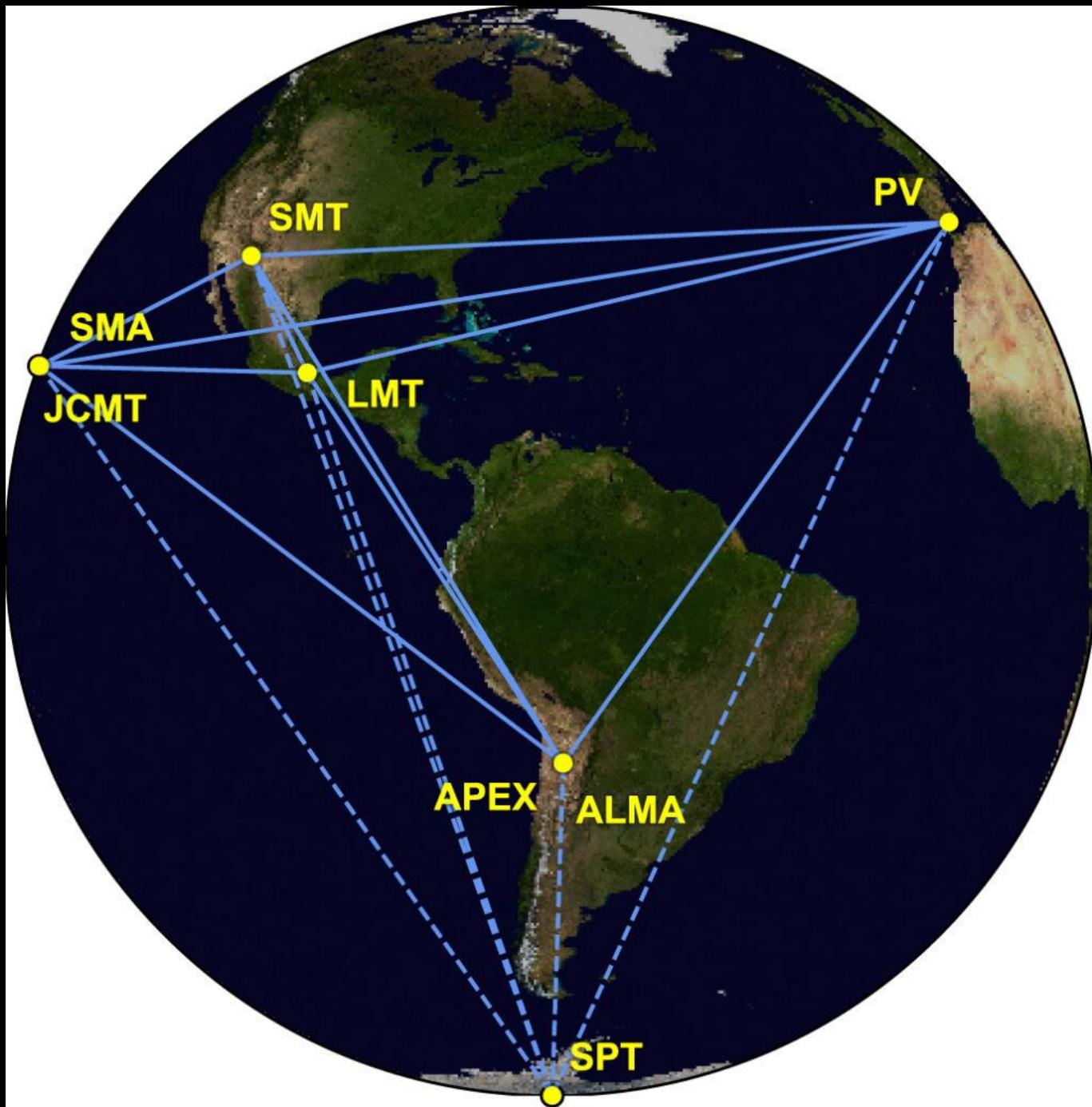
M87 Black Hole – Event Horizon Telescope

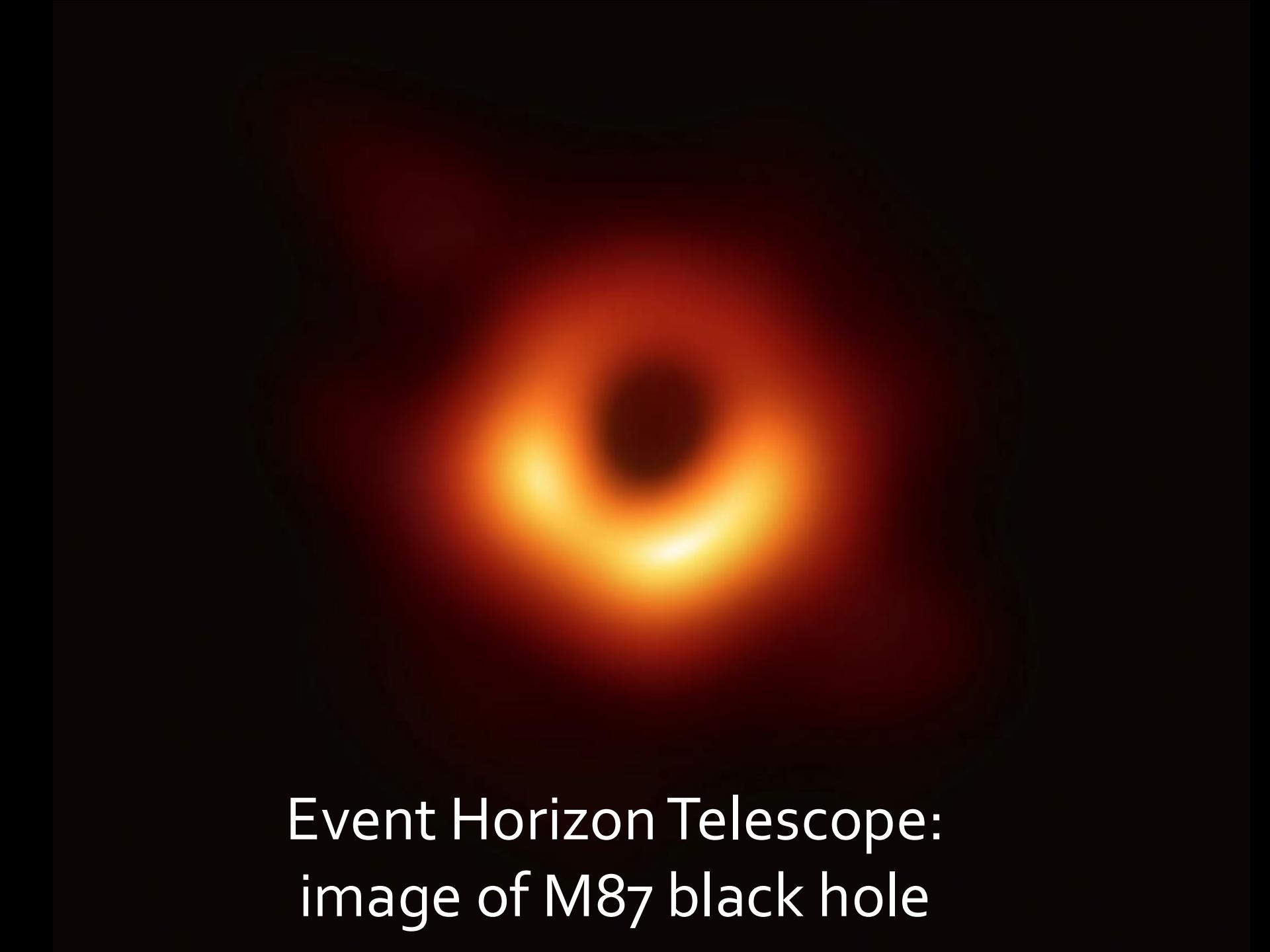


Strange beast

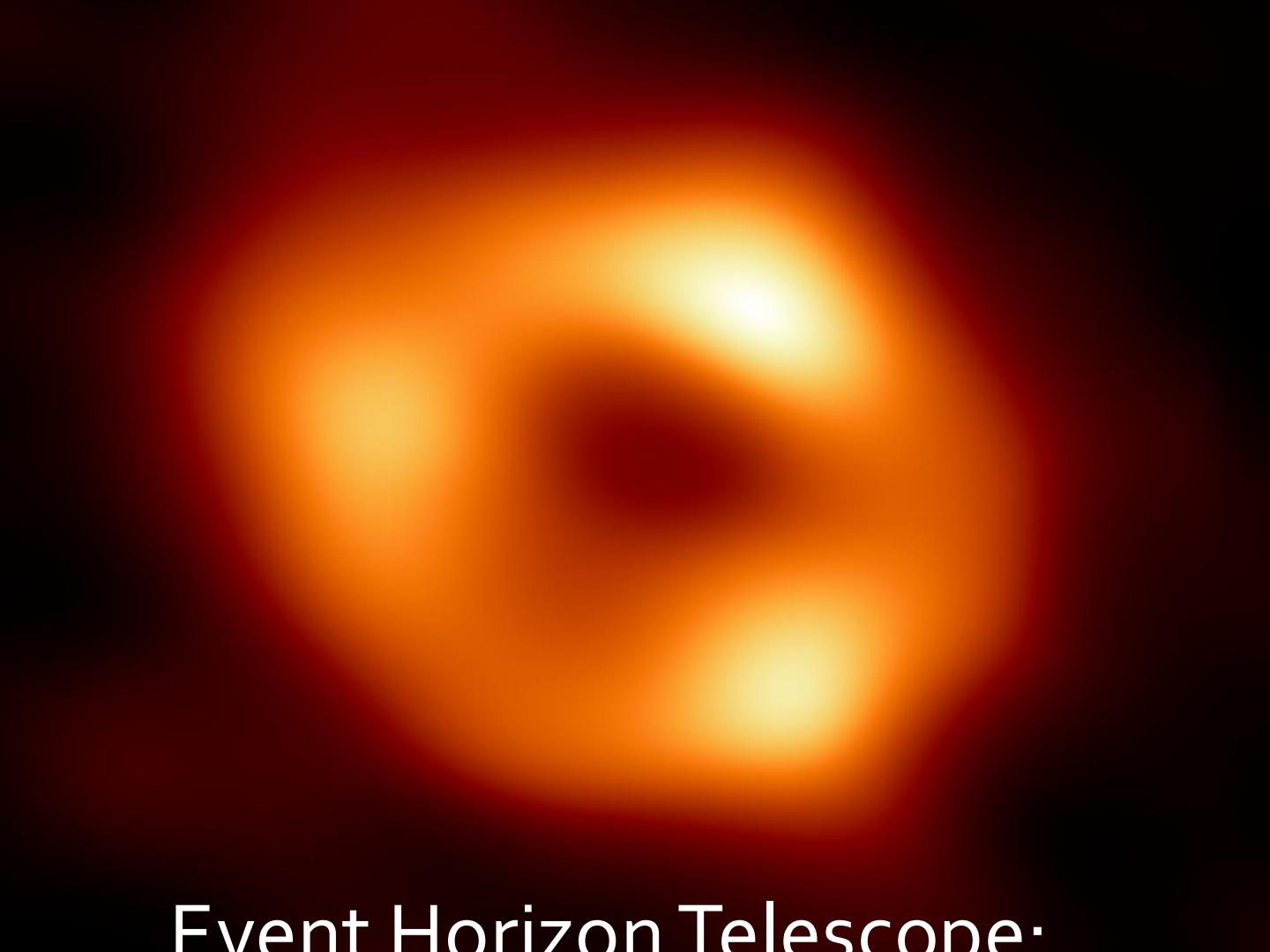
The Event Horizon Telescope (EHT) team took 2 years to produce an image of the black hole at the center of nearby galaxy Messier 87 (M87), which feeds on a swirling disk of bright matter. Its gravity is so strong that photons orbit it, creating a bright ring. Gravitational lensing magnifies the black hole's event horizon into a larger dark shadow, which may be partially filled by material in front of the hole.



