

Deep Learning

Lecture 7: Attention and transformers

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Today

Attention is all you need!

- Encoder-decoder
- Bahdanau attention
- Attention layers
- Transformers
- Applications

Encoder-decoder

Many real-world problems require to process a signal with a **sequence** structure.

- Sequence classification:

- sentiment analysis in text
- activity/action recognition in videos
- DNA sequence classification

- Sequence synthesis:

- text synthesis
- music synthesis
- motion synthesis

- Sequence-to-sequence translation:

- speech recognition
- text translation
- part-of-speech tagging

Given a set \mathcal{X} , if $S(\mathcal{X})$ denotes the set of sequences of elements from \mathcal{X} ,

$$S(\mathcal{X}) = \cup_{t=1}^{\infty} \mathcal{X}^t,$$

then we formally define:

Sequence classification

$$f : S(\mathcal{X}) \rightarrow \Delta^C$$

Sequence synthesis

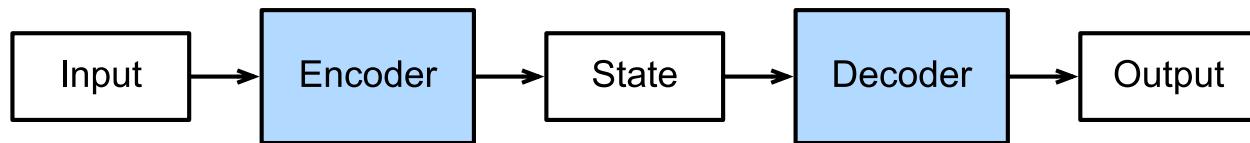
$$f : \mathbb{R}^d \rightarrow S(\mathcal{X})$$

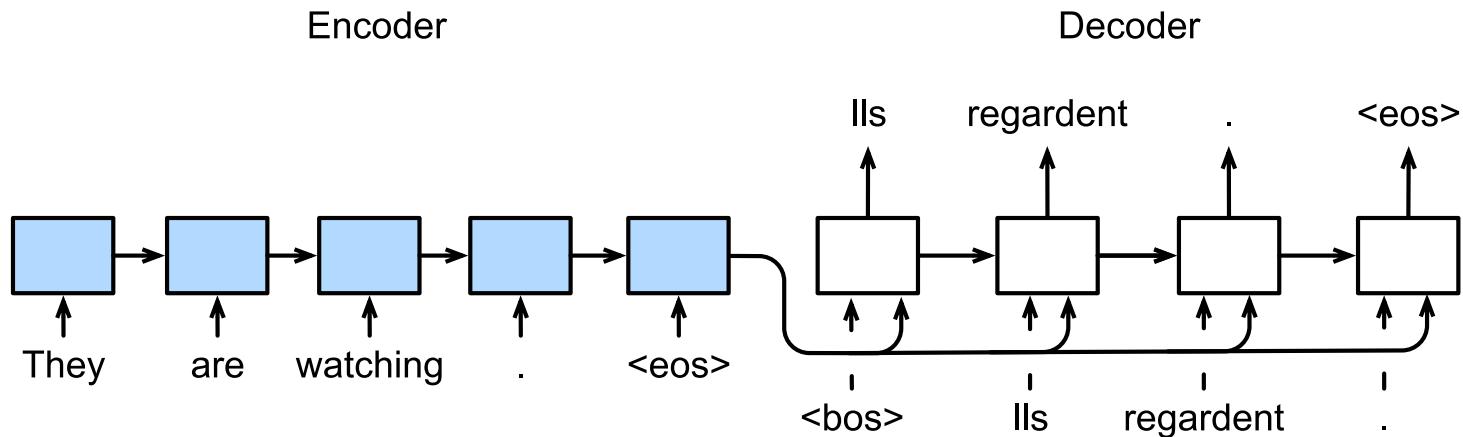
Sequence-to-sequence translation

$$f : S(\mathcal{X}) \rightarrow S(\mathcal{Y})$$

In the rest of the slides, we consider only time-indexed signal, although it generalizes to arbitrary sequences.

When the input is a sequence $\mathbf{x} \in S(\mathbb{R}^p)$ of variable length, the historical approach is to use a recurrent **encoder-decoder** architecture that first compresses the input into a single vector v and then uses it to generate the output sequence.



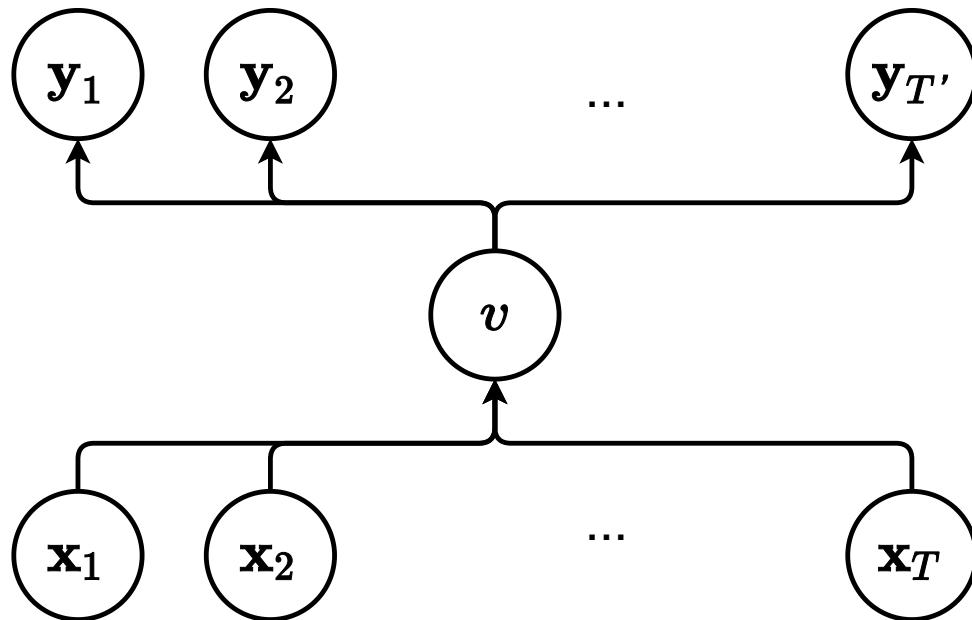


Recurrent encoder-decoder models compress an input sequence $\mathbf{x}_{1:T}$ into a single thought vector v , and then produce an output sequence $\mathbf{y}_{1:T'}$ from an autoregressive generative model

$$\mathbf{h}_t = \phi(\mathbf{x}_t, \mathbf{h}_{t-1})$$

$$v = \mathbf{h}_T$$

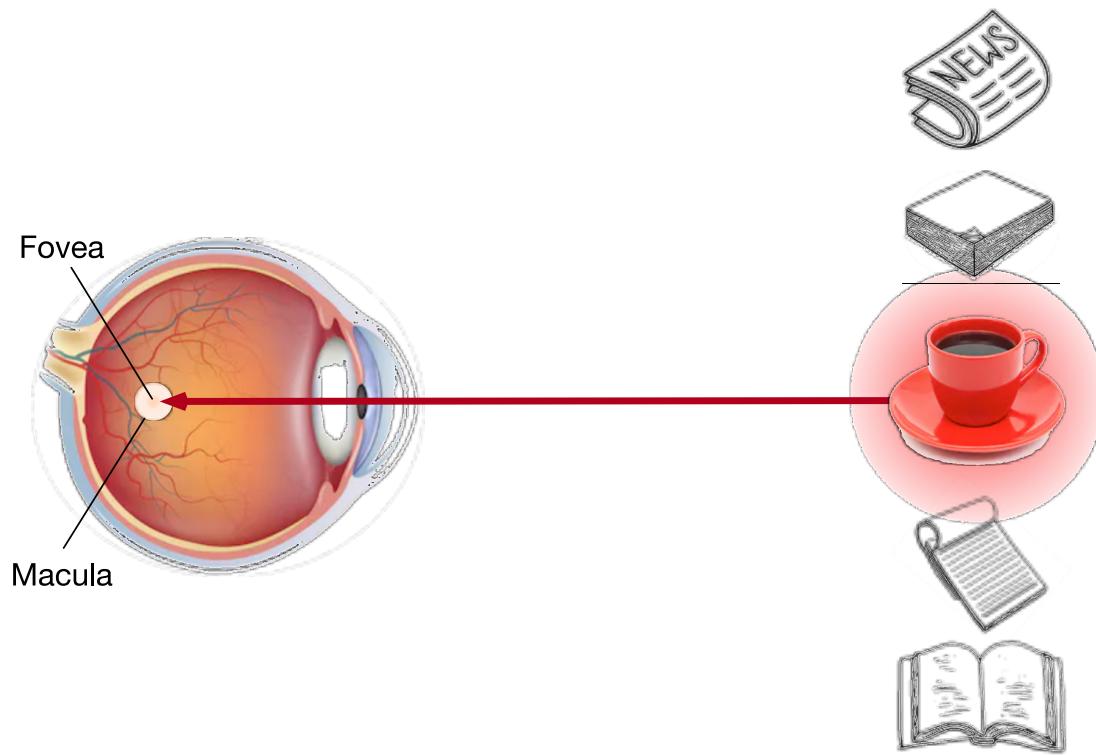
$$\mathbf{y}_i \sim p(\cdot | \mathbf{y}_{1:i-1}, v).$$



