corrfitter Documentation

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G.P. Lepage

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CORREITTER - LEAST-SQUARES FIT TO CORRELATORS

1.1 Introduction

This module contains tools that facilitate least-squares fits, as functions of time t, of simulation (or other statistical) data for 2-point and 3-point correlators of the form

```
Gab(t) = \langle b(t) \ a(0) \rangle
Gavb(t,T) = \langle b(T) \ V(t) \ a(0) \rangle
```

Each correlator is modeled using corrfitter.Corr2 for 2-point correlators, or corrfitter.Corr3 for 3-point correlators in terms of amplitudes for each source a, sink b, and vertex V, and the energies associated with each intermediate state. The amplitudes and energies are adjusted in the least-squares fit to reproduce the data; they are specified in a shared prior (typically a dictionary).

An object of type corrfitter. CorrFitter describes a collection of correlators and is used to fit multiple models to data simultaneously. Any number of correlators may be described and fit by a single corrfitter. CorrFitter object. corrfitter. CorrFitter objects can also be used to to extract the appropriate fit data from gdev. Dataset objects.

1.2 Basic Fits

To illustrate, consider data for two 2-point correlators: Gaa with the same source and sink (a), and Gab which has source a and (different) sink b. The data are contained in a dictionary data, where data['Gaa'] and data['Gab'] are one-dimensional arrays containing values for Gaa(t) and Gab(t), respectively, with t=0,1,2...63. Each array element in data['Gaa'] and data['Gab'] is a gaussian deviate of type gdev.GDev, and specifies the mean and standard deviation for the corresponding data point:

```
>> print data['Gaa']
[0.159791 +- 4.13311e-06 0.0542088 +- 3.06973e-06 ...]
>> print data['Gab']
[0.156145 +- 1.83572e-05 0.102335 +- 1.5199e-05 ...]
```

gdev. GDevs can also capture any statistical correlations between different pieces of data.

We want to fit this data to the following formulas:

```
Gaa(t,N) = sum_i=0..N-1 a[i]**2 * exp(-E[i]*t)

Gab(t,N) = sum_i=0..N-1 a[i]*b[i] * exp(-E[i]*t)
```

Our goal is to find values for the amplitudes, a[i] and b[i], and the energies, E[i], so that these formulas reproduce the average values for Gaa(t, N) and Gab(t, N) that come from the data, to within the data's statistical errors. We use the same a[i]s and E[i]s in both formulas. The fit parameters used by the fitter are the a[i]s and b[i]s, as well as the differences dE[i]=E[i]-E[i-1] for i>0 and dE[0]=E[0]. The energy differences are usually positive by construction (see below) and are easily converted back to energies using:

```
E[i] = sum_j=0..i dE[j]
```

A typical code has the following structure:

from corrfitter import CorrFitter

```
data = make_data('mcfile')  # user-supplied routine
models = make_models()  # user-supplied routine
N = 4  # number of terms in fit functions
prior = make_prior(N)  # user-supplied routine
fitter = CorrFitter(models=models)
fit = fitter.lsqfit(data=data,prior=prior)  # do the fit
print_results(fit,prior,data)  # user-supplied routine
```

We discuss each user-supplied routine in turn.

1.2.1 make_data('mcfile')

make_data('mcfile') creates the dictionary containing the data that is to be fit. Typically such data comes from a Monte Carlo simulation. Imagine that the simulation creates a file called 'mcfile' with layout

```
# first correlator: Gaa(t) for t=0,1,2...63
Gaa    0.159774739530e+00    0.541793561501e-01    ...
Gaa    0.159751906801e+00    0.542054488624e-01    ...
Gaa    ...

.

# second correlator: Gab(t)
Gab    0.155764170032e+00    0.102268808986e+00    ...
Gab    0.156248435021e+00    0.102341455176e+00    ...
Gab    ...
.
```

where each line is one Monte Carlo measurement for one or the other correlator, as indicated by the tags at the start of each line. (Lines for Gab may be interspersed with lines for Gaa since every line has a tag.) The data can be analyzed using class gvar.Dataset:

```
import gvar

def make_data(filename):
    return gvar.avg_data(gvar.Dataset(filename))
```

Then data = make_data('mcfile') creates a dictionary where, as discussed above, data['Gaa'] is an array of gdev.GDevs obtained by averaging over the Gaa data in the 'mcfile', and data['Gab'] is a similar array for the Gab correlator.

1.2.2 make models()

make_models () identifies which correlators in the fit data are to be fit, and specifies theoretical models (that is, fit functions) for these correlators:

For each correlator, we specify: the tag used in the input data dictionary data for that correlator (datatag); the values of t for which results are given in the input data (tdata); the values of t to keep for fits (tfit, here the same as the range in the input data, but could be any subset); and fit-parameter labels for the source (a) and sink (b) amplitudes, and for the intermediate energy-differences (dE). The fit-parameter labels are connected with the actual fit parameters in the prior (they are the dictionary keys), as discussed below. Here the two models, for Gaa and Gab, are identical except for the data tags and the sinks. make_models() returns a list of models; the only parts of the input fit data that are fit are those for which a model is specified in make_models().