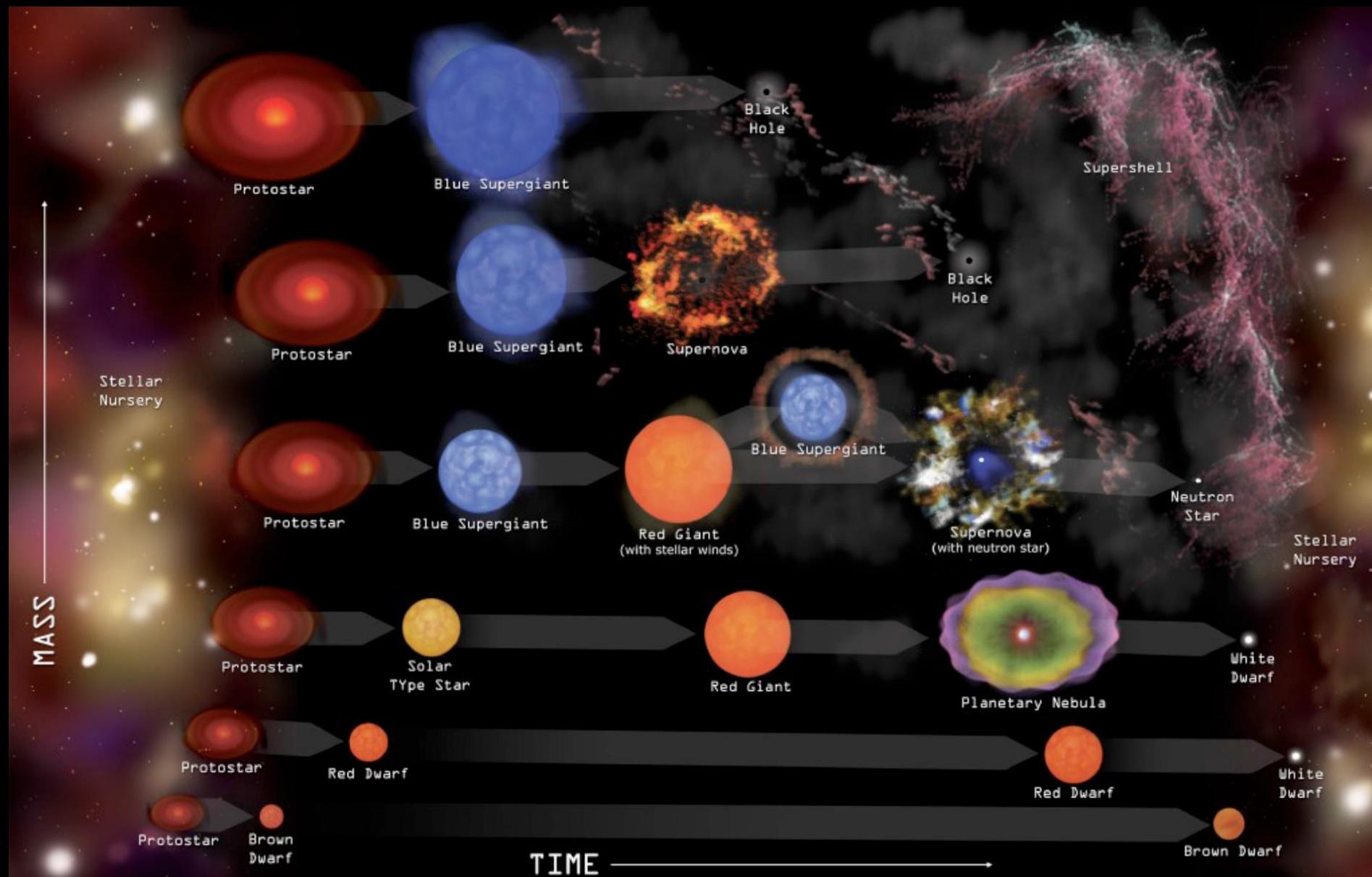


The image shows a black hole's event horizon as a bright, orange-yellow ring against a dark background.

Event Horizon Telescope:
image of M87 black hole

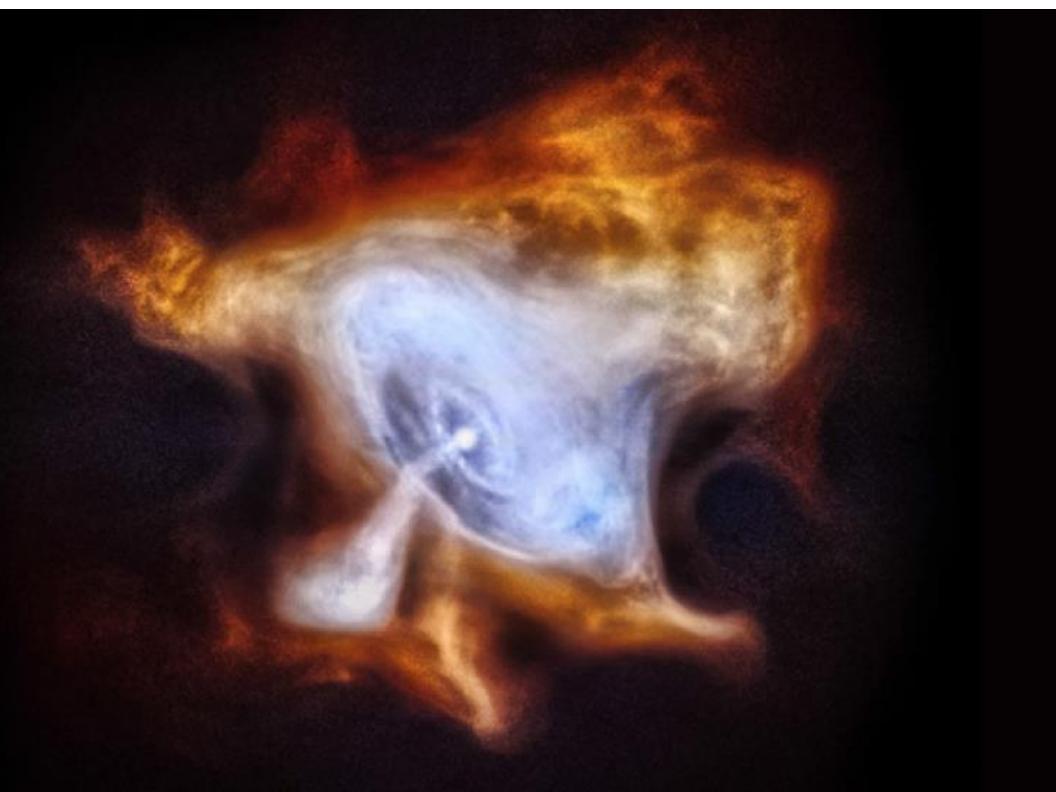
A black and white image showing a central point of intense light surrounded by concentric, slightly distorted rings, resembling a black hole's event horizon.

Event Horizon Telescope:
image of Milky Way black hole



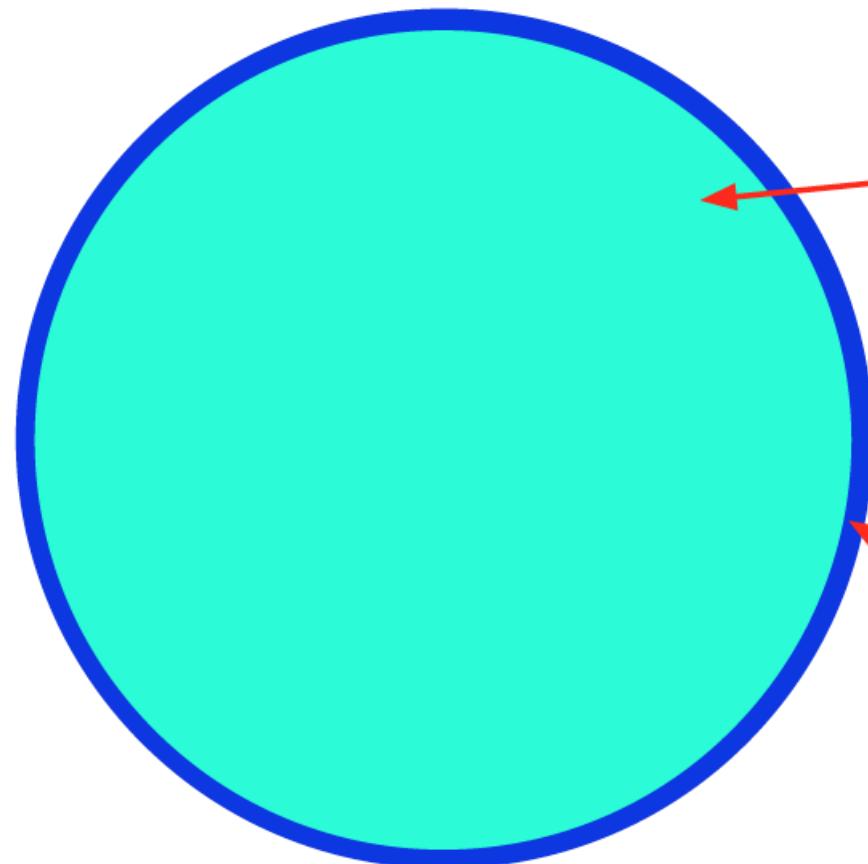
Properties of a Typical White Dwarf and a Neutron Star

| Property | White Dwarf | Neutron Star |
|----------------|-----------------------------------|-----------------------------|
| Mass (Sun = 1) | 0.6 (always <1.4) | Always >1.4 and <3 |
| Radius | 7000 km | 10 km |
| Density | 8×10^5 g/cm ³ | 10^{14} g/cm ³ |