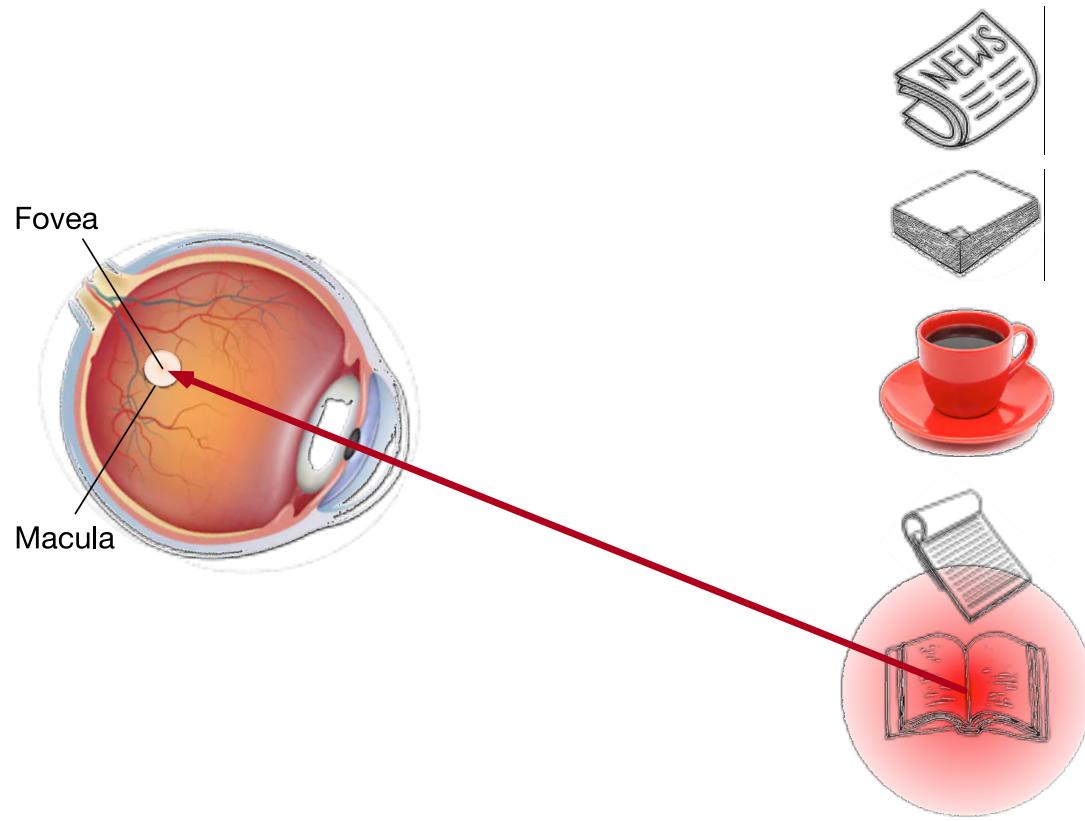
This architecture assumes that the sole vector v carries enough information to generate entire output sequences. This is often **challenging** for long sequences.

Bahdanau attention

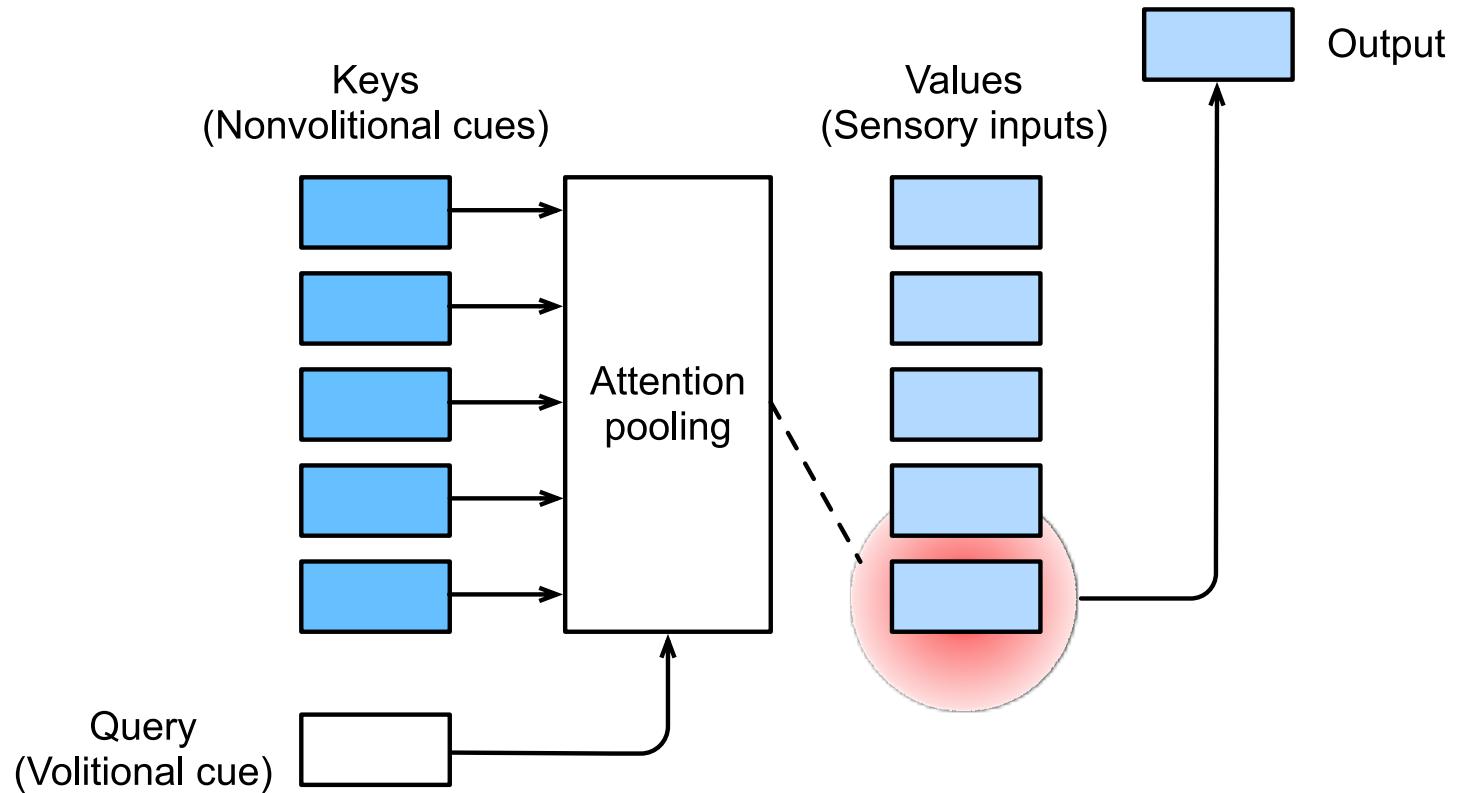




Using the nonvolitional cue based on saliency (red cup, non-paper), attention is involuntarily directed to the coffee.

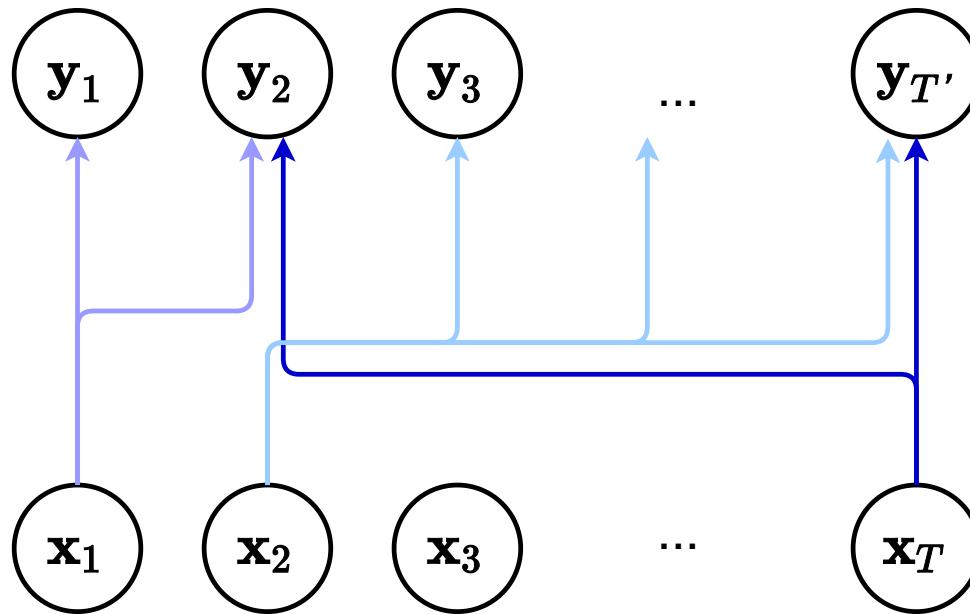


Using the volitional cue (want to read a book) that is task-dependent, attention is directed to the book under volitional control.

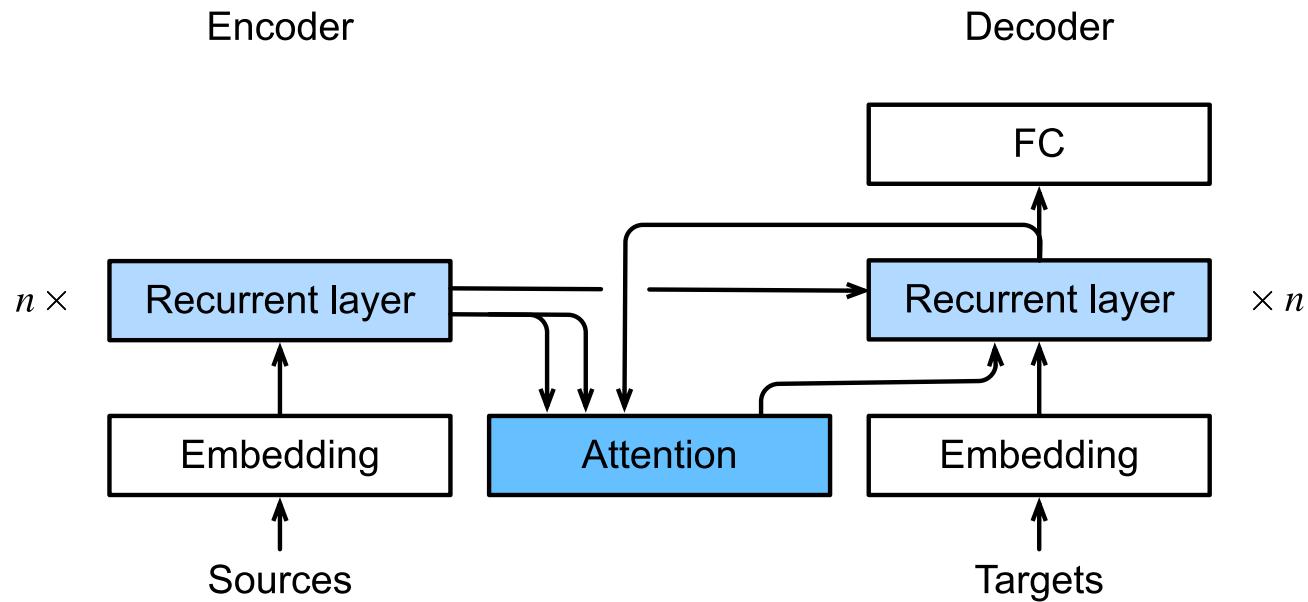


Attention mechanisms can transport information from parts of the input signal to parts of the output **specified dynamically**.

Under the assumption that each output token comes from one or a handful of input tokens, the decoder should attend to only those tokens that are relevant for producing the next output token.



Attention-based machine translation



Following Bahdanau et al. (2014), the encoder is specified as a bidirectional recurrent neural network (RNN) that computes an annotation vector for each input token,

$$\mathbf{h}_j = (\overrightarrow{\mathbf{h}}_j, \overleftarrow{\mathbf{h}}_j)$$

for $j = 1, \dots, T$, where $\overrightarrow{\mathbf{h}}_j$ and $\overleftarrow{\mathbf{h}}_j$ respectively denote the forward and backward hidden recurrent states of the bidirectional RNN.