Note that if there is data for Gba(t, N) in addition to Gab(t, N), and Gba = Gab, then the (weighted) average of the two data sets will be fit if models[1] is replace by:

```
Corr2(datatag='Gab',tdata=range(64),tfit=range(64),
    a=('a',None),b=('b',None),dE=('dE',None),
    othertags=['Gba'])
```

The additional argument othertags lists other data tags that correspond to the same physical quantity; the data for all equivalent data tags is averaged before fitting (using lsqfit.wavg()). Alternatively (and equivalently) one could add a third Corr2 to models for Gba, but it is more efficient to combine it with Gab in this way if they are equivalent.

1.2.3 make_prior(N)

This routine defines the fit parameters that correspond to each fit-parameter label used in make_models() above. It also assigns *a priori* values to each parameter, expressed in terms of gaussian deviates (gdev.GDevs), with a mean and standard deviation. The prior is built using class gvar.BufferDict:

```
import lsqfit
import gvar

def make_prior(N):
    prior = gvar.BufferDict()  # prior = {} works too
    prior['a'] = [gvar.gvar(0.1,0.5) for i in range(N)]
    prior['b'] = [gvar.gvar(1.,5.) for i in range(N)]
    prior['dE'] = [gvar.gvar(0.25,0.25) for i in range(N)]
    return prior
```

(gvar.BufferDict can be replaced by an ordinary Python dictionary; it is used here because it remembers the order in which the keys are added.) make_prior(N) associates arrays of N gaussian deviates (gdev.GDevs) with each fit-parameter label, enough for N terms in the fit function. These are the *a priori* values for the fit parameters, and they can be retrieved using the label: setting prior=make_prior(N), for example, implies that prior['a'][i], prior['b'][i] and prior['de'][i] are the *a priori* values for a[i], b[i] and dE[i]

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in the fit functions (see above). The *a priori* value for each a [i] here is set to 0.1+-0.5, while that for each b [i] is 1+-5:

```
>>> print prior['a']
[0.1 +- 0.5 0.1 +- 0.5 0.1 +- 0.5]
>>> print prior['b']
[1 +- 5 1 +- 5 1 +- 5 1 +- 5]
```

Similarly the *a priori* value for each energy difference is 0.25+-0.25. (See the lsqfit documentation for further information on priors.)

The priors assign an *a priori* gaussian or normal distribution to each parameter. It is possible instead to assign a lognormal distribution, which forces the parameter to be positive. This is done by choosing a label that begins with "log": for example, 'logde' instead of 'de'. The fitter implements the log-normal distribution by using the parameter's logarithm, instead of the parameter itself, as a new fit parameter; the logarithm has a gaussian/normal distribution. The original parameter is recovered by taking the exponential of the new fit parameter.

Using log-normal distributions where possible can significantly improve the stability of a fit. This is because otherwise the fit functions typically have many symmetries that lead to large numbers of equivalent but different best fits. For example, the fit functions Gaa(t,N) and Gab(t,N) above are unchanged by exchanging a[i],b[i] and E[i] with a[j],b[j] and E[j] for any i and j. We can remove this degeneracy by using a log-normal distribution for the dE[i]s since this guarantees that all dE[i]s are positive, and therefore that E[0],E[1],E[2]... are ordered (in decreasing order of importance to the fit).

Another symmetry of Gaa and Gab, which leaves both fit functions unchanged, is replacing a[i], b[i] by -a[i], -b[i]. Yet another is to add a new term to the fit functions with a[k], b[k], dE[k] where a[k]=0 and the other two have arbitrary values. Both of these symmetries can be removed by using a log-normal distribution for the a[i] priors, thereby forcing all a[i]>0.

The log-normal distributions for the a[i] and dE[i] are introduced into the code example by changing the corresponding labels in make_models() and make_prior(N), and taking logarithms of the corresponding prior values:

```
from gvar import log
                                             # numpy.log() works too
def make_models():
    models = [ Corr2(datatag='Gaa',tdata=range(64),tfit=range(64),
                    a='loga', b='loga', dE='logdE'),
               Corr2 (datatag='Gab', tdata=range(64), tfit=range(64),
                    a='loga',b='b',dE='logdE')
             ]
    return models
def make_prior(N):
                                             # prior = {} works too
    prior = gvar.BufferDict()
    prior['loga'] = [log(gvar.gvar(0.3,0.3)) for i in range(N)]
    prior['b'] = [gvar.gvar(1.,5.) for i in range(N)]
    prior['logdE'] = [log(gvar.gvar(0.25, 0.25))  for i in range(N)]
    return prior
```

This replaces the original fit parameters, a[i] and dE[i], by new fit parameters, log(a[i]) and log(dE[i]). The *a priori* distributions for the logarithms are gaussian/normal, with priors of log(0.3+-0.3) and $log(0.25_++0.25)$ for the log(a) s and log(dE) s respectively.