X-ray image
of accreting
neutron star

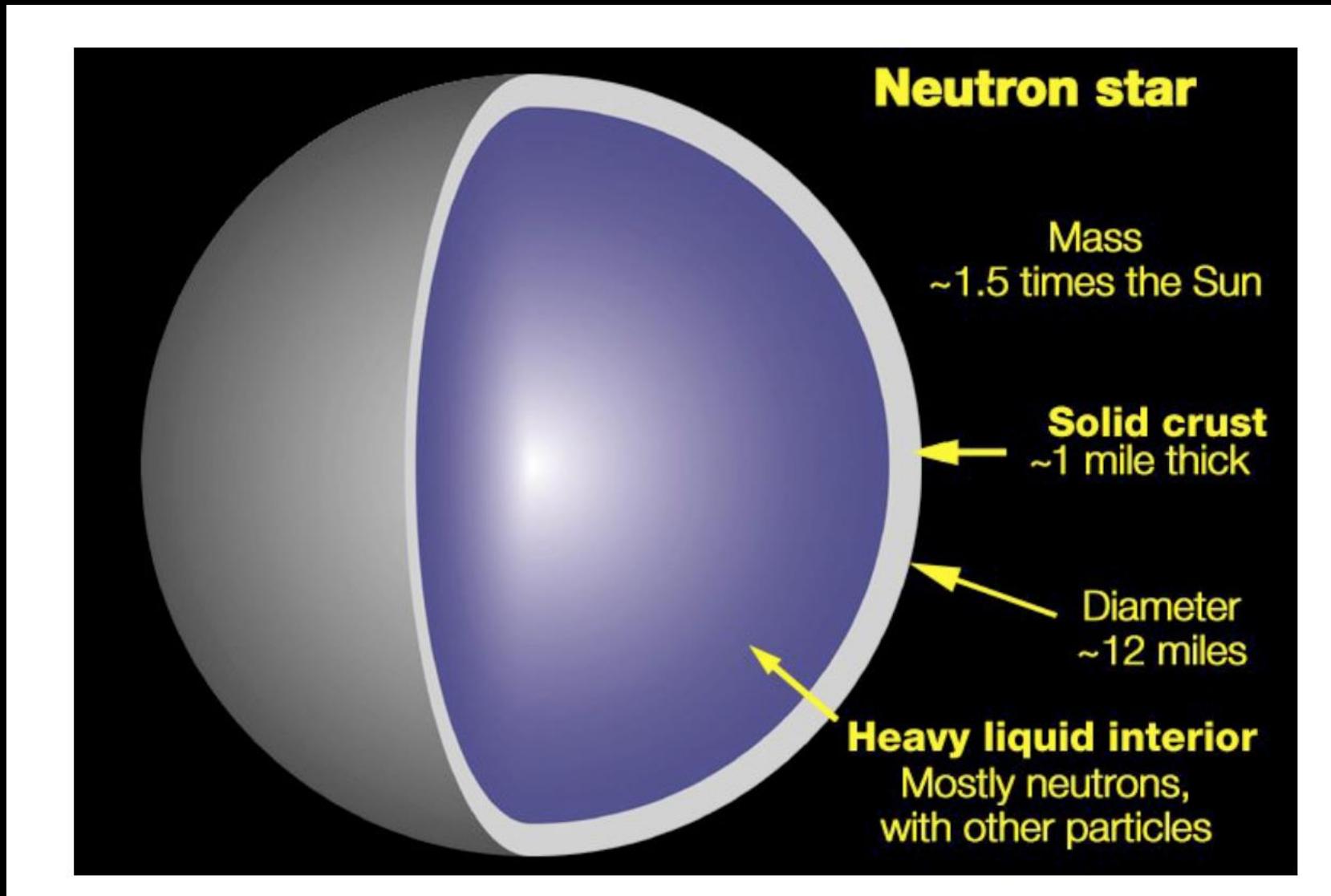
White dwarf



C+O nuclei plus
degenerate electrons
 $T \sim 10^6$ degrees

normal matter
 $T \sim 10,000$ degrees

Neutron star: density of nucleus!



- **white dwarf:** electrons run out of room and halt the collapse of the star

*maximum mass
1.4 solar masses*



- **neutron star:** neutrons run out of room and halt the collapse of the star

*maximum mass
~3 solar masses*



- **black hole:** gravity wins: collapse continues

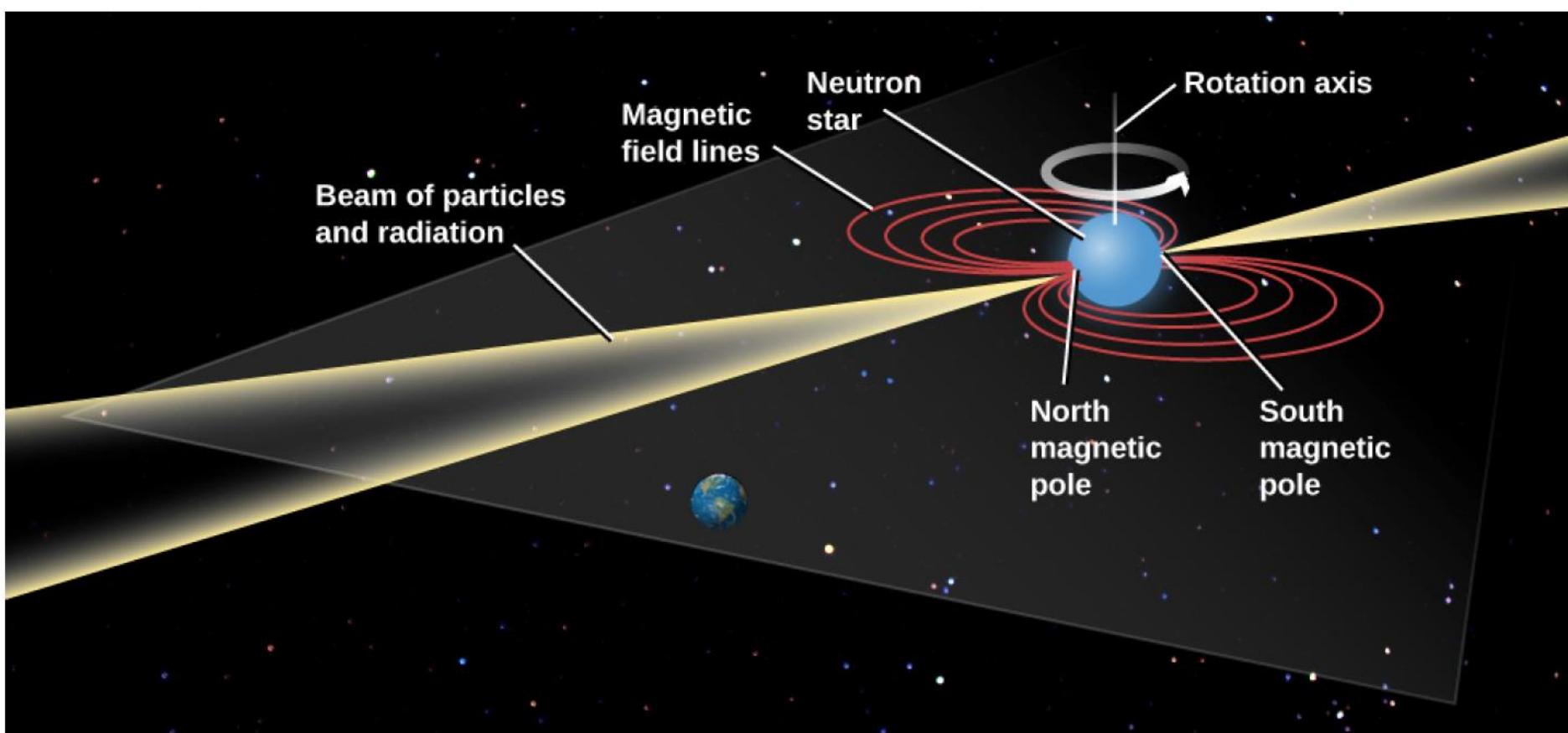
Sun: size 1.4×10^6 km

rotation period 27 days = 2.3×10^6 s

Neutron star: size 14 km = 1 million times smaller

👉 rotation period 1 million times shorter = 2.3 s

Pulsar: neutron star with beamed light pulses from electrons

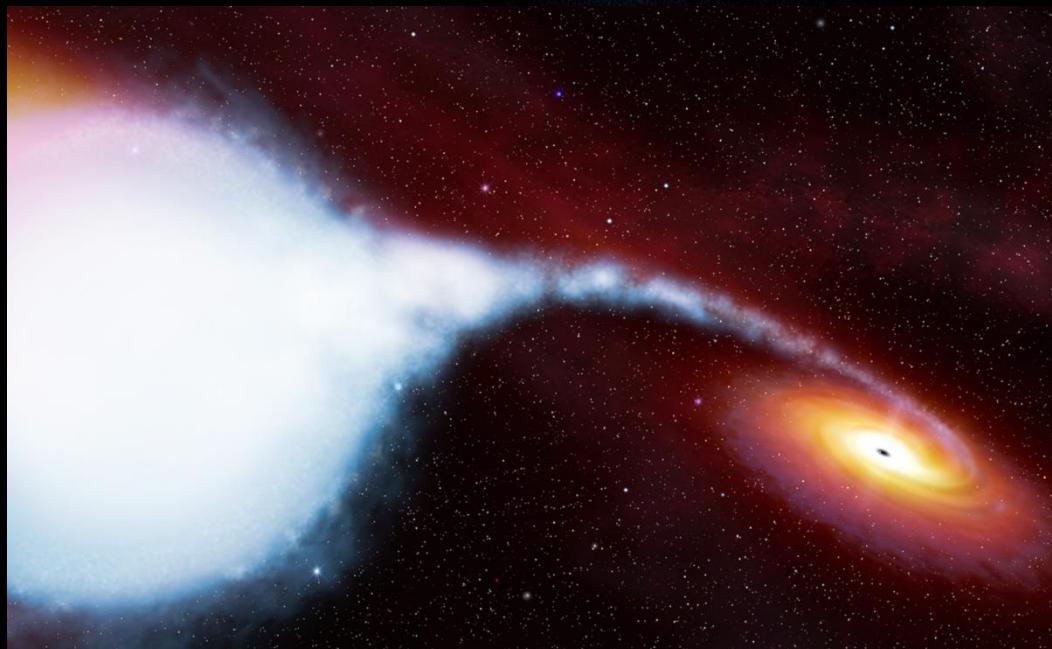




Jocelyn Bell:
Found pulsars
(discovery won Nobel
Prize, but she did not)

Cygnus X-1: first accepted black hole

- Black holes in binary systems can “steal” mass from the companion
- Accretion disk: very hot
 - Strong X-rays
- Some X-ray binaries identified as stellar mass black holes



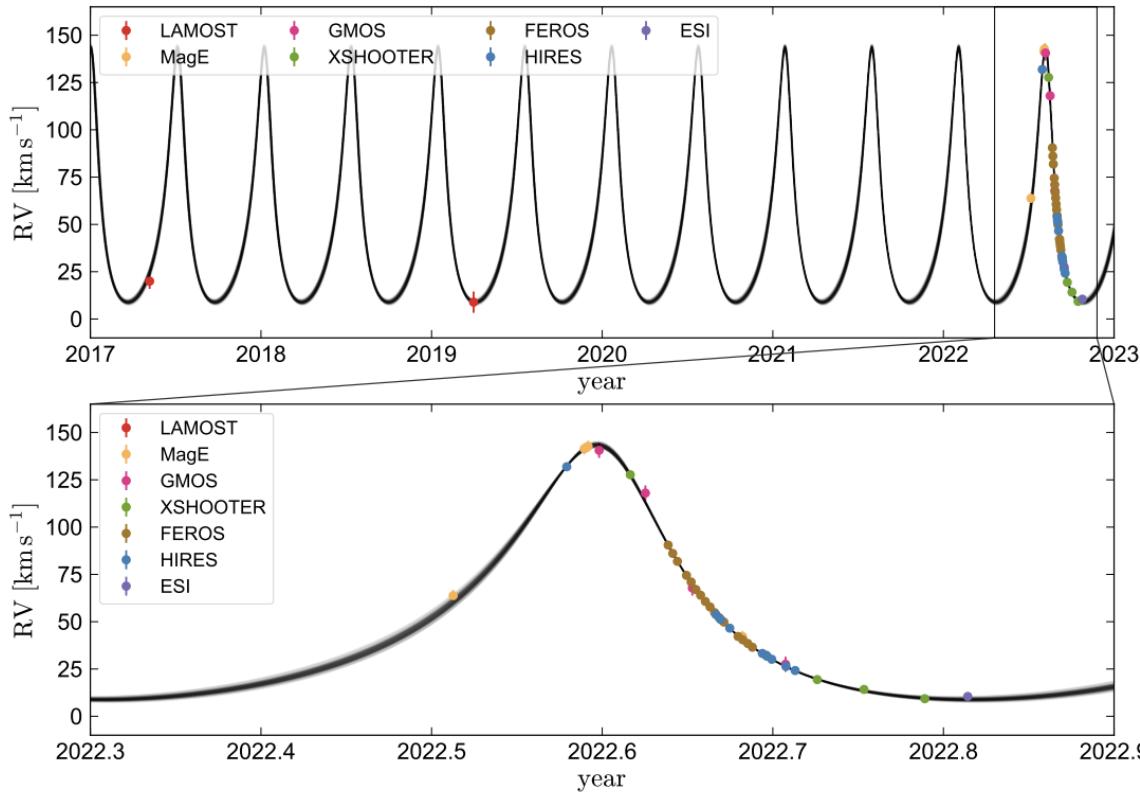
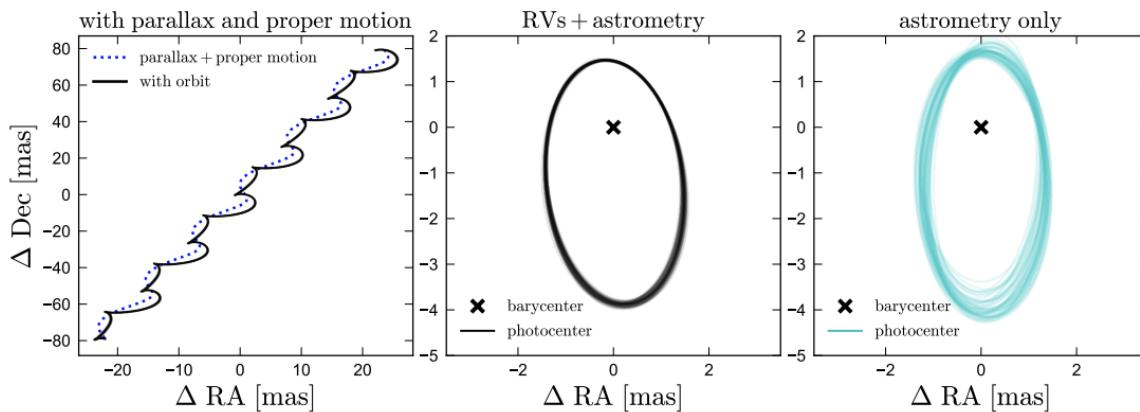