From this, they compute a new process $\mathbf{s}_i, i = 1, \dots, T'$, which looks at weighted averages of the \mathbf{h}_j where the **weights are functions of the signal**.

Given $\mathbf{y}_1, \dots, \mathbf{y}_{i-1}$ and $\mathbf{s}_1, \dots, \mathbf{s}_{i-1}$, first compute an attention vector

$$\alpha_{i,j} = \text{softmax}_j(a(\mathbf{s}_{i-1}, \mathbf{h}_j))$$

for $j = 1, \dots, T$, where a is an [attention scoring function](#), here specified as a one hidden layer [tanh](#) MLP.

Then, compute the context vector from the weighted \mathbf{h}_j 's,

$$\mathbf{c}_i = \sum_{j=1}^T \alpha_{i,j} \mathbf{h}_j.$$

The model can now make the prediction \mathbf{y}_i as

$$\begin{aligned}\mathbf{s}_i &= f(\mathbf{s}_{i-1}, y_{i-1}, c_i) \\ \mathbf{y}_i &\sim g(\mathbf{y}_{i-1}, \mathbf{s}_i, \mathbf{c}_i),\end{aligned}$$

where f is a GRU.

This is **context attention**, where \mathbf{s}_{i-1} modulates what to look in $\mathbf{h}_1, \dots, \mathbf{h}_T$ to compute \mathbf{s}_i and sample \mathbf{y}_i .

L' accord sur la zone économique européenne a été signé en août 1992.

The agreement on the European Economic Area was signed in August 1992.

. <end>

(a)

Il convient de noter que l'environnement marin est le moins connu de l'environnement.

It should be noted that the marine environment is the least known of environments.

. <end>

(b)

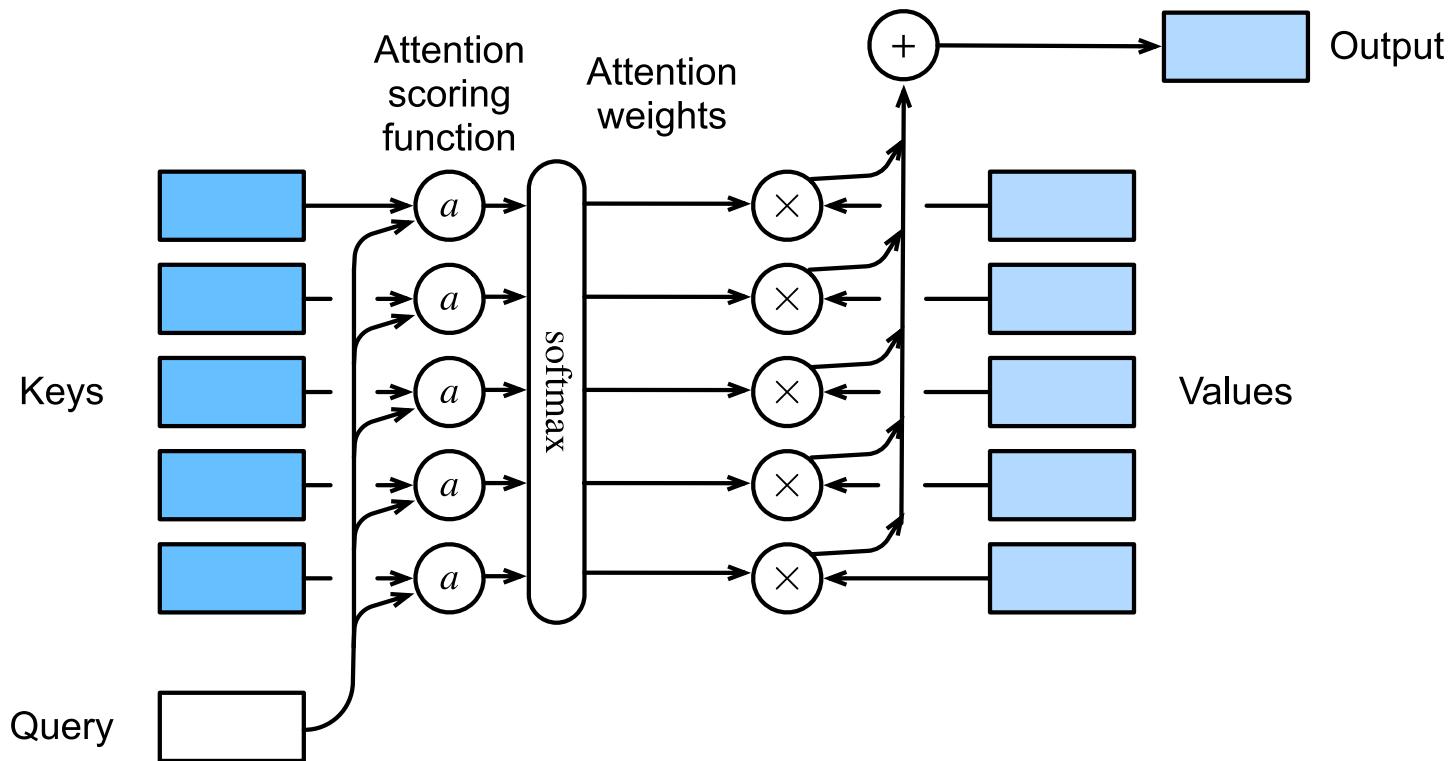
Attention layers

The attention mechanisms can be defined generically as follows.

Given a context or query vector $\mathbf{q} \in \mathbb{R}^q$, a key tensor $\mathbf{K} \in \mathbb{R}^{m \times k}$, and a value tensor $\mathbf{V} \in \mathbb{R}^{m \times v}$, an attention layer computes an output vector $\mathbf{y} \in \mathbb{R}^v$ with

$$\mathbf{y} = \sum_{i=1}^m \text{softmax}_i(a(\mathbf{q}, \mathbf{K}_i; \theta)) \mathbf{V}_i,$$

where $a : \mathbb{R}^q \times \mathbb{R}^k \rightarrow \mathbb{R}$ is a scalar attention scoring function.



Additive attention

When queries and keys are vectors of different lengths, we can use an additive attention as the scoring function.

Given $\mathbf{q} \in \mathbb{R}^q$ and $\mathbf{k} \in \mathbb{R}^k$, the **additive attention** scoring function is

$$a(\mathbf{q}, \mathbf{k}) = \mathbf{w}_v^T \tanh(\mathbf{W}_q^T \mathbf{q} + \mathbf{W}_k^T \mathbf{k})$$

where $\mathbf{w}_v \in \mathbb{R}^h$, $\mathbf{W}_q \in \mathbb{R}^{q \times h}$ and $\mathbf{W}_k \in \mathbb{R}^{k \times h}$ are learnable parameters.

Scaled dot-product attention

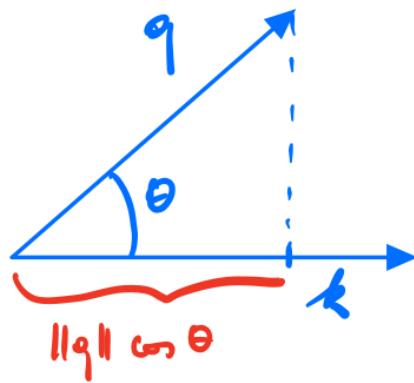
When queries and keys are vectors of the same length d , we can use a scaled dot-product attention as the scoring function.

Given $\mathbf{q} \in \mathbb{R}^d$ and $\mathbf{k} \in \mathbb{R}^d$, the **scaled dot-product attention** scoring function is

$$a(\mathbf{q}, \mathbf{k}) = \frac{\mathbf{q}^T \mathbf{k}}{\sqrt{d}}.$$

For n queries $\mathbf{Q} \in \mathbb{R}^{n \times d}$, keys $\mathbf{K} \in \mathbb{R}^{m \times d}$ and values $\mathbf{V} \in \mathbb{R}^{m \times v}$, the scaled dot-product attention layer computes an output tensor

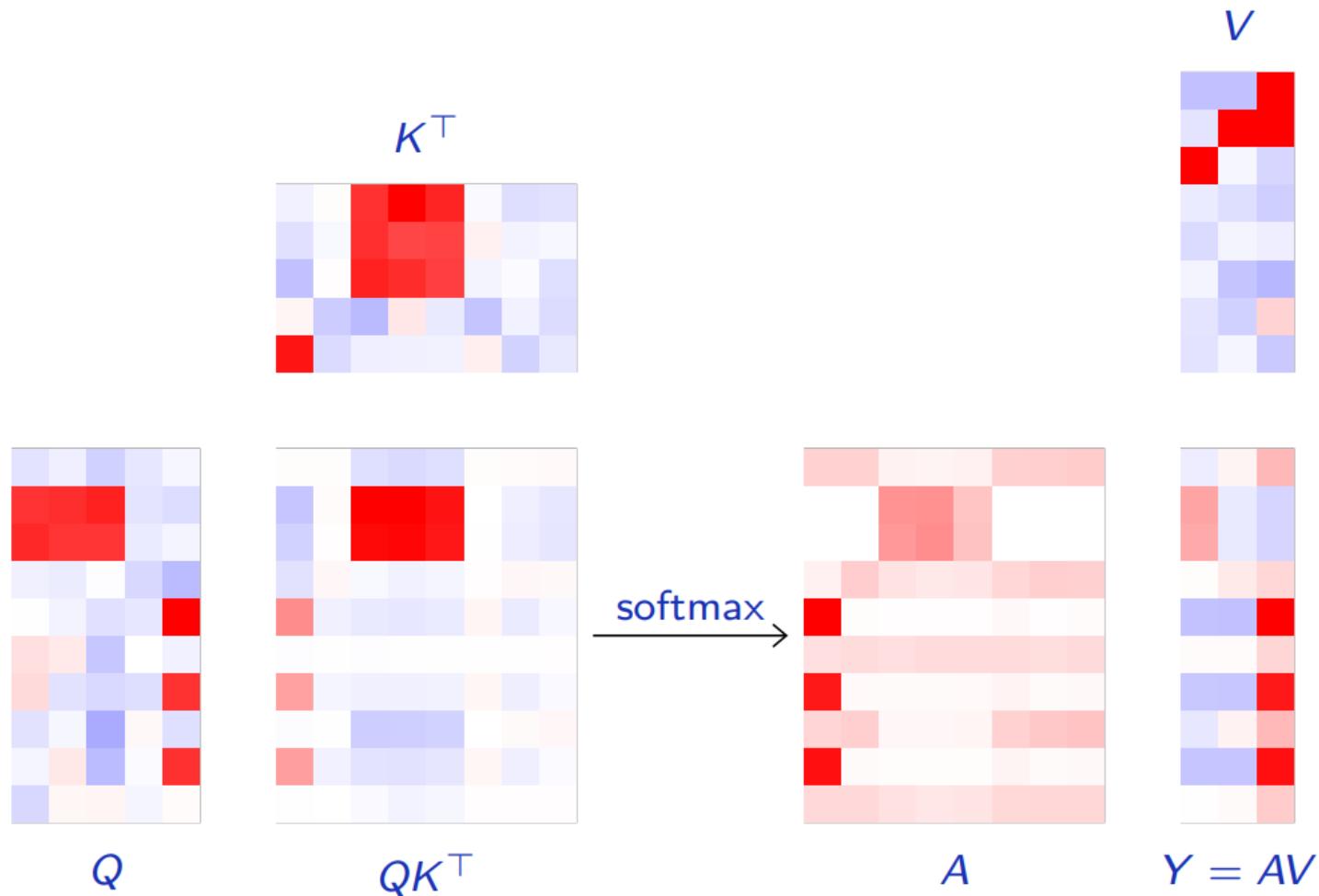
$$\mathbf{Y} = \underbrace{\text{softmax} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d}} \right)}_{\text{attention matrix } \mathbf{A}} \mathbf{V} \in \mathbb{R}^{n \times v}.$$



$$q^T k = \|q\| \|k\| \cos \theta$$

Recall that the dot product is simply a un-normalised cosine similarity, which tells us about the alignment of two vectors.