1.2.4 print_results(fit, prior, data)

The actual fit is done by fit=fitter.lsqfit(...), and the results of the fit reported by print_results(fit,prior,data): for example,

```
def print_results(fit, prior, data):
   print fit.format()
                                                 # summary of fit info
   a = fit.p['a']
                                                 # array of a[i]s
   b = fit.p['b']
                                                 # array of b[i]s
   dE = fit.p['dE']
                                                 # array of dE[i]s
   E = [sum(dE[:i+1]) for i in range(len(dE))] # array of E[i]s
    print 'Best fit values:
    print '
               a[0] =', a[0]
    print '
                b[0] =', b[0]
    print '
               E[0] = ', E[0]
    print 'b[0]/a[0] = ',b[0]/a[0]
    outputs = {'E0':E[0],'a0':a[0],'b0':b[0],'b0/a0':b[0]/a[0]}
    inputs = {'a'=prior['a'],'b'=prior['b'],'dE'=prior['dE'],
              'data' = [data[k] for k in data])
    print fit.fmt_errorbudget(outputs,inputs)
```

The best-fit values from the fit are contained in fit.p and are accessed using the labels defined in the prior and the corrfitter.Corr2 models. Variables like a [0] and E [0] are gdev.GDev objects that contain means and standard deviations, as well as information about any correlations that might exist between different variables (which is relevant for computing functions of the parameters, like b[0]/a[0] in this example).

The last line of print_results (fit, prior, data) prints an error budget for each of the best-fit results for a [0], b [0], E [0] and b [0]/a [0], which are identified in the print output by the labels 'a0', 'b0', 'E0' and 'b0/a0', respectively. The error for any fit result comes from uncertainties in the inputs — in particular, from the fit data and the priors. The error budget breaks the total error for a result down into the components coming from each source. Here the sources are the *a priori* errors in the priors for the 'a' amplitudes, the 'b' amplitudes, and the 'dE' energy differences, as well as the errors in the fit data data. These sources are labeled in the print output by 'a', 'b', 'dE', and 'data', respectively. (See the lsqfit documentation for further details on partial standard deviations and fit.fmt_errorbudget().)

Note that only three lines in print_results (fit, prior, data) would change if we had used log-normal priors for a and dE, as discussed in the previous section:

Plots of the fit data divided by the fit function, for each correlator, are displayed by calling fitter.display_plots() provided the matplotlib module is present.

1.3 Faster Fits

Good fits often require fit functions with several exponentials and many parameters. Such fits can be costly. One strategy that can speed things up is to use fits with fewer terms to generate estimates for the most important parameters. These estimates are then used as starting values for the full fit. The smaller fit is usually faster, because it has fewer

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parameters, but the fit is not adequate (because there are too few parameters). Fitting the full fit function is usually faster given reasonable starting estimates, from the smaller fit, for the most important parameters. Continuing with the example from the previous section, the code

```
data = make_data('mcfile')
fitter = CorrFitter(models=make_models())
p0 = None
for N in [1,2,3,4,5,6,7,8]:
    prior = make_prior(N)
    fit = fitter.lsqfit(data=data,prior=prior,p0=p0)
    print_results(fit,prior,data)
    p0 = fit.pmean
```

does fits using fit functions with N=1...8 terms. Parameter mean-values fit.pmean from the fit with N exponentials are used as starting values p0 for the fit with N+1 exponentials, hopefully reducing the time required to find the best fit for N+1.

Often we care only about parameters in the leading term of the fit function, or just a few of the leading terms. The non-leading terms are needed for a good fit, but we are uninterested in the values of their parameters. In such cases the non-leading terms can be absorbed into the fit data, leaving behind only the leading terms to be fit (to the modified fit data) — non-leading parameters are, in effect, integrated out of the analysis, or *marginalized*. The errors in the modified data are adjusted to account for uncertainties in the marginalized terms, as specified by their priors. The resulting fit function has many fewer parameters, and so the fit can be much faster.

Continuing with the example above, imagine that Nmax=8 terms are needed to get a good fit, but we only care about parameter values for the first couple of terms. The code above can be rearranged to fit only the leading N terms where N<Nmax, while incorporating the remaining, non-leading terms as corrections to the data:

```
Nmax = 8
data = make_data('mcfile')
prior = make_prior(Nmax)  # build priors for Nmax terms
models = make_models()
p0 = None
for N in [1,2,3]:
    fitter = CorrFitter(models=models,nterm=N)  # fit only N terms
    fit = fitter.lsqfit(data=data,prior=prior,p0=p0)
    print_results(fit,prior,data)
    p0 = fit.pmean
```

Here the nterm parameter in corrfitter.CorrFitter specifies how many terms are used in the fit functions. The prior specifies Nmax terms in all, but only parameters in nterm=N terms are varied in the fit. The remaining terms specified by the prior are automatically incorporated into the fit data by corrfitter.CorrFitter.