Figure 2. Radial velocities. Points with error bars are measurements; gray lines are draws from the posterior when jointly fitting these RVs and the *Gaia* astrometric constraints. Top panel shows all available RVs, including observations by the LAMOST survey in 2017 and 2019; bottom panel highlights our follow-up in 2022. The best-fit solution has a period of 186 days, eccentricity 0.45, and RV semi-amplitude of 67 km s^{-1} . Together with the inclination constraint from astrometry, this implies a companion mass of $9.62 \pm 0.18 M_{\odot}$.

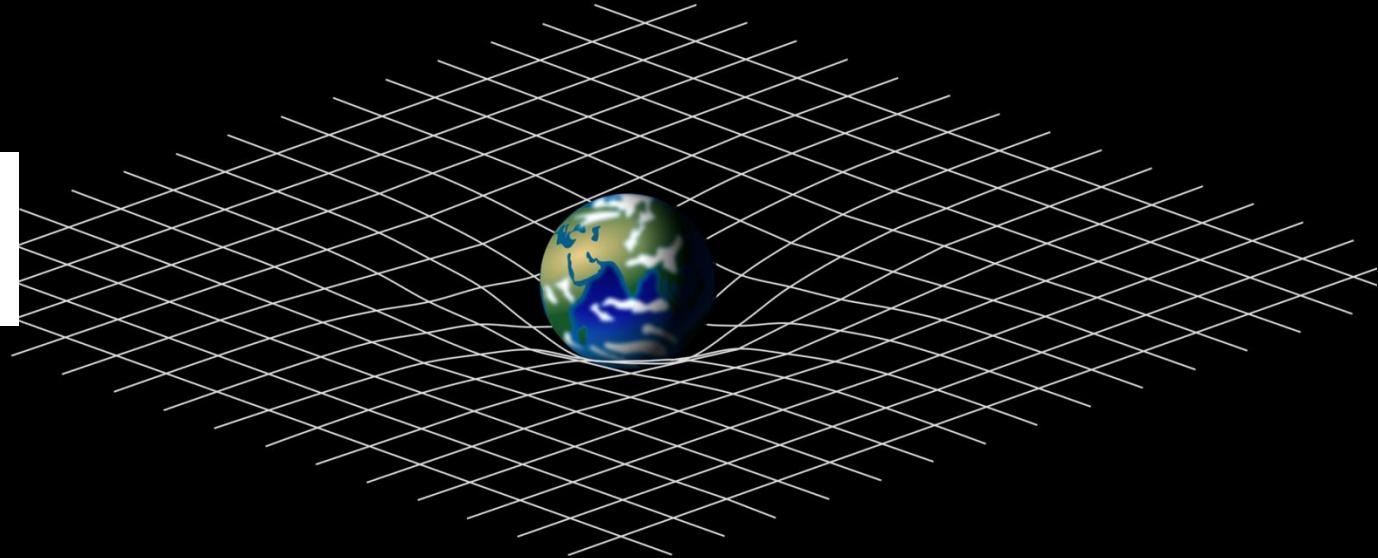


Gaia BH1

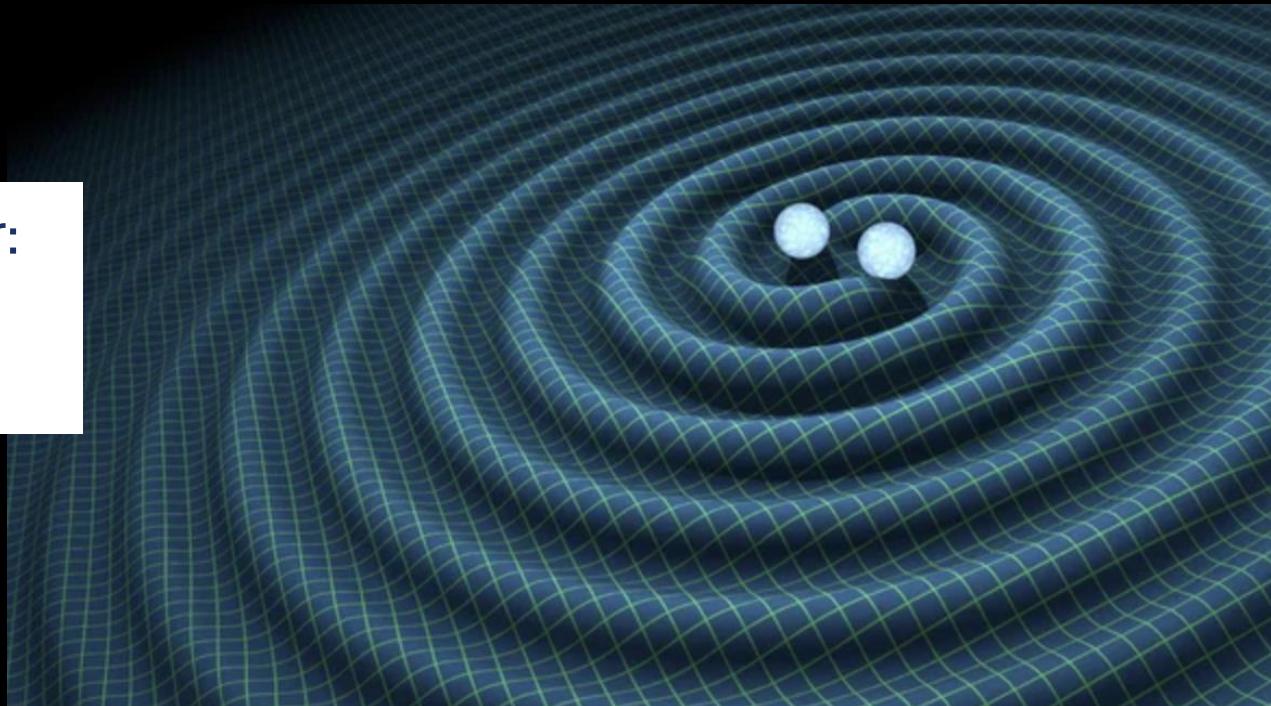
First “quiet”
stellar-mass
black hole

Found by orbit of
a star

Mass: curves
space-time

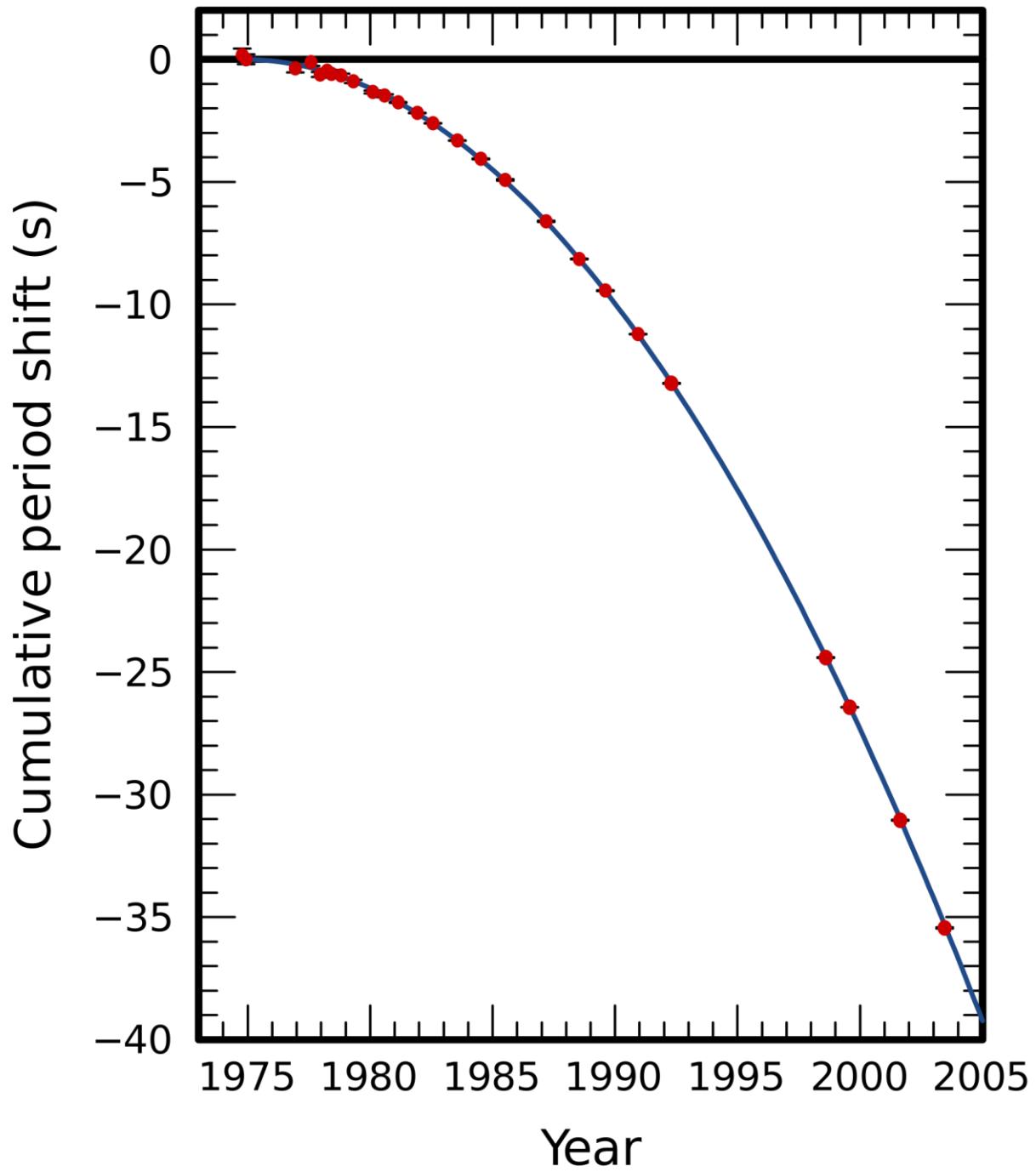


Binary merger:
gravitational
waves

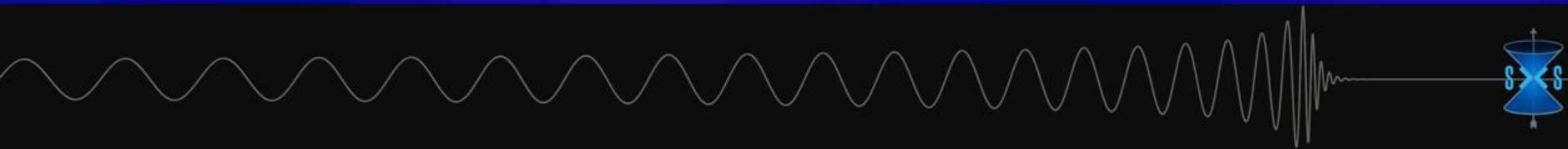
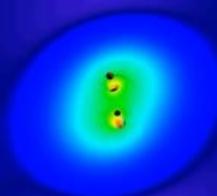