Therefore, the \mathbf{QK}^T matrix is a **similarity matrix** between queries and keys.



In the currently standard models for sequences, the queries, keys and values are linear functions of the inputs.

Given the learnable matrices $\mathbf{W}_q \in \mathbb{R}^{d \times x}$, $\mathbf{W}_k \in \mathbb{R}^{d \times x'}$, and $\mathbf{W}_v \in \mathbb{R}^{v \times x'}$, and two input sequences $\mathbf{X} \in \mathbb{R}^{n \times x}$ and $\mathbf{X}' \in \mathbb{R}^{m \times x'}$, we have

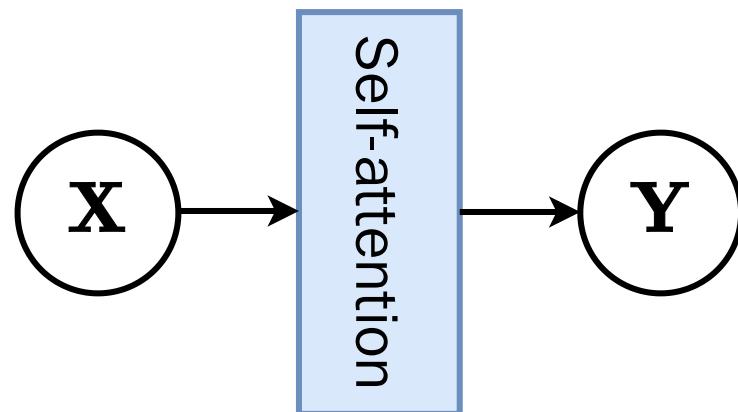
$$\begin{aligned}\mathbf{Q} &= \mathbf{X} \mathbf{W}_q^T \in \mathbb{R}^{n \times d} \\ \mathbf{K} &= \mathbf{X}' \mathbf{W}_k^T \in \mathbb{R}^{m \times d} \\ \mathbf{V} &= \mathbf{X}' \mathbf{W}_v^T \in \mathbb{R}^{m \times v}.\end{aligned}$$

Self-attention

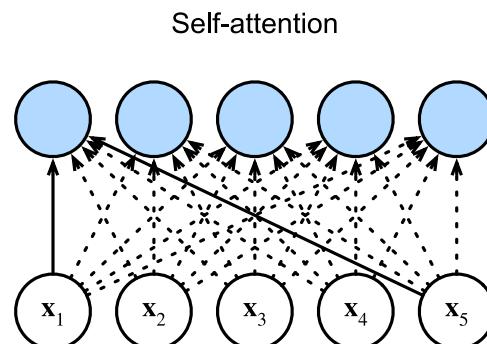
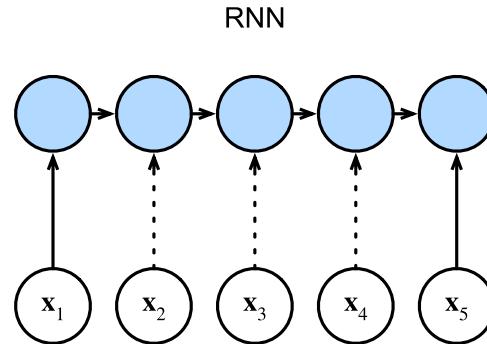
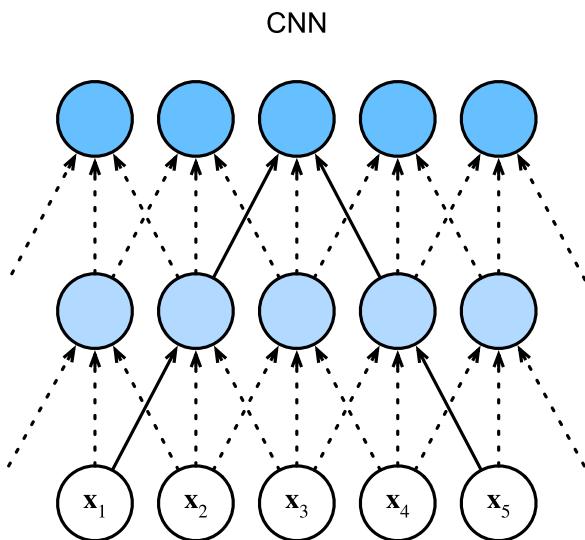
When the queries, keys and values are derived from the same inputs, the attention mechanism is called **self-attention**.

For the scaled dot-product attention, the self-attention layer is obtained when $\mathbf{X} = \mathbf{X}'$.

Therefore, self-attention can be used as a regular feedforward-kind of layer, similarly to fully-connected or convolutional layers.



CNNs vs. RNNs vs. self-attention

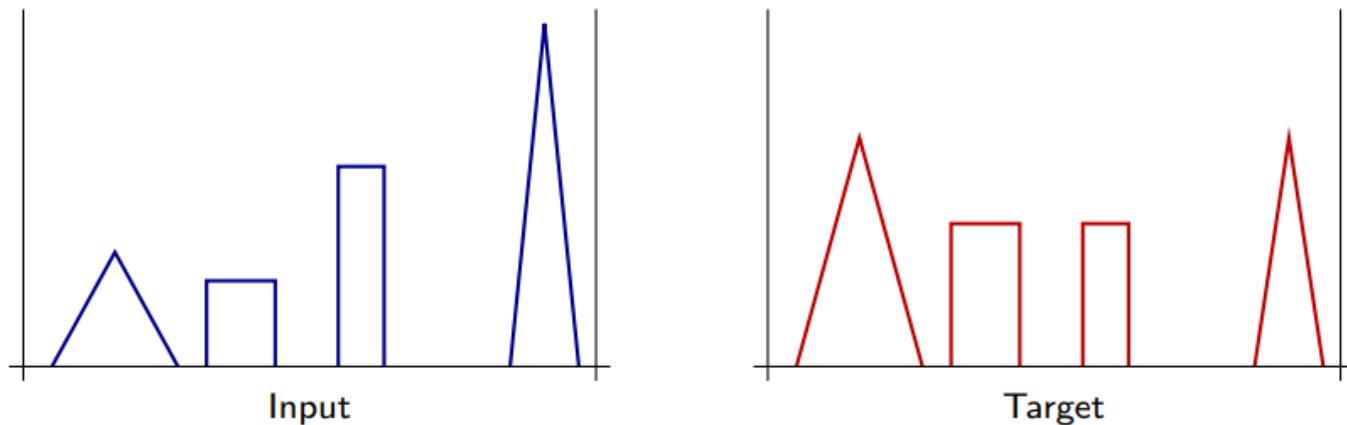


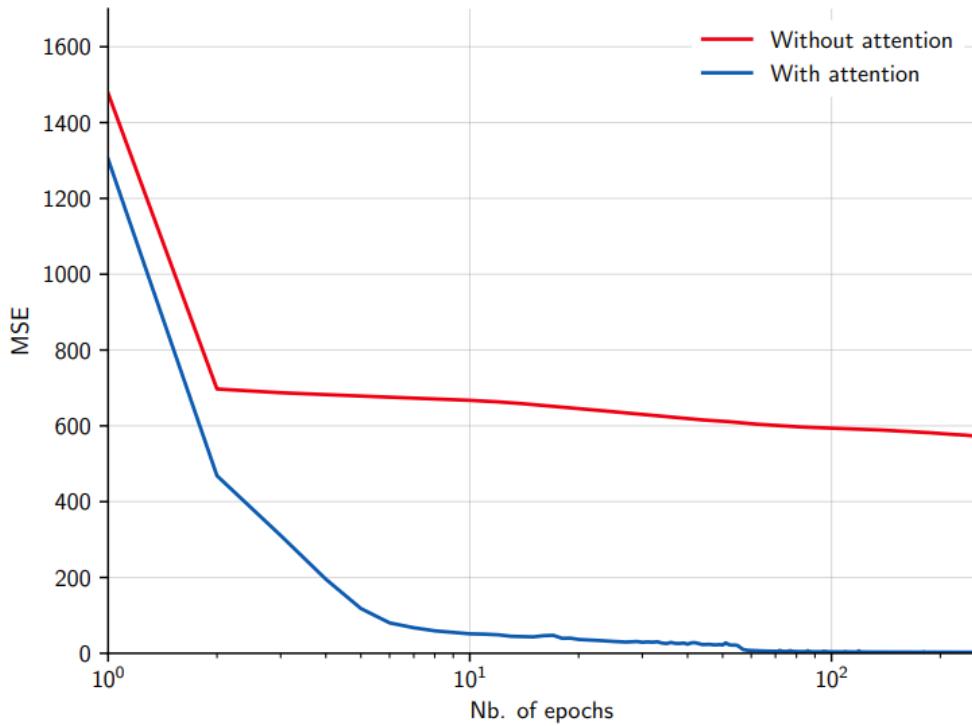
Layer Type	Complexity per Layer	Sequential Operations	Maximum Path Length
Self-Attention	$O(n^2 \cdot d)$	$O(1)$	$O(1)$
Recurrent	$O(n \cdot d^2)$	$O(n)$	$O(n)$
Convolutional	$O(k \cdot n \cdot d^2)$	$O(1)$	$O(\log_k(n))$

where n is the sequence length, d is the embedding dimension, and k is the kernel size of convolutions.