Remarkably this method is usually as accurate with N=1 or 2 as a full Nmax-term fit with the original fit data; but it is much faster. If this is not the case, check for singular priors, where the mean is much smaller than the standard deviation. These can lead to singularities in the covariance matrix for the corrected fit data. Such priors are easily fixed: for example, use gvar.gvar(0.1,1.) rather than gvar.gvar(0.0,1.) or gvar.gvar(0.001,1.). In some situations an svd cut (see below) can also help.

1.4 Variations

Any 2-point correlator can be turned into a periodic function of t by specifying the period through parameter tp. Doing so causes the replacement

```
\exp(-E[i]*t) -> \exp(-E[i]*t) + \exp(-E[i]*(tp-t))
```

in the fit function.

Also (or alternatively) oscillating terms can be added to the fit by modifying parameter s and by specifying sources, sinks and energies for the oscillating pieces. For example, one might want to replace the sum of exponentials with two sums

```
sum_i a[i] **2 * exp(-E[i] *t) - sum_i ao[i] **2 (-1) **t * exp(-Eo[i] *t)
```

in a (nonperiodic) fit function. Then an appropriate model would be, for example,

where ao and dEo refer to additional fit parameters describing the oscillating component. In general parameters for amplitudes and energies can be tuples with two components: the first describing normal states, and the second describing oscillating states. To omit one or the other, put None in place of a label. Parameter s[0] is an overall factor multiplying the non-oscillating terms, and s[1] is the corresponding factor for the oscillating terms.

An *svd* cut can be applied to the covariance matrix for the data by specifying parameters svdcut and/or svdnum. (See documentation for lsqfit; it is useful to set svdnum equal to the number of measurements used to determine the covariance matrix for G(t) since that is the largest number of eigenmodes possible in the covariance matrix.)

1.5 3-Point Correlators

Correlators $Gavb(t,T) = \langle b(T) \ V(t) \ a(0) \rangle$ can also be included in fits as functions of t. In the illustration above, for example, we might consider additional Monte Carlo data describing a form factor with the same intermediate states before and after V(t). Assuming the data is tagged by aVbT15 and describes T=15, the corresponding entry in the collection of models might then be:

```
Corr3(datatag="aVbT15",T=15,tdata=range(16),tfit=range(16),Vnn='Vnn',
    a='a',dEa='logdE',  # parameters for a->V
    b='b',dEb='logdE',  # parameters for V->b
    )
```

This models the Monte Carlo data for the 3-point function using the following formula:

```
sum_i, j a[i] * exp(-Ea[i]*t) * Vnn[i, j] * b[j] * exp(-Eb[j]*t)
```

where the Vnn[i,j]s are new fit parameters related to a->V->b form factors. Obviously multiple values of T can be studied by including multiple corrfitter.Corr3 models, one for each value of T. Either or both of the initial and final states can have oscillating components (include sa and/or sb), or can be periodic (include tpa and/or tpb). If there are oscillating states then additional Vs must be specified: Vno connecting a normal state to an oscillating state, Von connecting oscillating to normal states, and Voo connecting oscillating to oscillating states.

There are two cases that require special treatment. One is when simultaneous fits are made to a->V->b and b->V->a. Then the Vnn, Vno, *etc.* for b->V->a are the (matrix) transposes of the same matrices for a->V->b. In this case the models for the two would look something like:

```
),
```

The same Vs are specified for the second correlator, but setting transpose_V=True means that the transpose of each matrix is used in the fit for that correlator.

The second special case is for fits to a->v->a where source and sink are the same. In that case, Vnn and Voo are symmetric matrices, and Von is the transpose of Vno. The model for such a case would look like:

Here Vno and Von are set equal to the same matrix, but specifying $symmetric_V=True$ implies that the transpose will be used for Von. Furthermore Vnn and Voo are symmetric matrices when $symmetric_V==True$ and so only the upper part of each matrix is needed. In this case Vnn and Voo are treated as one-dimensional arrays with N(N+1)/2 elements corresponding to the upper parts of each matrix, where N is the number of exponentials (that is, the number of a [i]s).

1.6 Bootstrap Analyses

A *bootstrap analysis* gives more robust error estimates for fit parameters and functions of fit parameters than the conventional fit when errors are large, or fluctuations are non-gaussian. A typical code looks something like:

```
import quar as qu
from corrfitter import CorrFitter
# fit
dset = gv.Dataset('mcfile')
                             # create fit data
data = gv.avg_data(dset)
fitter = Corrfitter(models=make_models())
                                    # number of terms in fit function
prior = make_prior(N)
fit = fitter.lsqfit(prior=prior,data=data) # do standard fit
print 'Fit results:'
print 'a', exp(fit.p['loga']) # fit results for 'a' amplitudes
print 'dE', exp(fit.p['logdE']) # fit results for 'dE' energies
. . .
# bootstrap analysis
print 'Bootstrap fit results:'
nbootstrap = 10
                                   # number of bootstrap iterations
bs_datalist = (avg_data(d) for d in dset.bootstrap_iter(nbootstrap))
bs = qv.Dataset()
                                   # bootstrap output stored in bs
for bs_fit in fitter.bootstrap_iter(bs_datalist): # bs_fit = lsqfit output
    p = bs fit.pmean # best fit values for current bootstrap iteration
   bs.append('a',exp(p['loga'])) # collect bootstrap results for a[i]
   bs.append('dE',exp(p['logdE'])) # collect results for dE[i]
                                   # include other functions of p
bs = gv.avg_data(bs,bstrap=True) # medians + error estimate
print 'a',bs['a']
                                  # bootstrap result for 'a' amplitudes
print 'dE',bs['dE']
                                   # bootstrap result for 'dE' energies
```