Hulse-Taylor
binary pulsar

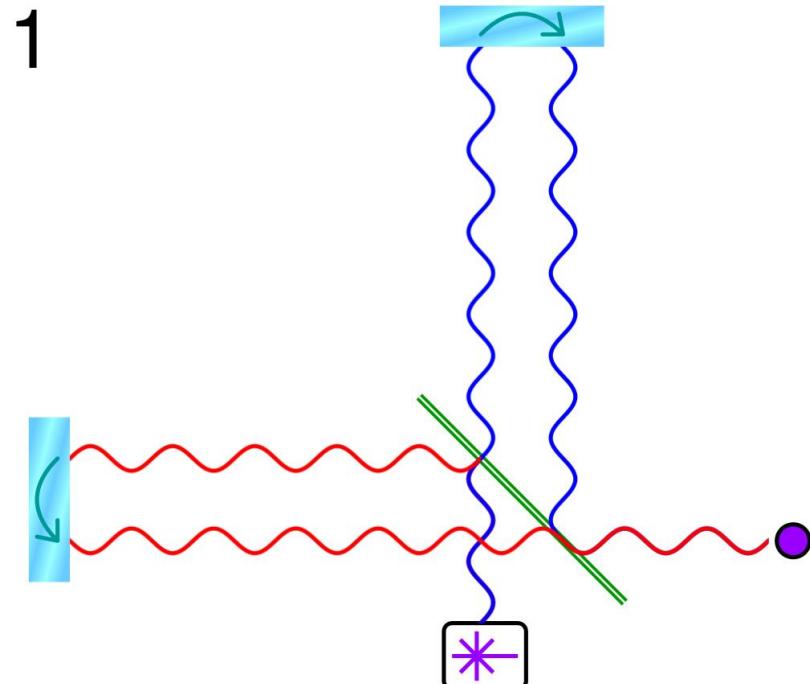
Orbital decay
requires
gravitational
waves



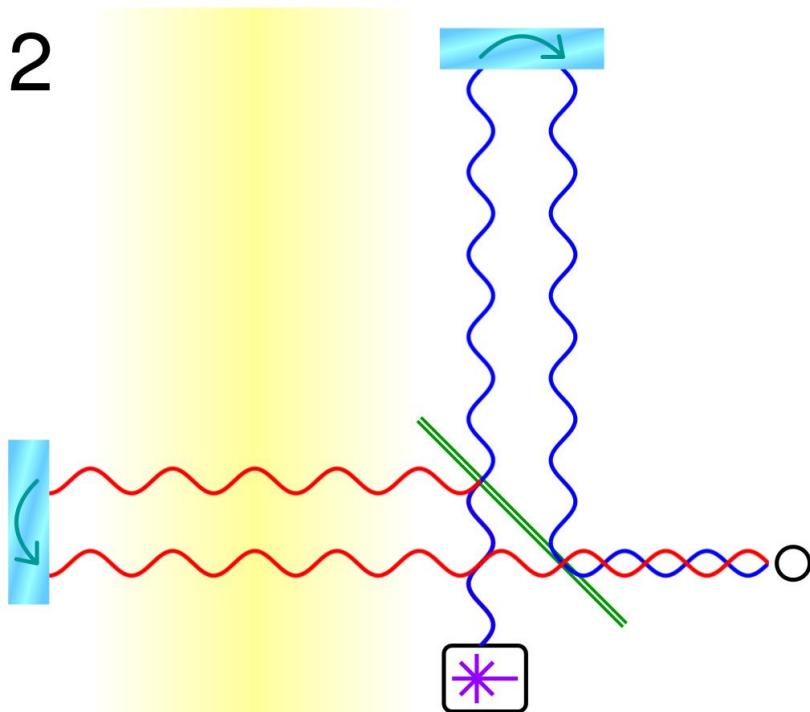
-0.76s



1

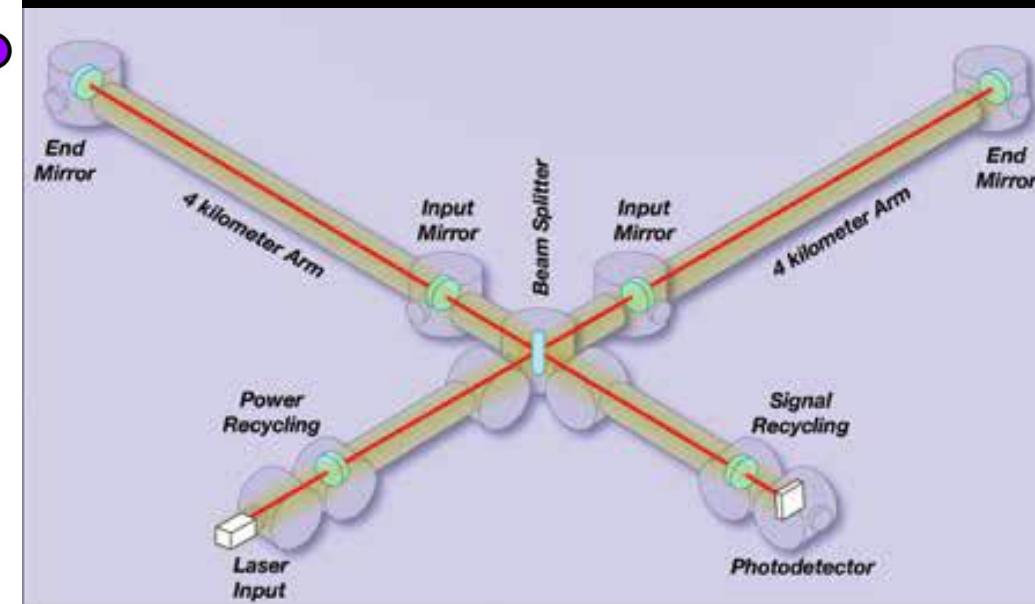


2

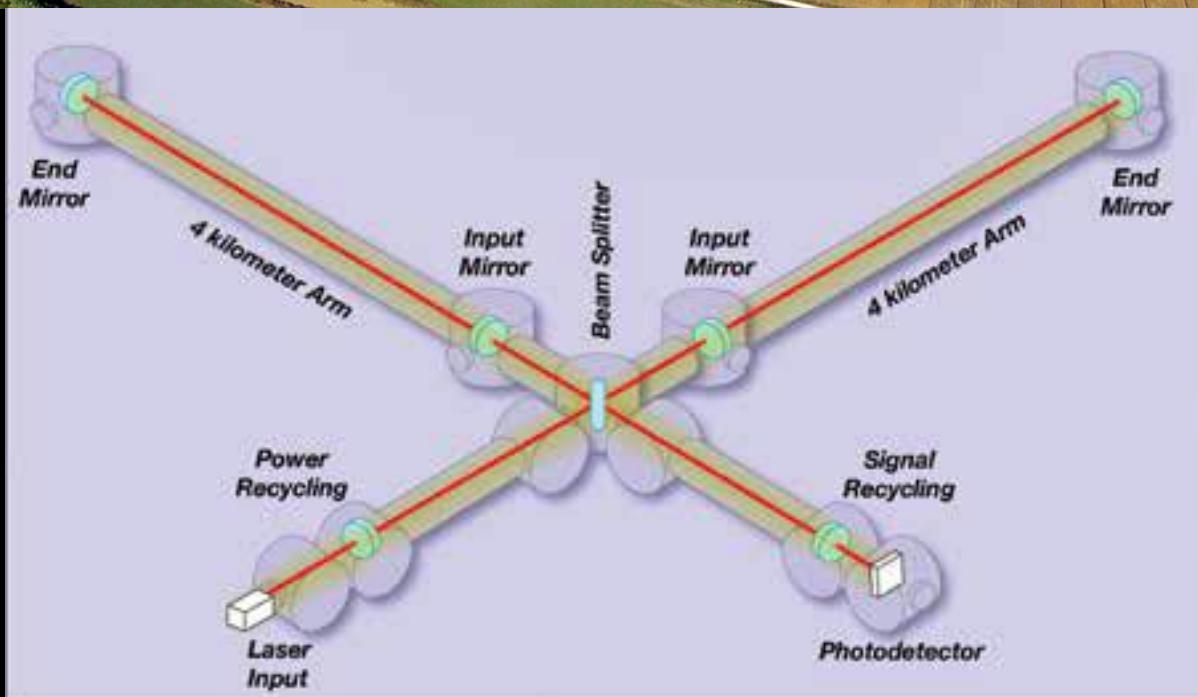


How to detect gravitational waves: ripples in space time?

Gravitational wave detectors



Gravitational waves: distort space by 10^{-19} m (smaller than proton)