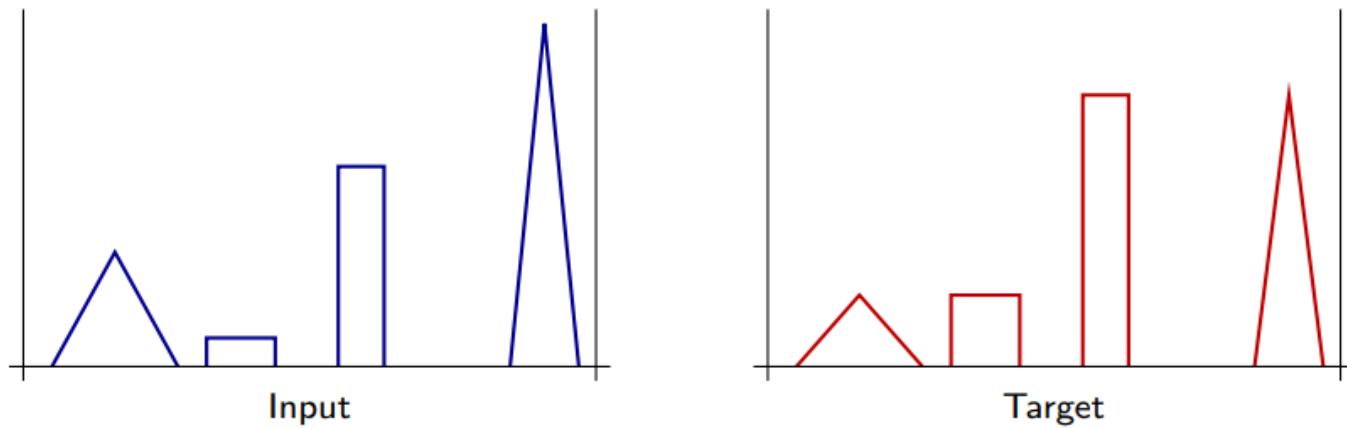
A toy example

To illustrate the behavior of the attention mechanism, we consider a toy problem with 1D sequences composed of two triangular and two rectangular patterns. The target sequence averages the heights in each pair of shapes.





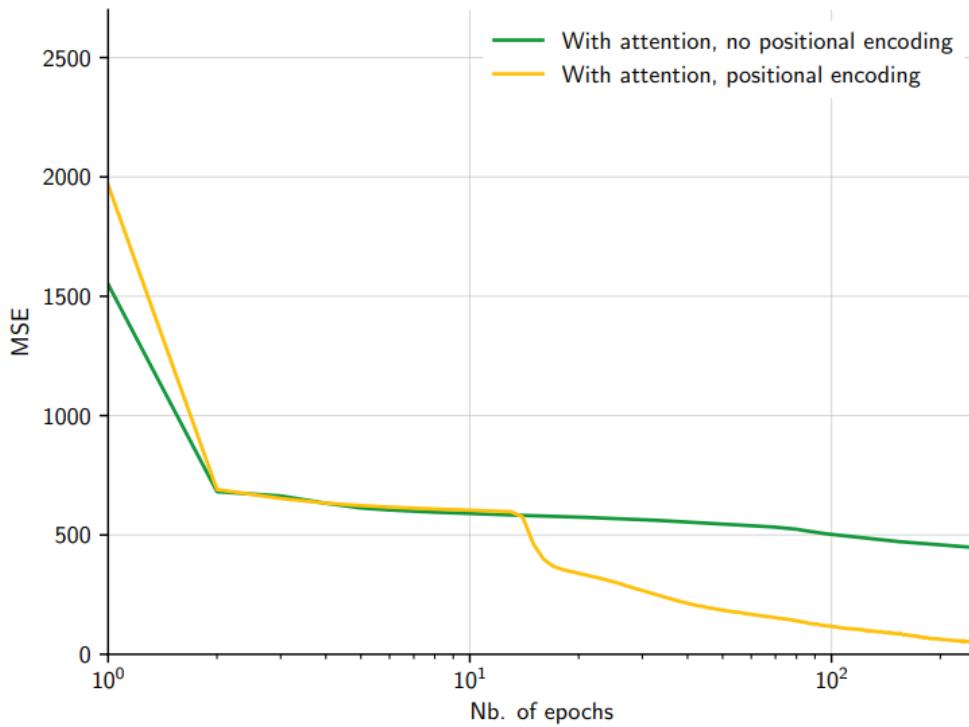
We can modify the toy problem to consider targets where the pairs to average are the two right and leftmost shapes.



The performance is expected to be poor given the inability of the self-attention layer to take into account absolute or relative positions. Indeed, self-attention is permutation-invariant:

$$\begin{aligned}\mathbf{y} &= \sum_{i=1}^m \text{softmax}_i \left(\frac{\mathbf{q}^T \mathbf{K}_i^T}{\sqrt{d}} \right) \mathbf{V}_i \\ &= \sum_{i=1}^m \text{softmax}_i \left(\frac{\mathbf{q}^T \mathbf{K}_{\sigma(i)}^T}{\sqrt{d}} \right) \mathbf{V}_{\sigma(i)}\end{aligned}$$

for any permutation σ of the key-value pairs.



However, this problem can be fixed by providing positional encodings explicitly to the attention layer.

Transformers

Vaswani et al. (2017) proposed to go one step further: instead of using attention mechanisms as a supplement to standard convolutional and recurrent layers, they designed a model, the **transformer**, combining only attention layers.

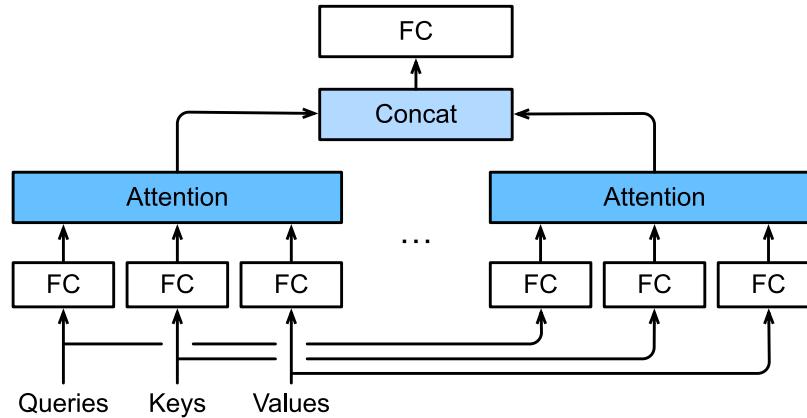
The transformer was designed for a sequence-to-sequence translation task, but it is currently key to state-of-the-art approaches across NLP tasks.

Scaled dot-product attention

The first building block of the transformer architecture is a scaled dot-product attention module

$$\text{attention}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{softmax} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}} \right) \mathbf{V}$$

where the $1/\sqrt{d_k}$ scaling is used to keep the (softmax's) temperature constant across different choices of the query/key dimension d_k .



Multi-head attention

The transformer projects the queries, keys and values $h = 8$ times with distinct linear projections to $d_k = 64$, $d_k = 64$ and $d_v = 64$ dimensions respectively.

$$\text{multihead}(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = \text{concat} (\mathbf{H}_1, \dots, \mathbf{H}_h) \mathbf{W}^O$$

$$\mathbf{H}_i = \text{attention}(\mathbf{Q}\mathbf{W}_i^Q, \mathbf{K}\mathbf{W}_i^K, \mathbf{V}\mathbf{W}_i^V)$$