This code first prints out the standard fit results for the 'a' amplitudes and 'dE' energies. It then makes 10 bootstrap copies of the original input data, and fits each using the best-fit parameters from the original fit as the starting point for the bootstrap fit. The variation in the best-fit parameters from fit to fit is an indication of the uncertainty in those parameters. This example uses a gvar. Dataset object bs to accumulate the results from each bootstrap fit, which are computed using the best-fit values of the parameters (ignoring their standard deviations). Other functions of the fit parameters could be included as well. At the end avg_data(bs,bstrap=True) finds median values for each quantity in bs, as well as a robust estimate of the uncertainty (to within 30% since nbootstrap is only 10).

The list of bootstrap data sets bs_datalist can be omitted in this example in situations where the input data has high statistics. Then the bootstrap copies are generated internally by fitter.bootstrap_iter() from the means and covariance matrix of the input data (assuming gaussian statistics).

1.7 New Models

Classes to describe new models are usually derived from corrfitter.BaseModel. These can be for fitting new types of correlators. They can also be used in other ways — for example, to add constraints. Imagine a situation where one wants to constrain the third energy (E2) in a fit to be 0.60(1). This can be accomplished by adding E2_Constraint() to the list of models in corrfitter.CorrFitter where:

```
import gvar
import corrfitter

class E2_Constraint(corrfitter.BaseModel):
    def __init__(self):
        super(E2_Constraint,self).__init__('E2-constraint') # data tag

def fitfcn(self,x,p):
    dE = gvar.exp(p['logdE'])
    return sum(dE[:3]) # E2 formula in terms of p

def _builddata(self,d):
    return gvar.gvar(0.6,0.01) # E2 value
```

Any number of constraints like this can be added to the list of models.

Note that this constraint could instead be built into the priors for logdE by introducing correlations between different parameters.

1.8 Implementation

corrfitter.CorrFitter allows models to specify how many exponentials to include in the fit function (using parameters nterm, nterma and ntermb). If that number is less than the number of exponentials specified by the prior, the extra terms are incorporated into the fit data before fitting. The default procedure is to multiply the data by $G(t,p,N)/G(t,p,\max(N,\max))$ where: G(p,t,N) is the fit function with N terms for parameters p and time t;N is the number of exponentials specified in the models; Nmax is the number of exponentials specified in the prior; and here parameters p are set equal to their values in the prior (correlated gdev.GDevs).

An alternative implementation for the data correction is to add G(t,p,N)-G(t,p,max(N,Nmax)) to the data. This implementation is selected when parameter ratio in corrfitter. CorrFitter is set to False. Results are similar to the other implementation, though perhaps a little less robust.

The correction factor (or term) is evaluated using gdev. GDev arithmetic with the prior values for the parameters. Alternatively this factor may be estimated using a Monte Carlo simulation by setting corrfitter. CorrFitter parameter mc equal to the number of Monte Carlo samples to be used. The default is mc=None, which implies no

1.7. New Models

Monte Carlo; typical values range between 100 and 1000 if Monte Carlo estimates are preferred. The Monte Carlo estimates are more costly and often less accurate.

1.9 Correlator Model Objects

Correlator objects describe theoretical models that are fit to correlator data by varying the models' parameters.

A model object's parameters are specified through priors for the fit. A model assigns labels to each of its parameters (or arrays of related parameters), and these labels are used to identify the corresponding parameters in the prior. Parameters can be shared by more than one model object.

A model object also specifies the data that it is to model. The data is identified by the data tag that labels it in the input file or gdev.Dataset.

The fit parameters for the non-oscillating piece of Gab (first term) are an [i], bn [i], and dEn [i] where:

When tp is not None, the correlator is assumed to be symmetrical about tp/2, with Gab(t) = Gab(tp-t). Data from t>tp/2 is averaged with the corresponding data from t<tp/2 before fitting.

Parameters

- datatag (string) Tag used to label correlator in the input gdev. Dataset.
- a (string, or two-tuple of strings or None) Fit-parameter label for source amplitude an, or a two-tuple of labels for source amplitudes (an, ao). Each label represents an array of amplitudes. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding amplitudes, which amplitudes must then be positive.
- **b** (string, or two-tuple of strings or None) Fit-parameter label for source amplitude bn, or a two-tuple of labels for source amplitudes (bn, bo). Each label represents an array of amplitudes. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding amplitudes, which amplitudes must then be positive.