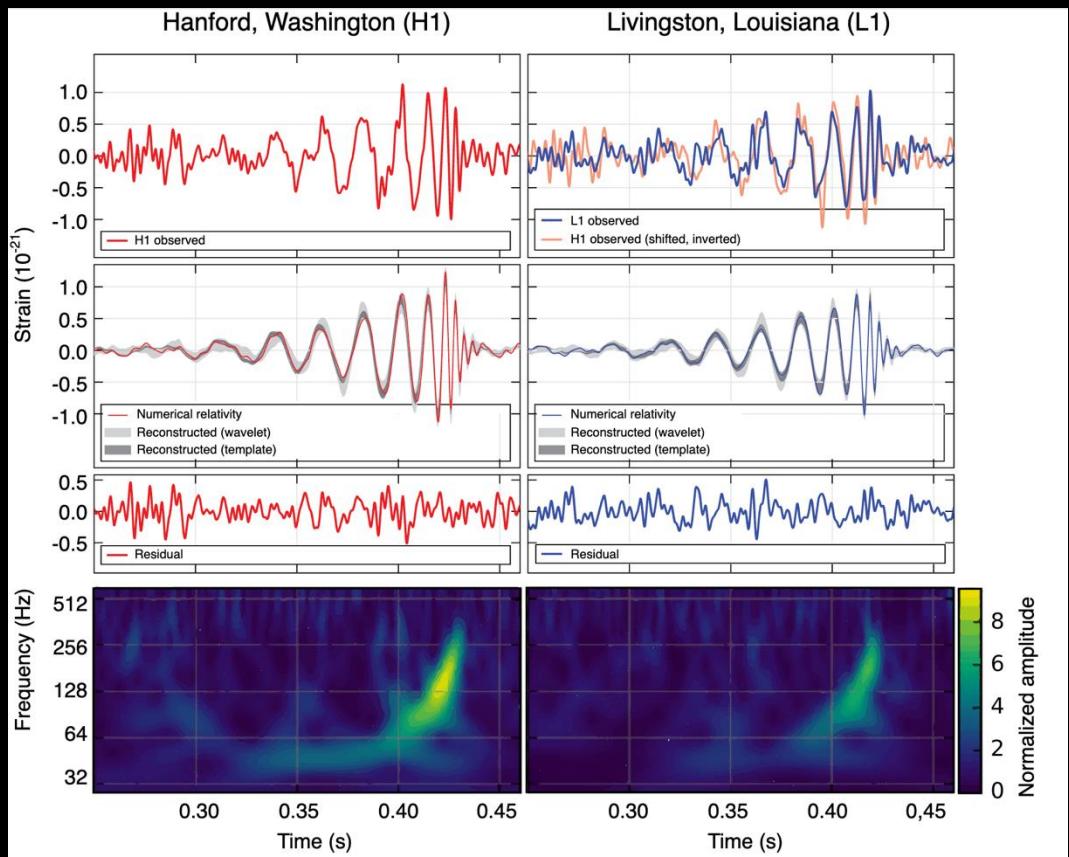


Operational
Under Construction
Planned

Gravitational Wave Observatories

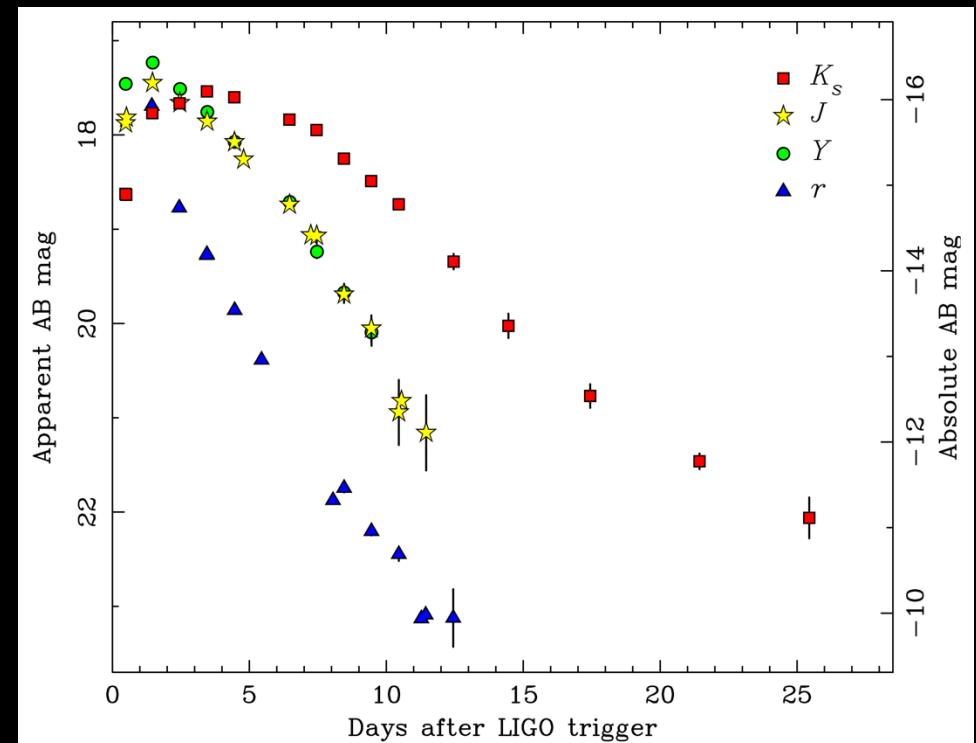
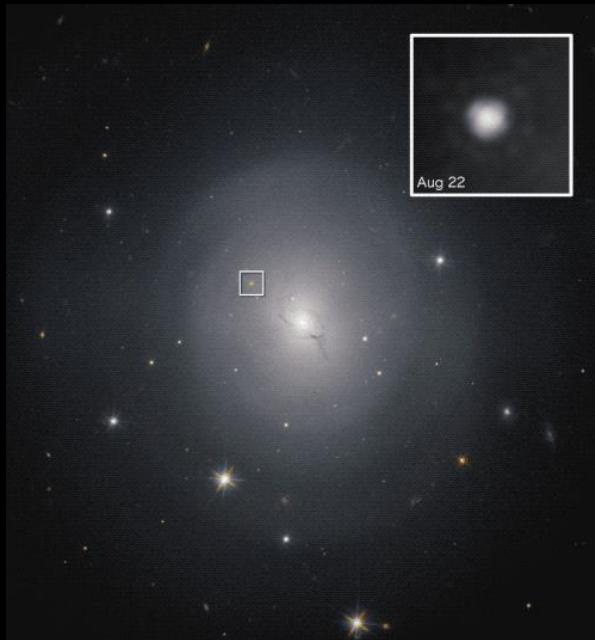
First direct gravitational wave detection

- LIGO in 2015
- Merger of two 30 solar mass black holes
 - Surprising: did not know that black holes of that mass existed
 - Stellar remnant: failed supernova?



Gravitational wave detection

- About 90 events to date!
- Neutron star-neutron star merger:
 - optical and gamma ray counterparts help to understand the explosion, production of heavy elements



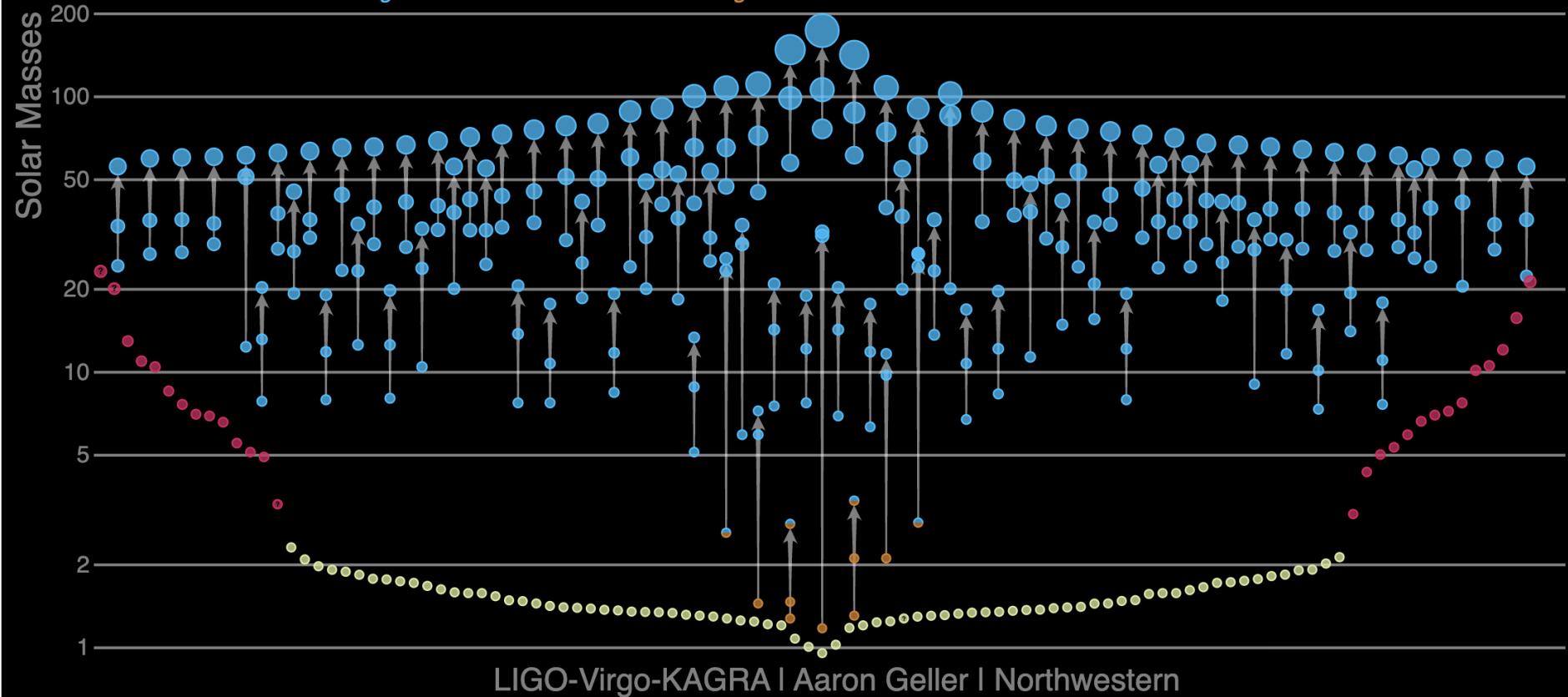
The Origin of the Solar System Elements

| | | | | | | | | | | | | |
|----------|---|--|----------|----------|----------|--|---|--|----------|----------|----------|--|
| 1 H | big bang fusion  | | | | | cosmic ray fission  | | | | | 2 He | |
| 3 Li | 4 Be | merging neutron stars?  | | | | | exploding massive stars  | | | | | |
| 11 Na | 12 Mg | dying low mass stars  | | | | | exploding white dwarfs  | | | | | |
| 19 K | 20 Ca | 21 Sc | 22 Ti | 23 V | 24 Cr | 25 Mn | 26 Fe | 27 Co | 28 Ni | 29 Cu | 30 Zn | |
| 37 Rb | 38 Sr | 39 Y | 40 Zr | 41 Nb | 42 Mo | 43 Tc | 44 Ru | 45 Rh | 46 Pd | 47 Ag | 48 Cd | |
| 55 Cs | 56 Ba | 72 Hf | 73 Ta | 74 W | 75 Re | 76 Os | 77 Ir | 78 Pt | 79 Au | 80 Hg | 81 Tl | |
| 87 Fr | 88 Ra | 57 La | 58 Ce | 59 Pr | 60 Nd | 61 Pm | 62 Sm | 63 Eu | 64 Gd | 65 Tb | 66 Dy | |
| | | 89 Ac | 90 Th | 91 Pa | 92 U | 93 Np | 94 Pu | Very radioactive isotopes; nothing left from stars | | | | |