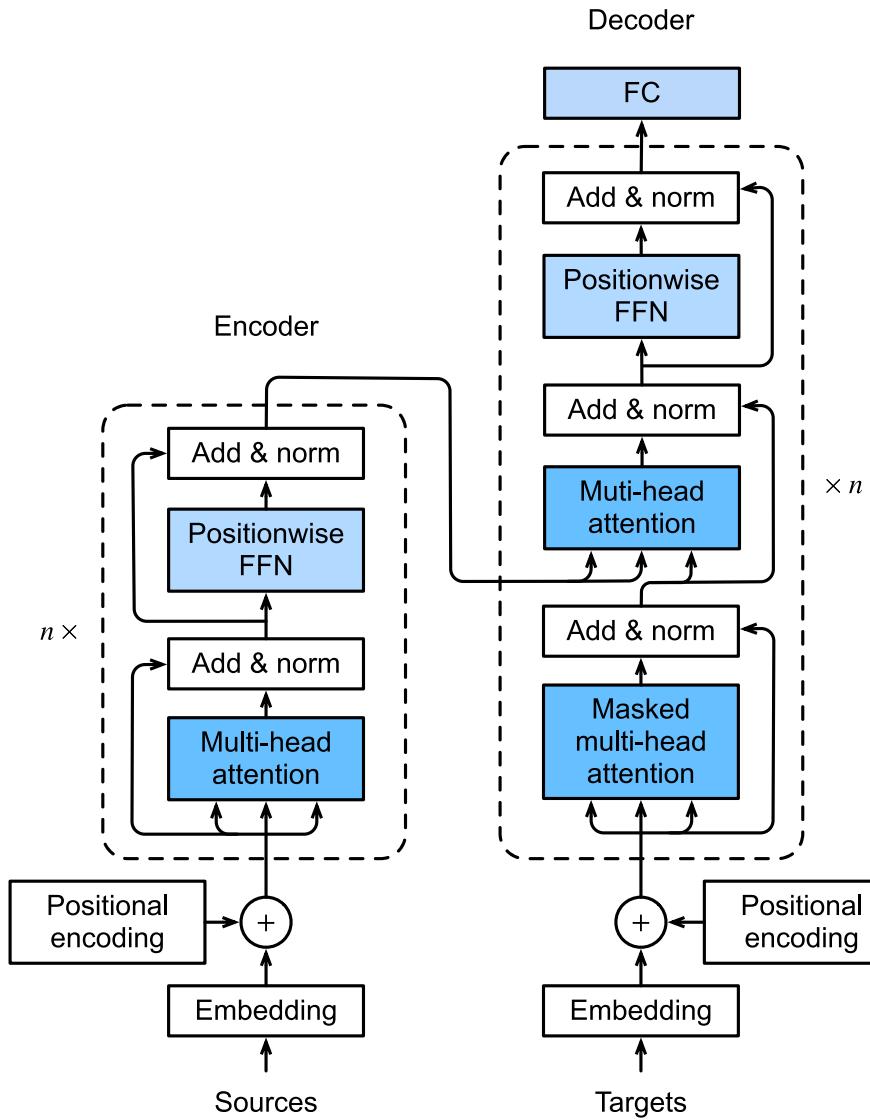
with

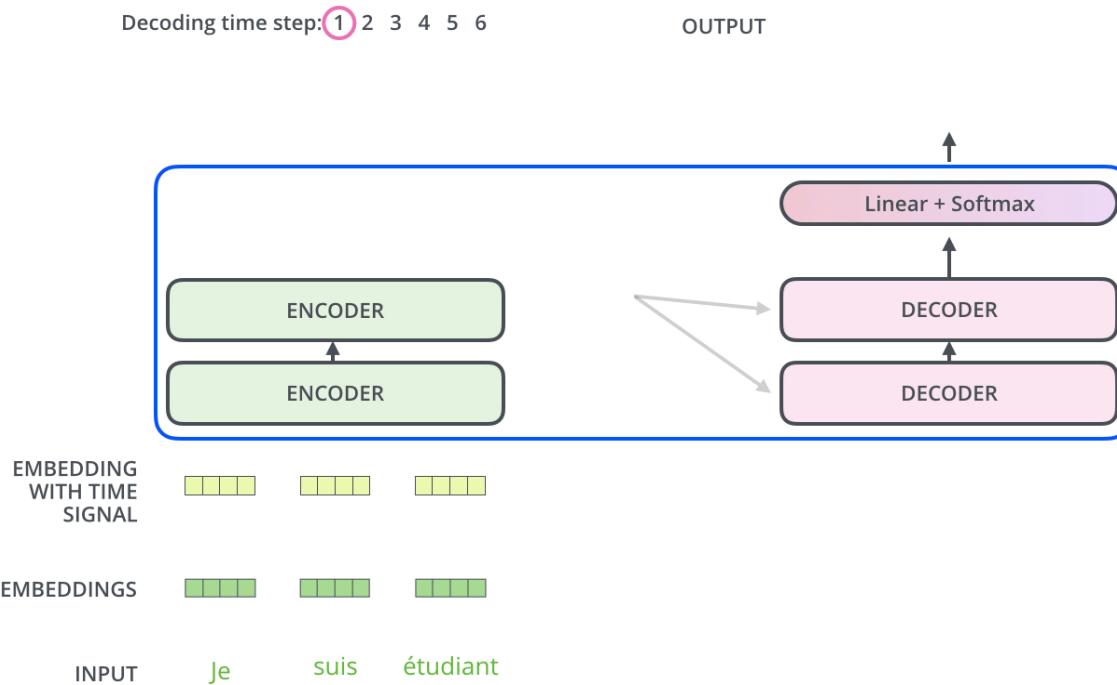
$$\mathbf{W}_i^Q \in \mathbb{R}^{d_{\text{model}} \times d_k}, \mathbf{W}_i^K \in \mathbb{R}^{d_{\text{model}} \times d_k}, \mathbf{W}_i^V \in \mathbb{R}^{d_{\text{model}} \times d_v}, \mathbf{W}_i^O \in \mathbb{R}^{hd_v \times d_{\text{model}}}$$

Encoder-decoder architecture

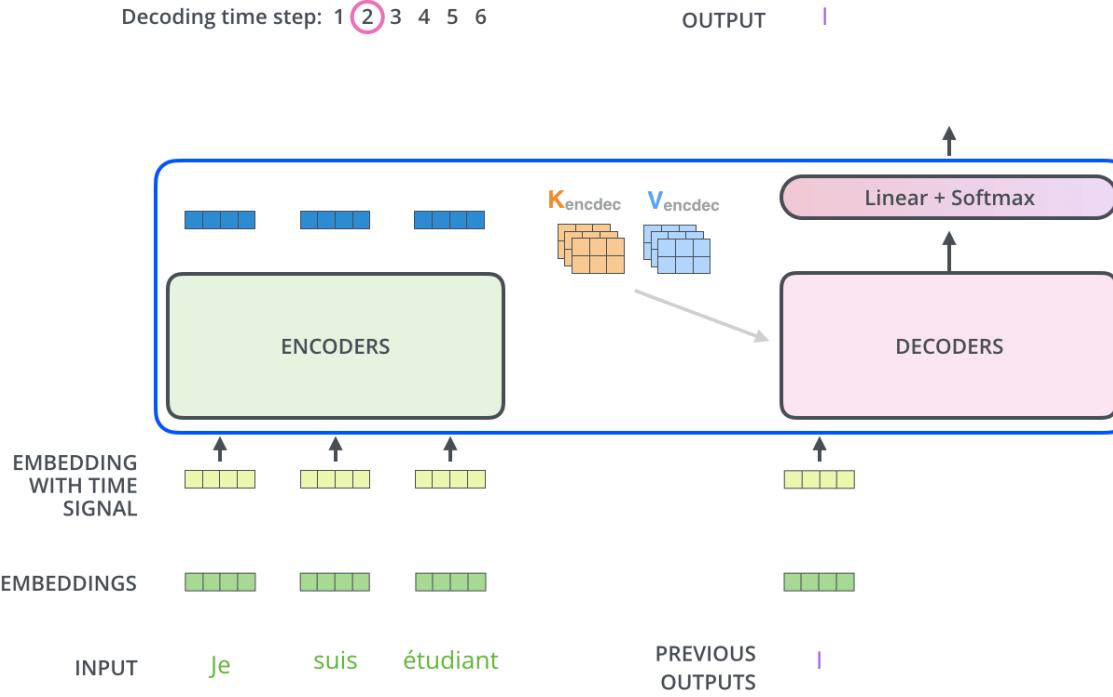
The transformer model is composed of:

- An encoder that combines $N = 6$ modules, each composed of a multi-head attention sub-module, and a (per-component) one-hidden-layer MLP, with residual pass-through and layer normalization. All sub-modules and embedding layers produce outputs of dimension $d_{\text{model}} = 512$.
- A decoder that combines $N = 6$ modules similar to the encoder, but using masked self-attention to prevent positions from attending to subsequent positions. In addition, the decoder inserts a third sub-module which performs multi-head attention over the output of the encoder stack.





The encoders start by processing the input sequence. The output of the top encoder is then transformed into a set of attention vectors **K** and **V** that will help the decoders focus on appropriate places in the input sequence.



Each step in the decoding phase produces an output token, until a special symbol is reached indicating the transformer decoder has completed its output.

The output of each step is fed to the bottom decoder in the next time step, and the decoders bubble up their decoding results just like the encoders did.

In the decoder:

- The first masked self-attention sub-module is only allowed to attend to earlier positions in the output sequence. This is done by masking future positions.
- The second multi-head attention sub-module works just like multi-head self-attention, except it creates its query matrix from the layer below it, and takes the keys and values matrices from the output of the encoder stack.

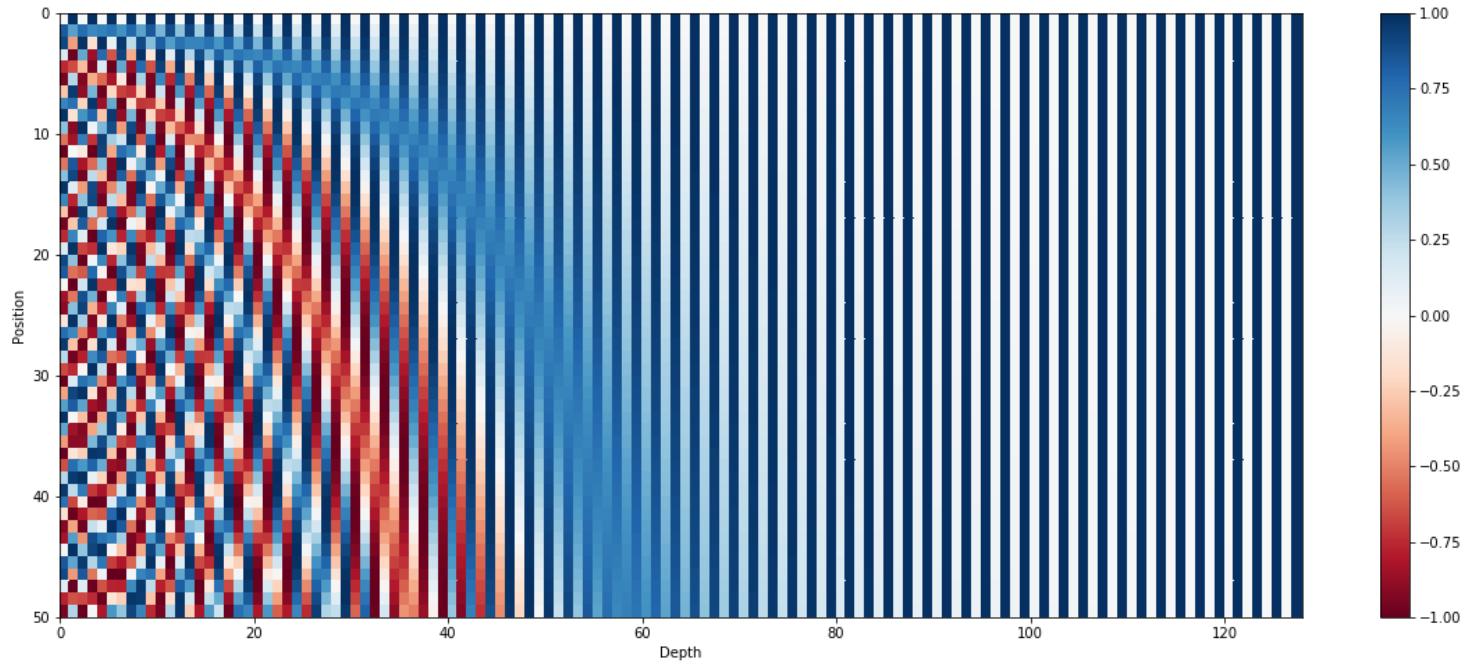
Positional encoding

As each word in a sentence *simultaneously* flows through the encoder/decoder stack, the model itself does not have any sense of position/order for each word.

Positional information is provided through an **additive** positional encoding of the same dimension d_{model} as the internal representation and is of the form

$$\begin{aligned}\text{PE}_{t,2i} &= \sin\left(\frac{t}{10000^{\frac{2i}{d_{\text{model}}}}}\right) \\ \text{PE}_{t,2i+1} &= \cos\left(\frac{t}{10000^{\frac{2i}{d_{\text{model}}}}}\right).\end{aligned}$$

After adding the positional encoding, words will be closer to each other based on the similarity of their meaning and their relative position in the sentence, in the d_{model} -dimensional space.