- **dE** (string, or two-tuple of strings or None) Fit-parameter label for intermediate-state energy differences dEn, or two-tuple of labels for the differences (dEn, dEo). Each label represents an array of energy differences. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding energy differences, which differences must then be positive.
- **s** (*number or two-tuple of numbers*) Overall factor sn, or two-tuple of overall factors (sn, so).
- tdata (list of integers) The ts corresponding to data entries in the input gdev. Dataset.
- tfit (list of integers) List of ts to use in the fit. Only data with these ts (all of which should be in tdata) is used in the fit.
- tp (integer or None) If not None, the correlator is assumed to be periodic with Gab(t)=Gab(tp-t). Setting tp=None implies that the correlator is not periodic, but rather continues to fall exponentially as t is increased indefinitely.
- othertags (sequence of strings) List of additional data tags for data to be averaged with the self.datatag data before fitting.

builddata(data)

Assemble fit data from dictionary data.

Extracts parts of array data[self.datatag] that are needed for the fit, as specified by self.tp and self.tfit. The entries in the (1-D) array data[self.datatag] are assumed to be gdev.GDevs and correspond to the t''s in ''self.tdata.

```
fitfcn (p, nterm=None)
```

Return fit function for parameters p. (Ingores x.)

class corrfitter. Corr3 (datatag, T, tdata, tfit, Vnn, a, b, dEa=None, dEb=None, logdEa=None, logdEb=None, sa=1.0, sb=1.0, Vno=None, Von=None, Voo=None, $transpose_V=False$, $symmetric_V=False$, tpa=None, tpb=None)

Three-point correlators $Gavb(t, T) = \langle b(T) \ V(t) \ a(0) \rangle$.

corrfitter.Corr3 models the t dependence of a 3-point correlator Gavb(t, T) using

```
Gavb(t, T) =
  sum_i, j san*an[i]*fn(Ean[i],t)*Vnn[i,j]*sbn*bn[j]*fn(Ebn[j],T-t)
+sum_i, j san*an[i]*fn(Ean[i],t)*Vno[i,j]*sbo*bo[j]*fo(Ebo[j],T-t)
+sum_i, j sao*ao[i]*fo(Eao[i],t)*Von[i,j]*sbn*bn[j]*fn(Ebn[j],T-t)
+sum_i, j sao*ao[i]*fo(Eao[i],t)*Voo[i,j]*sbo*bo[j]*fo(Ebo[j],T-t)
```

where

```
fn(E, t) = exp(-E*t) + exp(-E*(tp-t)) # periodic
or exp(-E*t) # if tp is None (nonperiodic)

fo(E, t) = (-1)**t * fn(E, t)
```

The fit parameters for the non-oscillating piece of Gavb (first term) are Vnn[i,j], an [i], bn [j], dEan [i] and dEbn [j] where, for example:

```
dEan[0] = Ean[0] > 0

dEan[i] = Ean[i]-Ean[i-1] > 0 (for i>0)
```

and therefore Ean[i] = sum_j=0..i dEan[j]. The parameters for the other terms are similarly defined.

Parameters

- datatag (string) Tag used to label correlator in the input gdev. Dataset.
- a (string, or two-tuple of strings or None) Fit-parameter label for a->V source amplitudes an, or a two-tuple of labels for source amplitudes (an, ao). Each label represents an array of amplitudes. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding amplitudes, which amplitudes must then be positive.
- **b** (string, or two-tuple of strings or None) Fit-parameter label for V->b source amplitudes bn, or a two-tuple of labels for source amplitudes (bn, bo). Each label represents an array of amplitudes. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding amplitudes, which amplitudes must then be positive.
- dEa (string, or two-tuple of strings or None) Fit-parameter label for a->V intermediatestate energy differences dEan, or two-tuple of labels for the differences (dEan, dEao). Each label represents an array of energy differences. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding energy differences, which differences must then be positive.
- **dEb** (string, or two-tuple of strings or None) Fit-parameter label for V->b intermediatestate energy differences dEbn, or two-tuple of labels for the differences (dEbn, dEbo). Each label represents an array of energy differences. Replacing either label by None causes the corresponding term in the correlator function to be dropped. Fit parameters with labels that begin with "log" are replaced by their exponentials in the fit function; here, therefore, these parameters would be logarithms of the corresponding energy differences, which differences must then be positive.
- sa (number, or two-tuple of numbers) Overall factor san for the non-oscillating a->V terms in the correlator, or two-tuple containing the overall factors (san, sao) for the non-oscillating and oscillating terms.
- **sb** (*number*, *or two-tuple of numbers*) Overall factor sbn for the non-oscillating V->b terms in the correlator, or two-tuple containing the overall factors (sbn, sbo) for the non-oscillating and oscillating terms.
- Vnn (string or None) Fit-parameter label for the matrix of current matrix elements Vnn[i,j] connecting non-oscillating states. Labels that begin with "log" indicate that the corresponding matrix elements are replaced by their exponentials; these parameters are logarithms of the corresponding matrix elements, which must then be positive.
- Vno (string or None) Fit-parameter label for the matrix of current matrix elements Vno[i,j] connecting non-oscillating to oscillating states. Labels that begin with "log" indicate that the corresponding matrix elements are replaced by their exponentials; these parameters are logarithms of the corresponding matrix elements, which must then be positive.
- Von (string or None) Fit-parameter label for the matrix of current matrix elements Von[i,j] connecting oscillating to non-oscillating states. Labels that begin with "log" indicate that the corresponding matrix elements are replaced by their exponentials; these parameters are logarithms of the corresponding matrix elements, which must then be positive.
- **Voo** (string or None) Fit-parameter label for the matrix of current matrix elements Voo[i,j] connecting oscillating states. Labels that begin with "log" indicate that the

corresponding matrix elements are replaced by their exponentials; these parameters are logarithms of the corresponding matrix elements, which must then be positive.