Masses in the Stellar Graveyard

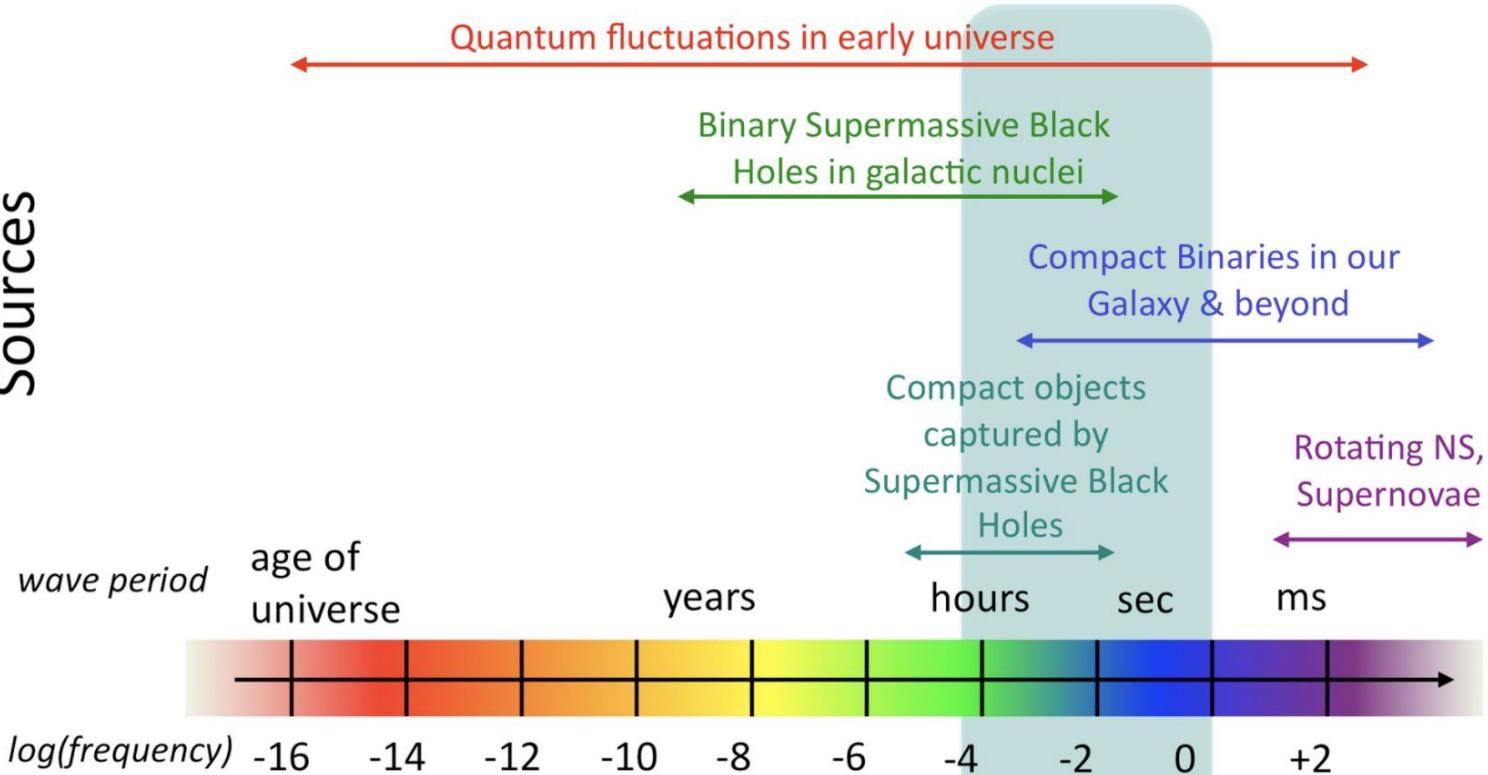


LIGO-Virgo-KAGRA Black Holes LIGO-Virgo-KAGRA Neutron Stars EM Black Holes EM Neutron Stars

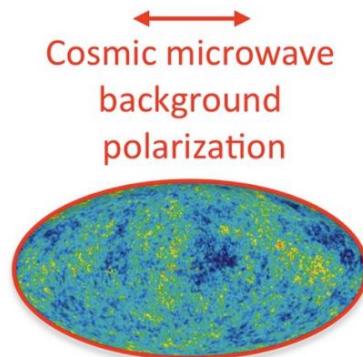


The Gravitational Wave Spectrum

Sources



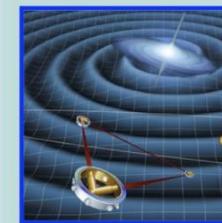
Detectors



Cosmic microwave background polarization



Pulsar Timing



Space Interferometers



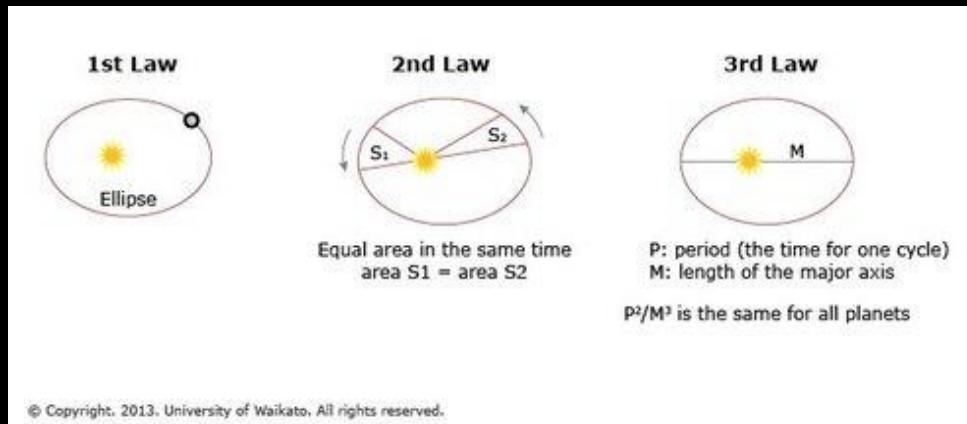
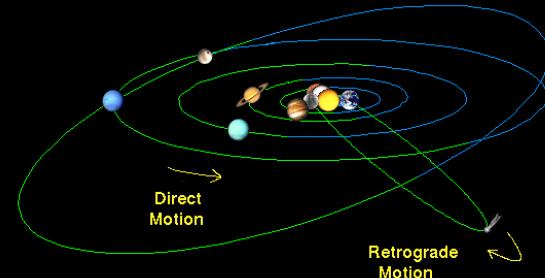
Terrestrial Interferometers

Primordial black holes

- Quantum fluctuations soon after big bang
- Initial mass as low as $1e-8$ kg
- Anything below $1e11$ kg would have evaporated away
 - Hawking radiation: black holes evaporate
 - Relativistic+quantum effects: radiation released outside black hole
- Any measurements will help constrain cosmology

History of gravitational theories

- Copernicus: Earth orbits the sun
- Kepler's laws
 - 1st law: planetary orbits are ellipses
 - 2nd law: orbit sweeps out equal areas from sun in equal time
 - 3rd law: $P^2 = a^3$ (period² = orbital distance³)



- Newton: connected planetary motion to gravity on Earth

$$F = G \frac{m_1 m_2}{r^2}$$

Special Relativity

- Laws of physics are invariant in all inertial frames of reference
- Speed of light in a vacuum is the same for all observers



Time Dilation and length contraction

- To an observer at rest, the time of something moving quickly will appear much longer than in the faster reference frame

$$\Delta t' = \frac{\Delta t}{\sqrt{1 - \frac{v^2}{c^2}}}$$

- An object would be measured to be shorter in the inertial frame
- As an object's speed approaches the speed of light, the relativistic mass increases towards infinity

$$L = L_0 \sqrt{1 - v^2/c^2}$$

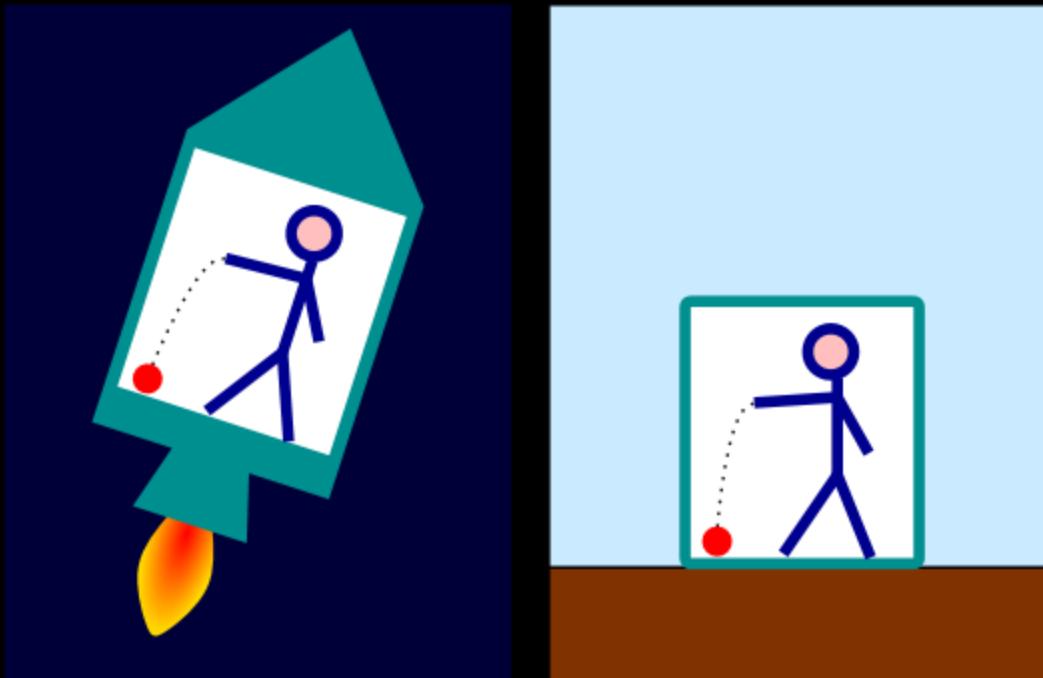
$$m_{\text{rel}} = \frac{m}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Implications of special relativity

- Information cannot travel faster than the speed of light
 - It would take infinite energy to accelerate any mass to the speed of light
- Mass-energy equivalence ($E=mc^2$)
- No absolute reference frame
 - Previous idea: aether in space is absolute state of rest

General relativity: geometric theory of gravity

- Curvature of spacetime is directly related to energy and momentum
- Specified by Einstein field equations



Elevator thought experiment:

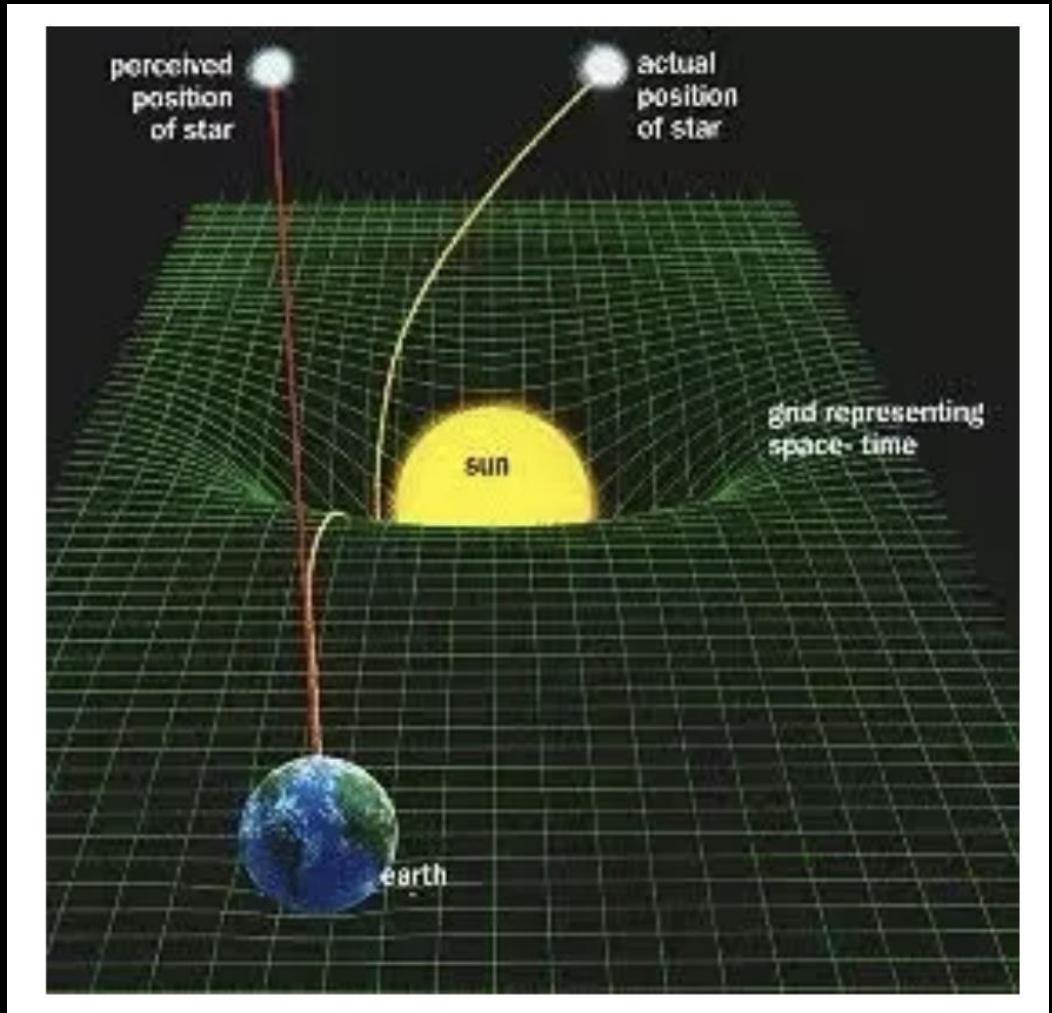
No way to tell whether the ball is

(a) falling to a gravitational well

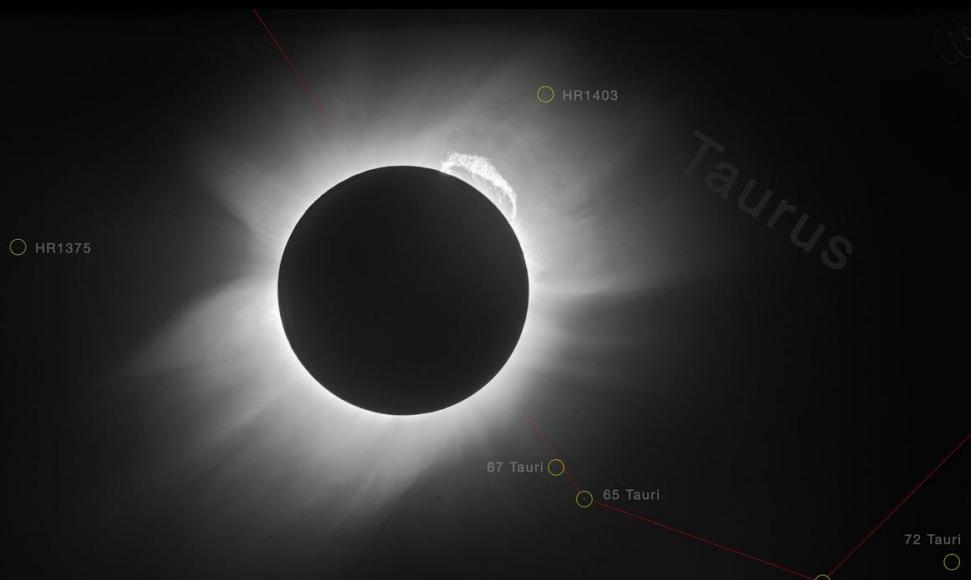
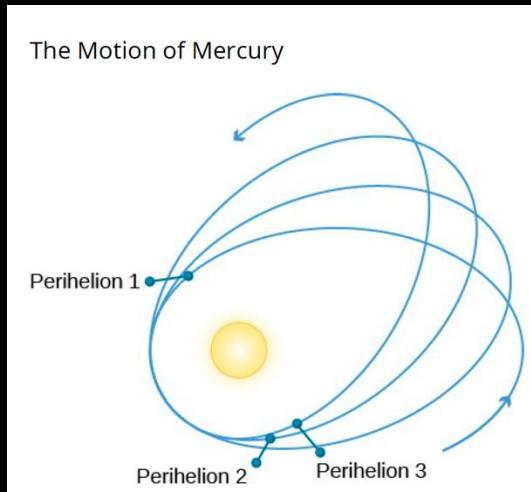
(b) Falling because the
elevator is accelerating

Implications of general relativity

- Gravitational lensing
 - Gravitational waves
 - Black holes
 - Everything!
-
- Newton's laws are limiting (non-relativistic) case of general relativity



Test of General Relativity



LIGHTS ALL ASKEW IN THE HEAVENS

Men of Science More or Less
Agog Over Results of Eclipse
Observations.

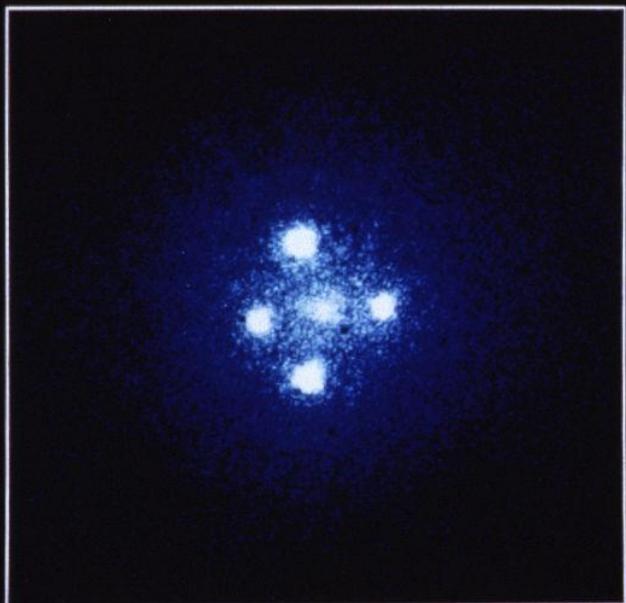
EINSTEIN THEORY TRIUMPHS

Stars Not Where They Seemed
or Were Calculated to be,
but Nobody Need Worry.

A BOOK FOR 12 WISE MEN

No More in All the World Could
Comprehend It, Said Einstein When
His Daring Publishers Accepted It.

Test in 1919 eclipse: precise measurement of Mercury's position

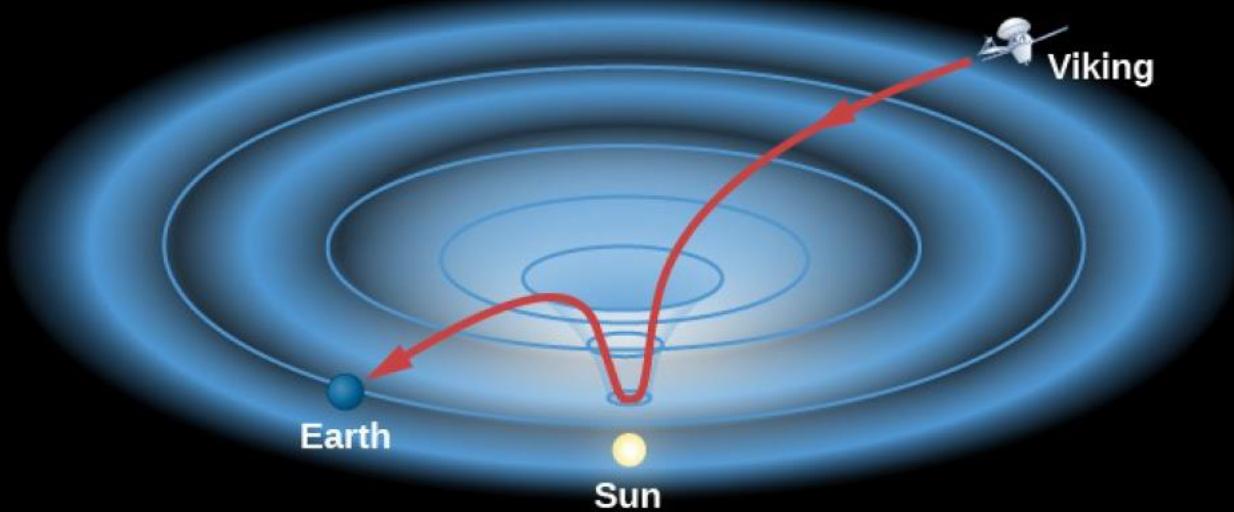


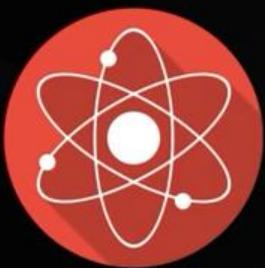
Gravitational Lens G2237+0305

Tests of general relativity

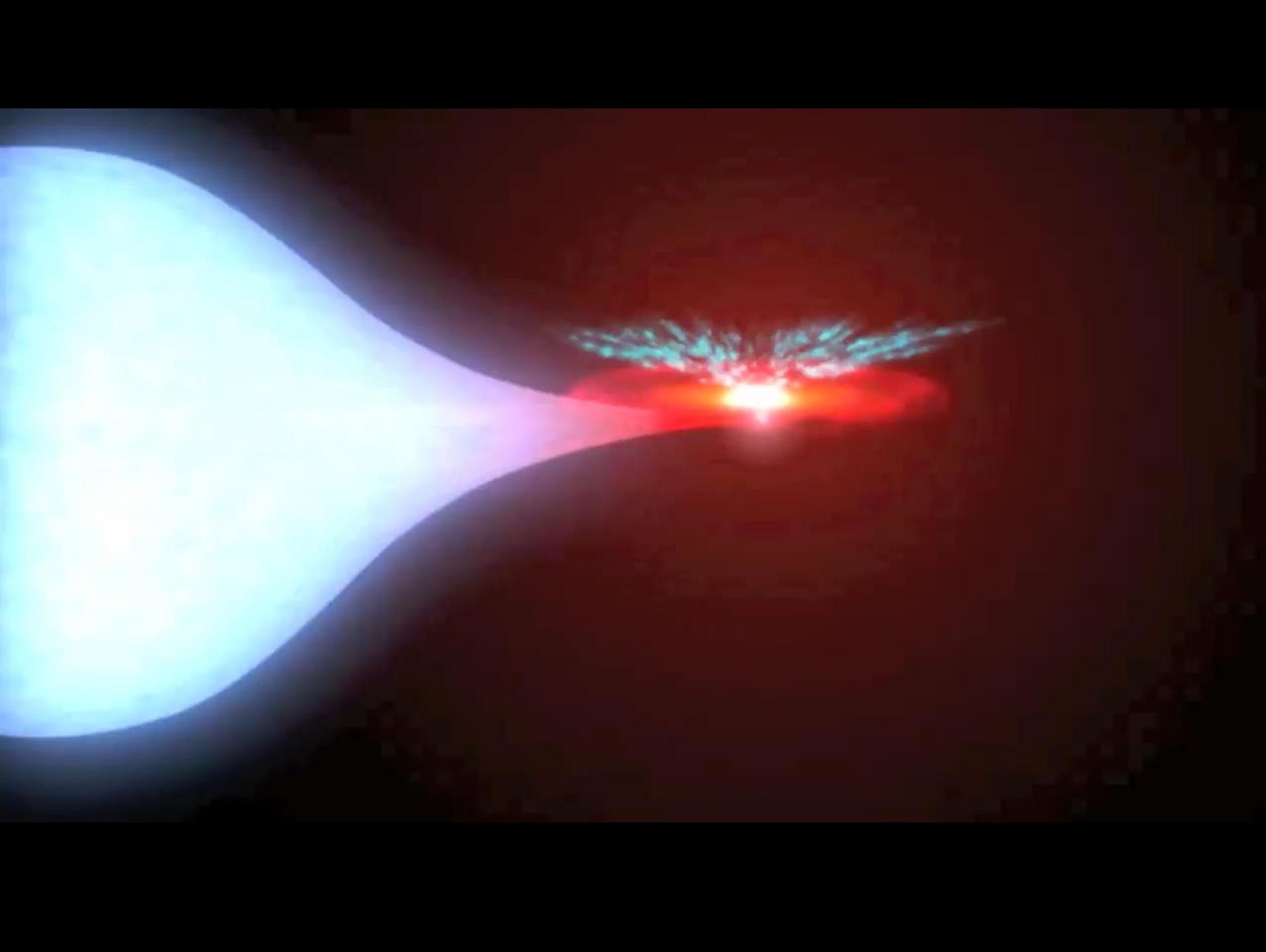
Gravitational lens

Bending of signal from Viking Mission





ScienceClic
Alessandro Roussel



Gravity and black holes

- General relativity governs our universe
 - Every experiment has confirmed general relativity
- Gravity: best tested in extreme environments: black holes
- Black holes are common
 - Stellar mass black holes: stellar remnants
 - Centers of galaxies (primordial? Early formation from massive stars?)
 - Primordial black holes

Next week: our solar system!