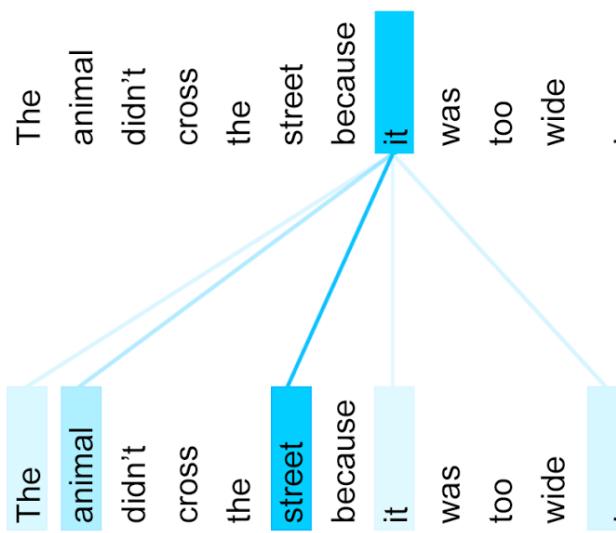
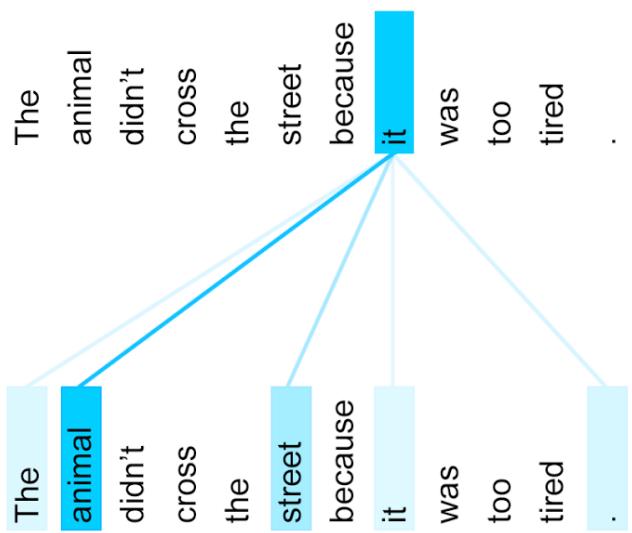


128-dimensional positonal encoding for a sentence with the maximum lenght of 50. Each row represents the embedding vector.

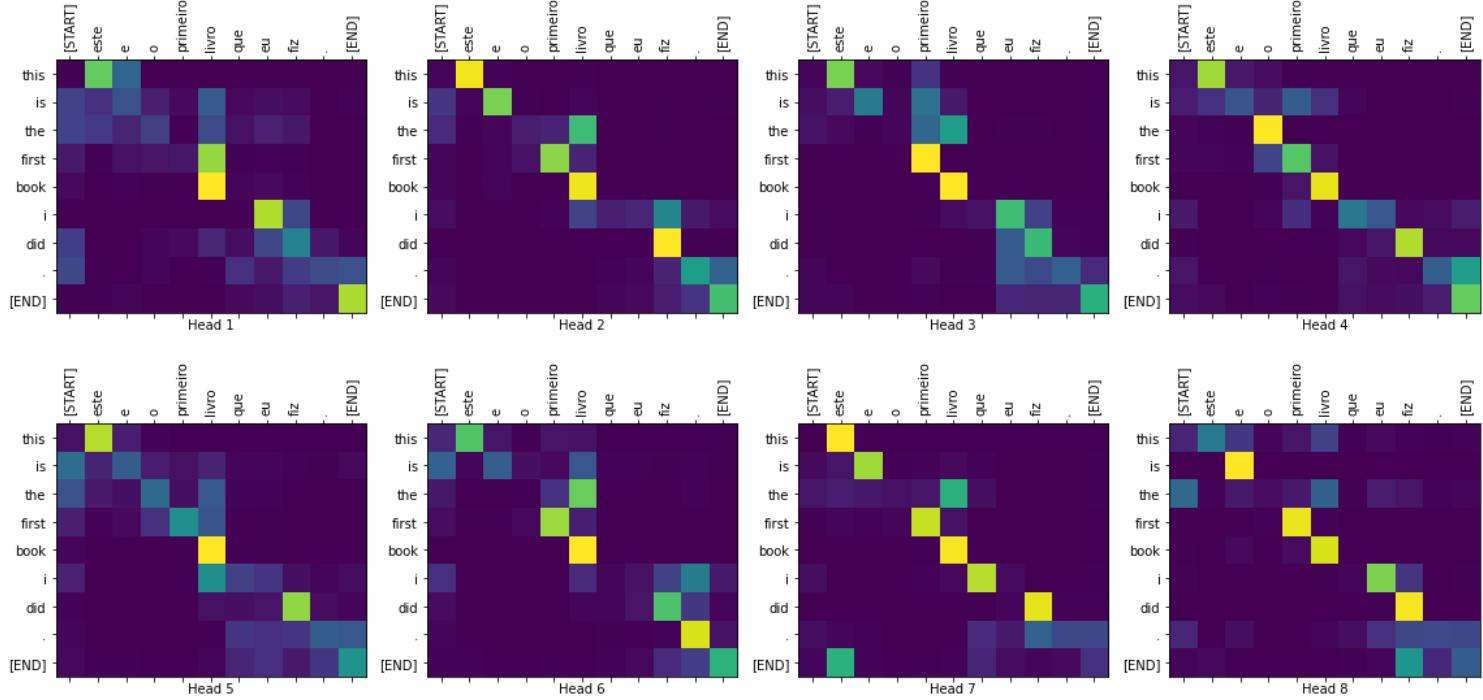
Machine translation

The transformer architecture was first designed for machine translation and tested on English-to-German and English-to-French translation tasks.

- English-to-German: 4.5M sentence pairs, 37k tokens vocabulary.
- English-to-French: 36M sentence pairs, 32k tokens vocabulary.
- 8 P100 GPUs (150 TFlops, FP16), 0.5 day for the small model, 3.5 days for the large one.



Self-attention layers learned that "it" could refer to different entities, in different contexts.

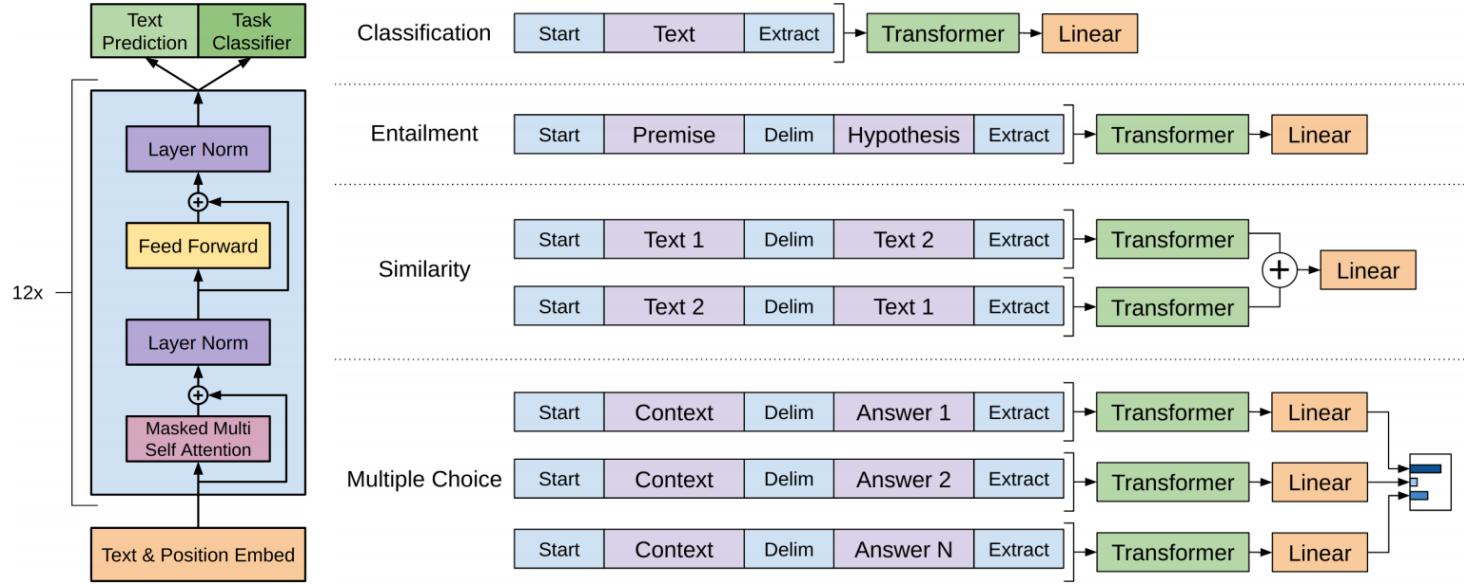


Attention maps extracted from the multi-head attention modules
show how input tokens relate to output tokens.

Language pre-training

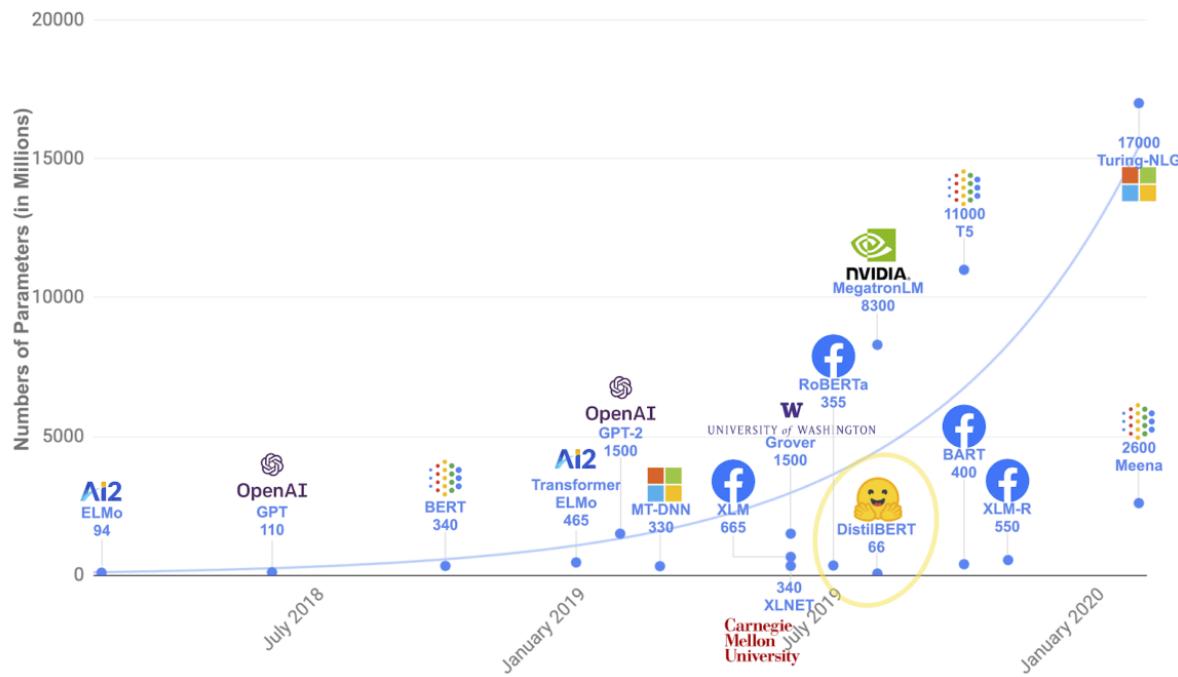
Similar to pre-training computer vision models on ImageNet, language models can be pre-trained for tasks in natural language processing.