- transpose_V (boolean) If True, the transpose V[j,i] is used in place of V[i,j] for each current matrix element in the fit function. This is useful for doing simultaneous fits to a->V->b and b->V->a, where the current matrix elements for one are the transposes of those for the other. Default value is False.
- symmetric_V (boolean) If True, the fit function for a->V->b is unchanged (symmetrical) under the the interchange of a and b. Then Vnn and Voo are square, symmetric matrices with V[i,j]=V[j,i] and their priors are one-dimensional arrays containing only elements V[i,j] with j>=i in the following layout:

Furthermore the matrix specified for Von is transposed before being used by the fitter; normally the matrix specified for Von is the same as the matrix specified for Vno when the amplitude is symmetrical. Default value is False.

- tdata (list of integers) The ts corresponding to data entries in the input gdev. Dataset.
- **tfit** (*list of integers*) List of ts to use in the fit. Only data with these ts (all of which should be in tdata) is used in the fit.
- **tpa** (integer or None) If not None, the a->V correlator is assumed to be periodic with period tpa. Setting tpa=None implies that the correlators are not periodic.
- **tpb** (integer or None) If not None, the V->b correlator is assumed to be periodic with period tpb. Setting tpb=None implies that the correlators are not periodic.

builddata(data)

Assemble fit data from dictionary data.

Extracts parts of array data[self.datatag] that are needed for the fit, as specified by self.tfit. The entries in the (1-D) array data[self.datatag] are assumed to be gdev.GDevs and correspond to the t``s in ``self.tdata.

fitfcn (p, nterm=None)

Return fit function for parameters p.

class corrfitter.BaseModel (datatag)

Base class for correlator models.

Correlator models are derived from corrfitter.BaseModel. Every correlator model must have at least the following attribute and method:

datatag

The (string) label used to identify Monte Carlo data for the correlator in the input gdev.Dataset. The datatag is stored in the corrfitter.BaseModel and is passed to it at initiation.

fitfcn(self, x, p)

Compute the model's fit function as a function of parameters p. This function should return correlator values in the same format used for the input data (usually a one-dimensional array).

Optionally, correlator models can also define the following attribute and methods for use by corrfitter. CorrFitter:

abscissa

Array of abscissa values used in plots of the data and fit corresponding to the model. Plots are not made for a model that doesn't specify this attribute.

_builddata (self, data)

Construct fit data, possibly using data stored in data. The format of the data must correspond to that returned by self.fitfcn(x, p) (usually a one-dimensional array).

Parameters datatag (*string*) – Tag used to label correlator in the input gdev. Dataset.

builddata(data)

Construct fit data.

Format of output must be same as format for fitfen output.

fitfcn (p, nterm=None)

Compute fit function for x and fit parameters p.

priorsize(nterm=None)

Return dict containing number of entries for each prior label.

1.10 corrfitter.CorrFitter Objects

corrfitter.CorrFitter objects are wrappers for lsqfit.nonlinear_fit() which is used to fit a collection of models to a collection of Monte Carlo data.

Nonlinear least-squares fitter for a collection of correlators.

Parameters

- models (list of correlator models) Correlator models used to fit statistical input data.
- svdcut (number or None or 2-tuple) If svdcut is positive, eigenvalues ev[i] of the (rescaled) data covariance matrix that are smaller than svdcut*max(ev) are replaced by svdcut*max(ev) in the covariance matrix. If svdcut is negative, eigenvalues less than |svdcut|*max(ev) are set to zero in the covariance matrix. The covariance matrix is left unchanged if svdcut is set equal to None (default). If svdcut is a 2-tuple, svd cuts are applied to both the correlator data (svdcut[0]) and to the prior (svdcut[1]).
- svdnum (integer or None or 2-tuple) At most svdnum eigenmodes are retained in the (rescaled) data covariance matrix; the modes with the smallest eigenvalues are discarded. svdnum is ignored if it is set to None. If svdnum is a 2-tuple, *svd* cuts are applied to both the correlator data (svdnum[0]) and to the prior (svdnum[1]).
- **tol** (*positive number less than 1*) Tolerance used in lsqfit.nonlinear_fit() for the least-squares fits (default=1e-10).
- maxit (integer) Maximum number of iterations to use in least-squares fit (default=500).
- **nterm** (number or None; or two-tuple of numbers or None) Number of terms fit in the non-oscillating parts of fit functions; or two-tuple of numbers indicating how many terms to fit for each of the non-oscillating and oscillating pieces in fits. If set to None, the number is specified by the number of parameters in the prior.
- mc (integer or None) Number of Monte Carlo samples to use to estimate fit-data corrections when the prior specifies more terms than are used in the fit. Setting mc=None (the default) results implies that Monte Carlo estimates are not used.