Notably, the models can be pre-trained in a **unsupervised manner** from very large datasets and then fine-tuned on supervised tasks with small data-sets.



GPT, Radford et al. (2018)

Increasing the training data and the model size leads to significant improvement of transformer language models. These models are now **the largest in deep learning**.



Applications

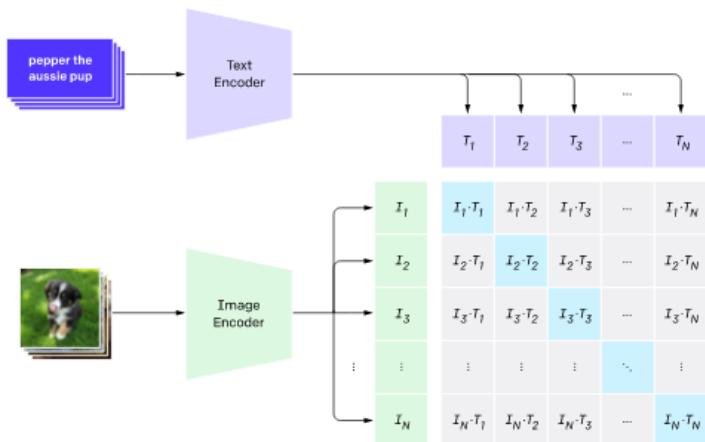
ChatGPT

 Examples	 Capabilities	 Limitations
"Explain quantum computing in simple terms" →	Remembers what user said earlier in the conversation	May occasionally generate incorrect information
"Got any creative ideas for a 10 year old's birthday?" →	Allows user to provide follow-up corrections	May occasionally produce harmful instructions or biased content
"How do I make an HTTP request in Javascript?" →	Trained to decline inappropriate requests	Limited knowledge of world and events after 2021

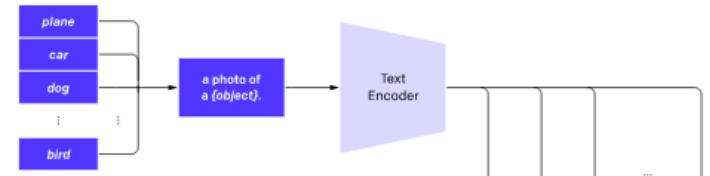
ChatGPT Feb 13 Version. Free Research Preview. Our goal is to make AI systems more natural and safe to interact with. Your feedback will help us improve.

ChatGPT generates text samples in response to arbitrary inputs.

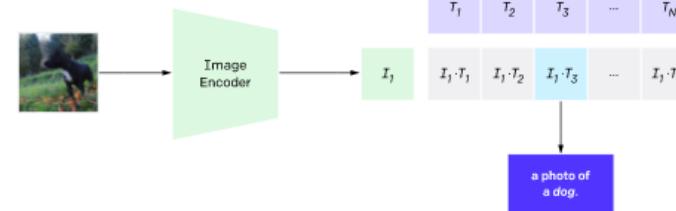
1. Contrastive pre-training



2. Create dataset classifier from label text



3. Use for zero-shot prediction



CLIP: connecting text and images for zero-shot classification (see [demo](#)).



Vision transformers (ViTs)

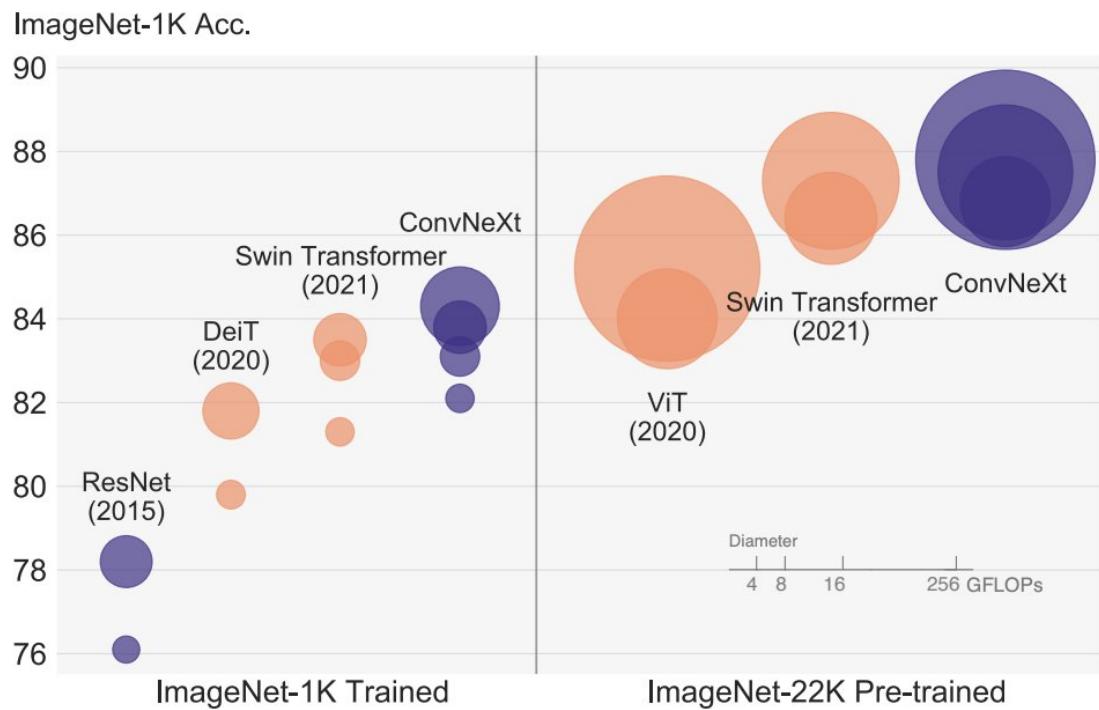
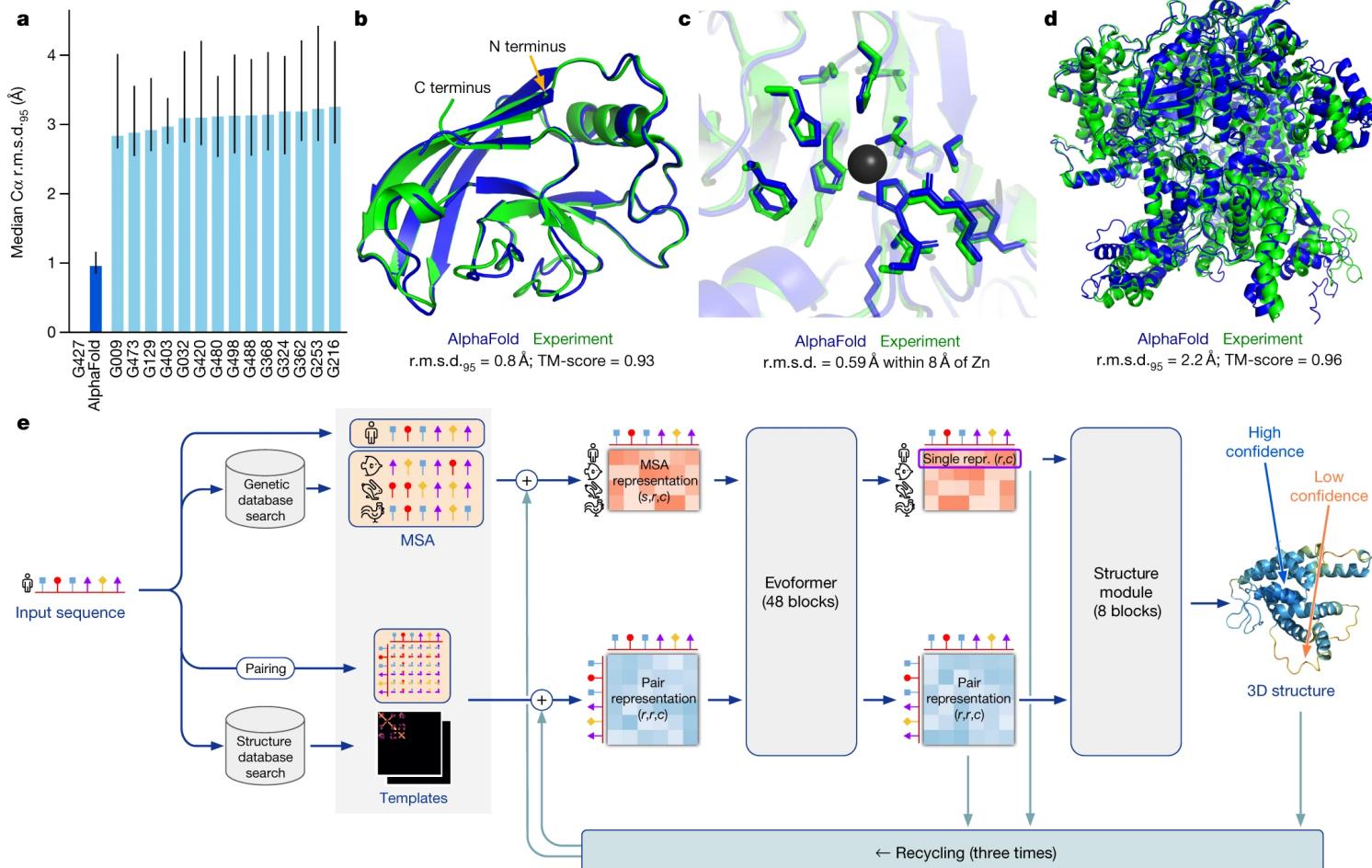


Figure 1. ImageNet-1K classification results for ● ConvNets and ○ vision Transformers. Each bubble's area is proportional to FLOPs of a variant in a model family. ImageNet-1K/22K models here take $224^2/384^2$ images respectively. We demonstrate that a standard ConvNet model can achieve the same level of scalability as hierarchical vision Transformers while being much simpler in design.



AlphaFold: Highly accurate protein structure prediction.

• • • \hat{R}_{t-1}

Decision Transformer: Reinforcement Learning via Sequence Modeling.

The end.