• ratio (boolean) - If True (the default), use ratio corrections for fit data when the prior specifies more terms than are used in the fit. If False, use difference corrections (see implementation notes, above).

bootstrap_iter (datalist=None, n=None)

Iterator that creates bootstrap copies of a corrfitter.CorrFitter fit using bootstrap data from list data_list.

A bootstrap analysis is a robust technique for estimating means and standard deviations of arbitrary functions of the fit parameters. This method creates an interator that implements such an analysis of list (or iterator) datalist, which contains bootstrap copies of the original data set. Each data_list[i] is a different data input for self.lsqfit() (that is, a dictionary containing fit data). The iterator works its way through the data sets in data_list, fitting the next data set on each iteration and returning the resulting lsqfit.LSQFit fit object. Typical usage, for an corrfitter.CorrFitter object named fitter, would be:

```
for fit in fitter.bootstrap_iter(datalist):
    ... analyze fit parameters in fit.p ...
```

Parameters

- data_list (sequence or iterator or None) Collection of bootstrap data sets for fitter. If None, the data_list is generated internally using the means and standard deviations of the fit data (assuming gaussian statistics).
- n (integer) Maximum number of iterations if n is not None; otherwise there is no maximum.

Returns Iterator that returns a lsqfit.LSQFit object containing results from the fit to the next data set in data_list.

builddata(data, prior)

Build fit data, corrected for marginalized terms.

buildprior (prior)

Build correctly sized prior for fit.

collect fitresults()

Collect results from last fit for plots, tables etc.

Returns

A dictionary with one entry per correlator model, containing (t,G,dG,Gth,dGth) — arrays containing:

```
\begin{array}{lll} t & = \text{times} \\ G(t) & = \text{data averages for correlator at times t} \\ dG(t) & = \text{uncertainties in } G(t) \\ Gth(t) & = \text{fit function for } G(t) \text{ with best-fit parameters} \\ dGth(t) & = \text{uncertainties in } Gth(t) \end{array}
```

display_plots()

Show plots of data/fit-function for each correlator.

Assumes matplotlib is installed (to make the plots). Plots are shown for one correlator at a time. Press key p to see the next correlator; press key p to see the previous one; press key q to quit the plot and return control to the calling program; press a digit to go directly to one of the first ten plots. Zoom, pan and save using the window controls.

fitfcn (*xdummy*, *p*, *nterm=None*) Composite fit function.

Parameters

- **p** (*dict-like*) Fit parameters.
- **nterm** (number or None; or two-tuple of numbers or None) Number of terms fit in the non-oscillating parts of fit functions; or two-tuple of numbers indicating how many terms to fit for each of the non-oscillating and oscillating pieces in fits. If set to None, the number is specified by the number of parameters in the prior.

Returns A dictionary containing the fit function results for parameters p from each model, indexed using the models' datatags.

Compute least-squares fit of the correlator models to data.

Parameters

- data (dictionary) Input data. The datatags from the correlator models are used as data labels, with data[datatag] being a 1-d array of gdev.GDevs corresponding to correlator values.
- **prior** (dictionary) Bayesian prior for the fit parameters used in the correlator models.
- p0 A dictionary, indexed by parameter labels, containing initial values for the parameters in the fit. Setting p0=None implies that initial values are extracted from the prior. Setting p0="filename" causes the fitter to look in the file with name "filename" for initial values and to write out best-fit parameter values after the fit (for the next call to self.lsqfit()).
- print_fit Print fit information to standard output if True; otherwise print nothing.
- svdcut (number or None) If svdcut is positive, eigenvalues ev[i] of the data covariance matrix that are smaller than svdcut*max(ev) are replaced by svdcut*max(ev) in the covariance matrix. If svdcut is negative, eigenvalues less than |svdcut|*max(ev) are set to zero in the covariance matrix. The covariance matrix is left unchanged if svdcut is set equal to None. If svdcut is a 2-tuple, svd cuts are applied to both the correlator data (svdcut[0]) and to the prior (svdcut[1]).
- **svdnum** (integer or None or 2-tuple) At most svdnum eigenmodes are retained in the (rescaled) data covariance matrix; the modes with the smallest eigenvalues are discarded. svdnum is ignored if it is set to None. If svdnum is a 2-tuple, *svd* cuts are applied to both the correlator data (svdnum[0]) and to the prior (svdnum[1]).
- **tol** (*positive number less than 1*) Tolerance used in lsqfit.nonlinear_fit() for the least-squares fits (default=1e-10).
- maxit (integer) Maximum number of iterations to use in least-squares fit (default=500).

CHAPTER

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